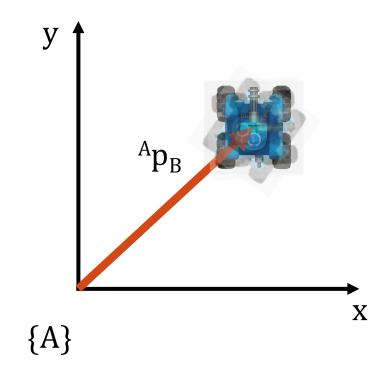
INTRODUCTION TO ROBOTICS

Lecture 04



POSITION



 $^{A}p_{\mathrm{B}}$

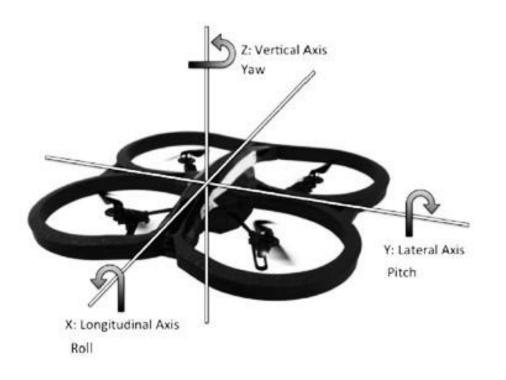
POSE IN 2D

describes the position and orientation

 (x, y, θ)

POSE IN 3D

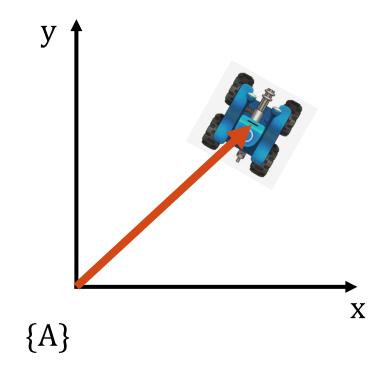




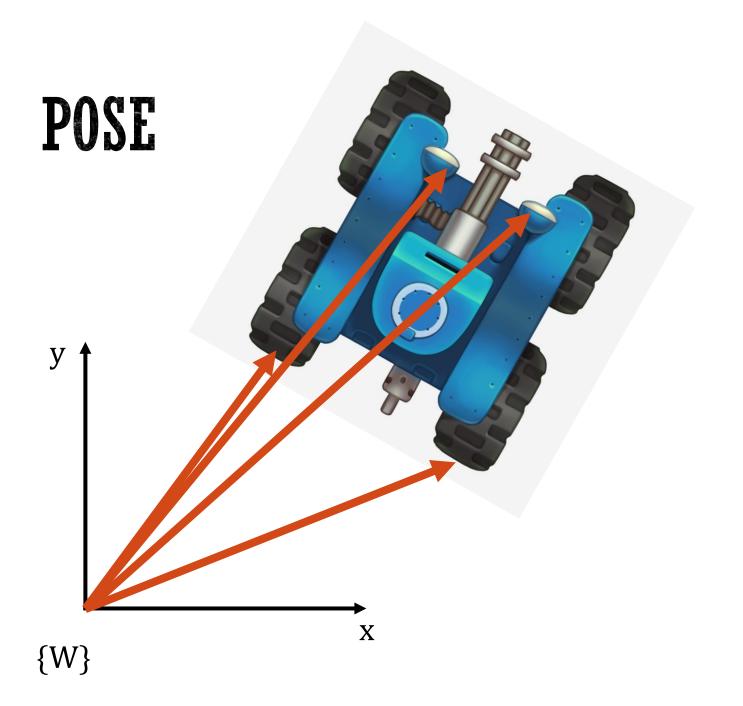
POSE IN 3D

To completely describe the pose of a rigid object in a 3-dimensional world we need 6 not 3 dimensions: 3 to describe its position and 3 to describe its orientation.

