

UNIVERSITI TEKNOLOGI MALAYSIA FINAL EXAMINATION SEMESTER 2, 2023/2024

SUBJECT CODE : SECI1143

SUBJECT NAME : PROBABILITY & STATISTICAL DATA ANALYSIS

SECTION : 01 - 12

TIME :

DATE/DAY :

VENUES :

INSTRUCTIONS:

- i. Answer ALL questions in the given ANSWER BOOKLET.
- ii. This paper consists of SIX (6) QUESTIONS:
- iii. DO ALL CALCULATION IN 3 DECIMAL POINTS.
- iv. Submit **BOTH Questions and Answer Booklet** at the end of the exam.

(Please Write Your Lecturer Name and Section in Your Answer Booklet)

Name	
I/C No.	
Year / Course	
Section	
Lecturer Name	

This question paper consists of **EIGHT (8)** printed pages including this page.

STRUCTURED QUESTIONS (100 MARKS)

INSTRUCTION:

This section consists of SIX (6) questions. Answer ALL questions in the answer booklet.

QUESTION 1 [10 MARKS]

a) A study in agriculture industry is conducted to estimate the average yield of wheat per acre in the farms. The study wants to determine the population mean yield and construct a confidence interval to provide a range within which the true population mean lies. Hence, 15 wheat fields are selected randomly from the farms and record the yields (in KG per acre). The data are as in **Table 1**:

Wheat fields 2 1 3 4 5 Yields (KG / acre) 50 55 48 52 49 Wheat fields 6 7 8 9 10 Yields (KG / acre) 56 53 47 51 50 Wheat fields 12 14 11 13 15 Yields (KG / acre) 54 52 48 50 55

Table 1: Data on yield of wheat per acre in the farms

i) Calculate a point estimate of the population mean, μ.

(2 Marks)

ii) Construct and interpret a 90% confidence interval for μ .

(5 Marks)

b) A financial analyst wants to determine if a sample of stock returns comes from a population with a mean return greater than 8%. The analyst obtains a simple random sample of 60 stock returns from a particular sector. The sample mean return is 9.2%, and the population standard deviation of stock returns in this sector is known to be 3.5%. The analyst decides to test the claim using a significance level of 0.05. Interpret and proof his assumption with statistic.

(3 Marks)

QUESTION 2 [20 MARKS]

a) A company is interested in comparing customer satisfaction scores for two different versions of its product. They collected satisfaction ratings from two independent samples of customers who used Version A and Version B of the product. The goal is to determine if there is a significant difference in customer satisfaction between the two versions. The summary of the data is in **Table 2**:

Table 2: Data on customer satisfaction scores for two different versions product

	Number of respondents, n_i	Mean, \underline{x}_i	Standard deviation, S_i
Version A	50	4.2	0.8
Version B	60	4.5	0.7

i) State the hypothesis statement.

(2 Marks)

ii) Calculate the test statistic.

(2 Marks)

iii) Calculate the degree of freedom.

(2 Marks)

iv) Test at $\alpha = 0.05$ level of significance whether there is a mean difference in customer satisfaction between the two versions.

(4 Marks)

b) A group of students are evaluated to test their performance before and after a tutoring program, and the results are shown in **Table 3.**

Table 3: Data on performance before and after a tutoring program

Before tutoring	72	68	75	80	78
After tutoring	82	85	88	90	86

i) State the null and alternative hypotheses

(1 Mark)

ii) By using a significance level of $\alpha = 0.05$, does a tutoring program have a significant effect on the improvement of test scores for students?

(9 Marks)

QUESTION 3 [20 MARKS]

a) A restaurant manager wants to analyse whether the distribution of customer reservations is uniform across weekdays. The manager recorded the number of reservations made each day during a randomly chosen week. The data is presented in **Table 4** below:

Table 4: Data on number of reservations made each day during a randomly chosen week

Day	Monday	Tuesday	Wednesday	Thursday	Friday
Reservation	30	25	35	28	40

i) Based on this data, conduct a hypothesis test.

(1 Mark)

ii) Calculate the expected frequency and the test statistic.

(4 Marks)

iii) Find the critical value. Do the data prove that the number of reservations is equally distributed throughout the weekdays. Use significance level, a = 0.05.

(3 Marks)

b) Internet has become the most important means of communication and gathering information. People with different age use Internet for different purposes. A random sample of 159 adults yielded the data shows in **Table 5** to find out the relationship between age and the usage of internet.

Table 5: The relationship between age and the usage of internet

		Ag	ge
		25- 64	65+
Internet Usage	Never	38	31
	Sometimes	31	4
Usage	Every day	50	5

i) State the null and alternative hypotheses.

(2 Marks)

ii) Calculate the expected count and the test statistic

(7 Marks)

iii) At the 1% significance level, do the data provide sufficient evidence to conclude that a relationship exists between age and Internet usage?

(3 Marks)

QUESTION 4 [15 MARKS]

Table 6 shows the blood pressure, *p* mmHG, and albumin, *a*, mg/gram level for 7 patients. High blood pressure may cause kidney disease or damage indicated by albumin level. An analysis must be conducted to understand the relationship between blood pressure and raised albumin levels.

Table 6: Blood pressure and albumin level

Patient	A	В	C	D	E	F	G
p	160	162	175	185	178	170	182
а	22	29	31	35	33	38	45

a) Draw (sketch) the scatterplot. Is there any relationship observed? If yes, determine whether the relationship is negative or positive.

(2 Marks)

b) Calculate the correlation coefficient for data in **Table 6**, given $\Sigma p^2 = 210402$ and $\Sigma a^2 = 8069$. Interpret the result.

(11 Marks)

c) Each patient in **Table 6** is given medication that lowers the blood pressure level, p, what will happen to albumin level, a, based on your findings in (b)?

(2 Marks)

QUESTION 5 [15 MARKS]

a) Kembara Motor Association (KMA) is analyzing the relationship between engine volume and mileage, given the same volume of petrol. **Table 7** is tabulated for liquidcooled 4-stroke 16-valve cylinder engines from different motorbikes manufacturers. The engine volume is in total cubic km.

Table 7: Engine Volume and Mileage of different Motorbikes Manufacturer

Motorbikes manufacturer	Engine volume, x (cubic km)	Mileage, y (km)
A	97	24
В	88	21
С	105	24
D	151	25
Е	140	22
F	134	23
G	118	22

Based on the given data,

i) Find the summation for x, y, x^2, y^2 and xy for the above data.

(5 Marks)

ii) Find the linear regression equation using the least-square method.

(4 Marks)

iii) Use the linear regression equation to estimate the mileage for a motorbike which has 120 cubic km engine volume.

(1 Mark)

b) Dr. Fatimah is monitoring 6 diabetic patients in her ward. After her morning round, she observed that her patient' blood pressure, (p mmHg) and their age (t years) as in **Table 8** below:

Table 8: Blood pressure ages of Dr. Fatimah's patients

Patient	1	2	3	4	5	6
t	35	74	48	60	42	26
p	88	130	120	135	98	80

i) Sketch a scatter diagram of the data and interpret the correlation coefficient.

(2 marks)

ii) Given the estimator of the standard error of the slope (s_{b_1}) is 0.07 and the linear regression equation for the data is $\hat{y} = 50.728 + 1.216x$, does the patient's age affect the blood pressure reading? Test the hypothesis using 95% confidence level.

(3 marks)

QUESTION 6 [20 MARKS]

Table 9 below examines departure delay times for AM Airline flights from Senai Johor to Kuching Sarawak. Departure delay times, measured in minutes, reflect the time difference between scheduled departure and actual departure.

The negative values denote flights departing earlier than scheduled (early take-off) and 0 means the flight departed on time (no delay). The objective of the study is to ascertain whether these departure delay times vary significantly across different flights.

Standard Flight No **Departure Delay Times (minutes)** Deviation, s_i AB103 -2 -1 -2 2 -2 0 -2 -3 $s_1 = 1.58$ $s_2 = 26.64$ -5 73 0 AB112 19 -4 -1 -4 1 AB108 18 60 142 -1 -11 -1 47 13 $s_3 = 50.25$

Table 9: Departure delay times for AM Airline flights

Let: \underline{x}_1 is the mean for flight AB103.

 \underline{x}_2 is the mean for flight AB112.

 x_3 is the mean for flight AB108.

