42.
$$A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{pmatrix}, B = \begin{pmatrix} -5 & -6 \\ 3 & 4 \\ 5 & 6 \end{pmatrix}$$

42.
$$A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{pmatrix}, B = \begin{pmatrix} -5 & -6 \\ 3 & 4 \\ 5 & 6 \end{pmatrix}$$
 43. $A = \begin{pmatrix} 4 & 2 & 1 \\ -1 & 5 & -1 \\ 2 & 7 & -6 \end{pmatrix}, B = \begin{pmatrix} 3 & 7 & 0 \\ -1 & 5 & -1 \\ 2 & 7 & -6 \end{pmatrix}$

44.
$$A = \begin{pmatrix} 1 & 2 & 5 & 2 \\ 0 & -1 & 3 & 4 \\ 5 & 0 & -2 & 7 \end{pmatrix}, B = \begin{pmatrix} 1 & 0 & 11 & 10 \\ 0 & -1 & 3 & 4 \\ 5 & 0 & -2 & 7 \end{pmatrix}$$

45.
$$A = \begin{pmatrix} a & b \\ g & d \end{pmatrix}, B = \begin{pmatrix} g & d \\ a & b \end{pmatrix}$$

46.
$$A = \begin{pmatrix} \alpha & \beta \\ \gamma & \delta \\ \varepsilon & \zeta \\ \iota & \kappa \end{pmatrix}, B = \begin{pmatrix} \alpha & \beta \\ \gamma & \delta \\ -4\gamma + \varepsilon & -4\delta + \zeta \\ \iota & \kappa \end{pmatrix}$$

De los problemas 47 a 63 encuentre la inversa de la matriz elemental dada.

47.
$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

48.
$$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

47.
$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$
 48. $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$ **49.** $\begin{pmatrix} 1 & 0 \\ -3 & 1 \end{pmatrix}$

50.
$$\begin{pmatrix} 4 & 0 \\ 0 & 1 \end{pmatrix}$$

51.
$$\begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$$

52.
$$\begin{pmatrix} 1 & 0 & -5 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

51.
$$\begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$$
 52. $\begin{pmatrix} 1 & 0 & -5 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$ **53.** $\begin{pmatrix} 1 & -2 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$ **54.** $\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 3 \\ 0 & 0 & 1 \end{pmatrix}$

$$\mathbf{54.} \quad \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 3 \\ 0 & 0 & 1 \end{pmatrix}$$

$$55. \begin{pmatrix} 1 & 0 & 0 \\ -7 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\mathbf{56.} \begin{pmatrix} 1 & 0 & -a \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

57.
$$\begin{pmatrix} -\frac{2}{9} & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$58. \begin{pmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\mathbf{59.} \quad \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & b & 0 & 1 \end{pmatrix}$$

$$\mathbf{60.} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & -3 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\begin{array}{ccccc}
\mathbf{61.} & \begin{pmatrix}
0 & 0 & 0 & 1 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & 0 \\
1 & 0 & 0 & 0
\end{pmatrix}$$

$$\mathbf{63.} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ -6 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

De los problemas 64 a 73 demuestre que cada matriz es invertible y escríbala como un producto de matrices elementales.

64.
$$\begin{pmatrix} 2 & 1 \\ 3 & 2 \end{pmatrix}$$

65.
$$\begin{pmatrix} -3 & 1 \\ 1 & -2 \end{pmatrix}$$

66.
$$\begin{pmatrix} 1 & 1 & 1 \\ 0 & 2 & 3 \\ 5 & 5 & 1 \end{pmatrix}$$

67.
$$\begin{pmatrix} 1 & 0 & -a \\ 0 & 1 & 0 \\ -a & 0 & 0 \end{pmatrix}$$

68.
$$\begin{pmatrix} 1 & 0 & 2 \\ 0 & 1 & 0 \\ \frac{1}{2} & 0 & 1 \end{pmatrix}$$

69.
$$\begin{pmatrix} \frac{13}{4} & 3 & 0 \\ 1 & 1 & 0 \\ 2 & -3 & 1 \end{pmatrix}$$