### CSCI 3104 Fall 2021 Instructors: Profs. Grochow and Waggoner

# Midterm 1- Standard 2

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St	ıdent ID	<b>4326364</b>
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### 1 Instructions

- The solutions **should be typed**, using proper mathematical notation. We cannot accept hand-written solutions. Here's a short intro to LATEX.
- You should submit your work through the **class Canvas page** only. Please submit one PDF file, compiled using this LATEX template.
- You may not need a full page for your solutions; pagebreaks are there to help Gradescope automatically find where each problem is. Even if you do not attempt every problem, please submit this document with no fewer pages than the blank template (or Gradescope has issues with it).
- You may not collaborate with other students. Copying from any source is an Honor Code violation. Furthermore, all submissions must be in your own words and reflect your understanding of the material. If there is any confusion about this policy, it is your responsibility to clarify before the due date.
- Posting to any service including, but not limited to Chegg, Discord, Reddit, StackExchange, etc., for help on an assignment is a violation of the Honor Code.
- You **must** virtually sign the Honor Code (see Section 2). Failure to do so will result in your assignment not being graded.

# 2 Honor Code (Make Sure to Virtually Sign)

## Problem 1.

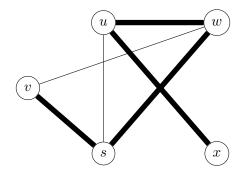
- My submission is in my own words and reflects my understanding of the material.
- I have not collaborated with any other person.
- I have not posted to external services including, but not limited to Chegg, Discord, Reddit, StackExchange, etc.
- I have neither copied nor provided others solutions they can copy.

Agreed	(Abeal Sileshi	agrees).		
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## 3 Standard 2- BFS and DFS

### 3.1 Problem 2

**Problem 2.** Consider the undirected, unweighted graph G = (V, E) with  $V = \{s, u, v, w, x\}$  and  $E = \{su, sv, sw, uw, ux, vw\}$ , and let  $T \subseteq E$  be  $T = \{sv, sw, uw, ux\}$ . This is pictured below with T represented by wide edges.



Carefully explain why T cannot be output by BFS with start vertex s for any choices of iteration order over neighborhoods in the algorithm.

#### Answer.

T cannot be output because when traversing with BFS from s, either v or w will be selected. This is initially fine because  $\{s,v\}$  and  $\{s,w\}$  are both edges in T. But after adding v and w to the queue, it'll pop either v or w. Say it pops v first, v's only unvisited neighbor is w, but  $\{v,w\}$  is not a valid edge in T. The other scenario where BFS fails is if it pops w first. w has unvisited neighbors v and u and if it tries to traverse to v, it won't be a valid vertex in T. This is why T cannot be output by BFS with start vertex s for any choices of iteration order over neighborhoods in the algorithm.