- a) Find:
 - i) \underline{x} for each category.

(3 Marks)

ii) Variance between samples.

(5 Marks)

iii) Variance within samples.

(4 Marks)

b) Use a 0.05 significance level to test the claim that the different flights have the same mean departure delay time.

(8 Marks)

-END OF QUESTIONS PAPER-

List of Formula:

(a) Hypothesis Testing for one sample:

$$Test \, Statistic, z = \frac{\hat{p} - p}{\sqrt{\frac{pq}{n}}}$$

$$Test \, Statistic, t_0 = \frac{\bar{x} - \mu}{s/\sqrt{n}}$$

$$Test \, Statistic, z_0 = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}}$$

$$Test \, Statistic, \chi^2 = \frac{(n-1)s^2}{\sigma^2}$$

(b) Hypothesis Testing for two samples:

$$Test \, Statistic, z = \frac{(\widehat{p_1} - \widehat{p_2}) - (p_1 - p_2)}{\sqrt{\frac{\overline{p}\overline{q}}{n_1} + \frac{\overline{p}\overline{q}}{n_2}}}$$

$$Test \, Statistic, z_0 = \frac{\bar{x}_1 - \bar{x}_2 - \Delta_0}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$$

$$Test \, Statistic, t_0 = \frac{\bar{x}_1 - \bar{x}_2 - \Delta_0}{s_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}; s_p^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$$

$$Test \, Statistic, T_0 = \frac{\bar{x}_1 - \bar{x}_2 - \Delta_0}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}; v = \frac{\left(\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}\right)^2}{\left(\frac{s_1^2}{n_1} - 1\right)^2 + \left(\frac{s_2^2}{n_2} + \frac{s_2^2}{n_2}\right)^2}$$

Test Statistic,
$$F_0 = \frac{s_1^2}{s_2^2}$$
; Degree of Freedom = $F_{(n_1-1,n_2-1)}$

$$\textit{Test Statistic}, t = \frac{\overline{D} - \mu_D}{\frac{S_D}{\sqrt{n}}} \; ; \; \textit{Degree of Freedom} = \; n-1$$

$$\overline{D} = \frac{\sum D}{n}$$
; $S_D = \sqrt{\frac{\sum D^2 - \frac{(\sum D^2)}{n}}{n-1}}$

(c) Chi-Square Test

Test Statistic,
$$\chi^2 = \sum_{i}^{n} \frac{(o_i - e_i)^2}{e_i}$$

Degree of Freedom for one – way contigency table = k-1

$$Test \, Statistic, \chi^2 = \sum_{i}^{n} \frac{\left(o_{ij} - e_{ij}\right)^2}{e_{ij}}, \, e_{ij} = \frac{(i^{th} Row \, total)(j^{th} Column \, total)}{Total \, sample \, size}$$

Degree of Freedom for two – way contigency table = (r-1)(c-1)

(d) Correlation

Pearson Correlation Coefficient,
$$r = \frac{\sum xy - \frac{(\sum x \sum y)}{n}}{\sqrt{\left(\sum x^2 - \frac{(\sum x)^2}{n}\right)\left(\sum y^2 - \frac{(\sum y)^2}{n}\right)}}$$

Spearman Correlation Coefficient,
$$r_s = 1 - \frac{6\sum d_i^2}{n(n^2 - 1)}$$
 where $d_i = y_i - x_i$

$$Test \, Statistic, t = \frac{r}{\sqrt{\frac{1 - r^2}{n - 2}}}$$

(e) Regression

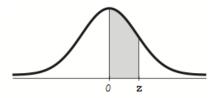
$$b_{1} = \frac{\sum xy - \frac{(\sum x \sum y)}{n}}{\sum x^{2} - \frac{(\sum x)^{2}}{n}} ; b_{0} = \bar{y} - b_{1}\bar{x}$$

$$\textit{Test Statistic}, t = \frac{b_1 - \beta_1}{S_{b_1}} \; ; \; \textit{Degree of Freedom} \; = n-2$$

(f) Analysis of variance (ANOVA)

$$Test \, Statistic, F = \frac{ns^{\frac{2}{x}}}{s_p^2}$$

- numerator degrees of freedom = k 1
- denominator degrees of freedom = k(n 1)



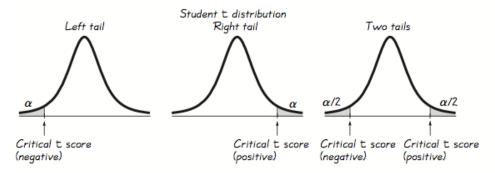
z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.0
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.03
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.07
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.11
0.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.15
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.18
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.22
0.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2517	.25
0.7	.2580	.2611	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.28
0.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.31
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.33
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.36
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.38
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.40
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.41
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.43
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.44
1.6	.4452	.4463	.4474	.4484		* .4505	.4515	.4525	.4535	.45
1.7	.4554	.4564	.4573	.4582		.4599	.4608	.4616	.4625	.46
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.47
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.47
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.48
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.48
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.48
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.49
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.49
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	11212	* .4951	.49
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.49
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.49
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.49
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.49
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.49
3.10										
and	.4999									
nigher										

2 score Area
1.645 0.4500
2.575 0.4950

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$\overline{}$	RD NORN									
Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
-3.9	.00005	.00005	.00004	.00004	.00004	.00004	.00004	.00004	.00003	.00003
-3.8	.00007	.00007	.00007	.00006	.00006	.00006	.00006	.00005	.00005	.00005
-3.7	.00011	.00010	.00010	.00010	.00009	.00009	.00008	.00008	.00008	.00000
-3.6	.00016	.00015	.00015	.00014	.00014	.00013	.00013	.00012	.00012	.00011
-3.5	.00023	.00022	.00022	.00021	.00020	.00019	.00019	.00018	.00017	.00017
-3.4	.00034	.00032	.00031	.00030	.00029	.00028	.00027	.00026	.00025	.00024
-3.3	.00048	.00047	.00045	.00043	.00042	.00040	.00039	.00038	.00036	.00033
-3.2	.00069	.00066	.00064	.00062	.00060	.00058	.00056	.00054	.00052	.0005
-3.1	.00097	.00094	.00090	.00087	.00084	.00082	.00079	.00076	.00074	.0007
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-2.9	.00187	.00181	.00175	.00169	.00164	.00159	.00154	.00149	.00144	.00139
-2.8	.00256	.00248	.00240	.00233	.00226	.00219	.00212	.00205	.00199	.00193
-2.7	.00347	.00336	.00326	.00317	.00307	.00298	.00289	.00280	.00272	.0026
-2.6	.00466	.00453	.00440	.00427	.00415	.00402	.00391	.00379	.00368	.0035
-2.5	.00621	.00604	.00587	.00570	.00554	.00539	.00523	.00508	.00494	.0048
-2.4	.00820	.00798	.00776	.00755	.00734	.00714	.00695	.00676	.00657	.0063
-2.3	.01072	.01044	.01017	.00990	.00964	.00939	.00914	.00889	.00866	.0084
-2.2	.01390	.01355	.01321	.01287	.01255	.01222	.01191	.01160	.01130	.0110
-2.1	.01786	.01743	.01700	.01659	.01618	.01578	.01539	.01500	.01463	.0142
-2.0	.02275	.02222	.02169	.02118	.02068	.02018	.01970	.01923	.01876	.0183
-1.9	.02872	.02807	.02743	.02680	.02619	.02559	.02500	.02442	.02385	.0233
-1.8	.03593	.03515	.03438	.03362	.03288	.03216	.03144	.03074	.03005	.0293
-1.7	.04457	.04363	.04272	.04182	.04093	.04006	.03920	.03836	.03754	.0367
-1.6	.05480	.05370	.05262	.05155	.05050	.04947	.04846	.04746	.04648	.0455
-1.5	.06681	.06552	.06426	.06301	.06178	.06057	.05938	.05821	.05705	.0559
-1.4	.08076	.07927	.07780	.07636	.07493	.07353	.07215	.07078	.06944	.0681
-1.3	.09680	.09510	.09342	.09176	.09012	.08851	.08691	.08534	.08379	.0822
-1.2	.11507	.11314	.11123	.10935	.10749	.10565	.10383	.10204	.10027	.0985
-1.1	.13567	.13350	.13136	.12924	.12714	.12507	.12302	.12100	.11900	.1170
-1.0	.15866	.15625	.15386	.15151	.14917	.14686	.14457	.14231	.14007	.1378
-0.9	.18406	.18141	.17879	.17619	.17361	.17106	.16853	.16602	.16354	.1610
-0.8	.21186	.20897	.20611	.20327	.20045	.19766	.19489	.19215	.18943	.1867
-0.7	.24196	.23885	.23576	.23270	.22965	.22663	.22363	.22065	.21770	.2147
-0.6	.27425	.27093	.26763	.26435	.26109	.25785	.25463	.25143	.24825	.2451
-0.5	.30854	.30503	.30153	.29806	.29460	.29116	.28774	.28434	.28096	.2776
-0.4	.34458	.34090	.33724	.33360	.32997	.32636	.32276	.31918	.31561	.3120
-0.3	.38209	.37828	.37448	.37070	.36693	.36317	.35942	.35569	.35197	.3482
-0.2	.42074	.41683	.41294	.40905	.40517	.40129	.39743	.39358	.38974	.3859
-0.1	.46017	.45620	.45224	.44828	.44433	.44038	.43644	.43251	.42858	.4246