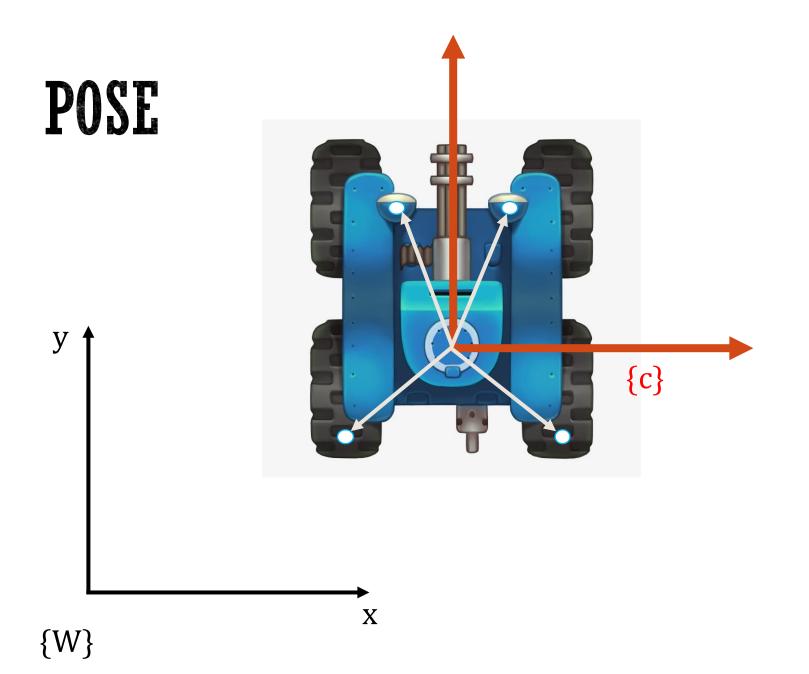
POSE

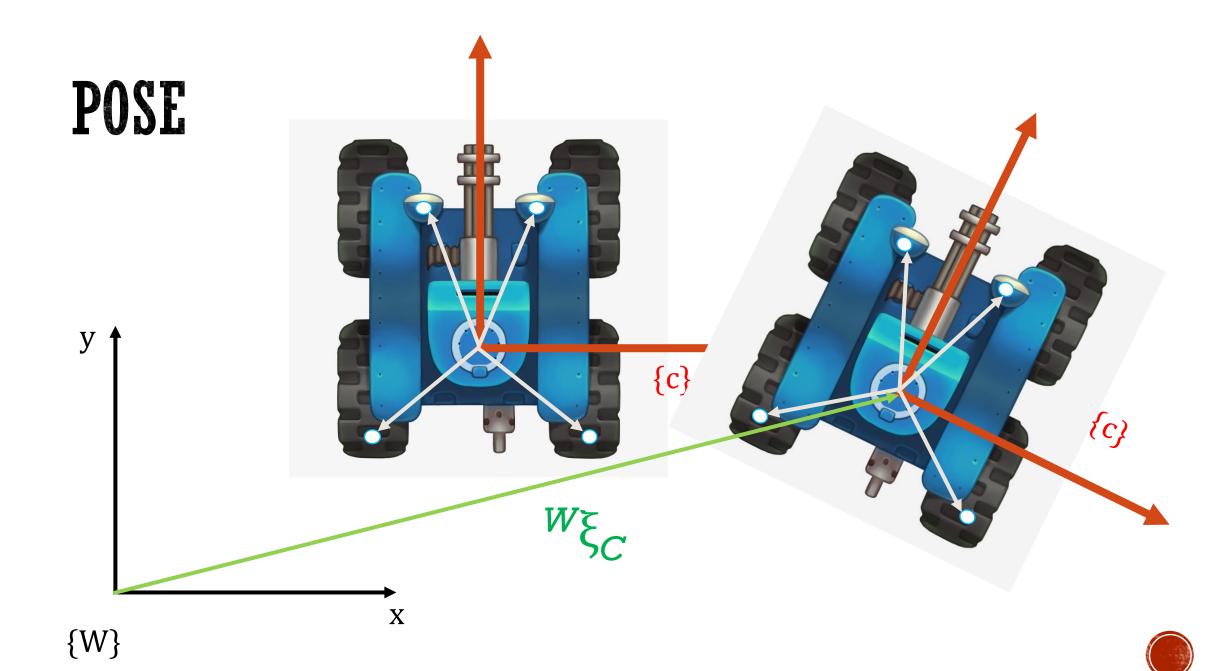


$$A\xi_B$$

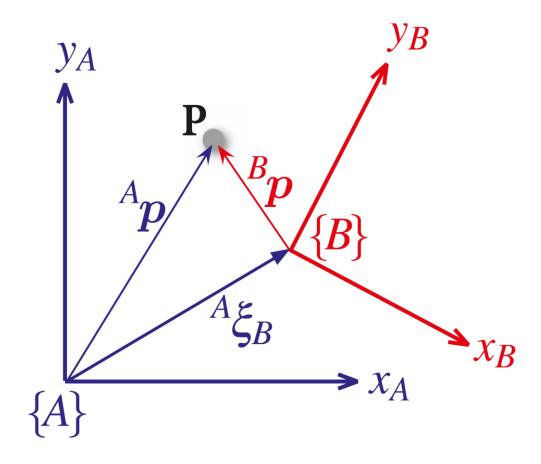


 $W\xi_B$

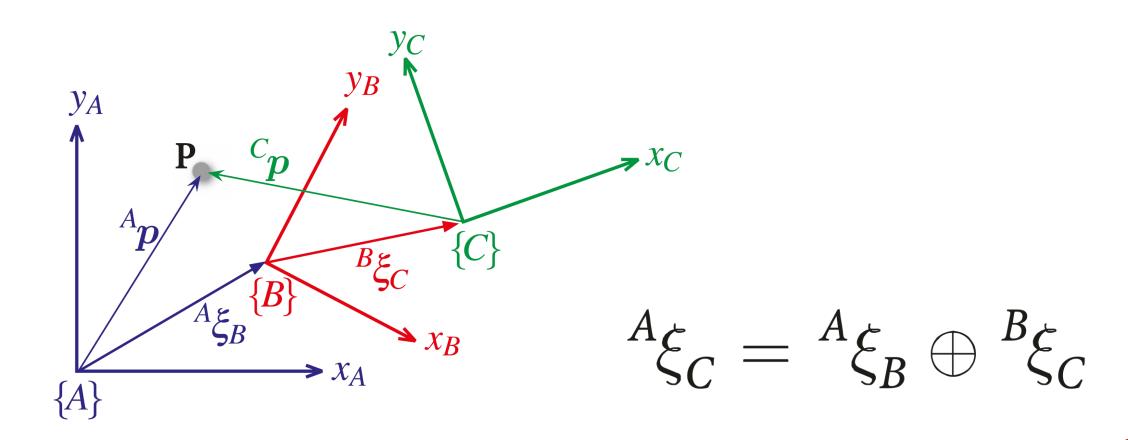


