Team Contest Reference getRandomNumber(){return 4;}

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1 Mathematische Algorithmen

1.1 Primzahlen

Für Primzahlen gilt immer (aber nicht nur für Primzahlen)

```
a^p \equiv a \mod p bzw. a^{p-1} \equiv 1 \mod p.
```

1.1.1 Sieb des Eratosthenes

```
static boolean[] sieve(int until) {
boolean[] a = new boolean[until + 1];
Arrays.fill(a, true);
for (int i = 2; i < Math.sqrt(a.length); i++) {
   if (a[i]) {
      for (int j = i * i; j < a.length; j += i) a[j] = false;
}</pre>
```

```
7   }
8  }
9  return a; // a[i] == true, iff. i is prime. a[0] is ignored
10 }
```

1.1.2 Primzahlentest

```
1 static boolean isPrim(int p) {
2    if (p < 2 || p > 2 && p % 2 == 0) return false;
3    for (int i = 3; i <= Math.sqrt(p); i += 2)
4        if (p % i == 0) return false;
5    return true;
6 }</pre>
```

1.2 Binomial Koeffizient

```
1 static int[][] mem = new int[MAX_N][(MAX_N + 1) / 2];
2 static int binoCo(int n, int k) {
3    if (k < 0 || k > n) return 0;
4    if (2 * k > n) binoCo(n, n - k);
5    if (mem[n][k] > 0) return mem[n][k];
6    int ret = 1;
7    for (int i = 1; i <= k; i++) {
8        ret *= n - k + i;
9        ret /= i;
10        mem[n][i] = ret;
11    }
12    return ret;
13 }</pre>
```

1.3 Modulare Arithmetik

Bedeutung der größten gemeinsamen Teiler:

$$d = ggT(a, b) = as + bt$$

Verwendung zu Berechnung des inversen Elements b zu a bezüglich einer Restklassengruppe n (a und n müssen teilerfremd sein):

$$ab \equiv 1 \mod n \iff s \equiv b \mod n \quad \text{für } 1 = ggT(a, n)$$

1.3.1 Erweiterter Euklidischer Algorithmus

```
1 static int[] eea(int a, int b) {
2    int[] dst = new int[3];
3    if (b == 0) {
4        dst[0] = a;
5        dst[1] = 1;
6        return dst; // a, 1, 0
7    }
8    dst = eea(b, a % b);
9    int tmp = dst[2];
10    dst[2] = dst[1] - ((a / b) * dst[2]);
11    dst[1] = tmp;
12    return dst;
13 }
```

1.4 Matrixmultiplikation

Strassen-Algorithmus: C = AB $A, B, C \in \mathbb{R}^{2^n \times 2^n}$

$$\begin{array}{lll} \mathbf{C}_{1,1} & = & \mathbf{A}_{1,1}\mathbf{B}_{1,1} + \mathbf{A}_{1,2}\mathbf{B}_{2,1} \\ \mathbf{C}_{1,2} & = & \mathbf{A}_{1,1}\mathbf{B}_{1,2} + \mathbf{A}_{1,2}\mathbf{B}_{2,2} \\ \mathbf{C}_{2,1} & = & \mathbf{A}_{2,1}\mathbf{B}_{1,1} + \mathbf{A}_{2,2}\mathbf{B}_{2,1} \\ \mathbf{C}_{2,2} & = & \mathbf{A}_{2,1}\mathbf{B}_{1,2} + \mathbf{A}_{2,2}\mathbf{B}_{2,2} \end{array}$$

2 Datenstukturen

2.1 Fenwick Tree (Binary Indexed Tree)

```
class FenwickTree {
    private int[] values;
    private int n;
    public FenwickTree(int n) {
      this.n = n;
      values = new int[n];
    public int get(int i) { //get value of i
      int x = values[0];
      while (i > 0) {
10
11
        x += values[i];
12
        i -= i & -i; }
13
      return x;
14
    public void add(int i, int x) { // add x to interval [i,n]
15
      if (i == 0) values[0] += x;
16
        while (i < n) {
18
19
           values[i] += x;
           i += i & -i; }
20
21
22
    }
23 }
```

3 Graphenalgorithmen

3.1 Topologische Sortierung

```
static List<Integer> topoSort(Map<Integer, List<Integer>> edges,
      Map<Integer, List<Integer>> revedges) {
    Queue < Integer > q = new LinkedList < Integer > ();
    List<Integer> ret = new LinkedList<Integer>();
    Map<Integer, Integer> indeg = new HashMap<Integer, Integer>();
    for (int v : revedges.keySet()) {
      indeg.put(v, revedges.get(v).size());
      if (revedges.get(v).size() == 0)
        q.add(v);
10
11
    while (!q.isEmpty()) {
      int tmp = q.poll();
12
13
      ret.add(tmp);
14
      for (int dest : edges.get(tmp)) {
        indeg.put(dest, indeg.get(dest) - 1);
15
        if (indeg.get(dest) == 0)
          q.add(dest);
17
18
      }
    }
19
20
    return ret;
```