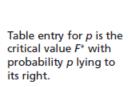
z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
$\overline{}$.50000	.50399	.50798	.51197	.51595	.51994	.52392	.52790	.53188	.5358
0.0										
0.1	.53983	.54380	.54776	.55172	.55567	.55962	.56356	.56749	.57142	.5753
0.2		.58317	.58706	.59095	.59483	.59871	.60257	.60642	.61026	.6140
0.3	.61791	.62172	.62552	.62930	.63307	.63683	.64058	.64431	.64803	.6517
0.4	.65542	.65910	.66276	.66640	.67003	.67364	.67724	.68082	.68439	.6879
0.5	.69146	.69497	.69847	.70194	.70540	.70884	.71226	.71566	.71904	.7224
0.6	.72575	.72907	.73237	.73565	.73891	.74215	.74537	.74857	.75175	.7549
0.7	.75804	.76115	.76424	.76730	.77035	.77337	.77637	.77935	.78230	.7852
0.8	.78814	.79103	.79389	.79673	.79955	.80234	.80511	.80785	.81057	.8132
0.9	.81594	.81859	.82121	.82381	.82639	.82894	.83147	.83398	.83646	.8389
1.0	.84134	.84375	.84614	.84849	.85083	.85314	.85543	.85769	.85993	.862
1.1	.86433	.86650	.86864	.87076	.87286	.87493	.87698	.87900	.88100	.8829
1.2	.88493	.88686	.88877	.89065	.89251	.89435	.89617	.89796	.89973	.901
1.3	.90320	.90490	.90658	.90824	.90988	.91149	.91309	.91466	.91621	.917
1.4	.91924	.92073	.92220	.92364	.92507	.92647	.92785	.92922	.93056	.9318
1.5	.93319	.93448	.93574	.93699	.93822	.93943	.94062	.94179	.94295	.944
1.6	.94520	.94630	.94738	.94845	.94950	.95053	.95154	.95254	.95352	.954
1.7	.95543	.95637	.95728	.95818	.95907	.95994	.96080	.96164	.96246	.963
1.8	.96407	.96485	.96562	.96638	.96712	.96784	.96856	.96926	.96995	.970
1.9	.97128	.97193	.97257	.97320	.97381	.97441	.97500	.97558	.97615	.976
2.0	.97725	.97778	.97831	.97882	.97932	.97982	.98030	.98077	.98124	.981
2.1	.98214	.98257	.98300	.98341	.98382	.98422	.98461	.98500	.98537	.985
2.2	.98610	.98645	.98679	.98713	.98745	.98778	.98809	.98840	.98870	.988
2.3	.98928	.98956	.98983	.99010	.99036	.99061	.99086	.99111	.99134	.991
2.4	.99180	.99202	.99224	.99245	.99266	.99286	.99305	.99324	.99343	.993
2.5	.99379	.99396	.99413	.99430	.99446	.99461	.99477	.99492	.99506	.995
2.6	.99534	.99547	.99560	.99573	.99585	.99598	.99609	.99621	.99632	.996
2.7	.99653	.99664	.99674	.99683	.99693	.99702	.99711	.99720	.99728	.997
2.8	.99744	.99752	.99760	.99767	.99774	.99781	.99788	.99795	.99801	.998
2.9	.99813	.99819	.99825	.99831	.99836	.99841	.99846	.99851	.99856	.998
3.0	.99865	.99869	.99874	.99878	.99882	.99886	.99889	.99893	.99896	.999
3.1	.99903	.99906	.99910	.99913	.99916	.99918	.99921	.99924	.99926	.999
3.2	.99931	.99934	.99936	.99938	.99940	.99942	.99944	.99946	.99948	.999
3.3	.99952	.99953	.99955	.99957	.99958	.99960	.99961	.99962	.99964	.999
3.4	.99966	.99968	.99969	.99970	.99971	.99972	.99973	.99974	.99975	.999
3.5	.99977	.99978	.99978	.99979	.99980	.99981	.99981	.99982	.99983	.999
3.6	.99984	.99985	.99985	.99986	.99986	.99987	.99987	.99988	.99988	.999
3.7	.99989	.99990	.99990	.99990	.99991	.99991	.99992	.99992	.99992	.999
3.8	.99993	.99993	.99993	.99994	.99994	.99994	.99994	.99995	.99995	.999
3.9	.99995	.99995	.99996	.99996	.99996	.99996	.99996	.99996	.99997	.9999

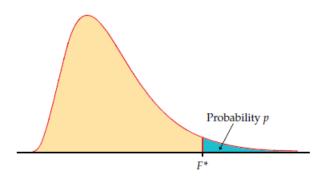


			α			
	.005	.01	.025	.05	.10	.25
Degrees	(one tail)					
of	.01	.02	.05	.10	.20	.50
Freedom	(two tails)					
1	63.657	31.821	12.706	6.314	3.078	1.000
2	9.925	6.965	4.303	2.920	1.886	.816
3	5.841	4.541	3.182	2.353	1.638	.765
4	4.604	3.747	2.776	2.132	1.533	.741
5	4.032	3.365	2.571	2.015	1.476	.727
6	3.707	3.143	2.447	1.943	1.440	.718
7	3.500	2.998	2.365	1.895	1.415	.711
8	3.355	2.896	2.306	1.860	1.397	.706
9	3.250	2.821	2.262	1.833	1.383	.703
10	3.169	2.764	2.228	1.812	1.372	.700
11	3.106	2.718	2.201	1.796	1.363	.697
12	3.054	2.681	2.179	1.782	1.356	.696
13	3.012	2.650	2.160	1.771	1.350	.694
14	2.977	2.625	2.145	1.761	1.345	.692
15	2.947	2.602	2.132	1.753	1.341	.691
16	2.921	2.584	2.120	1.746	1.337	.690
17	2.898	2.567	2.110	1.740	1.333	.689
18	2.878	2.552	2.101	1.734	1.330	.688
19	2.861	2.540	2.093	1.729	1.328	.688
20	2.845	2.528	2.086	1.725	1.325	.687
21	2.831	2.518	2.080	1.721	1.323	.686
22	2.819	2.508	2.074	1.717	1.321	.686
23	2.807	2.500	2.069	1.714	1.320	.685
24	2.797	2.492	2.064	1.711	1.318	.685
25	2.787	2.485	2.060	1.708	1.316	.684
26	2.779	2.479	2.056	1.706	1.315	.684
27	2.771	2.473	2.052	1.703	1.314	.684
28	2.763	2.467	2.048	1.701	1.313	.683
29	2.756	2.462	2.045	1.699	1.311	.683
Large (z)	2.575	2.326	1.960	1.645	1.282	.675

