Using Iris for Program Verification

Abel Nieto

March 27, 2020

1 Monotone Counter

 ${\color{red} \triangleright}\ \mathbf{Coq}\ \mathbf{code:}\ \mathtt{https://github.com/abeln/iris-practice/blob/master/counter.v} \mathrel{\vartriangleleft}$

This is the counter example from Section 7.7 of the notes. The module exports three methods:

 newCounter creates a new counter. Counters are represented simply with an int reference.

```
Definition newCounter : val := \lambda: <>, ref #0.
```

• read returns the value currently stored in a counter.

```
Definition read : val := \lambda: "c", !"c".
```

• incr takes a counter, increments it, and returns unit.

```
Definition incr : val :=
  rec: "incr" "c" :=
  let: "n" := !"c" in
  let: "m" := #1 + "n" in
  if: CAS "c" "n" "m" then #() else "incr" "c".
```

The client for the counter is a program that instantiates a counter, spawns two threads each incrementing the counter, and then reads the value off the counter:

```
Definition client : val :=
  \lambda: <>,
   let: "c" := newCounter #() in
   ((incr "c") ||| (incr "c")) ;;
  read "c".
```

1.1 Specs

We can prove two different specs for the code above:

• Authoritative RA

In the first spec, our resource algebra is AUTH(\mathbb{N}). Elements of this RA are of the form either $\bullet n$ (authoritative) or $\circ n$ (non-authoritative), where $n \in \mathbb{N}$.

The important properties of this RA (for the counter example) are:

- $-\bullet 0\cdot \circ 0\in \mathcal{V}$
- $-\bullet m \cdot \circ n \in \mathcal{V} \text{ implies } m \geq n$
- $-\bullet m \cdot \circ n \leadsto \bullet (m+1) \cdot \circ (n+1)$
- $-\mid \circ n \mid = \circ n$

Then we can define our predicate for the counter:

$$isCounter(l, n, \gamma) = \left[\circ \bar{n} \right]^{\gamma \gamma} * \exists s. \quad \exists m.l \hookrightarrow m \land \left[\bar{\bullet} \bar{m} \right]^{\gamma \gamma}$$

This predicate is persistent because the invariant component is persistent and $\circ n$ is also persistent (via the Persistently-core rule), because the core of $\circ n$ is $\circ n$ itself.

The intuition behind the predicate is that if we own is Counter (l, n, γ) then, at an atomic step (e.g. a load), we can know that l is allocated and it points to a value that's $\geq n$.

Additionally, after an increment, we can update the resource to is Counter $(l, n+1, \gamma)$.

We then prove the following specs for the counter methods:

- $\{ \top \}$ newCounter () $\{ l. \exists \gamma. isCounter(l, 0, \gamma) \}$
- {isCounter (l, n, γ) } read l { $v.v \ge n$ }. Notice how we don't have to give the counter back, because it's persistent.
- {isCounter (l, n, γ) } incr l {isCounter $(l, n + 1, \gamma)$ }

We can also prove the client spec:

$$\{\top\}$$
client $()\{n.n \ge 1\}$

The "problem" with this specification *isCounter* doesn't tell us anything about what other threads are doing with the counter. So in the verification of the client code, after both threads return, we know

$$isCounter(l, 1, \gamma) * isCounter(l, 1, \gamma) \equiv isCounter(l, 1, \gamma)$$

So we know that the counter must be ≥ 1 , but we don't know that it's 2.

• Authoritative RA + Fractions

The second spec we can give is more precise, and allows us to conclude that the client reads exactly 2 once the two threads finish.

The resource algebra we use is $Auth((\mathbb{Q}_p \times \mathbb{N})_?)$:

- $-\mathbb{Q}_p$ is the RA of positive fractions, where the valid elements are those ≤ 1 .
- The ? is the *optional RA* construction. In this case, it's needed because to use the authoritative RA we need the argument algebra to be *unital*. And $\mathbb{Q}_p \times \mathbb{N}$ is not unital because 0 is not an element of \mathbb{Q}_p .

