

JEE Main/Boards

Exercise 1

Q.1 How many odd numbers less than 1000 can be formed using the digits 0, 1, 4 and 7 if repetition of digits is allowed?

Q.2 In how many ways can five people be seated in a car with two people in the front seat and three in the rear, if two particular persons out of the five cannot drive?

Q.3 A team consisting of 7 boys and 3 girls play singles matches against another team consisting of 5 boys and 5 girls. How many matches can be scheduled between the two teams if a boy plays against a girl and a girl plays against a boy?

Q.4 Prove that $\frac{(2n+1)}{n!} = 2^n[1.3.5...(2n-1)(2n+1)]$

Q.5 If ${}^n P_4 = 360$, find n.

Q.6 Find the number of numbers between 300 and 3000 which can be formed with the digits 0, 1, 2, 3, 4 and 5, with no digit being repeated in any number.

Q.7 How many even numbers are there with three digits such that if 5 is one of the digits in a number then 7 is the next digit in that number?

Q.8 Find the sum of 3 digit numbers formed by digits 1, 2, 3 is

Q.9 A telegraph has 5 arms and each arm is capable of 4 distinct positions, including the position of rest. What is the total number of signals that can be made?

Q.10 In telegraph communication, the Morse code is used in which all the letters of the English alphabet, digits 0 to 9 and even the punctuation marks, all usually referred as characters, are represented by 'dots' and 'dashes'

For example, E is represented by a dot (.), T by a dash (-), O by three dashes (- - -), S by three dots (...) and so on. Thus, SOS is represented by (... - - - ...).

(i) How many characters can be transmitted using one symbol (dot or dash), two symbols, three symbols, four symbols? Also find the total number of characters which can be transmitted using at most four symbols.

(ii) How many characters can be transmitted by using
(a) exactly five symbols? (b) at most five symbols?

Q.11 In how many of the distinct permutation of the letter in MISSISSIPPI do the four I's not come together?

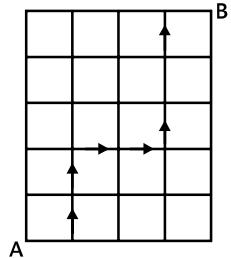
Q.12 In how many ways 4 boys and 3 girls can be seated in a row so that they are alternate?

Q.13 A biologist studying the genetic code is interested to know the number of possible arrangements of 12 molecules in a chain. The chain contains 4 different molecules represented by the initials A (for adenine), C (for Cytosine), G (for Guanine) and T (for Thymine) and 3 molecules of each kind. How many different such arrangements are possible in all?

Q.14 Find the number of rearrangement of the letters of the word 'BENEVOLENT'. How many of them end in L?

Q.15 How many words can be formed with the letters of the word PATALIPUTRA without changing the relative order of the vowels and consonants?

Q.16 A person is to walk from A to B. However, he is restricted to walk only to the right of A or upwards of A, but not necessarily in this order. One such path is shown in the given figure. Determine the total number of paths available to the person from A to B.



Q.17 In how many ways can three jobs I, II and III be assigned to three persons A, B and C, if one person is assigned only one job and all are capable of doing each job? Which assignment of jobs will take the least time to complete the jobs, if time taken (in hours) by an individual on each job as follows?

| Job persons | I | II | III |
|-------------|----------------|----------------|-----|
| A | 5 | 4 | 4 |
| B | $4\frac{1}{4}$ | $3\frac{1}{2}$ | 4 |
| C | 5 | 3 | 5 |

Q.18 If ${}^{15}C_{3r} = {}^{15}C_{r+3}$, find r.

Q.19 Prove that ${}^nC_r \times {}^rC_s = {}^nC_s \times {}^{n-s}C_{r-s}$.

Q.20 Find the value of the expression

$${}^{47}C_4 + \sum_{j=1}^5 {}^{52-j}C_3 .$$

Q.21 Prove that the product of r consecutive integers is divisible by $r!$.

Q.22 From a class of 25 students, 10 are to be chosen for a field trip. There are 3 students who decide that either all of them will join or none of them will join. In how many ways can the field trip members be chosen?

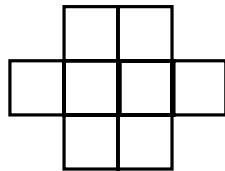
Q.23 There are ten points in a plane. Of these ten points, four points are in a straight line and with the exception of these four points, no three points are in the same straight line. Find-

- (i) The number of triangles formed.
- (ii) The number of straight lines formed
- (iii) The number of quadrilaterals formed, by joining these ten points.

Q.24 In an examination a minimum of 5 is to be secured in each of 5 subjects for a pass. In how many ways can a student fail?

Q.25 In how many ways 50 different objects can be divided in 5 sets three of them having 12 objects each and two of them having 7 objects each.

Q.26 Six "X"s (crosses) have to be placed in the squares of the figure given below, such that each row contains at least one X. In how many different ways can this be done?



Q.27 Five balls of different colors are to be placed in three boxes of different sizes. Each box can hold all five balls. In how many different ways can we place the balls so that no box remains empty?

Q.28 How many different words of 4 letters can be formed with the letters of the word "EXAMINATION"?

Exercise 2

Single Correct Choice Type

Q.1 If the letters of the word "VARUN" are written in all possible ways and then are arranged as in a dictionary, then rank of the word VARUN is:

- (A) 98 (B) 99 (C) 100 (D) 101

Q.2 Number of natural numbers between 100 and 1000 such that at least one of their digits is 7, is

- (A) 225 (B) 243 (C) 252 (D) none

Q.3 The 120 permutations of MAHES are arranged in dictionary order, as if each were an ordinary five-letter word. The last letter of the 86th word in the list is

- (A) A (B) H (C) S (D) E

Q.4 A new flag is to be designed with six vertical strips using some or all of the colors yellow green, blue and red. Then the number of ways this can be done such that no two adjacent strips have the same color is

- (A) 12×81 (B) 16×192 (C) 20×125 (D) 24×216

Q.5 The number of 10-digit numbers such that the product of any two consecutive digits in the number is a prime number, is

- (A) 1024 (B) 2048 (C) 512 (D) 64

Q.6 Consider the five points comprising of the vertices of a square and the intersection point of its diagonals. How many triangles can be formed using these points?

- (A) 4 (B) 6 (C) 8 (D) 10

Q.7 How many of the 900 three digit numbers have at least one even digit?

- (A) 775 (B) 875 (C) 100 (D) 101

Q.8 A 5 digit number divisible by 3 is to be formed using the numbers 0, 1, 2, 3, 4 & 5 without repetition. The total number of ways in which this can be done is:

- (A) 3125 (B) 600 (C) 240 (D) 216

Q.9 The number of different seven digit numbers that can be written using only three digits 1, 2 & 3 under the condition that the digit 2 occurs exactly twice in each number is

- (A) 672 (B) 640 (C) 512 (D) none

Q.10 Out of seven consonants and four vowels, the number of words of six letters, formed by taking four consonants and two vowels is (Assume that each ordered group of letter is a word):

- (A) 210 (B) 462 (C) 151200 (D) 332640

Q.11 All possible three digits even numbers which can be formed with the condition that if 5 is one of the digit, then 7 is the next digit is:

- (A) 5 (B) 325 (C) 345 (D) 365

Q.12 Number of 5 digit numbers which are divisible by 5 and each number containing the digit 5, digits being all different is equal to $k(4!)$, the value of k is

- (A) 84 (B) 168 (C) 188 (D) 208

Q.13 The number of six digit numbers that can be formed from the digits 1, 2, 3, 4, 5, 6, & 7 so that digits do not repeat and the terminal digit are even is:

- (A) 144 (B) 72 (C) 288 (D) 720

Q.14 The number of natural numbers from 1000 to 9999 (both inclusive) that do not have all 4 different digits is

- (A) 4048 (B) 4464 (C) 4518 (D) 4536

Q.15 Number of positive integers which have no two digits having the same value with sum of their digits being 45, is

- (A) 10! (B) 9! (C) 9.9! (D) 17.8!

Q.16 Number of 3 digit number in which the digit at hundredth's place is greater than the other two digit is

- (A) 285 (B) 281 (C) 240 (D) 204

Q.17 Number of permutation of 1, 2, 3, 4, 5, 6, 7, 8 and 9 taken all at a time, such that the digit 1 appearing somewhere to the left of 2, 3 appearing to somewhere the left of 4 and 5 somewhere to the left of 6, is (e.g. 815723946 would be one such permutation)

- (A) 9.7! (B) 8! (C) 5!.4! (D) 8!.4!

Q.18 Number of odd integers between 1000 and 8000 which have none of their digit repeated, is

- (A) 1014 (B) 810 (C) 690 (D) 1736

Q.19 The number of ways in which 5 different books can be distributed among 10 people if each person can get at most one book is:

- (A) 252 (B) 10^5 (C) 5^{10} (D) ${}^{10}C_5 \cdot 5!$

Q.20 A students have to answer 10 out of 13 questions in an examination. The number of ways in which he can answer if he must answer at least 3 of the first five questions is

- (A) 276 (B) 267 (C) 80 (D) 1200

Q.21 The number of three digit numbers having only two consecutive digits identical is:

- (A) 153 (B) 162 (C) 180 (D) 161

Q.22 The interior angles of a regular polygon measure 150° each. The number of diagonals of the polygon is

- (A) 35 (B) 44 (C) 54 (D) 78

Q.23 The number of n digit numbers which consists of the digits 1 & 2 only if each digit is to be used at least once, is equal to 510 then n is equal to:

- (A) 7 (B) 8 (C) 9 (D) 10

Q.24 Number of four digit numbers with all digits different and containing the digit 7 is

- (A) 2016 (B) 1828 (C) 1848 (D) 1884

Q.25 An English school and a Vernacular school are both under one superintendent. Suppose that the superintendentship, the four teachership of English and Vernacular school each, are vacant, if there be altogether 11 candidates for the appointments, 3 of whom apply exclusively for the superintendentship and 2 exclusively for the appointment in the English school, the number of ways in which the different appointment can be disposed of is :

- (A) 4320 (B) 268 (C) 1080 (D) 25920

Q.26 A committee of 5 is to be chosen from a group of 9 people. Number of ways in which it can be formed if two particular persons either serve together or not at all and two other particular persons refuse to serve with each other, is

- (A) 41 (B) 36 (C) 47 (D) 76

Q.27 A question paper on mathematics consists of twelve questions divided into three parts A, B and C, each containing four questions, in how many ways can an examinee answer five questions, selecting at least one from each part?

- (A) 624 (B) 208 (C) 1248 (D) 2304

Q.28 Number of ways in which 7 green bottles and 8 blue bottles can be arranged in a row if exactly 1 pair of green bottles is side by side, is (Assume all bottles to be alike except for the color).

- (A) 84 (B) 360 (C) 504 (D) None

Q.29 The kindergarten teacher has 25 kids in her class. She takes 5 of them at a time, to zoological garden as often as she can, without taking the same 5 kids more than once. Then the number of visits, the teacher makes to the garden exceeds that of a kid by:

- (A) ${}^{25}C_5 - {}^{24}C_5$ (B) ${}^{24}C_5$ (C) ${}^{24}C_4$ (D) None

Q.30 A rack has 5 different pairs of shoes. The number of ways in which 4 shoes can be chosen from it so that there will be no complete pair is:

- (A) 1920 (B) 200 (C) 110 (D) 80

Q.31 Number of ways in which 9 different toys can be distributed among 4 children belonging to different age groups in such a way that distribution among the 3 elder children is even and the youngest one is to receive one toy more, is:

- (A) $\frac{(5!)^2}{8}$ (B) $\frac{9!}{2}$ (C) $\frac{9!}{3!(2!)^3}$ (D) None

Q.32 There are 10 red balls of different shades & 9 green balls of identical shades. Then the number of such arrangements such that no two green balls are together in the row is:

- (A) $(10!).{}^{11}P_9$ (B) $(10!).{}^{11}C_9$ (C) $10!$ (D) $10! \cdot 9!$

Q.33 A shelf contains 20 different books of which 4 are in single volume and the others form sets of 8, 5 and 3 volumes respectively. Number of ways in which the books may be arranged on the shelf, if the volumes of each set are together and in their due order is

- (A) $\frac{20!}{8!5!3!}$ (B) 7! (C) 8! (D) $7.8!$

Q.34 Number of ways in which 3 men and their wives can be arranged in a line such that none of the 3 men stand in a position that is ahead of his wife, is

- (A) $3!.3!$ (B) $2.3!.3!$ (C) $3!$ (D) $\frac{6!}{2!.2!.2!}$

Q.35 The number of different ways in which five 'dashes' and eight 'dots' can be arranged, using only seven of these 13 'dashes' & 'dots' is

- (A) 1287 (B) 119 (C) 120 (D) 1235520

Q.36 Number of different words that can be formed using all the letters of the word "DEEPMALA" if two vowels are together and the other two are also together but separated from the first two is

- (A) 960 (B) 1200 (C) 2160 (D) 1440

Q.37 In a unique hockey series between India & Pakistan, they decide to play on till a team wins 5 matches. The number of ways in which the series can be won by India, if no match ends in a draw is:

- (A) 126 (B) 252 (C) 225 (D) None

Q.38 Sameer has to make a telephone call to his friend Harish, Unfortunately he does not remember the 7 digit phone number. But he remembers that the first three digits are 635 or 674, the number is odd and there is exactly one 9 in the number. The maximum number of trials that Sameer has to make to be successful is

- (A) 10,000 (B) 3402 (C) 3200 (D) 5000

Q.39 There are 12 guests at a dinner party. Supposing that the master and mistress of the house have fixed seats opposite one another, and that there are two specified guests who must always, be placed next to one another; the number of ways in which the company can be placed is :