TABLE A-4	Chi-S	quare $(\chi$	²) Distrib	oution						
				Are	a to the F	Right of the	Critical V	alue (
Degrees of										
Freedom	0.995	0.99	0.975	0.95	0.90	0.10	0.05	0.025	0.01	0.005
1	_	_	0.001	0.004	0.016	2.706	3.841	5.024	6.635	7.879
2	0.010	0.020	0.051	0.103	0.211	4.605	5.991	7.378	9.210	10.597
3	0.072	0.115	0.216	0.352	0.584	6.251	7.815	9.348	11.345	12.838
4	0.207	0.297	0.484	0.711	1.064	7.779	9.488	11.143	13.277	14.860
5	0.412	0.554	0.831	1.145	1.610	9.236	11.071	12.833	15.086	16.750
6	0.676	0.872	1.237	1.635	2.204	10.645	12.592	14.449	16.812	18.548
7	0.989	1.239	1.690	2.167	2.833	12.017	14.067	16.013	18.475	20.278
8	1.344	1.646	2.180	2.733	3.490	13.362	15.507	17.535	20.090	21.955
9	1.735	2.088	2.700	3.325	4.168	14.684	16.919	19.023	21.666	23.589
10	2.156	2.558	3.247	3.940	4.865	15.987	18.307	20.483	23.209	25.188
11	2.603	3.053	3.816	4.575	5.578	17.275	19.675	21.920	24.725	26.757
12	3.074	3.571	4.404	5.226	6.304	18.549	21.026	23.337	26.217	28.299
13	3.565	4.107	5.009	5.892	7.042	19.812	22.362	24.736	27.688	29.819
14	4.075	4.660	5.629	6.571	7.790	21.064	23.685	26.119	29.141	31.319
15	4.601	5.229	6.262	7.261	8.547	22.307	24.996	27.488	30.578	32.801
16	5.142	5.812	6.908	7.962	9.312	23.542	26.296	28.845	32.000	34.267
17	5.697	6.408	7.564	8.672	10.085	24.769	27.587	30.191	33.409	35.718
18	6.265	7.015	8.231	9.390	10.865	25.989	28.869	31.526	34.805	37.156
19	6.844	7.633	8.907	10.117	11.651	27.204	30.144	32.852	36.191	38.582
20	7.434	8.260	9.591	10.851	12.443	28.412	31.410	34.170	37.566	39.997
21	8.034	8.897	10.283	11.591	13.240	29.615	32.671	35.479	38.932	41.401
22	8.643	9.542	10.982	12.338	14.042	30.813	33.924	36.781	40.289	42.796
23	9.260	10.196	11.689	13.091	14.848	32.007	35.172	38.076	41.638	44.181
24	9.886	10.856	12.401	13.848	15.659	33.196	36.415	39.364	42.980	45.559
25	10.520	11.524	13.120	14.611	16.473	34.382	37.652	40.646	44.314	46.928
26	11.160	12.198	13.844	15.379	17.292	35.563	38.885	41.923	45.642	48.290
27	11.808	12.879	14.573	16.151	18.114	36.741	40.113	43.194	46.963	49.645
28	12.461	13.565	15.308	16.928	18.939	37.916	41.337	44.461	48.278	50.993
29	13.121	14.257	16.047	17.708	19.768	39.087	42.557	45.722	49.588	52.336
30	13.787	14.954	16.791	18.493	20.599	40.256	43.773	46.979	50.892	53.672
40	20.707	22.164	24.433	26.509	29.051	51.805	55.758	59.342	63.691	66.766
50	27.991	29.707	32.357	34.764	37.689	63.167	67.505	71.420	76.154	79.490
60	35.534	37.485	40.482	43.188	46.459	74.397	79.082	83.298	88.379	91.952
70	43.275	45.442	48.758	51.739	55.329	85.527	90.531	95.023	100.425	104.215
80	51.172	53.540	57.153	60.391	64.278	96.578	101.879	106.629	112.329	116.321
90	59.196	61.754	65.647	69.126	73.291	107.565	113.145	118.136	124.116	128.299
100	67.328	70.065	74.222	77.929	82.358	118.498	124.342	129.561	135.807	140.169

T-12 Tables





						Degrees of f	reedom in th	e numerator			
		p	1	2	3	4	5	6	7	8	9
	1	.100 .050 .025 .010 .001	39.86 161.45 647.79 4052.2 405284	49.50 199.50 799.50 4999.5 500000	53.59 215.71 864.16 5403.4 540379	55.83 224.58 899.58 5624.6 562500	57.24 230.16 921.85 5763.6 576405	58.20 233.99 937.11 5859.0 585937	58.91 236.77 948.22 5928.4 592873	59.44 238.88 956.66 5981.1 598144	59.86 240.54 963.28 6022.5 602284
	2	.100 .050 .025 .010 .001	8.53 18.51 38.51 98.50 998.50	9.00 19.00 39.00 99.00 999.00	9.16 19.16 39.17 99.17 999.17	9.24 19.25 39.25 99.25 999.25	9.29 19.30 39.30 99.30 999.30	9.33 19.33 39.33 99.33 999.33	9.35 19.35 39.36 99.36 999.36	9.37 19.37 39.37 99.37 999.37	9.38 19.38 39.39 99.39 999.39
enominator	3	.100 .050 .025 .010 .001	5.54 10.13 17.44 34.12 167.03	5.46 9.55 16.04 30.82 148.50	5.39 9.28 15.44 29.46 141.11	5.34 9.12 15.10 28.71 137.10	5.31 9.01 14.88 28.24 134.58	5.28 8.94 14.73 27.91 132.85	5.27 8.89 14.62 27.67 131.58	5.25 8.85 14.54 27.49 130.62	5.24 8.81 14.47 27.35 129.86
Degrees of freedom in the denominator	4	.100 .050 .025 .010 .001	4.54 7.71 12.22 21.20 74.14	4.32 6.94 10.65 18.00 61.25	4.19 6.59 9.98 16.69 56.18	4.11 6.39 9.60 15.98 53.44	4.05 6.26 9.36 15.52 51.71	4.01 6.16 9.20 15.21 50.53	3.98 6.09 9.07 14.98 49.66	3.95 6.04 8.98 14.80 49.00	3.94 6.00 8.90 14.66 48.47
Degrees of fr	5	.100 .050 .025 .010 .001	4.06 6.61 10.01 16.26 47.18	3.78 5.79 8.43 13.27 37.12	3.62 5.41 7.76 12.06 33.20	3.52 5.19 7.39 11.39 31.09	3.45 5.05 7.15 10.97 29.75	3.40 4.95 6.98 10.67 28.83	3.37 4.88 6.85 10.46 28.16	3.34 4.82 6.76 10.29 27.65	3.32 4.77 6.68 10.16 27.24
	6	.100 .050 .025 .010 .001	3.78 5.99 8.81 13.75 35.51	3.46 5.14 7.26 10.92 27.00	3.29 4.76 6.60 9.78 23.70	3.18 4.53 6.23 9.15 21.92	3.11 4.39 5.99 8.75 20.80	3.05 4.28 5.82 8.47 20.03	3.01 4.21 5.70 8.26 19.46	2.98 4.15 5.60 8.10 19.03	2.96 4.10 5.52 7.98 18.69
	7	.100 .050 .025 .010	3.59 5.59 8.07 12.25 29.25	3.26 4.74 6.54 9.55 21.69	3.07 4.35 5.89 8.45 18.77	2.96 4.12 5.52 7.85 17.20	2.88 3.97 5.29 7.46 16.21	2.83 3.87 5.12 7.19 15.52	2.78 3.79 4.99 6.99 15.02	2.75 3.73 4.90 6.84 14.63	2.72 3.68 4.82 6.72 14.33

Tables T-13

Probability pwith any to F^*

Table entry for p is the critical value F^* with probability p lying to its right.