The important properties of this RA are:

- $-\circ(1,0)\cdot\bullet(1,0)\in\mathcal{V}$
- $-\circ(p,n)\cdot\bullet(1,m)\in\mathcal{V}$ implies $m\geq n$
- $-\circ(1,n)\cdot\bullet(1,m)\in\mathcal{V}$ implies m=n. This is the rule that will allows us to give a more precise specification.
- $-\circ(p,n)\cdot\bullet(q,m)\leadsto\circ(p,n+1)\cdot\bullet(q,m+1)$

With this RA, we get the new counter resource

$$isCounter(l,n,p,\gamma) = \left[\circ(p,n) \right]^{\gamma} * \exists s. \quad \exists m.l \hookrightarrow m \land \left[\bullet(1,m) \right]$$

This resource is no longer persistent, because the core |p| is undefined. However, we can show the following

$$isCounter(l, n + m, p + q, \gamma) \dashv \vdash isCounter(l, n, p, \gamma) * isCounter(l, m, q, \gamma)$$

We then prove the following specs for the counter methods:

- $\{\top\}$ newCounter () $\{l.\exists \gamma. isCounter(l, 0, 1, \gamma)\}$
- {isCounter (l, n, p, γ) } read l { $v.v \ge n *$ isCounter(l, n, p,)}. Notice how we need to give back the counter in this case.
- {isCounter $(l, n, 1, \gamma)$ } read l {v.v = n * isCounter(l, n, p,)}. Notice that since we have the entire fraction, we can get the exact value of the counter.
- {isCounter (l, n, p, γ) } incr l {isCounter $(l, n + 1, p, \gamma)$ }

With this, we get the more precise client spec

$$\{\top\}$$
client $()\{n.n=2\}$

2 Locks and Coarse-Grained Bags

▷ Coq code: https://github.com/abeln/iris-practice/blob/master/lock.v ◁

This is the spin lock example from Section 7.6 of the notes. The spin lock is a module with three methods:

- newlock creates a new lock. Locks are represented as a reference to a boolean. If false, the lock is free; if true, then it's taken.
- acquire uses a CAS cycle to spin until it can acquire the lock.
- release just sets the lock to false.

The code is as above:

```
Definition newlock : val := \lam: <>, ref #false.

Definition acquire : val :=
   rec: "acquire" "l" :=
    if: CAS "l" #false #true then #() else "acquire" "l".

Definition release : val := \lam: "l", "l" <- #false.</pre>
```

2.1 Spec

The involved RA is EX(UNIT).

- Notice that unlike other RA constructions, Ex(S) just requires S to be a set, as opposed to another RA.
- The exclusive RA is defined by adding an element \bot to the carrier set. For any two elements $x, y \ne \bot$, we have $x \cdot y = \bot$. Every element except for \bot is valid.
- What this means is that if we own $\lceil \bar{x} \rceil^{\gamma\gamma}$, no other thread can own another $\lceil \bar{y} \rceil^{\gamma\gamma}$, because their product would be invalid.

The lock predicate is then

$$\mathrm{isLock}(l,P,\gamma) = \exists s \boxed{l \hookrightarrow \mathtt{false} \land P \land \mathtt{()} \lor l \hookrightarrow \mathtt{true}}^{s}$$

A first observation is that the lock protects an arbitrary predicate P, which is what the client uses to prove its correctness.

The intuition is the following:

- If the lock is unlocked ($l \hookrightarrow \mathtt{false}$), then we need to give away to the invariant the predicate P protected by the lock and the key (). Because () $\in \mathrm{Ex}(\mathrm{Unit})$, we know that no other key can be created.
- When the lock is *locked* ($l \hookrightarrow \mathsf{true}$), we don't need to give away any resources.

- When the lock transitions from unlocked to locked, we gain resources.
- When the lock transitions from locked to unlocked, we *lose* resources.

The last two points are reflected in the specs for the lock methods:

• $\{P\}$ newlock $()\{l.\exists \gamma.isLock(l,P,\gamma)\}.$

Notice that even though only one element of Ex(UNIT) is allowed, this restriction is $per\ location/ghost\ name$, so we're allowed to allocate a new (exclusive) ghost resource, proviced we furnish a new ghost name γ .

- {isLock (l, P, γ) }acquire $l\{P*()\}$ After acquiring the lock, we gain ownership of the predicate P and the key ().
- {isLock(l, P, γ) * P * ()}release $l\{\top\}$ To release the lock, we need to show that P continues to hold, and that we have the key ().

Also note that the lock predicate is *persistent*, since it's protected inside an invariant. This is important because multiple threads need to know that a given lock exists (so they can synchronize).

2.2 Client: Coarsed-Grained Bags