- (A) $20 \cdot 10!$ (B) $22 \cdot 10!$ (C) $44 \cdot 10!$ (D) None

Q.40 In a conference 10 speakers are present. If S_1 wants to speak before S_2 and S_2 wants to speak after S_3 , then the number of ways all the 10 speakers can give their speeches with the above restriction if the remaining seven speakers have no objection to speak at any number is

- (A) ${}^{10}C_3$ (B) ${}^{10}P_8$ (C) ${}^{10}P_3$ (D) $\frac{10!}{3}$

Q.41 The number of all possible selection of one or more questions from 10 given questions, each question having an alternative is:

- (A) 3^{10} (B) $2^{10} - 1$ (C) $3^{10} - 1$ (D) 2^{10}

Q.42 Number of 7 digit numbers the sum of whose digits is 61 is:

- (A) 12 (B) 24 (C) 28 (D) None

Q.43 There are 2 identical white balls, 3 identical red balls and 4 green balls of different shades. The number of ways in which they can be arranged in a row so that at least one ball is separated from the balls of the same color, is:

- (A) $6(7! - 4!)$ (B) $7(6! - 4!)$ (C) $8! - 5!$ (D) None

- Q.44** Product of all the even divisors of $N = 1000$, is
 (A) $32 \cdot 10^2$ (B) $64 \cdot 2^{14}$ (C) $64 \cdot 10^{18}$ (D) $128 \cdot 10^6$

Q.45 A lift with 7 people stops at 10 floors. People varying from zero to seven go out at each floor. The number of ways in which the lift can get emptied, assuming each way only differs by the number of people leaving at each floor, is

- (A) ${}^{16}C_6$ (B) ${}^{17}C_7$ (C) ${}^{16}C_7$ (D) None

Q.46 You are given an unlimited supply of each of the digits 1, 2, 3 or 4. Using only these four digits, you construct n digit numbers. Such n digit numbers will be called LEGITIMATE if it contains the digit 1 either an even number times or not at all. Number of n digit legitimate numbers are

- (A) $2^n + 1$ (B) $2^{n+1} + 2$ (C) $2^{n+2} + 4$ (D) $2^{n-1}(2^n + 1)$

Q.47 Distinct 3 digit numbers are formed using only the digits 1, 2, 3 and 4 with each digit used at most once in each number thus formed. The sum of all possible numbers so formed is

- (A) 6660 (B) 3330 (C) 2220 (D) None

Q.48 An ice cream parlor has ice creams in eight different varieties. Number of ways of choosing 3 ice creams taking at least two ice creams of the same variety, is (Assume that ice creams of the same variety to be identical & available in unlimited supply)

- (A) 56 (B) 64 (C) 100 (D) None

Q.49 There are 12 books on Algebra and Calculus in our library, the books of the same subject being different. If the number of selection each of which consists of 3 books on each topic is greatest then the number of books of Algebra and Calculus in the library are respectively:

- (A) 3 and 9 (B) 4 and 8 (C) 5 and 7 (D) 6 and 6

Q.50 A person writes letters to his 5 friends and addresses the corresponding envelopes. Number of ways in which the letters can be placed in the envelope, so that at least two of them are in the wrong envelopes, is,

- (A) 1 (B) 2 (C) 118 (D) 119

Q.51 For a game in which two partners oppose two other partners, 8 men are available. If every possible pair must play with every other pair, the number of games played is

- (A) ${}^8C_2 \cdot {}^6C_2$ (B) $8C2 \cdot {}^6C_2 \cdot 2$ (C) ${}^8C_4 \cdot 3$ (D) None

Q.52 The number 916238457 is an example of nine digit number which contains each of the digit 1 to 9 exactly once. It also has the property that the digits 1 to 5 occur in their natural order, while the digits 1 to 6 do not. Number of such numbers are

- (A) 2268 (B) 2520 (C) 2975 (D) 1560

Q.53 Number of functions defined from $f : \{1, 2, 3, 4, 5, 6\} \rightarrow \{7, 8, 9, 10\}$ such that the sum $f(1) + f(2) + f(3) + f(4) + f(5) + f(6)$ is odd, is

- (A) 2^{10} (B) 2^{11} (C) 2^{12} (D) $2^{12} - 1$

Multiple Correct Choice Type

Q.54 The continued product, $2 \cdot 6 \cdot 10 \cdot 14 \dots$ to n factors is equal to:

- (A) ${}^{2n}C_n$ (B) ${}^{2n}P_n$

- (C) ${}^{2n+1}C_n$ (D) None

Q.55 The maximum number of permutations of $2n$ letters in which there are only a's & b's, taken all at a time is given by :

- (A) ${}^{2n}C_n$

$$(B) \frac{2}{1} \cdot \frac{6}{2} \cdot \frac{10}{3} \cdots \frac{4n-6}{n-1} \cdot \frac{4n-2}{n}$$

$$(C) \frac{n+1}{1} \cdot \frac{n+2}{2} \cdot \frac{n+3}{3} \cdot \frac{n+4}{4} \cdots \frac{2n-1}{n-1} \cdot \frac{2n}{n}$$

$$(D) \frac{2^n [1 \cdot 3 \cdot 5 \cdots (2n-3)(2n-1)]}{n!}$$

- (E) All of the above

Q.56 Number of ways in which 3 numbers in A.P. can be selected from 1, 2, 3, ..., n is :

$$(A) \left(\frac{n-1}{2} \right)^2 \text{ if } n \text{ is even} \quad (B) \frac{n(n-2)}{4} \text{ if } n \text{ is odd}$$

$$(C) \frac{(n-1)}{4} \text{ if } n \text{ is odd} \quad (D) \frac{n(n-2)}{4} \text{ if } n \text{ is even}$$

Previous Years' Questions

Q.1 The value of the expression ${}^{47}C_4 + \sum_{j=1}^5 {}^{52-j}C_3$ is equal to (1982)

- (A) ${}^{47}C_5$ (B) ${}^{52}C_5$

- (C) ${}^{52}C_4$ (D) None of these

Q.2 Eight chairs are numbered 1 to 8. Two women and three men wish to occupy one chair each. First the women choose the chairs from amongst the chairs marked 1 to 4, and then the men select the chairs from amongst the remaining. The number of possible arrangements is **(1982)**

- (A) ${}^6C_3 \times {}^4C_2$ (B) ${}^4P_2 \times {}^4P_3$
 (C) ${}^4C_2 + {}^4P_3$ (D) None

Q.3 A five digits number divisible by 3 is to be formed using the numbers 0, 1, 2, 3, 4 and 5, without repetition. The total number of ways this can be done, is **(1989)**

- (A) 216 (B) 240 (C) 600 (D) 3125

Q.4 Number of divisors of the form $(4n + 2)$, $n \geq 0$ of integer 240 is **(1998)**

- (A) 4 (B) 8 (C) 10 (D) 3

Q.5 If r, s, t are prime numbers and p, q are the positive integers such that LCM of p, q is $r^2s^4t^2$, then the number of ordered pairs (p, q) is **(2006)**

- (A) 252 (B) 254 (C) 225 (D) 224

Q.6 The letters of the word COCHIN are permuted and all the permutations are arranged in an alphabetical order as in an English dictionary. The number of words that appear before the word COCHIN is **(2007)**

- (A) 360 (B) 192 (C) 96 (D) 48

Q.7 The number of seven digit integers, with sum of the digits equal to 10 and formed by using the digits 1, 2 and 3 only, is **(2009)**

- (A) 55 (B) 66 (C) 77 (D) 88

JEE Advanced/Boards

Exercise 1

Q.1 Consider all the six digit numbers that can be formed using the digits 1, 2, 3, 4, 5 and 6, each digit being used exactly once. Each of such six digit numbers have the property that for each digit, not more than two digits, smaller than that digit, appear to the right of that digit. Find the number of such six digit numbers having the desired property

Q.2 Find the number of five digit number that can be formed using the digits 1, 2, 3, 4, 5, 5, 7, 9 in which one digit appears once and two digits appear twice (e.g. 41174 is one such number but 75355 is not.)

Q.3 Find the number of ways in which 3 distinct numbers can be selected from the set $\{3^1, 3^2, 3^3, \dots, 3^{100}, 3^{101}\}$ so that they form a G.P.

Q.4 Find the number of odd numbers between 3000 to 6300 that have all different digits.

Q.5 A man has 3 friends. In how many ways he can invite one friend every day for dinner on 6 successive nights so that no friend is invited more than 3 times.

Q.6 In an election for the managing committee of a reputed club, the number of candidates contesting elections exceeds the number of members to be elected by r ($r > 0$). If a voter can vote in 967 different ways to elect managing committee by voting at least 1 of them & can vote in 55 different ways to elect $(r - 1)$ candidates by voting in the same manner. Find the number of candidates contesting the election & the number of candidates losing the elections.

Paragraph for question nos. 7 to 9:

2 American men; 2 British men; 2 Chinese men and one each of Dutch, Egyptian, French and German persons are to be seated for a round table conference.

Q.7 If the number of ways in which they can be seated if exactly two pairs of persons of same nationality are together is $p(6!)$, then find p .

Q.8 If the number of ways in which only American pair is adjacent is equal to $q(6!)$, then find q .

Q.9 If the number of ways in which no two people of the same nationality are together given by $r(6!)$, find r .

Q.10 For each positive integer k , let S_k denote the increasing arithmetic sequence of integers whose first term is 1 and whose common difference is k . For example, S_3 is the sequence 1, 4, 7, 10 Find the number of values of k for which S_k contain the term 36!

Q.11 A shop sells 6 different flavors of ice-cream. In how many ways can a customer choose 4 ice-cream cones if

- (i) They are all of different flavors
- (ii) They are not necessarily of different flavors
- (iii) They contain only 3 different flavors
- (iv) They contain only 2 or 3 different flavors?

Q.12 (a) How many divisors are there of the number 21600. Find also the sum of these divisors.

(b) In how many ways the number 7056 can be resolved as a product of 2 factors.

(c) Find the number of ways in which the number 300300 can be split into 2 factors which are relatively prime.

(d) Find the number of positive integers that are divisors of at least one of the number 10^{10} ; 15^7 ; 18^{11} .

Q.13 How many 15 letter arrangement of 5A's, 5B's and 5C's have no A's in the first 5 letters, no B's in the next 5 letters, and to C's in the last 5 letters.

Q.14 Determine the number of paths from the origin to the point (9, 0) in the Cartesian plane which never pass through (5, 5) in paths consisting only of steps going 1 unit North and 1 unit East.

Q.15 There are n triangles of positive area that have one vertex $A(0, 0)$ and the other two vertices whose coordinates are drawn independently with replacement from the set {0, 1, 2, 3, 4} e.g. (1, 2), (0, 1) (2, 2) etc. Find the value of n .

Q.16 How many different ways can 15 Candy bars be distributed between Ram, Shyam, Ghanshyam and Balram, if Ram cannot have more than 5 candy bars and Shyam must have at least two. Assume all Candy bars to be alike

Q.17 Find the number of three digits number from 100 to 999 inclusive which have any one digit that is the average of the other two.

Q.18 (a) Find the number of non-empty subsets S of {1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12} such that if, S contains k elements, then S contains no number less than k .

(b) If the number of ordered pairs (S, T) of subsets of {1, 2, 3, 4, 5, 6} are such that $S \cup T$ contains exactly three elements 10λ , then find the value of λ .

Q.19 Find the number of permutation of the digits 1, 2, 3, 4 and 5 taken all at a time so that the sum of the digits at the first two places is smaller than the sum of the digit at the last two places.

Q.20 In a league of 8 teams, each team played every other team 10 times. The number of wins of the 8 teams formed an arithmetic sequence. Find the least possible number of games won by the champion.

Q.21 Find the sum of all numbers greater than 10000 formed by using the digits 0, 1, 2, 4, 5 no. digit being repeated in any number.

Q.22 There are 3 cars of different make available to transport 3 girls and 5 boys on a field trip. Each car can hold up to 3 children. Find

(a) the number of ways in which they can be accommodated.

(b) the numbers of ways in which they can be accommodated if 2 or 3 girls are assigned to one of the cars.

In both the cases internal arrangement of children inside the car is considered to be immaterial.

Q.23 Find the number of three elements sets of positive integers $\{a, b, c\}$ such that $a \times b \times c = 2310$.

Q.24 Find the number of integer between 1 and 10000 with a least one 8 nd at least one 9 as digits

Q.25 Let N be the number of ordered pairs of non-empty sets A and B that have the following properties:

(a) $A \cup B = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$

(b) $A \cap B = \emptyset$

(c) The number of elements of A is not the element of B .

(d) The number of elements of B is not an element of A .

Find N .

Q.26 In how many other ways can be letters of the word MULTIPLE be arranged:

(i) Without changing the order of the vowels

(ii) Keeping the position of each vowel fixed and without changing the relative order/position or vowels & consonants.

Q.27 Let N denotes the number of all 9 digits numbers if

(a) The digit of each number are all from the set {5, 6, 7, 8, 9} and

(b) Any digit that appears in the number, repeats at least three times. Find the value of N/5.

Q.28 How many integers between 1000 and 9999 have exactly one pair of equal digit such as 4049 or 9902 but not 4449 or 4040?

Q.29 How many 6 digits odd numbers greater than 60,000 can be formed from the digits 5, 6, 7, 8, 9, 0 if

(i) Repetitions are not allowed

(ii) Repetitions are allowed.

Exercise 2

Single Correct Choice Type

Q.1 An eight digit number divisible by 9 is to be formed by using 8 digits out of the digits 0, 1, 2, 3, 4, 5, 6, 7 8, 9 without replacement. The number of ways in which this can be done is

- (A) 9! (B) 2(7!) (C) 4(7!) (D) (36) (7!)