TABLE	E									
F critic	al values	(continued)								
				Degrees of fi	reedom in th	e numerator				
10	12	15	20	25	30	40	50	60	120	1000
60.19	60.71	61.22	61.74	62.05	62.26	62.53	62.69	62.79	63.06	63.30
241.88	243.91	245.95	248.01	249.26	250.10	251.14	251.77	252.20	253.25	254.19
968.63	976.71	984.87	993.10	998.08	1001.4	1005.6	1008.1	1009.8	1014.0	1017.7
6055.8	6106.3	6157.3	6208.7	6239.8	6260.6	6286.8	6302.5	6313.0	6339.4	6362.7
605621	610668	615764	620908	624017	626099	628712	630285	631337	633972	636301
9.39 19.40 39.40 99.40 999.40	9.41 19.41 39.41 99.42 999.42	9.42 19.43 39.43 99.43	9.44 19.45 39.45 99.45	9.45 19.46 39.46 99.46	9.46 19.46 39.46 99.47 999.47	9.47 19.47 39.47 99.47 999.47	9.47 19.48 39.48 99.48 999.48	9.47 19.48 39.48 99.48 999.48	9.48 19.49 39.49 99.49	9,49 19,49 39,50 99,50
5.23	5.22	5.20	5.18	5.17	5.17	5.16	5.15	5.15	5.14	5.13
8.79	8.74	8.70	8.66	8.63	8.62	8.59	8.58	8.57	8.55	8.53
14.42	14.34	14.25	14.17	14.12	14.08	14.04	14.01	13.99	13.95	13.91
27.23	27.05	26.87	26.69	26.58	26.50	26.41	26.35	26.32	26.22	26.14
129.25	128.32	127.37	126.42	125.84	125.45	124.96	124.66	124.47	123.97	123.53
3.92	3.90	3.87	3.84	3.83	3.82	3.80	3.80	3.79	3.78	3.76
5.96	5.91	5.86	5.80	5.77	5.75	5.72	5.70	5.69	5.66	5.63
8.84	8.75	8.66	8.56	8.50	8.46	8.41	8.38	8.36	8.31	8.26
14.55	14.37	14.20	14.02	13.91	13.84	13.75	13.69	13.65	13.56	13.47
48.05	47.41	46.76	46.10	45.70	45.43	45.09	44.88	44.75	44.40	44.09
3.30	3.27	3.24	3.21	3.19	3.17	3.16	3.15	3.14	3.12	3.11
4.74	4.68	4.62	4.56	4.52	4.50	4.46	4.44	4.43	4.40	4.37
6.62	6.52	6.43	6.33	6.27	6.23	6.18	6.14	6.12	6.07	6.02
10.05	9.89	9.72	9.55	9.45	9.38	9.29	9.24	9.20	9.11	9.03
26.92	26.42	25.91	25.39	25.08	24.87	24.60	24.44	24.33	24.06	23.82
2.94	2.90	2.87	2.84	2.81	2.80	2.78	2.77	2.76	2.74	2.72
4.06	4.00	3.94	3.87	3.83	3.81	3.77	3.75	3.74	3.70	3.67
5.46	5.37	5.27	5.17	5.11	5.07	5.01	4.98	4.96	4.90	4.86
7.87	7.72	7.56	7.40	7.30	7.23	7.14	7.09	7.06	6.97	6.89
18.41	17.99	17.56	17.12	16.85	16.67	16.44	16.31	16.21	15.98	15.77
2.70	2.67	2.63	2.59	2.57	2.56	2.54	2.52	2.51	2.49	2.47
3.64	3.57	3.51	3.44	3.40	3.38	3.34	3.32	3.30	3.27	3.23
4.76	4.67	4.57	4.47	4.40	4.36	4.31	4.28	4.25	4.20	4.15
6.62	6.47	6.31	6.16	6.06	5.99	5.91	5.86	5.82	5.74	5.66
14.08	13.71	13.32	12.93	12.69	12.53	12.33	12.20	12.12	11.91	11.72

(Continued)

T-14 Tables

		lues (cor									
					I	Degrees of fr	reedom in th	e numerato	r		
		p	1	2	3	4	5	6	7	8	9
		.100	3.46	3.11	2.92	2.81	2.73	2.67	2.62	2.59	2.56
		.050	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39
	8	.025	7.57	6.06	5.42	5.05	4.82	4.65	4.53	4.43	4.3
		.010	11.26	8.65	7.59	7.01 14.39	6.63	6.37	6.18	6.03	5.9
		.001	25.41	18.49	15.83	14.39	13.48	12.86	12.40	12.05	11.7
		.100	3.36 5.12	3.01	2.81 3.86	2.69	2.61 3.48	2.55 3.37	2.51	2.47 3.23	2.4
	9	.050		4.26 5.71		3.63 4.72	4.48	4.32	3.29 4.20		3.1 4.0
	9	.025 .010	7.21 10.56	8.02	5.08 6.99	6.42	6.06	5.80	5.61	4.10 5.47	5.3
		.001	22.86	16.39	13.90	12.56	11.71	11.13	10.70	10.37	10.1
		.100	3.29	2.92	2.73	2.61	2.52	2.46	2.41	2.38	2.3
		.050	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.0
	10	.025	6.94	5.46	4.83	4.47	4.24	4.07	3.95	3.85	3.7
		.010	10.04	7.56	6.55	5.99	5.64	5.39	5.20	5.06	4.9
		.001	21.04	14.91	12.55	11.28	10.48	9.93	9.52	9.20	8.9
		.100	3.23	2.86	2.66	2.54	2.45	2.39	2.34	2.30	2.2
		.050	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.9
L.	11	.025	6.72	5.26	4.63	4.28	4.04	3.88	3.76	3.66	3.5
g		.010	9.65	7.21	6.22	5.67	5.32	5.07	4.89	4.74	4.6
ij		.001	19.69	13.81	11.56	10.35	9.58	9.05	8.66	8.35	8.1
iou		.100	3.18	2.81	2.61	2.48	2.39	2.33	2.28	2.24	2.2
ŏ	12	.050	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.8
ğ	12	.025 .010	6.55 9.33	5.10 6.93	4.47 5.95	4.12 5.41	3.89 5.06	3.73 4.82	3.61 4.64	3.51 4.50	3.4 4.3
Ē		.001	18.64	12.97	10.80	9.63	8.89	8.38	8.00	7.71	7.4
Degrees of freedom in the denominator		.100	3.14	2.76	2.56	2.43	2.35	2.28	2.23	2.20	2.1
S		.050	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.7
Ħ	13	.025	6.41	4.97	4.35	4.00	3.77	3.60	3.48	3.39	3.3
0		.010	9.07	6.70	5.74	5.21	4.86	4.62	4.44	4.30	4.1
5 E		.001	17.82	12.31	10.21	9.07	8.35	7.86	7.49	7.21	6.9
Deg		.100	3.10	2.73	2.52	2.39	2.31	2.24	2.19	2.15	2.1
		.050	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.6
	14	.025	6.30	4.86	4.24	3.89	3.66	3.50	3.38	3.29	3.2
		.010 .001	8.86 17.14	6.51 11.78	5.56 9.73	5.04 8.62	4.69 7.92	4.46 7.44	4.28 7.08	4.14	4.0 6.5
		.001	17.14	11./8	9.73	0.02	1.92	7.44	7.08	6.80	0.5
		.100	3.07	2.70	2.49	2.36	2.27	2.21	2.16	2.12	2.0
		.050	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.5
	15	.025	6.20 8.68	4.77 6.36	4.15 5.42	3.80 4.89	3.58 4.56	3.41 4.32	3.29 4.14	3.20 4.00	3.1 3.8
		.010 .001	16.59	11.34	9.34	8.25	7.57	7.09	6.74	6.47	6.2
		.100	3.05	2.67	2.46	2.33	2.24	2.18	2.13	2.09	2.0
	16	.050 .025	4.49 6.12	3.63 4.69	3.24 4.08	3.01 3.73	2.85 3.50	2.74 3.34	2.66 3.22	2.59 3.12	2.5 3.0
	10	.025	8.53	6.23	5.29	4.77	4.44	4.20	4.03	3.12	3.7
		.001	16.12	10.97	9.01	7.94	7.27	6.80	6.46	6.19	5.9
		.100	3.03	2.64	2.44	2.31	2.22	2.15	2.10	2.06	2.0
		.050	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.4
	17	.025	6.04	4.62	4.01	3.66	3.44	3.28	3.16	3.06	2.9
		.010	8.40	6.11	5.19	4.67	4.34	4.10	3.93	3.79	3.6
		.001	15.72	10.66	8.73	7.68	7.02	6.56	6.22	5.96	5.7