3.2 Prim (Minimum Spanning Tree)

```
1 #define WHITE 0
  #define BLACK 1
3 #define INF INT_MAX
5 int baum( int **matrix, int N){
    int i. sum = 0:
    int color[N];
    int dist[N];
      // markiere alle Knoten ausser 0 als unbesucht
11
    color[0] = BLACK;
12
    for( i=1; i< N; i++){
13
      color[i] = WHITE;
14
      dist[i] = INF;
15
16
17
      // berechne den Rand
18
    for( i=1; i<N; i++){</pre>
19
20
           if( dist[i] > matrix[i][nextIndex]){
21
               dist[i] = matrix[i][nextIndex];
22
      }
```

```
while( 1){
25
      int nextDist = INF, nextIndex = -1;
26
27
       /* Den naechsten Knoten waehlen */
28
29
      for (i=0; i<N; i++) {
         if( color[i] != WHITE) continue;
30
31
         if( dist[i] < nextDist){</pre>
32
           nextDist = dist[i];
33
34
           nextIndex = i;
35
         }
36
      }
37
       /* Abbruchbedingung*/
38
      if( nextIndex == -1) break;
39
       /* Knoten in MST aufnehmen */
41
42
      color[nextIndex] = RED;
      sum += nextDist;
43
44
45
       /* naechste kuerzeste Distanzen berechnen */
      for( i=0; i<N; i++){
46
               if( i == nextIndex || color[i] == BLACK ) continue;
47
               if( dist[i] > matrix[i][nextIndex]){
49
50
                    dist[i] = matrix[i][nextIndex];
51
52
53
    }
54
55
    return sum;
```