Q.2 Number of 4 digit numbers of the form N = abcd which satisfy following three conditions

(i) $4000 \leq N < 6000$

(ii) N is a multiple of 5

(iii) $3 \leq b < c \leq 6$ is equal to

- (A) 12 (B) 18 (C) 24 (D) 48

Q.3 5 Indian & 5 American couples meet at a party and shake hands. If no wife shakes hands with her own husband and no Indian wife shakes hands with a male then the number of handshakes that takes place in the party is

- (A) 95 (B) 110 (C) 135 (D) 150

Q.4 The 9 horizontal and 9 vertical lines on an 8×8 chessboard form 'r' rectangles and 's' squares, The ratio s/r in its lowest terms is

- (A) $\frac{1}{6}$ (B) $\frac{17}{108}$ (C) $\frac{4}{27}$ (D) None

Q.5 Number of different natural numbers which are smaller than two hundred million and use only the digits 1 or 2 is

- (A) (3) . $2^8 - 2$ (B) (3) . $2^8 - 1$
 (C) 2 ($2^9 - 1$) (D) None

Q.6 There are counters available in x different colors. The counters are all alike except for the color. The total number of arrangements consisting of y counters, assuming sufficient number of counters of each color, if no arrangement consists of all counters of the same color is:

- (A) $x^y - x$ (B) $x^y - y$ (C) $y^x - x$ (D) $y^x - y$

Q.7 If m denotes the number of 5 digit numbers of each successive digits are in their descending order magnitude and n is the corresponding figure, when the digits are in their ascending order of magnitude then $(m - n)$ has the value

- (A) ${}^{10}C_4$ (B) 9C_5 (C) ${}^{10}C_3$ (D) 9C_3

Q.8 There are m points on straight line AB & n points on the line AC none of them being the point A. Triangles are formed with these points as vertices, when

(i) A is excluded

(ii) A is included. The ration of number of triangles in the two cases is:

- (A) $\frac{m+n-2}{m+n}$ (B) $\frac{m+n-2}{m+n-1}$
 (C) $\frac{m+n-2}{m+n+2}$ (D) $\frac{n(n-1)}{(m+1)(n+1)}$

Q.9 The number of 5 digit numbers such that the sum of their digits is even is

- (A) 50000 (B) 45000 (C) 60000 (D) None

Q.10 Number of ways in which 8 people can be arranged in a line if A and B must be next each other and C must be somewhere behind D, is equal to

- (A) 10080 (B) 5040 (C) 5050 (D) 10100

Q.11 Seven different coins are to be divided amongst three persons. If no two of the persons receive the same number of coins but each receives at least one coin & none is left over, then the number of ways in which the division may be made is

- (A) 420 (B) 630 (C) 710 (D) None

Q.12 Let there be 9 fixed points on the circumference of a circle. Each of these points is joined to every one of the remaining 8 points by a straight line and the points are so positioned on the circumference that at most 2 straight lines meet in any interior point of the circle. The number of such interior intersection points is:

- (A) 126 (B) 351 (C) 756 (D) None

Q.13 The number of ways in which 8 distinguishable apples can be distributed among 3 boys such that every boy should get at least 1 apple & at most 4 apples is $K \cdot {}^7P_3$ where K has the value equal to

- (A) 14 (B) 66 (C) 44 (D) 22

Q.14 There are five different peaches and three different apples. Number of ways they can be divided into two packs of four fruits if each pack must contain at least one apple, is

- (A) 95 (B) 65 (C) 60 (D) 30

Q.15 Let P_n denote the number of ways in which three people can be selected out of 'n' people sitting in a row, if no two of them are consecutive. If $P_{n+1} - P_n = 15$ then the value of 'n' is

- (A) 7 (B) 8 (C) 9 (D) 10

Q.16 The number of positive integers not greater than 100, which are not divisible by 2, 3 or 5 is

- (A) 26 (B) 18 (C) 31 (D) None

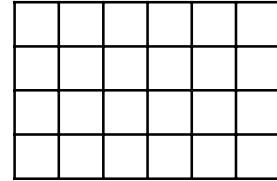
Q.17 There are six periods in each working day of a school. Number of ways in which 5 subjects can be arranged if each subject is allotted at least one period and no period remains vacant is

- (A) 210 (B) 1800 (C) 360 (D) 3600

Q.18 An old man while dialing a 7 digit telephone number remembers that the first four digits consists of one 1's, one 2's and two 3's. He also remembers that the fifth digit is either a 4 or 5 while has no memorizing of the sixth digit, he remembers that the seventh digit is 9 minus the sixth digit. Maximum number of distinct trials he has to try to make sure that he dials the correct telephone number, is

- (A) 360 (B) 240 (C) 216 (D) None

Q.19 Number of rectangles in the grid shown which are not squares is



- (A) 160 (B) 162 (C) 170 (D) 185

Q.20 All the five digit numbers in which each successive digit exceeds its predecessor are arranged in the increasing order of their magnitude. The 97th number in the list does not contains the digit

- (A) 4 (B) 5 (C) 7 (D) 8

Q.21 There are n identical red balls & m identical green balls. The number of different linear arrangements consisting of n red ball but not necessarily all the green balls' is ${}^x C_y$ then

- (A) $x = m + n, y = m$
 (B) $x = m + n + 1, y = ,m$
 (C) $x = m + n + 1, y = m + 1$
 (D) $x = m + n, y = n$

Q.22 A gentleman invites a party of $m + n$ ($m \neq n$) friends to a dinner & places m at one table T_1 and n at another table T_2 , the table being round, if not all people shall have the same neighbor in any two arrangement, then the number of ways in which he can arrange the guests, is

- (A) $\frac{(m+n)!}{4mn}$ (B) $\frac{1}{2} \frac{(m+n)!}{mn}$
 (C) $2 \frac{(m+n)!}{mn}$ (D) None

Q.23 Consider a determinant of order 3 all whose entries are either 0 or 1. Five of these entries are 1 and four of them are '0'. Also $a_{ij} = a_{ji} \forall 1 \leq i, j \leq 3$. The number of such determinants, is equal to

- (A) 6 (B) 8 (C) 9 (D) 12

Q.24 A team of 8 students goes on an excursion, in two cars, of which one can seat 5 and the other only 4. If internal arrangement inside the car does not matter then the number of ways in which they can travel, is

- (A) 91 (B) 182 (C) 126 (D) 3920

Q.25 One hundred management students who read at least one of the three business magazines are surveyed to study the readership pattern. It is found that 80 read Business India, 50 read Business world, and 30 read Business Today. Five students read all the three magazines. How many read exactly two magazines?

- (A) 50 (B) 10 (C) 95 (D) 45

Q.26 Six people are going to sit in a row on a bench. A and B are adjacent, C does not want to sit adjacent to D. E and F can sit anywhere. Number of ways in which these six people can be seated, is

- (A) 200 (B) 144 (C) 120 (D) 56

Q.27 Number of cyphers at the end of ${}^{2002}C_{1001}$ is

- (A) 0 (B) 1 (C) 2 (D) 200

Q.28 Three vertices of a convex n sided polygon are selected. If the number of triangles that can be constructed such that none of the sides of the triangle is also the side of the polygon is 30, then the polygon is a

- | | |
|--------------|-------------|
| (A) Heptagon | (B) Octagon |
| (C) Nonagon | (D) Decagon |

Q.29 Given 11 points, of which 5 lie on one circle, other than these 5, no 4 lie on one circle. Then the maximum number of circles that can be drawn so that each contains at least three of the given points is:

- (A) 216 (B) 156 (C) 172 (D) None

Q.30 Number of 5 digit numbers divisible by 25 that can be formed using only the digits 1, 2, 3, 4, 5, & 0 taken five at a time is

- (A) 2 (B) 32 (C) 42 (D) 52

Q.31 Let P_n denotes the number of ways of selecting 3 people out of 'n' sitting in a row, if no two of them are consecutive and Q_n is the corresponding figure when they are in a circle. If $P_n - Q_n = 6$, then 'n' is equal to

- (A) 8 (B) 9 (C) 10 (D) 12

Q.32 Let m denote the number of ways in which 4 different books are distributed among 10 persons, each receiving none or one only and let n denote the number of ways of distribution if the books are all alike. Then:

- (A) $m = 4n$ (B) $n = 4m$ (C) $m = 24n$ (D) none

Q.33 The number of ways of choosing a committee of 2 women & 6 men, if Mr. A refuses to serve on the committee if Mr. B is a member & Mr. B can only serve, if Miss C is the member of the committee, is

- (A) 60 (B) 84 (C) 124 (D) None

Q.34 Six person A, B, C, D, E and F are to be seated at a circular table. The number of ways this can be done if A must have either B or C on his right and B must have either C or D on his right is:

- (A) 36 (B) 12 (C) 24 (D) 18

Q.35 There are 100 different books in a shelf. Number of ways in which 3 books can be selected so that no two of which are adjacent is

- (A) ${}^{100}C_3 - 98$ (B) ${}^{97}C_3$ (C) ${}^{96}C_3$ (D) ${}^{98}C_3$

Q.36 Number of ways in which four different toys and five indistinguishable marbles can be distributed between Amar, Akbar and Anthony, if each child receives at least one toy and one marble, is

- (A) 42 (B) 100 (C) 150 (D) 216

Q.37 A 3 digit palindrome is a 3 digit number (not starting with zero) which reads the same backwards as forwards. For example 171. The sum of all even 3 digit palindromes, is

- (A) 22380 (B) 25700 (C) 22000 (D) 22400

Q.38 Two classrooms A and B having capacity of 25 and $(n-25)$ seats respectively A_n denotes the number of possible seating arrangements of room 'A', when 'n' students are to be seated in these rooms, starting from room 'A' which is to be filled up full to its capacity. If $A_n - A_{n-1} = 25! \cdot ({}^{49}C_{25})$ then 'n' equals

- (A) 50 (B) 48 (C) 49 (D) 51

Q.39 Number of positive integral solution satisfying the equation $(x_1 + x_2 + x_3)(y_1 + y_2) = 77$, is

- (A) 150 (B) 270 (C) 420 (D) 1024

Q.40 There are counters available in 3 different colors (at least four of each color). Counters are all alike except for the color. If 'm' denotes the number of arrangements of four counters if no arrangement consists of counters of same color and 'n' denotes the corresponding figure when every arrangement consists of counters of each color, then:

- | | |
|---------------|----------------|
| (A) $m = 2n$ | (B) $6m = 13n$ |
| (C) $3m = 5n$ | (D) $5m = 3n$ |

Q.41 Three digit numbers in which the middle one is a perfect square are formed using the digits 1 to 9. Their sum is:

- (A) 134055 (B) 270540
 (C) 170055 (D) none

Q.42 A guardian with 6 wards wishes every one of them to study either Law of Medicine or Engineering. Number of ways in which he can make up his mind with regard to the education of his wards if every one of them be fit for any of the branches to study, and at least one child is to be sent in each discipline is:

- (A) 120 (B) 216 (C) 729 (D) 540

Q.43 There are $(p + q)$ different books on different topics in Mathematics ($p \neq q$)

If L = The number of ways in which these books are distributed between two students X and Y such that X get p books and Y gets q books.

M = The number of ways in which these books are distributed between two students X and Y such that one of them gets p books and another gets q books.

N = The number of ways in which these books are divided into two groups of p books and q books then,

- (A) $L = M = N$ (B) $L = 2M = 2N$
 (C) $2L = M = 2N$ (D) $L = M = 2N$

Q.44 Number of ways in which 5A' and 6B's can be arranged in a row which reads the same backwards and forwards, is

- (A) 6 (B) 8 (C) 10 (D) 12

Q.45 Coefficient of $x^2 y^3 z^4$ in the expansion of $(x + y + z)^9$ is equal to

- (A) The number of ways in which 9 objects of which 2 alike of one kind, 3 alike of 2nd kind, and 4 alike of 3rd kind can be arranged.
 (B) The number of ways in which 9 identical objects can be distributed in 3 persons each receiving at least two objects.
 (C) The number of ways in which 9 identical objects can be distributed in 3 persons each receiving none one or more.
 (D) The number of ways in which 9 different books can be tied up in to three bundles one containing 2, other 3 and third containing 4 books.

Multiple Correct Choice Type

Q.46 The combinatorial coefficient $C(n, r)$ is equal to

- (A) number of possible subsets of r members from a set of n distinct members.
 (B) number of possible binary messages of length n with exactly r 1's.
 (C) number of non-decreasing 2-D paths from the lattice point $(0, 0)$ to (r, n) .
 (D) number of ways of selecting r objects out of n different objects when a particular object is always included plus the number of ways of selecting 'r' objects out of n, when a particular object out of n, when a particular object is always excluded.

Q.47 There are 10 questions, each question is either True or False. Number of different sequences of incorrect answers is also equal to

- (A) Number of ways in which a normal coin tossed 10 times would fall in a definite order if both Heads and Tails are present.
 (B) Number of ways in which a multiple choice question containing 10 alternatives with one or more than one correct alternatives, can be answered.
 (C) Number of ways in which it is possible to draw a sum of money with 10 coins of different denominations taken some or all at a time.
 (D) Number of different selection of 10 indistinguishable objects taken some or all at a time.

Q.48 The number of ways in which five different books can be distributed among 3 persons so that each person gets at least one book, is equal to the number of ways in which

- (A) 5 persons are allotted 3 different residential flats so that and each person is allotted at most one flat and no two persons are allotted the same flat.
 (B) Number of parallelograms (some of which may be overlapping) formed by one set of 6 parallel lines and other set of 5 parallel lines that goes in other direction.
 (C) 5 different toys are to be distributed among 3 children, so that each child gets at least one toy.
 (D) 3 mathematics professors are assigned five different lecturers to be delivered, so that each professor gets at least one lecturer.

Q.49 If k is odd then ${}^k C_r$ is maximum for r equal to

- (A) $r = \frac{1}{2}(k-1)$ (B) $r = \frac{1}{2}(k+1)$
 (C) $k-1$ (D) k

Q.50 Which of the following statements are correct?