Tables T-15

TABLE										
critica	al values (continued)								
			D	egrees of free	dom in the n	umerator				
10	12	15	20	25	30	40	50	60	120	1000
2.54	2.50	2.46	2.42	2.40	2.38	2.36	2.35	2.34	2.32	2.30
3.35	3.28	3.22	3.15	3.11	3.08	3.04	3.02	3.01	2.97	2.93
4.30	4.20	4.10	4.00	3.94	3.89	3.84	3.81	3.78	3.73	3.68
5.81	5.67	5.52	5.36	5.26	5.20	5.12	5.07	5.03	4.95	4.87
11.54	11.19	10.84	10.48	10.26	10.11	9.92	9.80	9.73	9.53	9.36
2.42	2.38	2.34	2.30	2.27	2.25	2.23	2.22	2.21	2.18	2.16
3.14	3.07	3.01	2.94	2.89	2.86	2.83	2.80	2.79	2.75	2.71
3.96	3.87	3.77	3.67	3.60	3.56	3.51	3.47	3.45	3.39	3.34
5.26	5.11	4.96	4.81	4.71	4.65	4.57	4.52	4.48	4.40	4.32
9.89	9.57	9.24	8.90	8.69	8.55	8.37	8.26	8.19	8.00	7.84
2.32	2.28	2.24	2.20	2.17	2.16	2.13	2.12	2.11	2.08	2.06
2.98	2.91	2.85	2.77	2.73	2.70	2.66	2.64	2.62	2.58	2.54
3.72	3.62	3.52	3.42	3.35	3.31	3.26	3.22	3.20	3.14	3.09
4.85	4.71	4.56	4.41	4.31	4.25	4.17	4.12	4.08	4.00	3.92
8.75	8.45	8.13	7.80	7.60	7.47	7.30	7.19	7.12	6.94	6.78
2.25	2.21	2.17	2.12	2.10	2.08	2.05	2.04	2.03	2.00	1.98
2.85	2.79	2.72	2.65	2.60	2.57	2.53	2.51	2.49	2.45	2.41
3.53	3.43	3.33	3.23	3.16	3.12	3.06	3.03	3.00	2.94	2.89
4.54	4.40	4.25	4.10	4.01	3.94	3.86	3.81	3.78	3.69	3.61
7.92	7.63	7.32	7.01	6.81	6.68	6.52	6.42	6.35	6.18	6.02
2.19	2.15	2.10	2.06	2.03	2.01	1.99	1.97	1.96	1.93	1.91
2.75	2.69	2.62	2.54	2.50	2.47	2.43	2.40	2.38	2.34	2.30
3.37	3.28	3.18	3.07	3.01	2.96	2.91	2.87	2.85	2.79	2.73
4.30	4.16	4.01	3.86	3.76	3.70	3.62	3.57	3.54	3.45	3.37
7.29	7.00	6.71	6.40	6.22	6.09	5.93	5.83	5.76	5.59	5.44
2.14	2.10	2.05	2.01	1.98	1.96	1.93	1.92	1.90	1.88	1.85
2.67	2.60	2.53	2.46	2.41	2.38	2.34	2.31	2.30	2.25	2.21
3.25	3.15	3.05	2.95	2.88	2.84	2.78	2.74	2.72	2.66	2.60
4.10	3.96	3.82	3.66	3.57	3.51	3.43	3.38	3.34	3.25	3.18
6.80	6.52	6.23	5.93	5.75	5.63	5.47	5.37	5.30	5.14	4.99
2.10	2.05	2.01	1.96	1.93	1.91	1.89	1.87	1.86	1.83	1.80
2.60	2.53	2.46	2.39	2.34	2.31	2.27	2.24	2.22	2.18	2.14
3.15	3.05	2.95	2.84	2.78	2.73	2.67	2.64	2.61	2.55	2.50
3.94	3.80	3.66	3.51	3.41	3.35	3.27	3.22	3.18	3.09	3.02
6.40	6.13	5.85	5.56	5.38	5.25	5.10	5.00	4.94	4.77	4.62
2.06	2.02	1.97	1.92	1.89	1.87	1.85	1.83	1.82	1.79	1.76
2.54	2.48	2.40	2.33	2.28	2.25	2.20	2.18	2.16	2.11	2.07
3.06	2.96	2.86	2.76	2.69	2.64	2.59	2.55	2.52	2.46	2.40
3.80	3.67	3.52	3.37	3.28	3.21	3.13	3.08	3.05	2.96	2.88
6.08	5.81	5.54	5.25	5.07	4.95	4.80	4.70	4.64	4.47	4.33
2.03	1.99	1.94	1.89	1.86	1.84	1.81	1.79	1.78	1.75	1.72
2.49	2.42	2.35	2.28	2.23	2.19	2.15	2.12	2.11	2.06	2.02
2.99	2.89	2.79	2.68	2.61	2.57	2.51	2.47	2.45	2.38	2.32
3.69	3.55	3.41	3.26	3.16	3.10	3.02	2.97	2.93	2.84	2.76
5.81	5.55	5.27	4.99	4.82	4.70	4.54	4.45	4.39	4.23	4.08
2.00	1.96	1.91	1.86	1.83	1.81	1.78	1.76	1.75	1.72	1.69
2.45	2.38	2.31	2.23	2.18	2.15	2.10	2.08	2.06	2.01	1.97
2.92	2.82	2.72	2.62	2.55	2.50	2.44	2.41	2.38	2.32	2.26
3.59	3.46	3.31	3.16	3.07	3.00	2.92	2.87	2.83	2.75	2.66
5.58	5.32	5.05	4.78			4.33	4.24	4.18	4.02	3.87

(Continued)

T-16 Tables

					De	grees of fre	edom in the	numerator	r		
		p	1	2	3	4	5	6	7	8	9
		.100	3.01	2.62	2.42	2.29	2.20	2.13	2.08	2.04	2.00
	10	.050	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46
	18	.025 .010	5.98 8.29	4.56 6.01	3.95 5.09	3.61 4.58	3.38 4.25	3.22 4.01	3.10 3.84	3.01 3.71	2.93 3.60
		.001	15.38	10.39	8.49	7.46	6.81	6.35	6.02	5.76	5.56
		.100	2.99	2.61	2.40	2.27	2.18	2.11	2.06	2.02	1.98
		.050	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42
	19	.025	5.92	4.51	3.90	3.56	3.33	3.17	3.05	2.96	2.88
		.010 .001	8.18 15.08	5.93 10.16	5.01 8.28	4.50 7.27	4.17 6.62	3.94 6.18	3.77 5.85	3.63 5.59	3.52 5.39
		.100	2.97	2.59	2.38	2.25	2.16	2.09	2.04	2.00	1.96
		.050	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39
	20	.025	5.87	4.46	3.86	3.51	3.29	3.13	3.01	2.91	2.84
		.010	8.10	5.85	4.94	4.43	4.10	3.87	3.70	3.56	3.46
		.001	14.82	9.95	8.10	7.10	6.46	6.02	5.69	5.44	5.24
		.100	2.96	2.57	2.36	2.23	2.14	2.08	2.02	1.98	1.95
	21	.050 .025	4.32 5.83	3.47 4.42	3.07 3.82	2.84 3.48	2.68 3.25	2.57 3.09	2.49 2.97	2.42 2.87	2.37
<u>5</u>	21	.010	8.02	5.78	4.87	4.37	4.04	3.81	3.64	3.51	3.40
ina		.001	14.59	9.77	7.94	6.95	6.32	5.88	5.56	5.31	5.11
nou		.100	2.95	2.56	2.35	2.22	2.13	2.06	2.01	1.97	1.93
8		.050	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34
the	22	.025 .010	5.79 7.95	4.38 5.72	3.78 4.82	3.44 4.31	3.22 3.99	3.05 3.76	2.93 3.59	2.84	2.76
ij		.001	14.38	9.61	7.80	6.81	6.19	5.76	5.44	3.45 5.19	3.35 4.99
Degrees of freedom in the denominator		.100	2.94	2.55	2.34	2.21	2.11	2.05	1.99	1.95	1.92
Je .		.050	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32
Ä	23	.025	5.75	4.35	3.75	3.41	3.18	3.02	2.90	2.81	2.73
ses		.010 .001	7.88 14.20	5.66 9.47	4.76 7.67	4.26 6.70	3.94 6.08	3.71 5.65	3.54 5.33	3.41 5.09	3.30 4.89
)egn		.100	2.93	2.54	2.33	2.19	2.10	2.04	1.98	1.94	1.91
_		.050	4.26	3.40	3.01	2.19	2.62	2.51	2.42	2.36	2.30
	24	.025	5.72	4.32	3.72	3.38	3.15	2.99	2.87	2.78	2.70
		.010	7.82	5.61	4.72	4.22	3.90	3.67	3.50	3.36	3.26
		.001	14.03	9.34	7.55	6.59	5.98	5.55	5.23	4.99	4.80
		.100 .050	2.92 4.24	2.53 3.39	2.32 2.99	2.18 2.76	2.09 2.60	2.02 2.49	1.97 2.40	1.93 2.34	1.89
	25	.025	5.69	4.29	3.69	3.35	3.13	2.49	2.40	2.75	2.68
	20	.010	7.77	5.57	4.68	4.18	3.85	3.63	3.46	3.32	3.22
		.001	13.88	9.22	7.45	6.49	5.89	5.46	5.15	4.91	4.71
		.100	2.91	2.52	2.31	2.17	2.08	2.01	1.96	1.92	1.88
	26	.050 .025	4.23 5.66	3.37 4.27	2.98 3.67	2.74 3.33	2.59 3.10	2.47 2.94	2.39 2.82	2.32 2.73	2.27
	26	.025	7.72	5.53	4.64	4.14	3.10	3.59	3.42	3.29	2.65
		.001	13.74	9.12	7.36	6.41	5.80	5.38	5.07	4.83	4.64
		.100	2.90	2.51	2.30	2.17	2.07	2.00	1.95	1.91	1.87
		.050	4.21	3.35	2.96	2.73	2.57	2.46	2.37	2.31	2.25
	27	.025	5.63	4.24	3.65	3.31	3.08	2.92	2.80	2.71	2.63
		.010 .001	7.68 13.61	5.49 9.02	4.60 7.27	4.11 6.33	3.78 5.73	3.56 5.31	3.39 5.00	3.26 4.76	3.15 4.5