3.3 Maximaler Fluss (Ford-Fulkerson)

```
#include <stdio.h>
2 #include <limits.h>
4 #define n_MAX 36
5 #define m_MAX 30
6 #define SIZE (m+6+2)
7 #define SIZE_MAX 38
8 #define QUELLE (m+6)
9 #define SENKE (m+7)
10 #define NONE -1
#define INF INT_MAX/2
13 int n, m;
int capacity[SIZE_MAX][SIZE_MAX];
int flow[SIZE_MAX][SIZE_MAX];
int queue[SIZE_MAX], *head, *tail;
int state[SIZE_MAX];
18 int pred[SIZE_MAX];
20 enum { XS, S, M, L, XL, XXL };
21 enum { UNVISITED, WAITING, PROCESSED };
23 int strToOffset( char *str);
24 int maxFlow( int quelle, int senke);
26 int main(){
      int numOfProps;
      scanf("%d\n", &numOfProps);
29
30
      while( numOfProps--){
31
          32
33
          int i, j;
34
35
          /* Matrix initialisieren */
          for( i=0; i< SIZE; i++){</pre>
37
              for( j=0; j< SIZE; j++){</pre>
38
39
                  capacity[i][j] = flow[i][j] = 0;
40
```

```
if( i == QUELLE && j < m){</pre>
                           capacity[i][j] = 1;
42
43
                           continue;
44
                      }
45
46
                      if(j == SENKE \&\& i >= m \&\& i < QUELLE){
                           capacity[i][j] = n/6;
47
48
                           continue;
49
                 }
50
51
             }
52
             char str[4];
53
54
             /* Matrix einlesen */
55
             \quad \textbf{for} \, (\ i = 0 \, ; \ i < \, m \, ; \ i + +) \, \{
56
                 scanf("%s", str);
                 capacity[i][m+strToOffset(str)] = 1;
58
                 scanf("%s", str);
59
                 capacity[i][m+strToOffset(str)] = 1;
60
             }
61
62
63
             int foo = maxFlow( QUELLE, SENKE);
printf("%s\n", foo >= m ? "YES" : "NO");
64
65
66
67
        }
68
        return 0;
69
70 }
71
72 int strToOffset( char *str){
73
        /*snip*/
74 }
75
   void enqueue( int x){
76
        *tail++ = x;
77
        state[x] = WAITING;
78
79 }
80
81 int dequeue(){
        int x = *head++;
82
        state[x] = PROCESSED;
83
84
        return x;
85 }
86
87 int bfs( int start, int target){
88
        int u, v;
        for( u=0; u < SIZE; u++){
             state[u] = UNVISITED;
90
91
        head = tail = queue;
92
        pred[start] = NONE;
93
94
        enqueue(start);
95
96
97
        while( head < tail){</pre>
            u = dequeue();
98
99
             for( v= 0; v< SIZE; v++){</pre>
100
                 if( state[v] == UNVISITED &&
101
102
                      capacity[u][v] - flow[u][v] > 0){
103
                      enqueue(v);
104
                      pred[v] = u;
                 }
106
107
             }
108
109
        return state[target] == PROCESSED;
110
111 }
112
int maxFlow( int quelle, int senke){
        int max_flow = 0;
114
115
        int u;
116
```

```
while( bfs( quelle, senke)){
118
119
           int increment = INF, temp;
120
           for( u= senke; pred[u] != NONE; u = pred[u]){
121
               temp = capacity[pred[u]][u] - flow[pred[u]][u];
122
               if( temp < increment){</pre>
123
124
                    increment = temp;
125
           }
126
127
           for( u= senke; pred[u] != NONE; u = pred[u]){
128
               flow[pred[u]][u] += increment;
129
               flow[u][pred[u]] -= increment;
131
132
           max_flow += increment;
133
      }
134
135
       return max_flow;
136
137 }
   * Ford Fulkersen
2
   * @param s source
   * @param d destination
   * @param c capacity
   * @param f flow, init with 0
   * @return
 9 static int ff(int s, int d, int[][] c, int[][] f) {
    List<Integer> path = dfs(s, d, c, f, new boolean[c.length]); // find path
10
11
    if (path.size() < 2) {
12
       int flow = 0;
       for (int i = 0; i < f[s].length; i++) { // leaving flow of source
13
         flow += f[s][i];
14
15
      return flow;
16
17
    int cap = Integer.MAX_VALUE; // capacity of current path
18
    for (int i = 0; i < path.size() - 1; i++) {</pre>
19
       int a = path.get(i), b = path.get(i + 1);
20
       cap = Math.min(cap, c[a][b] - f[a][b]);
21
22
    for (int i = 0; i < path.size() - 1; i++) { //update flow
23
24
      int a = path.get(i), b = path.get(i + 1);
       f[a][b] += cap;
25
      f[b][a] -= cap;
26
27
28
    return ff(s, d, c, f); // tail recursion
29 }
30
31 /**
   * depth first search in flow network
32
   * @param s source
   * @param d destination
34
    * @param c capacity
35
   * @param f flow
   * @param v visited, init with false
37
   * @return
38
   */
39
40 static List<Integer> dfs(int s, int d, int[][] c, int[][] f, boolean[] v) {
    v[s] = true;
    if (s == d) { // destination found
42
43
      LinkedList<Integer> path = new LinkedList<Integer>();
44
       path.add(d);
       return path;
45
46
47
     for (int i = 0; i < c[s].length; i++) {
      if (!v[i] && c[s][i] - f[s][i] > 0) {
48
49
         List<Integer> path = dfs(i, d, c, f, v);
         if (path.size() > 0) {
50
51
           ((LinkedList<Integer>) path).addFirst(s);
           return path;
52
53
54
      }
    }
55
```

```
return ((List<Integer>) Collections.EMPTY_LIST);

3.4 Floyd-Warshall

static int n;
static int[][] path = new int[n][n];
static int[][] next = new int[n][n];
static void floyd(int[][] ad) {
```

if (path[i][k] + path[k][j] < path[i][j]) {
 path[i][j] = path[i][k] + path[k][j];</pre>

// there is a negative circle iff. there is a i such that path[i][i] < 0

3.5 Dijkstra

10

11 12

14 15 } for (int i = 0; i < n; i++)

for (int i = 0; i < n; i++)
for (int j = 0; j < n; j++)
for (int k = 0; k < n; k++)</pre>

next[i][j] = k;

path[i] = Arrays.copyOf(ad[i], n);

```
Funktion Dijkstra(Graph, Startknoten):
       initialisiere(Graph, Startknoten, abstand[], vorgaenger[],Q)
                                                     // Der eigentliche Algorithmus
       solange Q nicht leer:
           u := Knoten in Q mit kleinstem Wert in abstand[]
                                                             // fuer u ist der kuerzeste Weg nun bestimmt
           entferne u aus Q
           fuer jeden Nachbarn v von u:
                falls v in Q:
                  distanz_update(u,v,abstand[],vorgaenger[]) // pruefe Abstand vom Startknoten zu v
       return vorgaenger[]
   Methode initialisiere(Graph, Startknoten, abstand[], vorgaenger[],Q):
11
       fuer jeden Knoten v in Graph:
12
13
           abstand[v] := unendlich
           vorgaenger[v] := null
14
       abstand[Startknoten] := 0
       Q := Die Menge aller Knoten in Graph
16
17
  Methode distanz_update(u,v,abstand[],vorgaenger[]):
       alternativ := abstand[u] + abstand_zwischen(u, v)
                                                             // Weglaenge vom Startknoten nach v ueber u
19
       falls alternativ < abstand[v]:</pre>
20
           abstand[v] := alternativ
           vorgaenger[v] := u
```