- (A) Number of words that can be formed with 6 only of the letters of the word "CENTRIFUGAL" if each word must contain all the vowels is $3 \cdot 7!$
- (B) There are 15 balls of which some are white and the rest black. If the number of ways in which the balls can be arranged in a row, is maximum then the number of white balls must be equal to 7 or 8. Assume balls of the same color to be alike.
- (C) There are 12 objects, 4 alike of one kind, 5 alike and of another kind and the rest are all different. The total number of combinations in 240
- (D) Number of selections that can be made of 6 letters from the word "COMMITTEE" is 35.

Q.51 Number of ways in which the letters of the word 'B U L B U L' can be arranged in a line is a definite order is also equal to the

- (A) Number of ways in which 2 alike Apples and 4 alike Mangoes can be distributed in 3 children so that each child receives any number of fruits.
- (B) Number of ways in which 6 different books can be tied up into 3 bundles, if each bundle is to have equal number of books.
- (C) Coefficient of $x^2y^2z^2$ in the expansion of $(x+y+z)^6$.
- (D) Number of ways in which 6 different prizes can be distributed equally in three children.

Comprehension Type

Paragraph 1: Consider the word $W = \text{MISSISSIPPI}$

Q.52 If N denotes the number of different selections of 5 letters from the word $W = \text{MISSISSIPPI}$ then N belongs to the set

- (A) {15, 16, 17, 18, 19} (B) {20, 21, 22, 23, 24}
 (C) {25, 26, 27, 28, 29} (D) {30, 31, 32, 33, 34}

Q.53 Number of ways in which the letters of the word W can be arranged if at least one vowel is separated from rest of the vowels

- (A) $\frac{8! \cdot 16!}{4! \cdot 4! \cdot 2!}$ (B) $\frac{8! \cdot 16!}{4 \cdot 4! \cdot 2!}$ (C) $\frac{8! \cdot 16!}{4! \cdot 2!}$ (D) $\frac{8!}{4! \cdot 2!} \cdot \frac{16!}{4!}$

Q.54 If the number of arrangements of the letters of the word W if all the S's and P's are separated is (k)

$$\left(\frac{10!}{4! \cdot 4!} \right) \text{ then } k \text{ equals}$$

- (A) $\frac{6}{5}$ (B) 1 (C) $\frac{4}{3}$ (D) $\frac{3}{2}$

Paragraph 2: 16 players $P_1, P_2, P_3, \dots, P_{16}$ take part in a tennis tournament. Lower suffix player is better than any higher suffix player. These players are to be divided into 4 groups each comprising of 4 players and the best from each group is selected for semifinals.

Q.55 Number of ways in which 16 players can be divided into four equal groups, is

- (A) $\frac{35}{27} \prod_{r=1}^8 (2r-1)$ (B) $\frac{35}{24} \prod_{r=1}^8 (2r-1)$
 (C) $\frac{35}{52} \prod_{r=1}^8 (2r-1)$ (D) $\frac{35}{6} \prod_{r=1}^8 (2r-1)$

Q.56 Number of ways in which they can be divided into 4 equal groups if the players P_1, P_2, P_3 and P_4 are in different groups, is:

- (A) $\frac{(11)!}{36}$ (B) $\frac{(11)!}{72}$ (C) $\frac{(11)!}{108}$ (D) $\frac{(11)!}{216}$

Match the Columns

Q.57

| Column-I | Column-II |
|---|----------------|
| (A) Number of increasing permutations of m symbols are there from the n set numbers $\{a_1, a_2, \dots, a_n\}$ where the order among the numbers is given by $a_1 < a_2 < a_3 < \dots < a_{n-1} < a_n$ is | (p) n^m |
| (B) There are m men and n monkeys. Number of ways in which every monkey has a master, if a man can have any number of monkeys | (q) ${}^m C_n$ |
| (C) Number of ways in which n red balls are $(m-1)$ green balls can be arranged in a line, so that no two red balls are together, is (balls of the same color are alike) | (r) ${}^n C_m$ |
| (D) Number of ways in which ' m ' different toys can be distributed in ' n ' children if every child may receive any number of toys, is | (s) m^n |

Q.58

| Column-I | Column-II |
|--|------------------|
| (A) Four different movies are running in a town. Ten students go to watch these four movies. The number of ways in which every movie is watched by at least one student, is (Assume each way differs only by number of students watching a movie) | (p) 11 |
| (B) Consider 8 vertices of a regular octagon and its center. If T denotes the number of triangles and S denotes the number of straight lines that can be formed with these 9 points then the value of $(T - S)$ equals | (q) 36 |
| (C) In an examination, 5 children were found to have their mobiles in their pocket. The Invigilator fired them and took their mobiles in his possession. Towards the end of the test, Invigilator randomly returned their mobiles. The number of ways in which at most two children did not get their own mobiles is | (r) 52 |
| (D) The product of the digits of 3214 is 24. The number of 4 digit natural numbers such that the product of their digits is 12, is | (s) 60 |
| (E) The number of ways in which a mixed double tennis game can be arranged from amongst 5 married couple if no husband & wife plays in the same game, is | (t) 84 |

Previous Years' Questions

Q.1 Five balls of different colors are to be placed in three boxes of different sizes. Each box can hold all five. In how many different ways can we place the balls so that no box remains empty? **(1981)**

Q.2 7 relatives of a man comprises 4 ladies and 3 gentlemen, his wife has also 7 relatives; 3 of them are ladies and 4 gentlemen. In how many ways can they invite a dinner party of 3 ladies and 3 gentlemen so that there are 3 of man's relative and 3 of the wife's relatives? **(1985)**

Q.3 A box contains two white balls, three black balls and four red balls. In how many ways can three balls be drawn from the box, if at least one black ball is to be included in the draw? **(1986)**

Q.4 Eighteen guests have to be seated half on each side of a long table. Four particular guests desire to sit one particular side and three other on the other side. Determine the number of ways in which the sitting arrangements can be made. **(1991)**

Q.5 A committee of 12 is to be formed from 9 women and 8 men. In how many ways this can be done if at least five women have to be included in a committee? In how many of these committees

(a) the women are in majority?

(b) the men are in majority? **(1994)**

Q.6 Match the conditions/expressions in column I with statement in column II.

Consider all possible permutations of the letters of the word ENDEANOEL. **(2008)**

| Column I | Column II |
|---|--------------------|
| (A) The number of permutations containing the word ENDEA. is | (p) $5!$ |
| (B) The number of permutations in which the letter E occurs in the first and the last positions, is | (q) $2 \times 5!$ |
| (C) The number of permutations in which none of the letters D, L, N occurs in the last five positions, is | (r) $7 \times 5!$ |
| (D) The number of permutations in which the letters A, E, O occur only in odd positions, is | (s) $21 \times 5!$ |

MASTERJEE Essential Questions

JEE Main/Boards

Exercise 1

Q.6 Q.10 Q.13 Q.16 Q.22
Q.26 Q.27

Exercise 2

Q.3 Q.13 Q.15 Q.18 Q.25
Q.33 Q.43 Q.46 Q.47 Q.50
Q.52

Previous Years' Questions

Q.4 Q.5 Q.7

JEE Advanced/Boards

Exercise 1

Q.5 Q.6 Q.12 Q.13 Q.16
Q.20 Q.22 Q.28 Q.30

Exercise 2

Q.1 Q.3 Q.8 Q.13 Q.20
Q.26 Q.32 Q.39 Q.42 Q.43
Q.49 Q.55 Q.58

Previous Years' Questions

Q.1 Q.3 Q.4 Q.6

Answer Key

JEE Main/Boards

Exercise 1

Q.1 $2 + 6 + 24 = 32$

Q.2 $3 \times 4 \times 3 \times 2 \times 1 = 72$

Q.3 $35 + 15 = 50$

Q.5 $n = 6$

Q.6 180

Q.7 365

Q.8 1332

Q.9 1023

Q.10 (i) $2^1 + 2^2 + 2^3 + 2^4 = 30$ (ii) $= 2^1 + 2^2 + 2^3 + 2^4 + 2^5 = 2 + 4 + 8 + 16 + 32 = 62$

Q.11 $34650 - 840 = 33810$

Q.12 $4! \cdot 3!$

Q.13 369600

Q.14 302399, 30240

Q.15 3600

Q.16 126

Q.17 $3 + 4 \frac{1}{4} + 4 = 11 \frac{1}{2}$ Hours.

Q.18 $r = 3$

Q.20 ${}^{52}C_4 = 270725$

Q.22 817190

Q.23 (i) 116 (ii) 40 (iii) 185

Q.24 31

Q.25 $\frac{50!}{(12!)^3 \cdot (7!)^2 \cdot 3!}$

Q.26 26

Q.27 150

Q.28 2454

Exercise 2**Single Correct Choice Type**

| | | | | | |
|---------------|---------------|---------------|---------------|---------------|---------------|
| Q.1 C | Q.2 C | Q.3 D | Q.4 A | Q.5 B | Q.6 C |
| Q.7 A | Q.8 D | Q.9 A | Q.10 C | Q.11 D | Q.12 B |
| Q.13 D | Q.14 B | Q.15 A | Q.16 A | Q.17 A | Q.18 D |
| Q.19 D | Q.20 A | Q.21 B | Q.22 C | Q.23 C | Q.24 C |
| Q.25 D | Q.26 A | Q.27 A | Q.28 C | Q.29 B | Q.30 D |
| Q.31 C | Q.32 B | Q.33 C | Q.34 D | Q.35 C | Q.36 D |
| Q.37 A | Q.38 B | Q.39 A | Q.40 D | Q.41 C | Q.42 C |
| Q.43 A | Q.44 C | Q.45 C | Q.46 D | Q.47 A | Q.48 B |
| Q.49 D | Q.50 D | Q.51 C | Q.52 B | Q.53 B | Q.54 B |
| Q.55 E | Q.56 D | | | | |

Previous Years' Questions

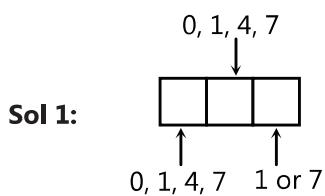
| | | | | | |
|--------------|--------------|--------------|--------------|--------------|--------------|
| Q.1 C | Q.2 D | Q.3 A | Q.4 A | Q.5 C | Q.6 C |
| Q.7 C | | | | | |

JEE Advanced/Boards**Exercise 1**

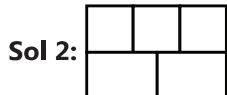
| | | | | | |
|---|--------------------------------|-----------------------------|------------------|---|------------------|
| Q.1 162 | Q.2 7560 | Q.3 2500 | Q.4 826 | Q.5 510 | Q.6 10, 3 |
| Q.7 60 | Q.8 64 | Q.9 244 | Q.10 24 | Q.11 (i) 15, (ii) 126, (iii) 60 (iv) 105 | |
| Q.12 (a) 72; 78120; (b) 23 (c) 32; (d) 435 | | | Q.13 2252 | Q.14 30980 | Q.15 276 |
| Q.16 440 | Q.17 121 | Q.18 (a) 128; (b) 54 | | Q.19 48 | Q.20 42 |
| Q.21 3119976 | Q.22 (a) 1680; (b) 1140 | | Q.23 40 | Q.24 974 | Q.25 186 |
| Q.26 (i) 3359; (ii) 59; (iii) 359 | | Q.27 4201 | Q.28 3888 | Q.29 (i) 240, (ii) 15552 | |

Exercise 2**Single Correct Choice Type**

| | | | | | |
|---------------|---------------|---------------|---------------|---------------|---------------|
| Q.1 D | Q.2 C | Q.3 C | Q.4 B | Q.5 A | Q.6 A |
| Q.7 B | Q.8 A | Q.9 B | Q.10 B | Q.11 B | Q.12 A |
| Q.13 D | Q.14 D | Q.15 D | Q.16 A | Q.17 B | Q.18 B |
| Q.19 A | Q.20 B | Q.21 B | Q.22 A | Q.23 D | Q.24 C |
| Q.25 A | Q.26 B | Q.27 B | Q.28 C | Q.29 B | Q.30 C |
| Q.31 C | Q.32 C | Q.33 C | Q.34 D | Q.35 D | Q.36 D |
| Q.37 C | Q.38 A | Q.39 C | Q.40 B | Q.41 A | Q.42 D |
| Q.43 C | Q.44 C | Q.45 D | | | |

Multiple Correct Choice Type**Q.46** A, B, D**Q.47** B, C**Q.48** B, C, D**Q.49** A, B**Q.50** B, D**Q.51** C, D**Comprehension Type****Q.52** C**Q.53** B**Q.54** B**Q.55** A**Q.56** C**Matrix Match Type****Q.57** A \rightarrow r; B \rightarrow s; C \rightarrow q; D \rightarrow p**Q.58** A \rightarrow t; B \rightarrow r; C \rightarrow p; D \rightarrow q; E \rightarrow s**Previous Years' Questions****Q.1** 300**Q.2** 485**Q.3** 64**Q.4** ${}^9P_4 \times {}^9P_3 \times (11)!$ **Q.5** 6062, (a) 2702 (b) 1008**Q.6** A \rightarrow p; B \rightarrow s; C \rightarrow q; D \rightarrow q.**Solutions****JEE Main/Boards****Exercise 1**

$$\text{Total numbers} = 4 \times 4 \times 2 = 32$$



First arrange those 3 persons in rear seats

Then remaining in front.

Total ways to seat = 5!