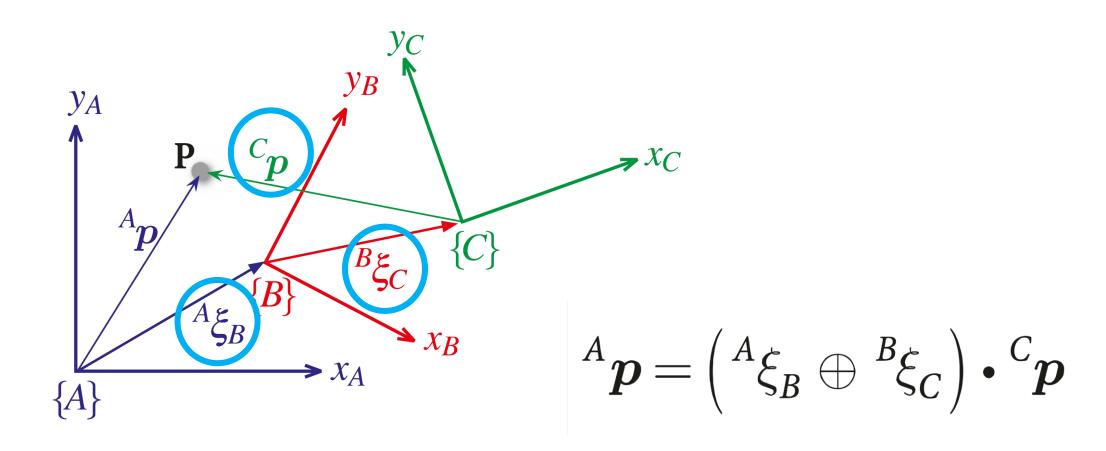


RELATIVE POSITION



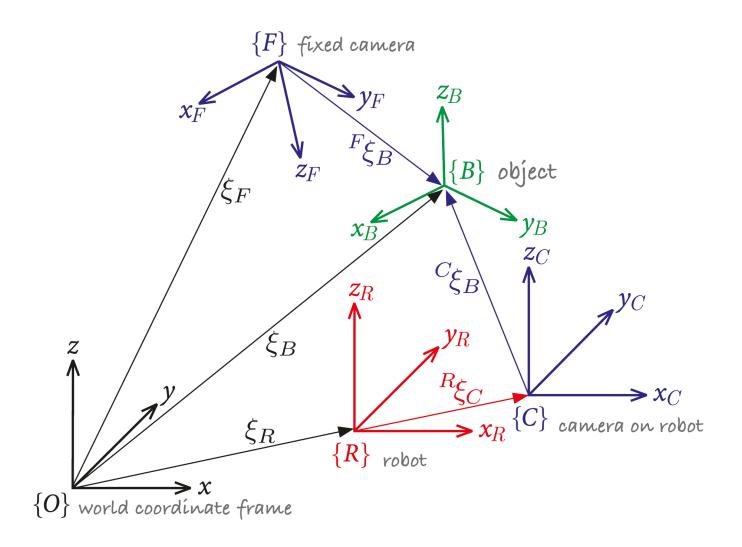
$${}^{A}\boldsymbol{p}={}^{A}\xi_{B}\cdot{}^{B}\boldsymbol{p}$$

