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Jawaban soal

No. 1.

```
[4]: #No: 1. Transfer fungsi
import numpy as np
import matplotlib.pyplot as plt
import control as ctrl

num = [4]
den = [3, 2, 1]
H = ctrl.tf(num, den)
print("Transfer Function H(s):")
print(H)

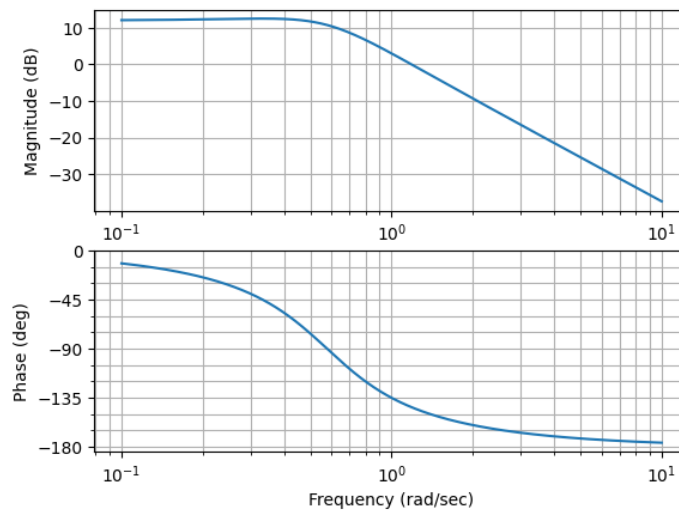
# Plot respon frekuensi
plt.figure()
ctrl.bode(H, dB=True)
plt.suptitle("Bode Plot H(s) = 4/(3s^2 + 2s + 1)")
plt.show()

# Cek kestabilan
poles = ctrl.pole(H)
print("Poles:", poles)
if np.all(np.real(poles) < 0):
    print("Sistem stabil karena semua pole berada di sisi kiri bidang s.")
else:
    print("Sistem tidak stabil karena terdapat pole di sisi kanan bidang s.")
```

Transfer Function H(s):

$$\frac{4}{3s^2 + 2s + 1}$$

Bode Plot $H(s) = 4/(3s^2 + 2s + 1)$

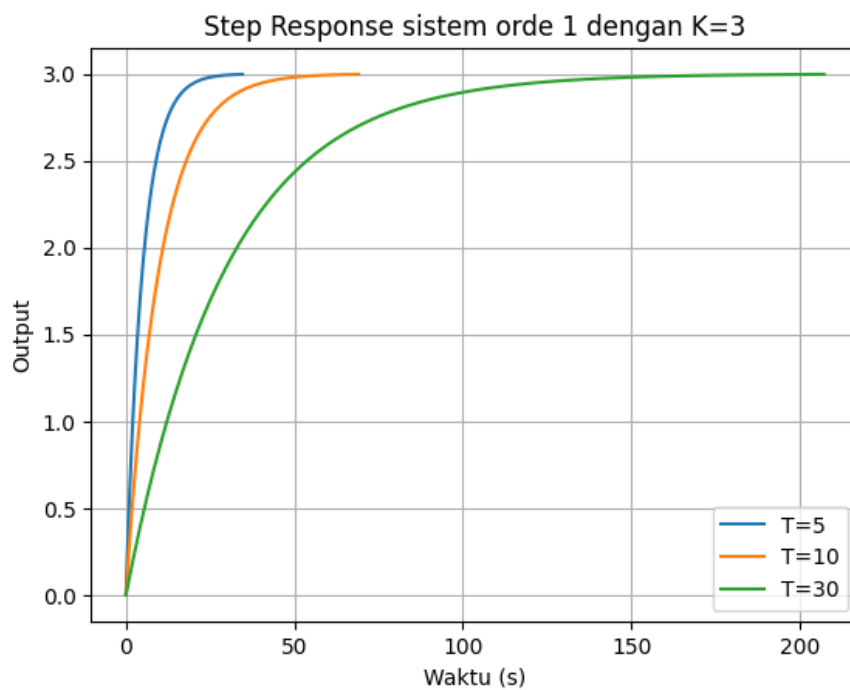


Poles: $[-0.33333333+0.47140452j \ -0.33333333-0.47140452j]$
Sistem stabil karena semua pole berada di sisi kiri bidang s.