Two particular people cannot seat on the driver self

So for this case total ways $\Rightarrow 4! + 4!$

Therefore, required number of ways = $5! - 4! - 4! = 4!(5-2) = 3 \times 4 \times 3 \times 2 \times 1 = 72$

Sol 3: ${}^7C_1 \times {}^5C_1 + {}^3C_1 \times {}^5C_1 = 35 + 15 = 50$

Sol 4: $(2n+1)! = 1 \times 2 \times 3 \dots (2n+1)$

$$= (2 \times 4 \times 6 \dots 2n)(1 \times 3 \times 5 \dots (2n+1))$$

$$= 2^n (1 \times 2 \times 3 \dots n)(1 \times 3 \times 5 \dots (2n+1))$$

$$= 2^n \cdot n! (1 \times 3 \times 5 \dots (2n+1))$$

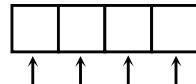
$$\frac{(2n+1)}{n!} = 2^n \cdot (1 \times 3 \times 5 \dots (2n+1))$$

Sol 5: ${}^nP_4 = 360$; $\frac{n!}{(n-4)!} = 360$

$$n(n-1)(n-2)(n-3) = 360 \Rightarrow 6 \times 5 \times 4 \times 3 = 360$$

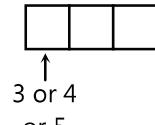
$$n = 6$$

Sol 6: Case-I: 4 digits



$$2 \times {}^5C_3 \times 3! = 120$$

Case-II: 3 digits

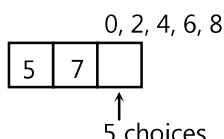


$$3 \times {}^5C_2 \times 2! = 60$$

$$\text{Total number of numbers} = 60 + 120 = 180$$

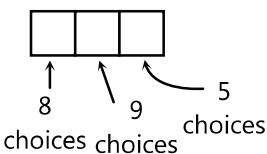
Sol 7: 5 can be there only in the thousand's digit

Case-I: 5 is there



Therefore, total number for case I = 5

Case-II: 5 is not there



Therefore, total number for case II = $8 \times 9 \times 5 = 360$

Total ways = $5 + 360 = 365$

Sol 8: $123+132+213+231+312+321 = 1332$

Sol 9: $4^5 - 1 = 1024 - 1 = 1023$

One case is excluded when all arms are at rest.

Sol 10: (i) $2^1 + 2^2 + 2^3 + 2^4 = 30$

(ii) (a) $2^5 = 32$ (b) $2^1 + 2^2 + 2^3 \dots 2^5 = 62$

Sol 11: M I S S I S S I P P I

M (1)

S (4)

I (4)

P (2)

Ways = Total permutations – Permutations with 4 I's together

$$= \frac{11!}{4! 4! 2!} - \frac{8!}{4! 2!} = 33810$$

Sol 12: ↓↓↓↓ B B B B
 | G | G | G |
 x x x

first arrange girls → 3!

4 seats remains in which 4 boys will be

seated → 4!

Total ways = $3! \times 4! = 144$

Sol 13: $\frac{12!}{(3!)^4} = 369600$

Sol 14: BENEVOLENT

No. of letters = 10

B (1), E (3), N (2), V (1), O (1), L (1), T (1)

$$\text{Total rearrangements} = \frac{10!}{3! 2!} - 1 = 302400 - 1 = 302399$$

$$\text{Total rearrangements with L in the end} = \frac{9!}{3! 2!} = 30240$$

Sol 15: PATALI PUTRA

Vowels = 5

Consonants = 6

Vowels: A(3) I(1) U(1)

Consonants: P(2) T(2)L(1)R(1)

$$\text{Total no. of words} = \frac{5!}{3!} \times \frac{6!}{2! 2!} = 3600$$

Sol 16: $\frac{9!}{4! 5!} = 126$

Sol 17: 3! ways

A → III

B → I

C → II

$$\text{Time} = 4 + 4 \frac{1}{4} + 3 = 11 \frac{1}{4} \text{ hours}$$

Sol 18: ${}^{15}C_{3r} = {}^{15}C_{r+3}$

$$(1) 3r = r + 3 \Rightarrow r = \frac{3}{2}$$

$$(2) 3r + r + 3 = 15 \Rightarrow 4r = 12 \Rightarrow r = 3$$

$$r = \frac{3}{2} \text{ Not possible}$$

r = 3 Possible

Sol 19: ${}^nC_r \times {}^rC_s = {}^nC_s \times {}^{n-s}C_{r-s}$

$$\text{LHS: } {}^nC_r + {}^rC_s = \frac{n!}{r!(n-r)!}, \frac{r!}{s!(r-s)!}$$

$$= \frac{n!}{s!} \times \frac{(n-s)!}{(n-s)!} \times \frac{1}{(n-r)!(r-s)!} = \frac{n!}{s!(n-s)!} \times \frac{(n-s)!}{(n-r)!(r-s)!}$$

$$= {}^nC_s \times {}^{n-s}C_{r-s} = \text{RHS}$$

Sol 20: ${}^{47}C_4 + \sum_{j=1}^5 {}^{52-j}C_3$

$$= \underbrace{{}^{47}C_4 + {}^{47}C_3}_{+ {}^{48}C_3 + \dots + {}^{51}C_3} = {}^{48}C_4 + ({}^{48}C_3 + \dots + {}^{51}C_3)$$

$$= {}^{51}C_4 + {}^{51}C_3 = {}^{52}C_4 = 270725$$

Sol 21: Product = $(n+1)(n+2) \dots (n+r)$

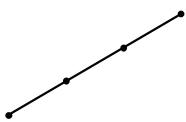
$$= \frac{(n+r)!}{n!} = r! \times \frac{(n+r)!}{n! \cdot r!} = r! \times {}^{n+r}C_r$$

${}^{n+r}C_r$ will be integer

Hence product is divisible by $r!$.

Sol 22: ${}^{22}C_{10} + {}^3C_3 {}^{22}C_7 = 817190$

Sol 23:



(i) No. of triangles = ${}^{10}C_3 - {}^4C_3 = 116$

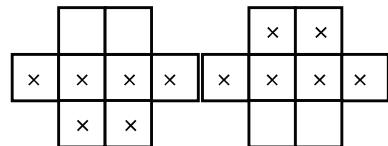
(ii) No. of straight lines = ${}^6C_2 + 6 \times 4 + 1 = 15 + 24 + 1 = 40$

(iii) No. of quadrilaterals = ${}^{10}C_4 - {}^4C_3 \times 6 - {}^4C_4 = 185$

Sol 24: $2^5 - 1 = 31$

Sol 25: $\frac{50!}{(12!)^3 3! (7!)^2 2!}$

Sol 26: Cases not allowed



$${}^8C_6 - 2 = 26$$

Sol 27: Possible groups

1 1 3

1 2 2

No. of ways

$$= 3! \times \left(\frac{5!}{1! 1! 3! (2!)} + \frac{5!}{1! 2! 2! (2!)} \right) = 60 + 90 = 150$$

Sol 28: EXAMINATION

4 DIFF

$${}^8C_4 \times 4! = 1680$$

2 diff. 2 alike

$${}^3C_1 \times {}^7C_2 \times \frac{4!}{2!} = 756$$

2A, 2A

$${}^3C_2 \times \frac{4!}{2! 2!} = 18$$

Total = 2454

Exercise 2

Single Correct Choice Type

Sol 1: (C)

| | | | | | |
|----|----|----|-----|---|----|
| A | N | R | U | V | 4! |
| | | | | | |
| N | A | R | U | V | |
| | | | | | |
| R | A | N | U | V | 4! |
| | | | | | |
| U | A | N | R | V | |
| | | | | | |
| V | A | N | R | U | 96 |
| | | | | | |
| V | A | N | U | R | |
| 97 | 98 | 99 | 100 | | |

V A N R U
V A N U R
V A R N U
V A R U N

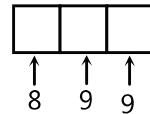
96
97
98
100

V A R U N

100

Sol 2: (C) Numbers = Total – Numbers with no digit 7

Total = 900

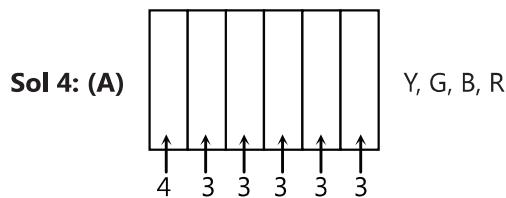


Number of numbers with at least

$$\text{One digit 7} = 900 - 8 \times 9 \times 9 = 252$$

Sol 3: (D)

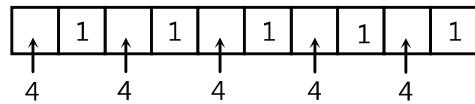
| | | | | | |
|---|---|---|---|---|----|
| A | E | H | M | S | 24 |
| | | | | | |
| A | S | M | H | E | 24 |
| | | | | | 24 |
| E | A | H | M | S | 48 |
| | | | | | |
| E | S | M | H | A | 48 |
| | | | | | 24 |
| H | A | E | M | S | 72 |
| | | | | | |
| H | S | M | E | A | 72 |
| | | | | | 73 |
| M | A | E | H | S | 73 |
| | | | | | |
| M | A | S | H | E | 78 |
| | | | | | 6 |
| M | E | A | H | S | 84 |
| | | | | | |
| M | E | S | H | A | 84 |
| | | | | | 6 |
| M | H | A | E | S | 86 |
| | | | | | |
| M | H | A | S | E | 86 |



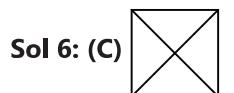
$$4 \times 3^5 = 12 \times 81$$

Sol 5: (B) Prime number in 0 – 9

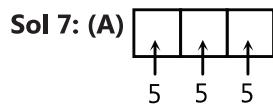
2, 3, 5, 7



$$2 \times 4^5 = 2048$$



$${}^5C_3 - 2 = 10 - 2 = 8$$



No. 5 with no even digit

$$900 - 5^3 = 775$$

Sol 8: (D) The sum of the 5-digits used must be divisible by 3.

Only possible combinations are:

1, 2, 3, 4, 5 & 0, 1, 2, 4, 5

$$\begin{matrix} \downarrow \\ 5! & 4.4! \end{matrix}$$

$$\text{Total} = 9.4!$$

$$= 9 \times 24 = 216$$

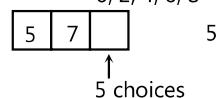
Sol 9: (A) ${}^7C_2 \times 2^5 = 672$

Sol 10: (C) ${}^7C_4 \times {}^4C_2 \times 6! = 151200$

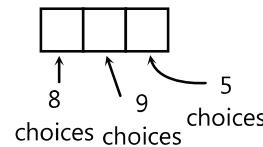
Sol 11: (D) 5 can be there only in the thousand's digit

Case-I: 5 is there

0, 2, 4, 6, 8



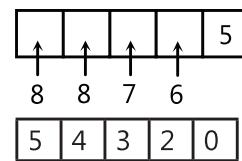
Case-II: 5 is not there



$$8 \times 9 \times 5 = 360$$

$$\text{Total ways} = 5 + 360 = 365$$

Sol 12: (B)



$${}^4C_1 \times 8 \times 7 \times 6$$

$$\text{Total ways} = 8 \times 8 \times 7 \times 6 + {}^4C_1 \times 8 \times 7 \times 6 = 168 \times 4!$$

Sol 13: (D) 4 odd, 3 even

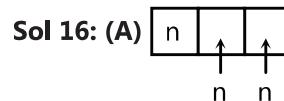
Arrangements: 4 + 2 3 + 3

$$\text{Total numbers} = {}^3C_2 \times 2 \times 4! + {}^4C_3 \times {}^3C_2 \times 2 \times 4! = 720$$

Sol 14: (B) $9000 - 9 \times 9 \times 8 \times 7 = 4464$

Sol 15: (A) It can be a digit number with digits 1 to 9 or a 10 digit number with digits 0 to 9

$$9! + 9.9! = 10!$$



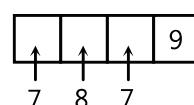
$$\sum_{n=1}^9 n^2 = \frac{9 \times 10 \times 19}{6} = 285$$

Sol 17: (A) Consider 1 & 2, 3 & 4, 5 & 6 to be identical

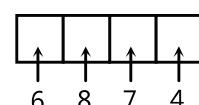
$$\text{Permutations} = \frac{9!}{(2!)^3} = 9.7!$$

Sol 18: (D)

Last digit 9



Last digit not 9



$$\text{Total} = 7 \times 8 \times 7 + 6 \times 8 \times 7 \times 4 = 1736$$

Sol 19: (D)

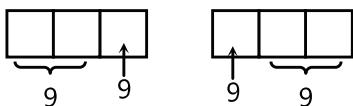
$$\begin{array}{cccccccccc} \downarrow & \downarrow \\ \times & \times \end{array}$$

10 persons

$$\frac{10}{10} C_5 \cdot 5!$$

Choose 5 persons from 10 getting books & distribute books to then 5! ways .

Sol 20: (A) ${}^5C_3 \times {}^8C_7 + {}^5C_4 \times {}^8C_6 + {}^5C_5 \times {}^8C_5$
 $= 80 + 5 \times 28 + 56 = 276$

Sol 21: (B)

Total = 162

Sol 22: (C) $\frac{(n-2)}{n} \times 180 = 150$

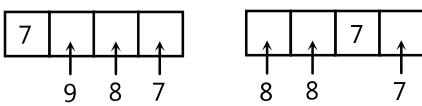
$6n - 12 = 5n \Rightarrow n = 12$

$\text{Diagonals} = {}^{12}C_2 - 12 = 54$

Sol 23: (C) $2^n - 2 = 510$

$2^n = 512$

$n = 9$

Sol 24: (C)

$9 \times 8 \times 7 + 8 \times 8 \times 7 \times 3 = 33 \times 8 \times 7 = 1848$

Sol 25: (D) Total appointment = 11

$11 \rightarrow \boxed{2} \boxed{3} \boxed{6}$

$\text{total ways to disposed} = (2! 3! 6!) \times 3 = 8640 \times 3 = 25920$

Sol 26: (A) Illegal ways = $2 \times {}^7C_4 + {}^7C_3 - 2 \times {}^5C_2 = 85$

$\text{No. of possible ways} = {}^9C_5 - 85 = 126 - 85 = 41$

Sol 27: (A) 1 1 3

1 2 2

$3 \times ({}^4C_1 \times {}^4C_1 \times {}^4C_3 + {}^4C_1 \times {}^4C_2 \times {}^4C_2)$

$= 3 \times (64 + 144) = 624$

Sol 28: (C) Combine those 2 green bottles

$\times \times \times \times \times \times \times$

9 spaces

$6 \times {}^9C_6 = 84 \times 6 = 504$

Sol 29: (B) ${}^{25}C_5 - {}^{24}C_4 = {}^{24}C_5$

Sol 30: (D) ${}^5C_4 \times 2^4 = 80$

Select 4 pairs out of 5 different pairs. Now in each pair you can choose 2 different shoes.