Tables |

TABLE	E									
F critica	al values	(continued)								
				Degrees of f	reedom in th	ne numerato	r			
10	12	15	20	25	30	40	50	60	120	1000
1.98	1.93	1.89	1.84	1.80	1.78	1.75	1.74	1.72	1.69	1.66
2.41	2.34	2.27	2.19	2.14	2.11	2.06	2.04	2.02	1.97	1.92
2.87	2.77	2.67	2.56	2.49	2.44	2.38	2.35	2.32	2.26	2.20
3.51	3.37	3.23	3.08	2.98	2.92	2.84	2.78	2.75	2.66	2.58
5.39	5.13	4.87	4.59	4.42	4.30	4.15	4.06	4.00	3.84	3.69
1.96	1.91	1.86	1.81	1.78	1.76	1.73	1.71	1.70	1.67	1.64
2.38	2.31	2.23	2.16	2.11	2.07	2.03	2.00	1.98	1.93	1.88
2.82	2.72	2.62	2.51	2.44	2.39	2.33	2.30	2.27	2.20	2.14
3.43	3.30	3.15	3.00	2.91	2.84	2.76	2.71	2.67	2.58	2.50
5.22	4.97	4.70	4.43	4.26	4.14	3.99	3.90	3.84	3.68	3.53
1.94	1.89	1.84	1.79	1.76	1.74	1.71	1.69	1.68	1.64	1.61
2.35	2.28	2.20	2.12	2.07	2.04	1.99	1.97	1.95	1.90	1.85
2.77	2.68	2.57	2.46	2.40	2.35	2.29	2.25	2.22	2.16	2.09
3.37	3.23	3.09	2.94	2.84	2.78	2.69	2.64	2.61	2.52	2.43
5.08	4.82	4.56	4.29	4.12	4.00	3.86	3.77	3.70	3.54	3.40
1.92	1.87	1.83	1.78	1.74	1.72	1.69	1.67	1.66	1.62	1.59
2.32	2.25	2.18	2.10	2.05	2.01	1.96	1.94	1.92	1.87	1.82
2.73	2.64	2.53	2.42	2.36	2.31	2.25	2.21	2.18	2.11	2.05
3.31	3.17	3.03	2.88	2.79	2.72	2.64	2.58	2.55	2.46	2.37
4.95	4.70	4.44	4.17	4.00	3.88	3.74	3.64	3.58	3.42	3.28
1.90	1.86	1.81	1.76	1.73	1.70	1.67	1.65	1.64	1.60	1.57
2.30	2.23	2.15	2.07	2.02	1.98	1.94	1.91	1.89	1.84	1.79
2.70	2.60	2.50	2.39	2.32	2.27	2.21	2.17	2.14	2.08	2.01
3.26	3.12	2.98	2.83	2.73	2.67	2.58	2.53	2.50	2.40	2.32
4.83	4.58	4.33	4.06	3.89	3.78	3.63	3.54	3.48	3.32	3.17
1.89	1.84	1.80	1.74	1.71	1.69	1.66	1.64	1.62	1.59	1.55
2.27	2.20	2.13	2.05	2.00	1.96	1.91	1.88	1.86	1.81	1.76
2.67	2.57	2.47	2.36	2.29	2.24	2.18	2.14	2.11	2.04	1.98
3.21	3.07	2.93	2.78	2.69	2.62	2.54	2.48	2.45	2.35	2.27
4.73	4.48	4.23	3.96	3.79	3.68	3.53	3.44	3.38	3.22	3.08
1.88	1.83	1.78	1.73	1.70	1.67	1.64	1.62	1.61	1.57	1.54
2.25	2.18	2.11	2.03	1.97	1.94	1.89	1.86	1.84	1.79	1.74
2.64	2.54	2.44	2.33	2.26	2.21	2.15	2.11	2.08	2.01	1.94
3.17	3.03	2.89	2.74	2.64	2.58	2.49	2.44	2.40	2.31	2.22
4.64	4.39	4.14	3.87	3.71	3.59	3.45	3.36	3.29	3.14	2.99
1.87	1.82	1.77	1.72	1.68	1.66	1.63	1.61	1.59	1.56	1.52
2.24	2.16	2.09	2.01	1.96	1.92	1.87	1.84	1.82	1.77	1.72
2.61	2.51	2.41	2.30	2.23	2.18	2.12	2.08	2.05	1.98	1.91
3.13	2.99	2.85	2.70	2.60	2.54	2.45	2.40	2.36	2.27	2.18
4.56	4.31	4.06	3.79	3.63	3.52	3.37	3.28	3.22	3.06	2.91
1.86	1.81	1.76	1.71	1.67	1.65	1.61	1.59	1.58	1.54	1.51
2.22	2.15	2.07	1.99	1.94	1.90	1.85	1.82	1.80	1.75	1.70
2.59	2.49	2.39	2.28	2.21	2.16	2.09	2.05	2.03	1.95	1.89
3.09	2.96	2.81	2.66	2.57	2.50	2.42	2.36	2.33	2.23	2.14
4.48	4.24	3.99	3.72	3.56	3.44	3.30	3.21	3.15	2.99	2.84
1.85	1.80	1.75	1.70	1.66	1.64	1.60	1.58	1.57	1.53	1.50
2.20	2.13	2.06	1.97	1.92	1.88	1.84	1.81	1.79	1.73	1.68
2.57	2.47	2.36	2.25	2.18	2.13	2.07	2.03	2.00	1.93	1.86
3.06	2.93	2.78	2.63	2.54	2.47	2.38	2.33	2.29	2.20	2.11
4.41	4.17	3.92	3.66	3.49	3.38	3.23	3.14	3.08	2.92	2.78

(Continued)