Jawaban soal

No. 2

```
[3]: # No: 2. Step Response untuk sistem orde 1
# =====
K = 3
T_values = [5, 10, 30]
plt.figure()
for T in T_values:
    sys = ctrl.tf([K], [T, 1])
    t, y = ctrl.step_response(sys)
    plt.plot(t, y, label=f"T={T}")
plt.title("Step Response sistem orde 1 dengan K=3")
plt.xlabel("Waktu (s)")
plt.ylabel("Output")
plt.legend()
plt.grid()
plt.show()
```



Jawaban soal

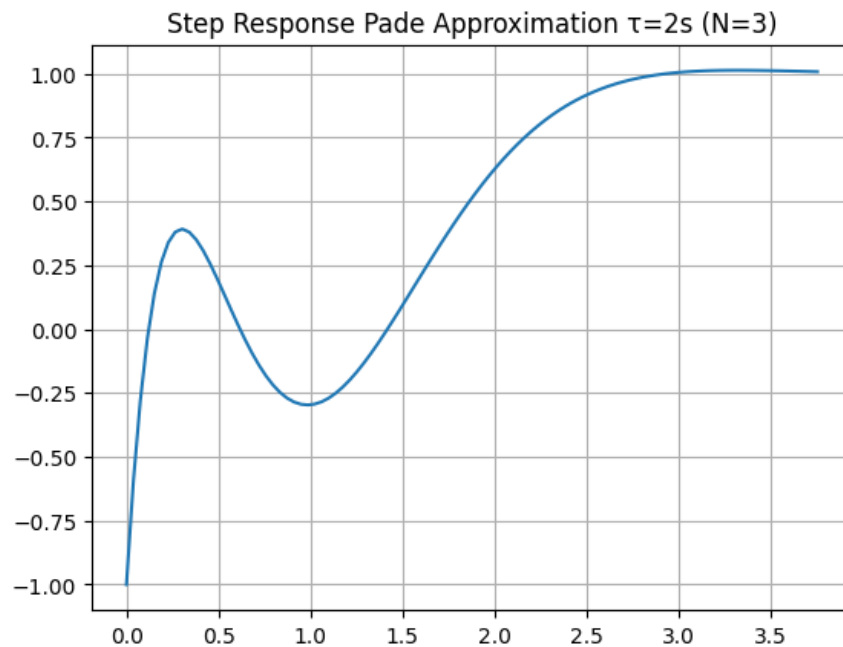
no.3

```
[5]: # No: 3. Pade Approximation ( $\tau = 2s$ ,  $N=3$ )
# =====
tau = 2
num_pade, den_pade = ctrl.pade(tau, 3)
delay_approx = ctrl.tf(num_pade, den_pade)
print("Pade Approximation  $\tau=2s$  orde  $N=3$ :")
print(delay_approx)

t, y = ctrl.step_response(delay_approx)
plt.figure()
plt.plot(t, y)
plt.title("Step Response Pade Approximation  $\tau=2s$  ( $N=3$ )")
plt.grid()
plt.show()
```

Pade Approximation $\tau=2s$ orde $N=3$:

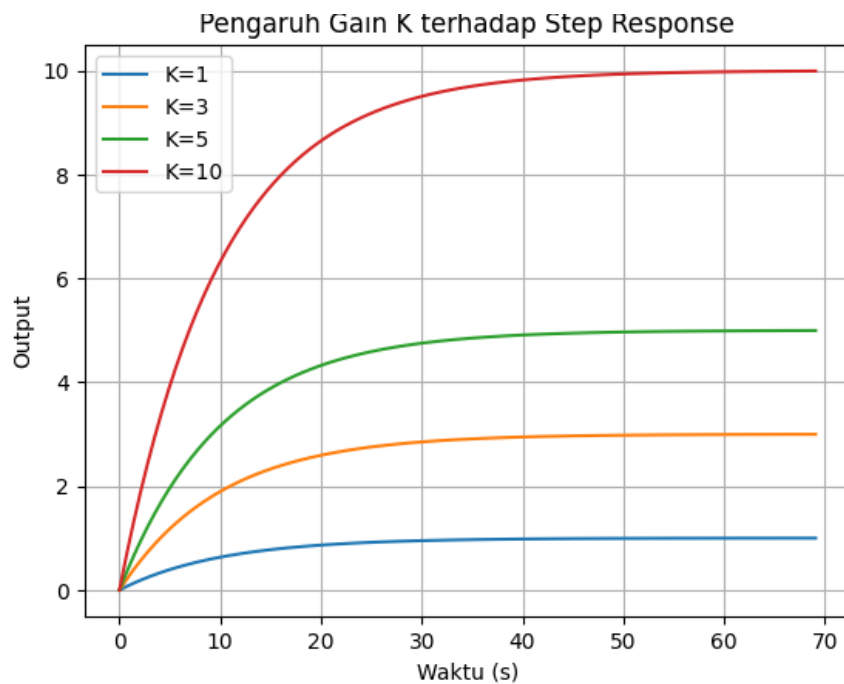
$$\frac{-s^3 + 6s^2 - 15s + 15}{s^3 + 6s^2 + 15s + 15}$$



Jawaban soal

no. 4

```
[6]: #No: 4. Pengaruh K (Gain) terhadap Step Response
# =====
K_values = [1, 3, 5, 10]
plt.figure()
for K in K_values:
    sys = ctrl.tf([K], [10, 1])
    t, y = ctrl.step_response(sys)
    plt.plot(t, y, label=f"K={K}")
plt.title("Pengaruh Gain K terhadap Step Response")
plt.xlabel("Waktu (s)")
plt.ylabel("Output")
plt.legend()
plt.grid()
plt.show()
```



Jawaban Soal

no. 5

```

•[7]: #No: 5. Pole-Zero Map dan Stabilitas
# =====
num = [1, 1]
den = [3, 1, 4, 1]
H = ctrl.tf(num, den)
print("H(s) =", H)

# a. Poles dan zeros
poles = ctrl.pole(H)
zeros = ctrl.zero(H)
print("Poles =", poles)
print("Zeros =", zeros)

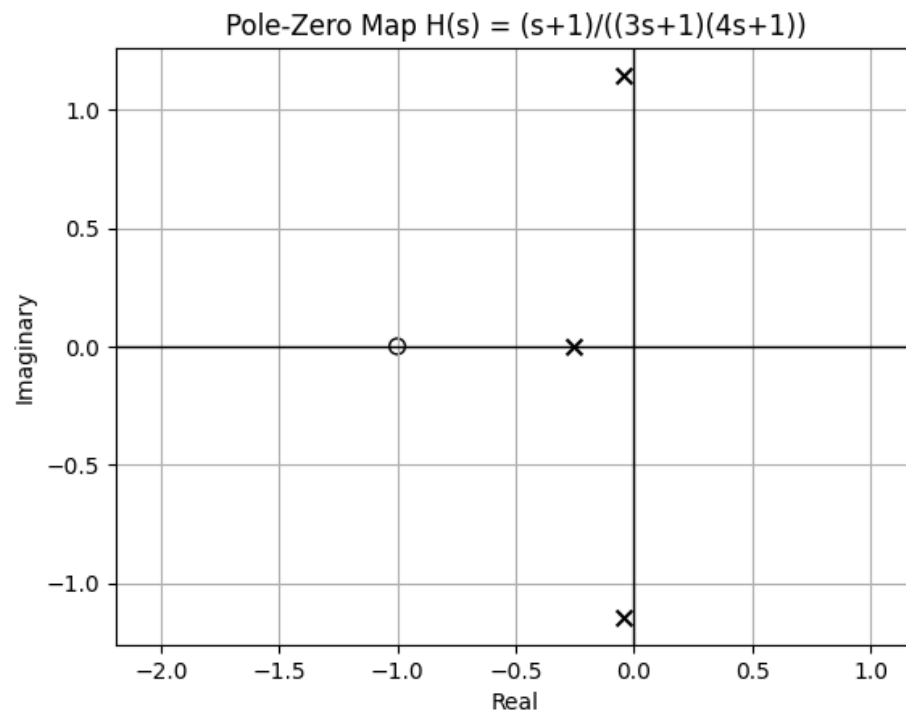
# b. Pole-zero map
plt.figure()
ctrl.pzmap(H, title="Pole-Zero Map H(s) = (s+1)/((3s+1)(4s+1))")
plt.grid()
plt.show()

# c. Interpretasi kestabilan
if np.all(np.real(poles) < 0):
    print("Sistem stabil karena semua pole di sisi kiri bidang s.")
else:
    print("Sistem tidak stabil karena ada pole di sisi kanan.")