Sol 31: (C) 2 2 2 3

$$\frac{3! 9!}{3! (2!)^3 3!} = \frac{9!}{3! (2!)^3}$$

Sol 32: (B) $\underbrace{\times \times \times \times \times \times \times \times \times}_{10 \text{ red balls}}$

11 spaces

choose 9 spaces to fill green balls. 10! ways to arrange red balls.

${}^{11}C_9 \times 10!$

Sol 33: (C) $7! \times 2^3$

7! ways to arrange

2 order (ascending/descending)

Sol 34: (D) $\frac{6!}{2! 2! 2!}$

Consider man and wife to be identical and arrange them.

Similar concept as used in Q. 18

Sol 35: (C) $\frac{7!}{7! 0!} + \frac{7!}{6! 1!} + \frac{7!}{5! 2!} + \dots + \frac{7!}{2! 5!}$

${}^7C_0 + {}^7C_1 + {}^7C_2 + \dots + {}^7C_5 = 2^7 - {}^7C_6 - {}^7C_7 = 128 - 7 - 1 = 120$

Sol 36: (D) $\downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow$
 $\times \quad \times \quad \times \quad \times$

EE AA

EAEA

AEAE

EAAE

$4! \times ({}^5C_2 \times (2! + 2! + 1 + 1)) = 1440$

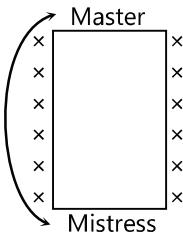
Sol 37: (A) The last match has to be won by India

$$1 + {}^5C_1 + {}^6C_2 + {}^7C_3 + {}^8C_4 = 126$$

Sol 38: (B)

$$2(9^3 \times 1 + 3 \times 4 \times 9^2) = 2(1701) = 3402$$

Sol 39: (A)



$$2 \times 10 \times 10! = \text{Sol.} 20 \quad 10!$$

Sol 40: (D) $S_1 S_3 S_2$

$$S_3 S_1 S_2$$

Consider $S_1 S_2 S_3$ identical & arrange

$$2 \times \frac{10!}{3!} = \frac{10!}{3}$$

Sol 41: (C) $3^{10} - 1$

3 choices question its alternative & no question.

Sol 42: (C) 9 9 9 9 9 9 7

9 9 9 9 9 8 8

$$\frac{7!}{6!} + \frac{7!}{5! 2!} f = 7 + 21 = 28$$

$$\text{Sol 43: (A)} \quad \frac{9!}{2! 3!} - 4! 3! = 6(7! - 4!) = 6(5040 - 24) = 30144$$

Sol 44: (C) $1000 = 2^3 \times 5^3$

The product of even divisors of 1000 will be

$$\begin{aligned} &= (2 \times 2^2 \times 2^3) \times (2 \times 5) \times (2 \times 5^2) \times (2 \times 5^3) \times (2^2 \times 5) \\ &\times (2^2 \times 5^2) \times (2^2 \times 5^3) \times (2^3 \times 5) \times (2^3 \times 5^2) \times (2^3 \times 5^3) \\ &= (2^6)^4 \times (5 \times 5^2 \times 5^3) = (2^6)^4 \times (5^6)^3 = 64 \times 10^{18} \end{aligned}$$

Sol 45: (C) $x_1 + x_2 + \dots + x_{10} = 7$

7 people are distributed to 10 floor

$$\text{Total ways} = {}^7 + {}^{10-1}C_{10-1} = {}^{16}C_9 = {}^{16}C_7$$

Sol 46: (D) Total ways = $3^n + {}^nC_2 \cdot 3^{n-2} + {}^nC_4 \cdot 3^{n-4} + \dots$

$$= \frac{(1+3)^n}{2} + \frac{2^n}{2} = 2^{2n-1} + 2^{n-1} = 2^{n-1}(2^n + 1)$$

Sol 47: (A) Each digit will be present at unit's ten's and hundred's place 6 times.

$$(1 + 2 + 3 + 4) \times 6 = 60$$

$$\begin{array}{r} 60 \\ 60 \times \\ \hline \text{Sum of digits} = \frac{60 \times \times}{6660} \end{array}$$

$$\text{Sol 48: (B)} \quad {}^8C_1 + {}^8C_1 \times {}^7C_1 = 64$$

Sol 49: (D) No. of books of algebra = No of books of calculus

Sol 50: (D) No. of ways = Total ways – No letter is in wrong envelope = $5! - 1 = 119$

Sol 51: (C) $P_1 P_2 P_3 P_4$

$$\frac{4!}{(2!)^2 2!} = 3$$

$$\text{Total matches} = {}^8C_4 \times 3$$

$$\text{Sol 52: (B)} \quad {}^9C_6 \times 5 \times 3! = 2520$$

$$\begin{aligned} \text{Sol 53: (B)} \quad &{}^6C_1 \times 2^1 \times 2^5 + {}^6C_3 \times 2^3 \times 2^3 + {}^6C_5 \\ &\times 2^5 \times 2^1 = 2^6 ({}^6C_1 + {}^6C_3 + {}^6C_5) \\ &= 2^6 \times \frac{2^6}{2} = 2^{11} \end{aligned}$$

Sol 54: (B) 2.6.10 $(4n - 2)$

$$= 2^n (1.3.5 \dots (2n-1)) \times \frac{n!}{n!} = \frac{(2n)!}{n!} = {}^{2n}P_n$$

Sol 55: (E) No. of permutations

$$= {}^{2n}C_n = \frac{(2n)!}{n! n!} = \frac{2^n \dots n! [1.3.5 \dots (2n-3)(2n-1)]}{n!}$$

Sol 56: (D) n is odd

$$1, 2, 3, \dots, \frac{n+1}{2}, \dots, n$$

$$\text{Total A.P.S.} = 0 + 1 + \dots + \frac{n-1}{2} + \dots + 1 + 0 = \frac{(n-1)^2}{4}$$

n is even

$$1, 2, \dots, \frac{n}{2}, \frac{n}{2} + 1, \dots, n$$

Total A.P.S

$$= 2 \times \left(0 + 1 + \dots + \frac{n}{2} - 1 \right) = \frac{n(n-2)}{4}$$

Previous Years' Questions

Sol 1: (C) Here, ${}^{47}C_4 + \sum_{j=1}^5 {}^{52-j}C_3$

$$= {}^{47}C_4 + {}^{51}C_3 + {}^{50}C_3 + {}^{49}C_3 + {}^{47}C_3$$

$$= ({}^{47}C_4 + {}^{47}C_3) + {}^{48}C_3 + {}^{49}C_3 + {}^{50}C_3 + {}^{51}C_3$$

$$(\text{using } {}^nC_r + {}^nC_{r-1} = {}^{n+1}C_r)$$

$$= ({}^{48}C_4 + {}^{48}C_3) + {}^{49}C_3 + {}^{50}C_3 + {}^{51}C_3$$

$$= ({}^{49}C_4 + {}^{49}C_3) + {}^{50}C_{43} + {}^{51}C_3$$

$$= ({}^{50}C_4 + {}^{50}C_3) + {}^{51}C_3 = {}^{51}C_4 + {}^{51}C_3 = {}^{52}C_4$$

Sol 2: (D) Since, the first 2 women select the chairs amongst 1 to 4 in 4P_2 ways

Now, from the remaining 6 chairs, three men could be arranged in 6P_3 .

$$\therefore \text{Total number of arrangements} = {}^4P_2 \times {}^6P_3.$$

Sol 3: (A) Since, a five digits number is formed using the digits {0, 1, 2, 3, 4 and 5} divisible by 3 ie, only possible when sum of the digits is multiple of three.

Case I : Using digits 0, 1, 2, 4, 5

$$\text{Number of ways} = 4 \times 4 \times 3 \times 2 \times 1 = 96$$

Case II : Using digits 1, 2, 3, 4, 5

$$\text{Number of ways} = 5 \times 4 \times 3 \times 2 \times 1 = 120$$

$$\therefore \text{Total number formed} = 120 + 96 = 216$$

Sol 4: (A) Since, $240 = 2^4 \times 3 \times 5$

$$\therefore \text{Total number of divisors} = (4+1)(2)(2) = 20$$

Out of these 2, 6, 10, and 30 are of the form $4n + 2$.

Therefore, (a) is the answer.

Sol 5: (C) Since, r, s, t are prime numbers.

\therefore Selection of p and q are as under

Pq Number of ways

R^0r^2 1 way

R^1r^1 1 way

R^2r^0, r^1, r^2 3 ways

\therefore Total number of ways to select r = 5.

Selection of s as under

s^0s^4 1 way

s^1s^4 1 way

s^2s^4 1 way

s^3s^4 1 way

s^4s^4 1 way

\therefore Total number of ways to select s = 9.

Similarly, the number of ways to select t = 5.

\therefore Total number of ways = $5 \times 9 \times 5 = 250$

Sol 6: (C) Arrange the letters of the word COCHIN as in the order of dictionary CCHINO.

Consider the words starting from C.

There are 5! Such words. Number of words with the two C's occupying first and second place = 4!

Sol 7: (C) There are two possible cases

Case-I Five 1's, one 2's, one 3's

$$\text{Number of numbers} = \frac{7!}{5!} = 42$$

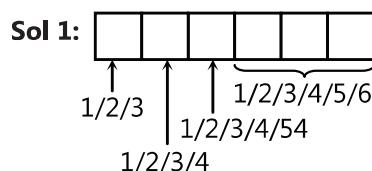
Case-II Four 1's three 2's

$$\text{Number of numbers} = \frac{7!}{4!3!} = 35$$

$$\text{Total number of numbers} = 42 + 35 = 77$$

JEE Advanced/Boards

Exercise 1



$$\underbrace{3 \times 3 \times 3 \times 3}_{\text{Filling first 4 places}} \times \underbrace{2}_{\text{last two places}} = 81 \times 2 = 162$$

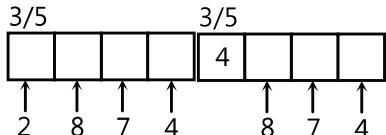
Sol 2: ${}^9C_1 \times {}^8C_2 \times \frac{5!}{2! 2!} = 9 \times 28 \times \frac{120}{84} = 7560$

Sol 3: $3^1 3^2 3^3 \dots 3^{51} \dots 3^{98} 3^{99} 3^{100} 3^{101}$

Fix the middle element of G.P. the find the number of G.P.S possible

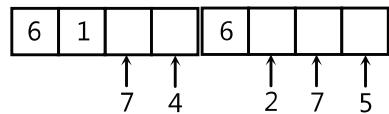
$$0 + 1 + 2 + \dots + 49 + 50 + 49 + \dots + 1 + 0 = 2500$$

Sol 4: 3/5



$$2 \times 8 \times 7 \times 4 = 448 \quad 8 \times 7 \times 5 = 280$$

0/2



$$7 \times 4 = 28 \quad 2 \times 7 \times 5 = 70$$

Total = 826

Sol 5: Case-I: 2 2 2

$$\frac{6!}{(2!)^3} = 90$$

Case-II: 1 2 3

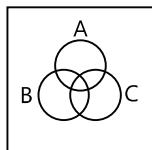
$$\frac{6!}{1! 2! 3!} \times 3! = 360$$

Case-III: 0 3 3

$$\frac{6!}{(3!)^2 2!} \times 3! = 60$$

Total = 90 + 360 + 60 = 510

Sol 6:



$$n(A) = 8! = n(B) = n(C)$$

$$n(A \cap B) = n(B \cap C) = n(A \cap C) = 7!$$

$$n(A \cap B \cap C) = 6!$$

Sol 7: $3 \times n(A \cap B) - 3n(A \cap B \cap C)$

$$3 \times 7! - 3 \times 6!$$

$$= (63 - 3)6! = 60(6!)$$

Sol 8: $n(A) - 2n(A \cap B) + 2n(A \cap B \cap C)$

$$= 8! - 2 \times 7! + 6! = (56 + 14 + 1)$$

$$6! = 436!$$

Sol 9: $9! - n(A \cup B \cup C)$

Sol 10: $\frac{360}{k}$ Should be an integer.