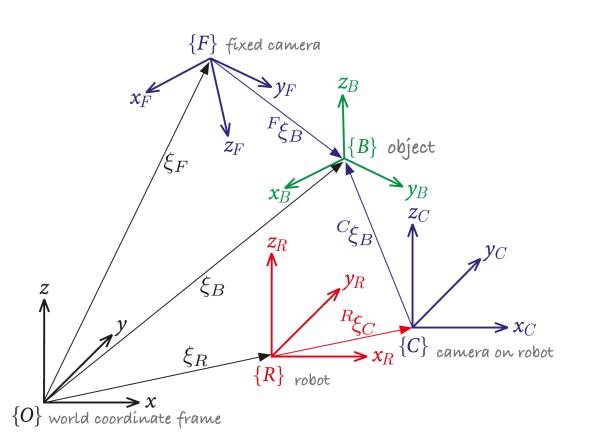


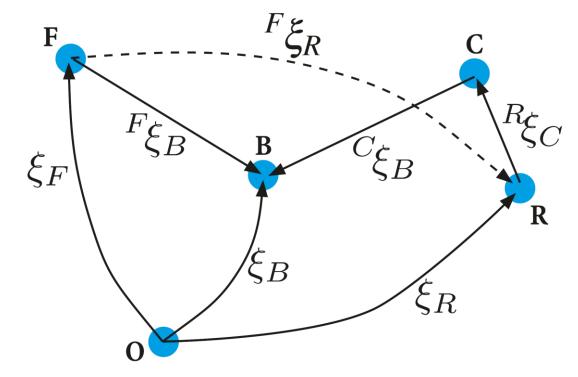


Relative poses can be composed

$${}^{A}\xi_{B}\oplus{}^{B}\xi_{C}$$

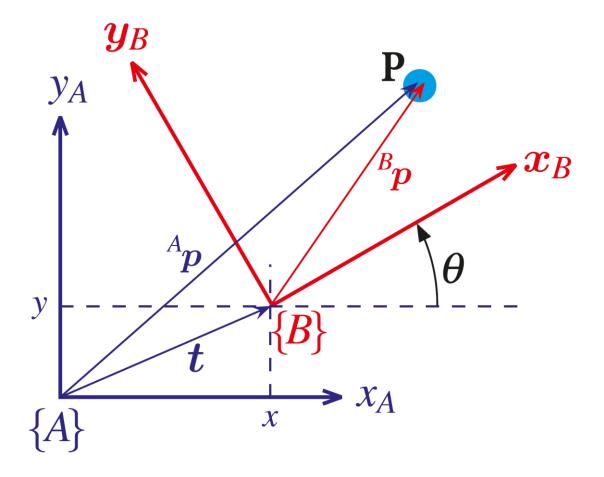


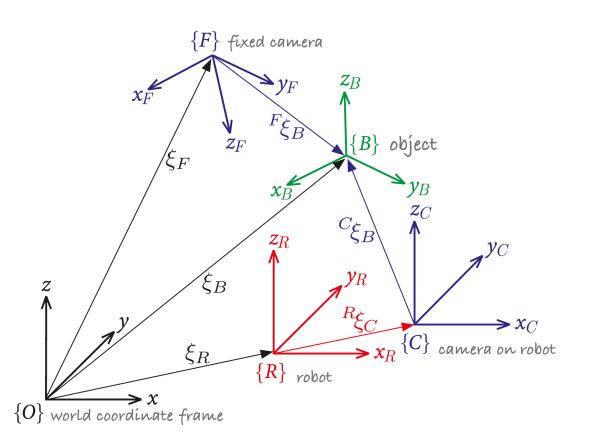


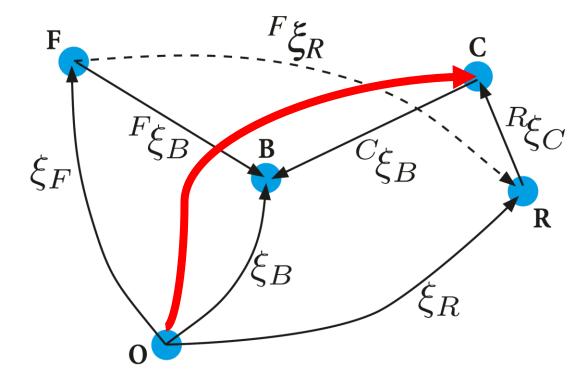


POSE

 $\begin{bmatrix} R & t \\ 0^T & 1 \end{bmatrix}$







ROTATION IN 3D (REVIEW)

$$R_x^{3D}(\omega) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos(\omega) & -\sin(\omega) \\ 0 & \sin(\omega) & \cos(\omega) \end{bmatrix} \quad R_y^{3D}(\phi) = \begin{bmatrix} \cos(\phi) & 0 & \sin(\phi) \\ 0 & 1 & 0 \\ -\sin(\phi) & 0 & \cos(\phi) \end{bmatrix}$$

