

$$15. T: \mathbb{R}^n \rightarrow \mathbb{R}^2; T \begin{pmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{pmatrix} = \begin{pmatrix} |x_4| \\ x_1 \end{pmatrix}$$

$$16. T: \mathbb{R} \rightarrow \mathbb{R}^n; T(x) = \begin{pmatrix} x \\ x \\ \vdots \\ x \end{pmatrix}$$

$$17. T: \mathbb{R}^4 \rightarrow \mathbb{R}^2; T \begin{pmatrix} x \\ y \\ z \\ w \end{pmatrix} = \begin{pmatrix} x + z \\ y + w \end{pmatrix}$$

$$18. T: \mathbb{R}^2 \rightarrow \mathbb{M}_{22}; T \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} x+y & x-y \\ y-x & 2x \end{pmatrix}$$

$$19. T: M_{nn} \rightarrow M_{nn}; T(A) = AB, \text{ donde } B \text{ es una matriz fija de } n \times n$$

$$20. T: M_{nn} \rightarrow M_{nn}; T(A) = A^T A$$

$$21. T: \mathbb{M}_{pq} \rightarrow \mathbb{M}_{pq}; T(A) = A^T$$

$$22. T: \mathbb{M}_{mn} \rightarrow \mathbb{M}_{qn}; T(A) = BA, \text{ donde } B \text{ es una matriz fija de } q \times m$$

$$23. T: \mathbb{D}_n \rightarrow \mathbb{D}_n; T(A) = A + A', \text{ donde } \mathbb{D}_n \text{ es el conjunto de matrices diagonales de } n \times n.$$

$$24. T: D_5 \rightarrow \mathbb{R}^3; T(D) = \begin{pmatrix} d_{11} + 2d_{33} \\ d_{22} - 3d_{33} \\ d_{35} \end{pmatrix}$$

$$25. T: \mathbb{P}_1 \rightarrow \mathbb{P}_2; T(a_0 + a_1x) = a_1 + a_0x^2$$

$$26. T: \mathbb{P}_2 \rightarrow \mathbb{P}_2; T(a_0 + a_1x + a_2x^2) = a_0a_2x + a_1x^2$$

$$27. T: \mathbb{P}_2 \rightarrow \mathbb{M}_{22}; T(a_0 + a_1x + a_2x^2) = \begin{pmatrix} a_2 + a_1 & a_2 - a_0 \\ a_0 - a_1 & 0 \end{pmatrix}$$

$$28. T: \mathbb{R}^2 \rightarrow \mathbb{P}_4; T \begin{pmatrix} a \\ b \end{pmatrix} = a + bx + (a - b)x^2 + (a + b)x^4$$

$$29. T: \mathbb{P}_2 \rightarrow \mathbb{P}_4; T(p(x)) = (p(x))^2$$

$$30. T: \mathbb{P}_2 \rightarrow \mathbb{P}_4; T(p(x)) = p'(x) + x^2p(x)$$

$$31. T: C[0, 1] \rightarrow C[0, 1]; Tf(x) = f^2(x)$$

$$32. T: C[0, 1] \rightarrow C[0, 1]; Tf(x) = f(x) + 1$$

$$33. T: C[0, 1] \rightarrow C[0, 1]; Tf(x) = x^2f(x) + xf(x)$$

$$34. T: C[0, 1] \rightarrow \mathbb{R}; Tf = \int_0^1 f(x)g(x) dx, \text{ donde } g \text{ es una función fija en } C[0, 1]$$

$$35. T: C^1(0, 1) \rightarrow C(0, 1); T(f(x)) = (x^2p(x))'$$

$$36. T: C[0, 1] \rightarrow C[1, 2]; Tf(x) = f(x - 1)$$

$$37. T: C[0, 1] \rightarrow \mathbb{R}; Tf = f\left(\frac{1}{2}\right)$$

$$38. T: C^1(0, 1) \rightarrow \mathbb{R}; T(f) = f'\left(\frac{1}{3}\right)$$

$$39. T: \mathbb{M}_{nn} \rightarrow \mathbb{R}; T(A) = \det A$$

$$40. \text{ Sea } T: \mathbb{R}^2 \rightarrow \mathbb{R}^2 \text{ dado por } T(x, y) = (-x, -y). \text{ Describe } T \text{ geométricamente.}$$