$\therefore k$ is a factor of 360

$$360 = 3^2 \times 2^3 \times 5$$

$$\text{Total factors} = 4 \times 3 \times 2 = 24$$

Sol 11: (i) ${}^6C_4 = 15$

(ii) All, 4 diff. ${}^6C_4 = 15$

2diff, 2Alike ${}^6C_2 \times {}^4C_1 = 60$

2 alike, 2alike ${}^6C_2 = 15$

1 diff, 3alike $2 \times {}^6C_2 = 30$

4 alike ${}^6C_1 = 6$

126

(iii) 3 different flavours = 60

(iv) 2 or 3 different flavours = $60 + 15 + 30 = 105$

Sol 12: (a) $x = 21600$

$$x = 6^3 \times 100 = 2^5 3^3 5^2$$

$$\text{No. of divisors} = 6 \times 4 \times 3 = 72$$

$$\text{Sum} = (2^0 + 2^1 + \dots + 2^5)$$

$$(3^0 + 3^1 + \dots + 3^3)(5^0 + 5^1 + 5^2) = 60 \times 40 \times 31 = 78120$$

(b) $x = 7056$

$$x = 2^4 \times 3^2 \times 7^2$$

$$\text{Total factors} = 5 \times 3 \times 3 = 45$$

$$\text{Answer} = \frac{45+1}{2} = 23$$

$$(c) 300300 = 7 \times 11 \times 13 \times 10^2 \times 3$$

$$= 2^2 \times 3 \times 5^2 \times 7 \times 11 \times 13$$

$$\frac{2^6}{2} = 32$$

$$(d) 10^{10} 15^7 18^{11}$$

$$2^{10} \times 5^{10}, 3^7 \times 5^7, 2^{11} \times 3^{22}$$

$$\text{HCF of } 10^{10}, 15^7 \text{ & } 18^{11} = 1$$

$$\text{HCF of } 10^{10} \text{ & } 15^7 = 5^7$$

$$\text{HCF of } 10^{10} \text{ & } 18^{11} = 2^{10}$$

HCF of 15^7 & $18^{11} = 3^7$

Total divisors = $(11 \times 11 + 8 \times 8 + 12 \times 23) - (8 + 11 + 8) + 1 = 435$

$$\text{Sol 13: } \sum_{x=0}^5 (^5C_x)^3 = 1 + 5^3 + 10^3 + 10^3 + 5^3 + 1 = 2252$$

$$\text{Sol 14: } {}^{18}C_9 - {}^{10}C_5 \times {}^8C_4 = 48620 - 252 \times 70 = 30980$$

$$\text{Sol 15: } 5^2 - 1 = 24 \quad \therefore {}^{24}C_2 \text{ triangles}$$

$$\text{Sol 16: } x + y + 2 + w = 13$$

$$x \leq 5y \geq 2$$

$${}^{10}C_2 + {}^{11}C_2 + \dots + {}^{15}C_2 = 45 + 55 + 66 + 78 + 91 + 105 = 440$$

Sol 17: 2 digits should be odd or

2 digits should be even for average to be integer

111 222 999 each repeats 3 times

$${}^3C_2 \times \underbrace{{}^5C_1 \times {}^5C_1}_{\text{odd}} + {}^3C_2 \times \underbrace{{}^4C_1 \times {}^4C_1}_{\text{even/0}} + \underbrace{{}^2C_1 \times 4 \times 3}_{\text{zero}} - \underbrace{2 \times 9}_{\text{repetition}} = 121$$

$$\text{Sol 18: (a) 1 element } {}^{12}C_1 = 12$$

$$2 \text{ elements } {}^{10}C_2 = 45$$

$$3 \text{ elements } {}^8C_3 = 56$$

$$4 \text{ elements } {}^6C_4 = 15$$

$$5 \text{ elements } 0$$

$$\text{Total} = 128$$

(b) Select 3 elements

Each is this element is either present in S, T or both S and T

$$\therefore \text{Total} = {}^6C_3 \times 3^3 = 540$$

$$\lambda = 54$$

Sol 19: Sum at first places can be 6 at max.

4 3 1 2 5 not allowed

| | First 2 digits | Last 2 digits | Permutations |
|--------|----------------|---------------|--------------|
| Sum 6: | 15 | 43 | 4 |
| | 24 | 53 | 4 |
| Sum5: | 14 | 53/52 | 8 |
| | 23 | 54/51 | 8 |
| Sum4: | 13 | 54/52/42 | 12 |
| Sum3: | 12 | 54/53 | 12 |
| | | Total | 48 |

Sol 20: Total wins = Total matches = $10 \times {}^8C_2$

Wins of champion = A + 7d

$$\frac{8}{2} [2A + 7d] = 280$$

$$A = \frac{70 - 7d}{2}$$

Now d $\neq 0$ d = 2

$$A = 28$$

$$\text{Wins of champion} = 28 + 7 \times 2 = 42$$

$S_1 \quad S_2 \quad S_3 \quad S_4 \quad S_5$

Sol 21: 

$$S_1 = (1 + 2 + 4 + 5) \times 4! = 288$$

$$S_2 = S_3 = S_4 = S_5 = (1 + 2 + 4 + 5) \times 3 \times 3! = 216$$

$$\text{Sum} = S_1 \times 10^4 + S_2 (10^3 + 10^2 + 10 + 1)$$

$$= 288 \times 10^4 + 216(1111) = 3119976$$

$$\text{Sol 22: (a) } {}^8C_3 \times {}^5C_3 \times 3! = 1680$$

$$(b) {}^3C_1 \frac{5!}{3! 2!} 2 + {}^3C_2 \times 3 \times 2 \times \frac{5!}{1! 2! 2!} \times 2!$$

$$= 60 + 1080 = 1140$$

a, b, c distinct

$$\text{Sol 23: } \{1, x, x\} ({}^5C_1 + {}^5C_2) = 15$$

$$\{x, x, x\} \frac{5!}{1! 1! 3! 2!} + \frac{5!}{1! 2! 2! 2!} = 25$$

$$\text{Total} = 15 + 25 = 40$$

Sol 24: No. of integers

2 digit no. 89, 98 2

3 digit no.

Zero included 890, 809 4

980, 908

Zero excludes

$$2 \times {}^3C_2 + {}^7C_1 \times 3! 48$$

4 digit no.

Tow zeroes {}^3C_2 × 26

$$\text{One zero } {}^3C_1 \times ({}^7C_1 \times 3! + 6) 144$$

$$\text{No zero } 2 \times {}^4C_2 \times 7 \times 7 + 2 \times {}^4C_2 \times 2 \times 7 770 + 2 \times {}^4C_3 + {}^4C_2 = 974$$

Sol 25: A - 1B - 9 1

$$A - 2 B - 8 {}^8C_1$$

$$A - 3B = {}^7C_2$$

$$A - 4B = {}^6C_3$$

$$A - 5B = 50$$

$$N = 2(1 + {}^8C_1 + {}^8C_2 + {}^8C_3)$$

$$N = 186$$

Sol 26: (i) $M^U LT^I PL^E$

$$\frac{8!}{3! 2!} - 1 = 3359$$

$$(ii) \frac{5!}{2!} - 1 = 59$$

$$(iii) 3! \times \frac{5!}{2!} - 1 = 359$$

$$\text{Sol 27: } 3 \text{ digits } {}^5C_3 \times \frac{9!}{3! 3! 3!} = 16,800$$

$$2 \text{ digits } 2 \times {}^5C_2 \times \left(\frac{9!}{3! 6!} + \frac{9!}{4! 5!} \right) = 4,200$$

$$1 \text{ digit } {}^5C_1 = 5$$

$$\text{Total} = 21005$$

$$\frac{N}{5} = 4201$$

$$\text{Sol 28: } {}^3C_2 \times 9 \times 8 + 9 \times {}^3C_2 \times 8 \times 8 + 9 \times 3 \times 9 \times 8 = 3888$$

$$\text{Sol 29: (i)} 4 \times 4! + 2 \times 3 \times 4! = 240$$

$$(ii) 4 \times 6^4 \times 3 = 15552$$

Exercise 2

Single Correct Choice Type

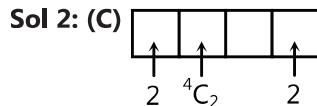
Sol 1: (D) We have $0 + 1 + 2 + 3 \dots + 8 + 9 = 45$

To obtain an eight digit number exactly divisible by 9, we must not use either (0, 9) or (2, 7) or (3, 6) or (4, 5). [Sum of the remaining eight digits is 36 which is exactly divisible by 9.]

When, we do not use (0, 9), then the number of required 8 digit number is $8!$.

When, one of (1, 8) or (2, 7) or (3, 6) or (4, 5) is not used, the remaining digits can be arranged in $8! - 7!$ ways as 0 cannot be at extreme left.

Hence, there are $8! + 4(8! - 7!) = (36)(7!)$ numbers in the desired category.



$$2 \times {}^4C_2 \times 2 = 24$$

$$\text{Sol 3: (C)} {}^{20}C_2 - 10 - 5 \times 9 = 190 - 10 - 45 = 135$$

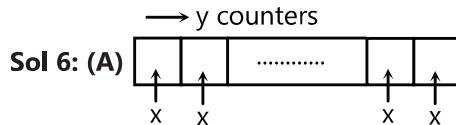
$$\text{Sol 4: (B)} r = {}^9C_2 \times {}^9C_2 = 36^2$$

$$s = 8^2 + 7^2 + 6^2 + \dots + 1^2 = \frac{8 \times 9 \times 17}{6}$$

$$\frac{s}{r} = \frac{17}{108}$$

$$\text{Sol 5: (A)} 200,000,000$$

$$2^8 + 2^8 + 2^7 + 2^6 + \dots + 2^1 = 2^8 + 2 \cdot \left(\frac{2^8 - 1}{2 - 1} \right) = 3 \cdot (2)^8 - 2$$



$$x^y - y$$

$$\text{Sol 7: (B)} M - n = {}^{10}C_5 - {}^9C_5 = {}^9C_5$$

$$\text{Sol 8: (A)} N_1 = {}^{m+n}C_3 - {}^mC_3 - {}^nC_3$$

$$N_2 = {}^{m+n+1}C_3 - {}^{m+1}C_3 - {}^{n+1}C_3$$

$$\frac{N_1}{N_2} = \frac{m+n-2}{m+n}$$

$$\text{Sol 9: (B)} 10000 \text{ to } 99999$$

$$\text{Number of numbers} = \frac{90000}{2} = 45000$$

Sol 10: (B) $\boxed{AB} D C E F G H$

$$2 \times \frac{7!}{2!} = 5040$$

$$\text{Sol 11: (B)} \frac{7!}{1! 2! 4!} \times 3! = 630$$

$$\text{Sol 12: (A)} {}^9C_4 = 126$$

Sol 13: (D) Case-I: 1 3 4

$$\frac{8!}{1! \ 3! \ 4!} \times 3!$$

Case-II: 2 3 3

$$\frac{8!}{2! \ 3! \ 3! \ 2!} \times 3!$$

Case-III: 2 2 4

$$\frac{8!}{2! \ 2! \ 4! \ 2!} \times 3!$$

$$\text{Total} = 4620 = 22 \times {}^7P_3$$

Sol 14: (D) Pack 1 Pack 2

Peaches Apples Peaches Apples

3 1 2 2

$${}^5C_3 \times {}^3C_1 = 30$$

Sol 15: (D)

(n - 2) choices. select 3

$$P_n = {}^{n-2}C_3$$

$$P_{n+1} - P_n = {}^{n-1}C_3 - {}^{n-2}C_3 = {}^{n-2}C_2 = 15$$

$$n - 2 = 6 \Rightarrow n = 8$$

Sol 16: (A) $n(2) = 50n(2 \cap 3) = 16$

$$n(3) = 33 \quad n(3 \cap 5) = 6 \quad n(2 \cap 3 \cap 5) = 5$$

$$n(5) = 20 \quad n(2 \cap 5) = 10$$

$$n(2 \cup 3 \cup 5) = (50 + 33 + 20) - (16 + 6 + 10) + 3$$

$$n(2 \cup 3 \cup 5) = 100 - 74 = 26$$

Sol 17: (B) ${}^5C_1 \times \frac{6!}{2!} = 1800$

Choose subject with two periods and then arrange.

Sol 18: (B)

240

Sol 19: (A) Rectangles = ${}^7C_2 \times {}^5C_2 = 21 \times 10 = 210$ Squares = $6 \times 4 + 5 \times 3 + 4 \times 2 + 3 \times 1$

$$= 24 + 15 + 8 + 3 = 50$$

$$\text{Rectangles which are not squares} = 210 - 50 = 160$$

Sol 20: (B)

$$\underline{\frac{1}{2}} \underline{\frac{3}{4}} \underline{\frac{5}{6}} \underline{\frac{7}{8}} \underline{\frac{9}{10}} \underline{\frac{11}{12}} \underline{\frac{13}{14}} \underline{\frac{15}{16}} \underline{\frac{17}{18}} \underline{\frac{19}{20}} \underline{\frac{21}{22}} \underline{\frac{23}{24}} \underline{\frac{25}{26}} \underline{\frac{27}{28}} \underline{\frac{29}{30}} \underline{\frac{31}{32}} \underline{\frac{33}{34}} \underline{\frac{35}{36}} \underline{\frac{37}{38}} \underline{\frac{39}{40}} \underline{\frac{41}{42}} \underline{\frac{43}{44}} \underline{\frac{45}{46}} \underline{\frac{47}{48}} \underline{\frac{49}{50}} = 70$$

$$2 \underline{3} \underline{4} \underline{5} \underline{6} \underline{7} \underline{8} \underline{9} = 20 + 70 = 90$$

$$2 \underline{4} \underline{5} \underline{6} \underline{7} \underline{8} \underline{9} = 6 + 90 = 96$$

$$2 \underline{4} \underline{6} \underline{7} \underline{8} = 97^{\text{th}}$$

Sol 21: (B) ${}^nC_n + {}^{n+1}C_n + {}^{n+2}C_n + \dots + {}^{n+m}C_n$

$$= {}^nC_0 + {}^{n+1}C_1 + {}^{n+2}C_2 + \dots + {}^{n+m}C_m = {}^{n+1}C_0 + {}^{n+2}C_1 + \dots + {}^{n+m}C_m = {}^{n+m+1}C_m$$

Sol 22: (A) $\frac{1}{2} \times \frac{1}{2} \times {}^{m+n}C_m (m-1)(n-1)!$

$$= \frac{1}{4} \times \frac{(m+n)!}{mn}$$

Sol 23: (D)

| | | |
|---|---|---|
| 1 | x | x |
| x | 1 | x |
| x | x | 1 |

$${}^3C_1 = 3$$

| | | |
|---|---|---|
| 1 | x | x |
| x | 0 | x |
| x | x | 0 |

$${}^3C_1 \times {}^3C_2 = 9$$

Total = 12

Sol 24: (C) 5 3 or 4 4

$${}^8C_5 + {}^8C_4 = 126$$

Sol 25: (A) $100 = (80 + 50 + 30) - n + 5$

$$n = 65$$

People reading exactly 2 magazines

$$= 65 - 3 \times 5 = 50$$

Sol 26: (B) $2(5! - 4! \times 2) = 144$ **Sol 27: (B)**Degree of 5 in prime factorization of ${}^{2002}C_{1001} = 1$ ${}^{2002}C_{1001}$ is clearly divisible by 2