```

$$H(s) = \frac{s + 1}{3s^3 + s^2 + 4s + 1}$$

Poles = [-0.03974588+1.14524027j -0.03974588-1.14524027j -0.25384157+0.j]
Zeros = [-1.+0.j]



Sistem stabil karena semua pole di sisi kiri bidang s.

Jawaban Soal

no.6

```

•[8]: # No: 6. State Space Model
# =====
A = np.array([[0, 1],
              [-1, 0]])
B = np.array([[0],
              [1]])
C = np.array([[1, 0]])
D = np.array([[0]])

sys_ss = ctrl.ss(A, B, C, D)
print("Model State-Space (A,B,C,D):\n", sys_ss)

# Step response
t, y = ctrl.step_response(sys_ss)
plt.figure()
plt.plot(t, y)
plt.title("Step Response dari Model State Space")
plt.xlabel("Waktu (s)")
plt.ylabel("Output y(t)")
plt.grid()
plt.show()

# Interpretasi stabilitas
eig_values = np.linalg.eigvals(A)
print("Eigenvalue =", eig_values)
if np.all(np.real(eig_values) < 0):
    print("Sistem stabil.")
else:
    print("Sistem tidak stabil (osilasi / marginally stable).")

```

```

Model State-Space (A,B,C,D):
<LinearIOSystem>: sys[31]
Inputs (1): ['u[0]']
Outputs (1): ['y[0]']
States (2): ['x[0]', 'x[1]']

```

```

A = [[ 0.  1.]
      [-1.  0.]]

```

```

B = [[0.]
      [1.]]

```

```

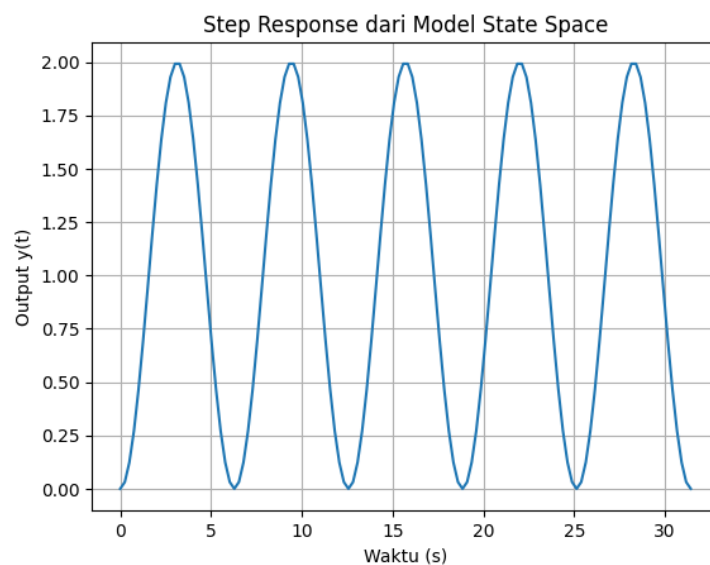
C = [[1.  0.]]

```

```

D = [[0.]]

```



```

Eigenvalue = [0.+1.j 0.-1.j]
Sistem tidak stabil (osilasi / marginally stable).