T-18 Table

	ical valu	es (continu	ued)								
7 (11)	icai vara	es (contin	ueu)		De	egrees of fre	eedom in th	e numerato	r		
		р	1	2	3	4	5	6	7	8	9
		.100	2.89	2.50	2.29	2.16	2.06	2.00	1.94	1.90	1.87
	28	.050 .025	4.20 5.61	3.34 4.22	2.95 3.63	2.71 3.29	2.56 3.06	2.45 2.90	2.36 2.78	2.29 2.69	2.24 2.61
	20	.010	7.64	5.45	4.57	4.07	3.75	3.53	3.36	3.23	3.12
		.001	13.50	8.93	7.19	6.25	5.66	5.24	4.93	4.69	4.50
		.100	2.89	2.50	2.28	2.15	2.06	1.99	1.93	1.89	1.86
	29	.050 .025	4.18 5.59	3.33 4.20	2.93 3.61	2.70 3.27	2.55 3.04	2.43 2.88	2.35 2.76	2.28 2.67	2.22 2.59
	29	.010	7.60	5.42	4.54	4.04	3.73	3.50	3.33	3.20	3.09
		.001	13.39	8.85	7.12	6.19	5.59	5.18	4.87	4.64	4.45
		.100	2.88	2.49	2.28	2.14	2.05	1.98	1.93	1.88	1.85
	20	.050	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21
	30	.025 .010	5.57 7.56	4.18 5.39	3.59 4.51	3.25 4.02	3.03 3.70	2.87 3.47	2.75 3.30	2.65 3.17	2.57 3.07
		.001	13.29	8.77	7.05	6.12	5.53	5.12	4.82	4.58	4.39
		.100	2.84	2.44	2.23	2.09	2.00	1.93	1.87	1.83	1.79
		.050	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12
÷.	40	.025	5.42	4.05	3.46	3.13	2.90	2.74	2.62	2.53	2.45
ato		.010 .001	7.31 12.61	5.18 8.25	4.31 6.59	3.83 5.70	3.51 5.13	3.29 4.73	3.12 4.44	2.99 4.21	2.89 4.02
mir		.001	12.01	0.23	6.39	5.70	5.15	4.73	4.44	4.21	4.02
oue		.100	2.81	2.41	2.20	2.06	1.97	1.90	1.84	1.80	1.76
e d	50	.050 .025	4.03 5.34	3.18 3.97	2.79 3.39	2.56 3.05	2.40 2.83	2.29 2.67	2.20 2.55	2.13 2.46	2.07 2.38
흎	50	.010	7.17	5.06	4.20	3.72	3.41	3.19	3.02	2.89	2.78
ii.		.001	12.22	7.96	6.34	5.46	4.90	4.51	4.22	4.00	3.82
гора		.100	2.79	2.39	2.18	2.04	1.95	1.87	1.82	1.77	1.74
L		.050	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04
of	60	.025 .010	5.29 7.08	3.93 4.98	3.34 4.13	3.01 3.65	2.79 3.34	2.63 3.12	2.51 2.95	2.41 2.82	2.33 2.72
Degrees of freedom in the denominator		.001	11.97	7.77	6.17	5.31	4.76	4.37	4.09	3.86	3.69
Deg		.100	2.76	2.36	2.14	2.00	1.91	1.83	1.78	1.73	1.69
		.050	3.94	3.09	2.70	2.46	2.31	2.19	2.10	2.03	1.97
	100	.025 .010	5.18 6.90	3.83 4.82	3.25 3.98	2.92 3.51	2.70 3.21	2.54 2.99	2.42 2.82	2.32 2.69	2.24 2.59
		.001	11.50	7.41	5.86	5.02	4.48	4.11	3.83	3.61	3.44
		.100	2.73	2.33	2.11	1.97	1.88	1.80	1.75	1.70	1.66
		.050	3.89	3.04	2.65	2.42	2.26	2.14	2.06	1.98	1.93
	200	.025	5.10	3.76	3.18	2.85	2.63	2.47	2.35	2.26	2.18
		.010 .001	6.76 11.15	4.71 7.15	3.88 5.63	3.41 4.81	3.11 4.29	2.89 3.92	2.73 3.65	2.60 3.43	2.50 3.26
		.100 .050	2.71 3.85	2.31 3.00	2.09 2.61	1.95 2.38	1.85 2.22	1.78 2.11	1.72 2.02	1.68 1.95	1.64 1.89
	1000	.025	5.04	3.70	3.13	2.80	2.58	2.42	2.30	2.20	2.13
		.010	6.66	4.63	3.80	3.34	3.04	2.82	2.66	2.53	2.43
		.001	10.89	6.96	5.46	4.65	4.14	3.78	3.51	3.30	3.13

Tables T-19

				Degrees of f	reedom in th	ne numerator	r			
10	12	15	20	25	30	40	50	60	120	1000
1.84	1.79	1.74	1.69	1.65	1.63	1.59	1.57	1.56	1.52	1.48
2.19	2.12	2.04	1.96	1.91	1.87	1.82	1.79	1.77	1.71	1.66
2.55	2.45	2.34	2.23	2.16	2.11	2.05	2.01	1.98	1.91	1.84
3.03	2.90	2.75	2.60	2.51	2.44	2.35	2.30	2.26	2.17	2.08
4.35	4.11	3.86	3.60	3.43	3.32	3.18	3.09	3.02	2.86	2.72
1.83	1.78	1.73	1.68	1.64	1.62	1.58	1.56	1.55	1.51	1.47
2.18	2.10	2.03	1.94	1.89	1.85	1.81	1.77	1.75	1.70	1.65
2.53	2.43	2.32	2.21	2.14	2.09	2.03	1.99	1.96	1.89	1.82
3.00	2.87	2.73	2.57	2.48	2.41	2.33	2.27	2.23	2.14	2.05
4.29	4.05	3.80	3.54	3.38	3.27	3.12	3.03	2.97	2.81	2.66
1.82	1.77	1.72	1.67	1.63	1.61	1.57	1.55	1.54	1.50	1.46
2.16	2.09	2.01	1.93	1.88	1.84	1.79	1.76	1.74	1.68	1.63
2.51	2.41	2.31	2.20	2.12	2.07	2.01	1.97	1.94	1.87	1.80
2.98	2.84	2.70	2.55	2.45	2.39	2.30	2.25	2.21	2.11	2.02
4.24	4.00	3.75	3.49	3.33	3.22	3.07	2.98	2.92	2.76	2.61
1.76	1.71	1.66	1.61	1.57	1.54	1.51	1.48	1.47	1.42	1.38
2.08	2.00	1.92	1.84	1.78	1.74	1.69	1.66	1.64	1.58	1.52
2.39	2.29	2.18	2.07	1.99	1.94	1.88	1.83	1.80	1.72	1.65
2.80	2.66	2.52	2.37	2.27	2.20	2.11	2.06	2.02	1.92	1.82
3.87	3.64	3.40	3.14	2.98	2.87	2.73	2.64	2.57	2.41	2.25
1.73	1.68	1.63	1.57	1.53	1.50	1.46	1.44	1.42	1.38	1.33
2.03	1.95	1.87	1.78	1.73	1.69	1.63	1.60	1.58	1.51	1.45
2.32	2.22	2.11	1.99	1.92	1.87	1.80	1.75	1.72	1.64	1.56
2.70	2.56	2.42	2.27	2.17	2.10	2.01	1.95	1.91	1.80	1.70
3.67	3.44	3.20	2.95	2.79	2.68	2.53	2.44	2.38	2.21	2.05
1.71	1.66	1.60	1.54	1.50	1.48	1.44	1.41	1.40	1.35	1.30
1.99	1.92	1.84	1.75	1.69	1.65	1.59	1.56	1.53	1.47	1.40
2.27	2.17	2.06	1.94	1.87	1.82	1.74	1.70	1.67	1.58	1.49
2.63	2.50	2.35	2.20	2.10	2.03	1.94	1.88	1.84	1.73	1.62
3.54	3.32	3.08	2.83	2.67	2.55	2.41	2.32	2.25	2.08	1.92
1.66	1.61	1.56	1.49	1.45	1.42	1.38	1.35	1.34	1.28	1.22
1.93	1.85	1.77	1.68	1.62	1.57	1.52	1.48	1.45	1.38	1.30
2.18	2.08	1.97	1.85	1.77	1.71	1.64	1.59	1.56	1.46	1.36
2.50	2.37	2.22	2.07	1.97	1.89	1.80	1.74	1.69	1.57	1.45
3.30	3.07	2.84	2.59	2.43	2.32	2.17	2.08	2.01	1.83	1.64
1.63	1.58	1.52	1.46	1.41	1.38	1.34	1.31	1.29	1.23	1.16
1.88	1.80	1.72	1.62	1.56	1.52	1.46	1.41	1.39	1.30	1.21
2.11	2.01	1.90	1.78	1.70	1.64	1.56	1.51	1.47	1.37	1.25
2.41	2.27	2.13	1.97	1.87	1.79	1.69	1.63	1.58	1.45	1.30
3.12	2.90	2.67	2.42	2.26	2.15	2.00	1.90	1.83	1.64	1.43
1.61	1.55	1.49	1.43	1.38	1.35	1.30	1.27	1.25	1.18	1.08
1.84	1.76	1.68	1.58	1.52	1.47	1.41	1.36	1.33	1.24	1.11
2.06	1.96	1.85	1.72	1.64	1.58	1.50	1.45	1.41	1.29	1.13
2.34	2.20	2.06	1.90	1.79	1.72	1.61	1.54	1.50	1.35	1.16
2.99	2.77	2.54	2.30	2.14	2.02	1.87	1.77	1.69	1.49	1.22