Sol 28: (C) No. of triangles = ${}^nC_3 - [(n(n-4)) + n]$

$$= \frac{n(n-1)(n-2)}{3!} - [(n^2 - 3n)] = 30 \Rightarrow n = 9$$

Sol 29: (B) ${}^{11}C_3 - {}^5C_3 + 1 = 156$

Sol 30: (C)



$$3! + 3 \times 2 \times 2! \cdot {}^4C_3 \times 3! = 18 = 24$$

$$\text{Total no.s} = 18 + 24 = 42$$

Sol 31: (C) $P_n - Q_n$

The difference in P_n & Q_n is the number of ways in which first and last person of the row is selected

$$P_n - Q_n = n - 4 = 6$$

$$n = 10$$

Sol 32: (C) $m = {}^{10}C_4 \times 4!$

$$n = {}^{10}C_4; m = 24 n$$

Sol 33: (C) No. of ways of selecting a committee of 2W and 3M from 5W and 6M

$$= {}^4C_1 \times {}^4C_2 + {}^5C_2 \times {}^5C_2 = 124$$

Sol 34: (D) ABC, ACD, ABD

$$3! + 3! + 3! = 18$$

Sol 35: (D) Ways in which 2 are neighbours

$$= 2 \times 97 + 97 \times 96 = 98 \times 97$$

ways in which all 3 are neighbours = 98

$$\text{Required ways} = {}^{100}C_3 - 98^2 = 152096 = {}^{98}C_3$$

Sol 36: (D) Make 3 groups of boys 1, 1, 2

$$\frac{4!}{2! (1!)^2 2!} \times 3! \text{ ways to distribute}$$

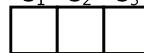
Identical marbles distribution

1 2 2 – 3 ways

1 1 3 – 3 ways

$$\text{Total ways} = \frac{4!}{2! 2!} \times 3! \times 6 = 216$$

Sol 37: (C) $S_1 \quad S_2 \quad S_3$



$$S_1 = S_3 = (2 + 4 + 6 + 8) \times 10 = 200$$

$$S_2 = (0 + 1 + 2 + \dots + 9) \times 4 = 180$$

$$\text{Sum} = 200 + 180 \times 10 + 200 \times 100 = 22000$$

Sol 38: (A) $A_n = {}^nC_{25} \times 25!$

$$A_n - A_{n-1} = 25! ({}^nC_{25} - {}^{n-1}C_{25}) = 25! ({}^{n-1}C_{24})$$

$$n = 50$$

Sol 39: (C) $(x_1 + x_2 + x_3)(y_1 + y_2) = 77 = 7 \times 11$

$$x_1 + x_2 + x_3 = 4 \text{ & } x_1 + x_2 + x_3 = 8$$

$$y_1 + y_2 = 9 \text{ & } y_1 + y_2 = 5$$

No. of possible solutions

$$= {}^6C_2 \times {}^{10}C_1 + {}^{10}C_2 \times {}^6C_1 = 15 \times 10 + 45 \times 6$$

$$= 150 + 270 = 420$$

Sol 40: (B) $m = 34 - 3 = 78$

$$n = 3^4 - [3(2^4 - 2) + 3] = 81 - 45 = 36$$

$$\text{Hence, } \frac{m}{n} = \frac{78}{36} = \frac{13}{6}$$

Sol 41: (A) Sum of digits at units place

$$= (1 + 2 + \dots + 9) \times 3 \times 9 = 45 \times 27 = 1215$$

Sum of digits at ten's place

$$= (1 + 4 + 9) \times 9 \times 9 = 14 \times 81 = 1134$$

Sum of digits at hundred's place

$$= (1 + 2 + \dots + 9) \times 3 \times 9 = 45 \times 27 = 1215$$

$$\begin{array}{r} 1215 \\ 1134 \times \\ \hline 1215 \times \\ 134055 \end{array}$$

Sol 42: (D) 3 possible distribution of wards for each subject.

$$\begin{array}{ccc} 1 & 1 & 4 \\ 1 & 2 & 3 \\ 2 & 2 & 2 \end{array}$$

$$\text{Total ways} = 3! \left(\frac{6!}{4! (1!)^2 2!} + \frac{6!}{1! 2! 3!} + \frac{6!}{(2!)^3 3!} \right) = 540$$

Sol 43: (C) $M = L \times 2!$

$$L = N \quad \therefore 2L = M = 2N$$

Sol 44: (C) There are 11 position

At the 6th position A should be present. In the 5 positions left to 6th positions 2positions will have A.

5C_2 ways

Sol 45: (D) ${}^9C_2 \times {}^7C_3 \times {}^4C_4$

$$(A) \frac{9!}{2! \ 3! \ 4!}$$

$$(D) \frac{9!}{2! \ 3! \ 4!}$$

Multiple Correct Choice Type

Sol 46: (A, B, D) ${}^{n-1}C_{r-1} + {}^{n-1}C_r = {}^nC_r$

Sol 47: (B, C) $2^{10} - 1$

Sol 48: (B, C, D) 2 2 1

$$\frac{5!}{(2!)^2 \ 1! \ 2!} \times 3! = \frac{120}{8} \times 6 = 90$$

Sol 49: (A, B) Let $k = 2n + 1$, then ${}^{2n+1}C_r$ is maximum when $r = n$. Also ${}^{2n+1}C_n = {}^{2n+1}C_{n+1}$. Thus, kC_r is maximum

$$\text{when } r = \frac{1}{2}(k-1) \quad \text{or} \quad r = \frac{1}{2}(k+1)$$

Sol 50: (B, D) (A) 4 vowels, 7 consonants

$${}^7C_2 \times 6! = 3.7!$$

$$(B) \frac{15}{n!(15-x)!} n = \text{no of white balls}$$

$$(C) \frac{12!}{4! \ 5!}$$

$$(D) 35$$

Sol 51: (C, D) BULBUL

$$\frac{6!}{2! \ 2! \ 2!} = 90$$

$$(A) {}^4C_2 \times {}^6C_2 = 6 \times 15 = 90$$

$$(B) \frac{6!}{(2!)^3 \ 3!} = 15$$

$$(C) \frac{6!}{(2!)^3} = 90$$

$$(D) \frac{6!}{(2!)^3 \ 3!} \times 3! = 90$$

Comprehension Type

Sol 52: (C) M I(4) S(4)P(2)

$$(i) {}^2C_1 \times {}^3C_1 = 6$$

$$(ii) {}^2C_1 \times {}^2C_1 = 4$$

$$(iii) {}^2C_1 \times {}^3C_1 = 6$$

$$(iv) {}^3C_2 \times 2 = 6$$

$$(v) {}^3C_1 = 3$$

Adding all these, we get = 25

Sol 53: (B) Total ways in which all vowels are together

$$= \frac{11!}{4! \ 4! \ 2!} - \frac{8!}{4! \ 2!} = \frac{8!}{4! \ 2!} \left(\frac{165}{4} - 1 \right) = \frac{8! \cdot 161}{4 \ 4! \ 2!}$$

$$\text{Sol 54: (B)} {}^6C_2 \times {}^8C_4 \times 5 = 1 \times \left(\frac{10!}{4! \ 4!} \right)$$

$$\text{Sol 55: (A)} \text{ No of ways} = \frac{16!}{(4!)^5}$$

$$= \frac{(1 \times 3 \times 5 \dots \times 15) \times 2^8 \times 8^1}{(4!)^5}$$

$$= \prod_{r=1}^8 (2r-1) \times \frac{2^8 \times 8 \times 7 \times 6 \times 5 \times 4!}{(4!)^5}$$

$$= 35 \prod_{r=1}^8 (2r-1) \times \frac{2^8 \times 48}{(24)^4} = \frac{35}{27} \prod_{r=1}^8 (2r-1)$$

$$\text{Sol 56: (C)} \frac{12!}{(3!)^4 \ 4!} \times 4! = \frac{12 \times 11!}{6^4} = \frac{11!}{108}$$

Match the Columns

Sol 57: A → r; B → s; C → q; D → p

$$(A) {}^nC_m \quad (B) m^n \quad (C) {}^mC_n \quad (D) n^m$$

Sol 58: A → t; B → r; C → p; D → q; E → s

(A) x_1, x_2, x_3 & x_4 are the students watching a particular movie

$$x_1 + x_2 + x_3 + x_4 = 10$$

$$x_i \geq 1$$

$${}^9C_3 = \frac{9 \times 8 \times 7}{6} = 84$$



$$(B) T = {}^9C_3 - 4 = 80$$

$$S = {}^8C_2 = 28$$

$$T - S = 52$$

$$(C) 1 + {}^5C_2 = 11$$

$$(D) 12 = 1 \times 2 \times 2 \times 3 = 1 \times 1 \times 4 \times 3 = 1 \times 1 \times 2 \times 6$$

$$\frac{4!}{2!} + \frac{4!}{2!} + \frac{4!}{2!} = 36$$

$$(E) {}^5C_2 \times {}^3C_2 \times 2 = 10 \times 3 \times 2 = 60$$

$$M_1 M_2 M_1 M_2$$

$$F_1 F_2 F_2 F_1$$

Previous Years' Questions

Sol 1: Since, each box can hold five balls.

∴ Number of ways in which balls could be distributed so that none is empty are (2, 21) or (3, 1, 1).

$$\text{ie, } ({}^5C_2 \cdot {}^3C_2 \cdot {}^1C_1 + {}^5C_3 \cdot {}^2C_1 \cdot {}^1C_1) \times 3!$$

$$= (30 + 20) \times 6 = 300$$

Sol 2: The possible cases are

Case-I: A man invites 3 ladies and women invites 3 gentlemen

$$\text{Number of ways} = {}^4C_3 \cdot {}^4C_3 = 16$$

Case-II: A man invites (2 ladies, 1 gentleman) and women invites (2 gentlemen, 1 lady).

Number of ways

$$= ({}^4C_2 \cdot {}^3C_1) \cdot ({}^3C_1 \cdot {}^4C_1) = 324$$

Case-III: A man invites (1 lady, 2 gentlemen) and women invites (2 ladies, 1 gentleman).

Number of ways

$$= ({}^4C_1 \cdot {}^3C_2) \cdot ({}^3C_2 \cdot {}^4C_1) = 144$$

Case-IV: A man invites (3 gentlemen) and women invites (3 ladies).

$$\text{Number of ways} = {}^3C_3 \cdot {}^3C_3 = 1$$

$$\therefore \text{Total number of ways} = 16 + 324 + 144 + 1 = 485$$

Sol 3: Case-I: When one black and two others ball S are drawn

$$\Rightarrow \text{number of ways} = {}^3C_1 \cdot {}^6C_2 = 45$$

Case-II: When two black and one other balls are drawn

$$\Rightarrow \text{Number of ways} = {}^3C_2 \cdot {}^6C_1 = 18$$

Case-III : When all three black balls are drawn

$$\Rightarrow \text{Number of ways} = {}^3C_3 = 1$$

$$\therefore \text{Total number of ways} = 45 + 18 + 1 = 64$$

Sol 4: Let the two sides be A and B. Assume that four particular guests wish to sit on side A. Four guests who wish to sit on side A can be accommodated on nine chairs in 9P_4 ways and there guests who wish to sit on side B and be accommodated in 9P_3 ways.

Now, the remaining guests are left who can sit on 11 chairs on both the sides of the table in $(11!)$ ways.

Hence, the total number of ways in which 18 persons can be seated $= {}^9P_4 \times {}^9P_3 \times (11)!$.

Sol 5: There are 9 women and 8 men. A committee of 12, consisting of at least 5 women, can be formed by choosing:

(i) 5 women and 7 men

(ii) 6 women and 6 men

(iii) 7 women and 5 men

(iv) 8 women and 4 men

(v) 9 women and 3 men

∴ Total number of ways forming the committee

$$= {}^9C_5 \times {}^8C_7 + {}^9C_6 \times {}^8C_6 + {}^9C_7 \times {}^8C_5 + {}^9C_8 \times {}^8C_4 + {}^9C_9 \times {}^8C_3$$

$$= 126 \times 8 + 84 \times 28 + 36 \times 56 + 9 \times 70 + 1 \times 56 = 6062$$

(i) Clearly, women are in majority in (iii), (iv) and (v) cases as discussed above.

(ii) So, total number of committees in which women are in majority

$$= {}^9C_7 \times {}^8C_5 + {}^9C_8 \times {}^8C_4 + {}^9C_9 \times {}^8C_3$$

$$= 36 \times 56 + 9 \times 70 + 1 \times 56 = 2702$$

Clearly, men are in majority in only (i) case as discussed above.

So, total number of committees in which men are in majority

$$= {}^9C_5 \times {}^8C_7 = 126 \times 8 = 1008$$

Sol 6: A → p; B → s; C → q; D → q

(A) If ENDEA is fixed word, then assume this as a single letter.

Total number of letters = 5

Total number of arrangements = 5!

(B) If E is at first and last places, then total number of permutation of $\frac{7!}{2!} = 21 \times 5!$

(C) If D, L, N are not in last five positions

← D, I, N, N → ← E, E, E, A, O →

Total number of permutation

$$= \frac{4!}{2!} \times \frac{5!}{3!} = 2 \times 5!$$

(D) Total number of odd position = 5

Permutation of AEEEO are $\frac{5!}{3!}$

Total number of even positions = 4

Number of permutations of N, N, D, L = $\frac{4!}{2!}$

Hence, total number of permutation = $\frac{5!}{3!} \times \frac{4!}{2!} = 2 \times 5!$