```

Jawaban Soal

no.7

```
[9]: #No: 7. State-Space → Transfer Function
# =====
A = np.array([[0, 1],
              [-1, -3]])
B = np.array([[0],
              [1]])
C = np.array([[1, 0]])
D = np.array([[0]])

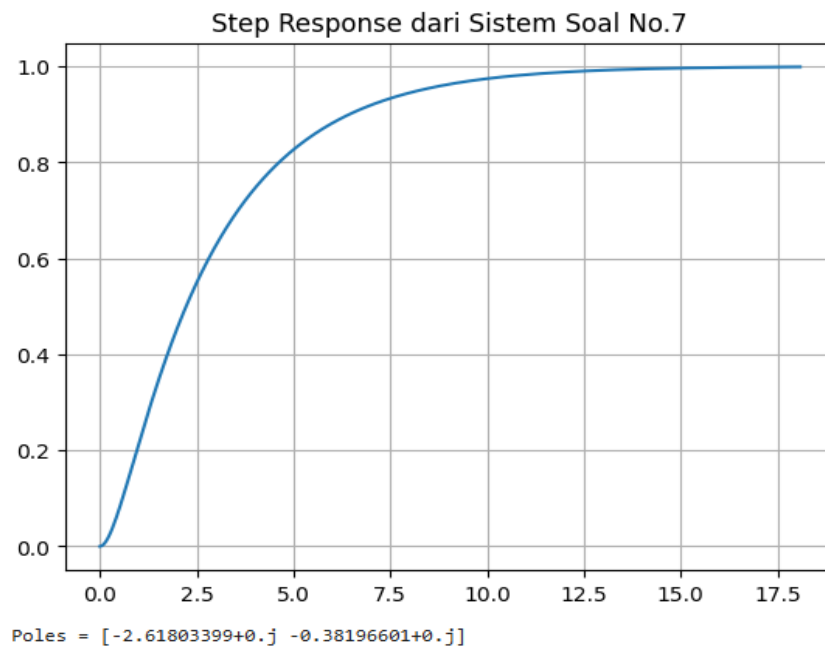
sys_ss2 = ctrl.ss(A, B, C, D)
sys_tf = ctrl.ss2tf(sys_ss2)
print("Transfer Function hasil konversi dari State-Space:")
print(sys_tf)

# Step response
t, y = ctrl.step_response(sys_tf)
plt.figure()
plt.plot(t, y)
plt.title("Step Response dari Sistem Soal No.7")
plt.grid()
plt.show()

# Cek stabilitas
poles = ctrl.pole(sys_tf)
print("Poles =", poles)
```

Transfer Function hasil konversi dari State-Space:

$$\frac{1}{s^2 + 3s + 1}$$



Jawaban Soal

no.8

```
[10]: #No: 8. Discrete System (Euler method)
# =====
Ts = 0.1
sys_d = ctrl.c2d(sys_ss2, Ts, method='euler')
print("Model Diskrit (Euler, Ts=0.1):\n", sys_d)

t, y = ctrl.step_response(sys_d)
plt.figure()
plt.step(t, y)
plt.title("Step Response Sistem Diskrit (Euler, Ts=0.1)")
plt.grid()
plt.show()
```

```

Model Diskrit (Euler, Ts=0.1):
  <LinearIOSystem>: sys[32]$sampled
Inputs (1): ['u[0]']
Outputs (1): ['y[0]']
States (2): ['x[0]', 'x[1]']

A = [[ 1.    0.1]
      [-0.1  0.7]]

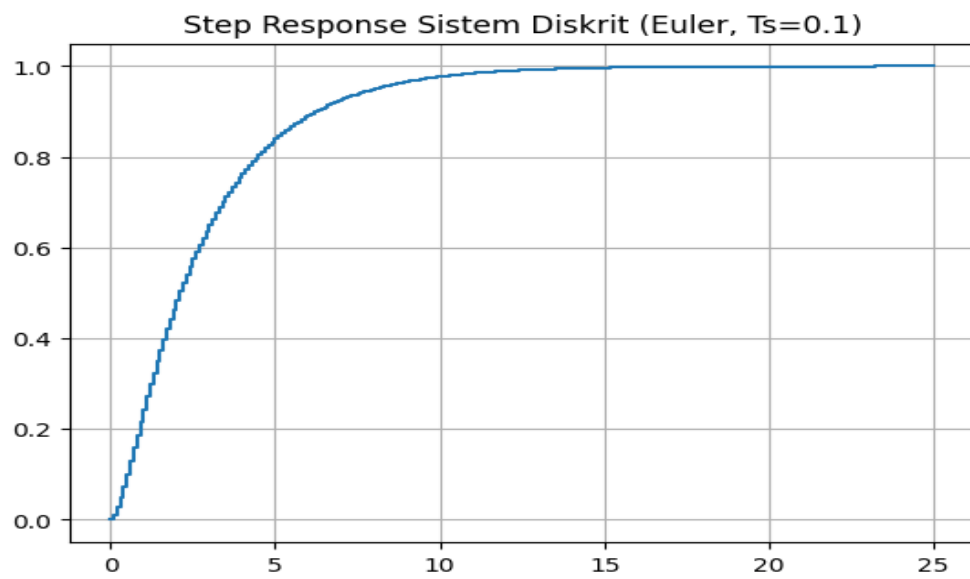
B = [[0. ]
      [0.1]]

C = [[1. 0.]]

D = [[0.]]

dt = 0.1