$$R_y^{3D}(\phi) = \begin{bmatrix} \cos(\phi) & 0 & \sin(\phi) \\ 0 & 1 & 0 \\ -\sin(\phi) & 0 & \cos(\phi) \end{bmatrix}$$

$$R_z^{3D}(\kappa) = \begin{bmatrix} \cos(\kappa) & -\sin(\kappa) & 0\\ \sin(\kappa) & \cos(\kappa) & 0\\ 0 & 0 & 1 \end{bmatrix}$$

ORDER OF ROTATION

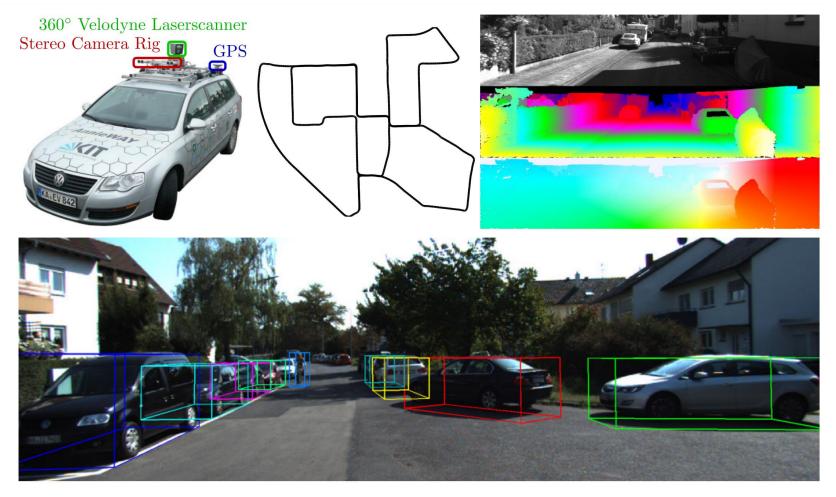
EULER'S ROTATION THEOREM

Any two independent orthonormal coordinate frames can be related by a sequence of rotations (not more than 3) about coordinate axes, where no two successive rotations may be about the same axis.

XYX XYZ XZY XZX YXY YXZ YZX YZY ZXY ZXZ ZYX ZYZ



KITTI



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KITTI