```



Jawaban Soal

no.9

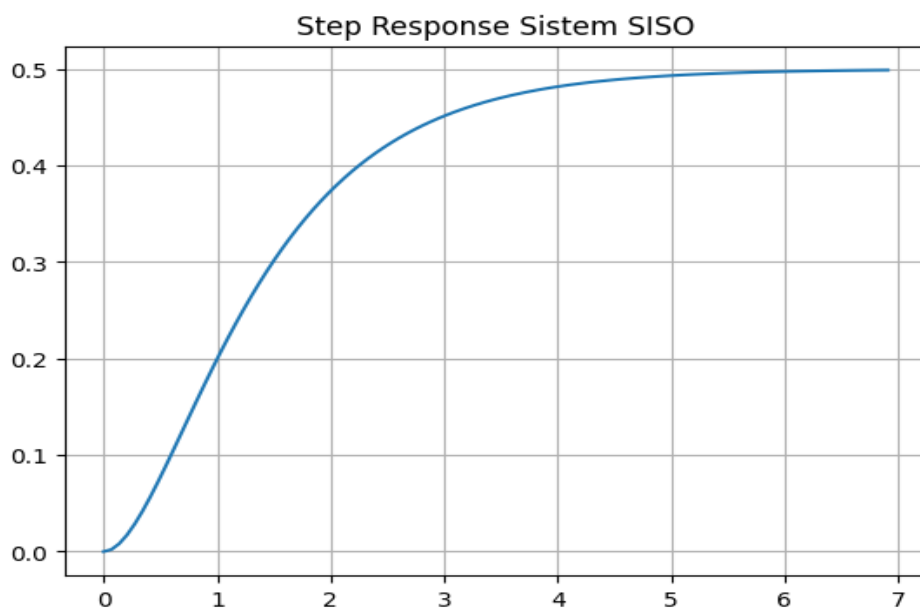
```
[11]: #No: 9. Single Input Single Output (SISO)
# =====
A = np.array([[0, 1],
              [-2, -3]])
B = np.array([[0],
              [1]])
C = np.array([[1, 0]])
D = 0

sys_asiso = ctrl.ss(A, B, C, D)
H_asiso = ctrl.ss2tf(sys_asiso)
print("Transfer Function H(s) untuk SISO:")
print(H_asiso)

t, y = ctrl.step_response(sys_asiso)
plt.figure()
plt.plot(t, y)
plt.title("Step Response Sistem SISO")
plt.grid()
plt.show()
```

Transfer Function H(s) untuk SISO:

$$\frac{8.882e-16 s + 1}{s^2 + 3 s + 2}$$



Jawaban Soal

no.10

[12]: #No: 10. Multiple Input Single Output (MISO)

```
# =====
A = np.array([[0, 1],
              [-1, -3]])
B = np.array([[0, 1],
              [2, 4]])
C = np.array([[1, 0]])
D = np.array([[0, 0]])

sys_miso = ctrl.ss(A, B, C, D)
print("Model MISO (A,B,C,D):\n", sys_miso)

# Dua transfer function masing-masing input
H1 = ctrl.ss2tf(A, B[:, [0]], C, 0)
H2 = ctrl.ss2tf(A, B[:, [1]], C, 0)
print("H1(s):", H1)
print("H2(s):", H2)

# Bandingkan step response
t, y1 = ctrl.step_response(H1)
_, y2 = ctrl.step_response(H2)
plt.figure()
plt.plot(t, y1, label="Input 1 → Output")
plt.plot(t, y2, label="Input 2 → Output")
plt.title("Perbandingan Step Response H1(s) dan H2(s)")
plt.legend()
plt.grid()
plt.show()
```

```
Model MISO (A,B,C,D):
<LinearIOSystem>: sys[39]
Inputs (2): ['u[0]', 'u[1]']
Outputs (1): ['y[0]']
States (2): ['x[0]', 'x[1]']
```

```
A = [[ 0.  1.]
      [-1. -3.]]
```

```
B = [[0. 1.]
      [2. 4.]]
```

```
C = [[1. 0.]]
```

```
D = [[0. 0.]]
```

```
H1(s):
8.882e-16 s + 2
-----
s^2 + 3 s + 1
```

```
H2(s):
      s + 7
-----
s^2 + 3 s + 1
```

```
C:\Users\mahasiswa\AppData\Local\Programs\Python\Python311\Lib\site-packages\scipy\signal\_filter_design.py:1746: BadCoefficients: Badly conditioned filter coefficients (numerator): the results may be meaningless
warnings.warn("Badly conditioned filter coefficients (numerator): the "
```

```
ValueError                                Traceback (most recent call last)
```

```
Cell In[12], line 24
    22 plt.figure()
    23 plt.plot(t, y1, label="Input 1 → Output")
--> 24 plt.plot(t, y2, label="Input 2 → Output")
    25 plt.title("Perbandingan Step Response H1(s) dan H2(s)")
    26 plt.legend()
```

```
File ~\AppData\Local\Programs\Python\Python311\Lib\site-packages\matplotlib\pyplot.py:3575, in plot(scalex, scaley, data, *args, **kwargs)
    3567 @_copy_docstring_and_deprecators(Axes.plot)
    3568 def plot(
    3569     *args: float | ArrayLike | str,
    3570     (...)
    3571     **kwargs,
```

```

3567 @_copy_docstring_and_deprecators(Axes.plot)
3568 def plot(
3569     *args: float | ArrayLike | str,
3570     (...)
3571     **kwargs,
3572 ) -> list[Line2D]:
-> 3575     return gca().plot(
3576         *args,
3577         scalex=scalex,
3578         scaley=scaley,
3579         **({"data": data} if data is not None else {}),
3580         **kwargs,
3581     )

```

File ~\AppData\Local\Programs\Python\Python311\Lib\site-packages\matplotlib\axes_axes.py:1721, in Axes.plot(self, scalex, scaley, data, *args, **kwargs)

```

1478 """
1479 Plot y versus x as lines and/or markers.
1480 (...)
1481 ('green') or hex strings ('#008000').
1482 """
1483 kwargs = cbook.normalize_kwargs(kwargs, mlines.Line2D)
-> 1721 lines = [*self._get_lines(self, *args, data=data, **kwargs)]
1722 for line in lines:
1723     self.add_line(line)

```

File ~\AppData\Local\Programs\Python\Python311\Lib\site-packages\matplotlib\axes_base.py:303, in _process_plot_var_args.__call__(self, axes, data, *args, **kwargs)

```

301     this += args[0],
302     args = args[1:]
-> 303 yield from self._plot_args(
304     axes, this, kwargs, ambiguous_fmt_datakey=ambiguous_fmt_datakey)

```

File ~\AppData\Local\Programs\Python\Python311\Lib\site-packages\matplotlib\axes_base.py:499, in _process_plot_var_args._plot_args(self, axes, tup, kwargs, return_kwargs, ambiguous_fmt_datakey)

```

496     axes.yaxis.update_units(y)
497 if x.shape[0] != y.shape[0]:
-> 499     raise ValueError(f"x and y must have same first dimension, but "
500                       f"have shapes {x.shape} and {y.shape}")
501 if x.ndim > 2 or y.ndim > 2:
502     raise ValueError(f"x and y can be no greater than 2D, but have "
503                       f"shapes {x.shape} and {y.shape}")

```

ValueError: x and y must have same first dimension, but have shapes (344,) and (100,)