4 Geometrische Algorithmen

4.1 Graham Scan (Convex Hull)

```
ı class P {
   double x, y;
   P(double x, double y) {
      this.x = x;
      this.y = y;
6
   // polar coordinates (not used in graham scan)
   double r() { return Math.sqrt(x * x + y * y); }
   double d() { return Math.atan2(y, x); }
10
11 }
12
_{13} // turn is counter-clockwise if > 0; collinear if = 0; clockwise else
14 static double ccw(P p1, P p2, P p3) {
   16 }
18 static List<P> graham(List<P> 1) {
   if (1.size() < 3)
19
20
     return 1;
   P temp = 1.get(0);
   for (P p : 1)
22
23
     if (temp.y > p.y \mid \mid temp.y == p.y \&\& temp.x > p.x)
       temp = p;
```

```
final P start = temp; // min y (then leftmost)
26
27
    Collections.sort(1, new Comparator<P>() {
      public int compare(P o1, P o2) {
28
        if (new Double(Math.atan2(o1.y - start.y, o1.x - start.x)) // same angle
29
             .compareTo(Math.atan2(o2.y - start.y, o2.x - start.x)) == 0)
30
          return new Double((o1.x - start.x) * (o1.x - start.x)
31
               + (o1.y - start.y) * (o1.y - start.y))
32
              .compareTo((o2.x - start.x) * (o2.x - start.x)
              + (o2.y - start.y) * (o2.y - start.y)); // use distance
34
        return new Double(Math.atan2(o1.y - start.y, o1.x - start.x))
35
            .compareTo(Math.atan2(o2.y - start.y, o2.x - start.x));
36
      }
37
    });
38
    Stack<P> s = new Stack<P>();
39
40
    s.add(start);
    s.add(1.get(1));
    for (int i = 2; i < 1.size(); i++) {</pre>
42
43
      while (s.size() >= 2
          && ccw(s.get(s.size() - 2), s.get(s.size() - 1), l.get(i)) <= 0)
44
45
        s.pop();
46
      s.push(l.get(i));
47
48
    return s;
49 }
```

4.2 Maximum Distance in a Point Set

```
List<P> hull = graham(list);
2 maxDist(hull);
4 static double dist(P p1, P p2) {
    return Math.sqrt((p1.x - p2.x) * (p1.x - p2.x)
        + (p1.y - p2.y) * (p1.y - p2.y));
7 }
9 static double maxDist(List<P> hull) {
    double max = 0, tmp = 0;
10
    int j = 0, n = hull.size();
11
    for (P p : hull) {
12
      while (tmp < dist(p, hull.get((j + 1) % n))) {
13
14
        j = (j + 1) \% n;
        tmp = dist(p, hull.get(j));
15
16
      max = Math.max(max, tmp);
17
18
19
    return max;
```

4.3 Punkt in Polygon

```
* -1: A liegt links von BC (ausser unterer Endpunkt)
   * 0: A auf BC
   * +1: sonst
  public static int KreuzProdTest(double ax, double ay, double bx, double by,
      double cx, double cy) {
    if (ay == by && by == cy) \{
      if ((bx <= ax && ax <= cx) || (cx <= ax && ax <= bx)) return 0;</pre>
      else return +1;
10
11
    if (by > cy) {
12
      double tmpx = bx, tmpy = by;
13
      bx = cx;
14
      by = cy;
15
16
      cx = tmpx;
17
      cy = tmpy;
18
    if (ay == by && ax == bx) return 0;
    if (ay \le by \mid \mid ay > cy) return +1;
20
    double delta = (bx - ax) * (cy - ay) - (by - ay) * (cx - ax);
    if (delta > 0) return -1;
    else if (delta < 0) return +1;</pre>
23
24
    else return 0;
25 }
```

```
27 /**
  * Input: P[i] (x[i],y[i]); P[0]:=P[n]
28
  * -1: Q ausserhalb Polygon
   * 0: Q auf Polygon
30
  * +1: Q innerhalb des Polygons
  */
32
33 public static int PunktInPoly(double[] x, double[] y, double qx, double qy) {
    for (int i = 0; i < x.length - 1; i++)
35
      t = t * KreuzProdTest(qx, qy, x[i], y[i], x[i + 1], y[i + 1]);
36
37
    return t;
38 }
```

5 Verschiedenes

5.1 Potenzmenge

```
static <T> Iterator<List<T>> powerSet(final List<T> 1) {
     \textbf{return new} \  \, \texttt{Iterator} < \texttt{List} < \texttt{T} >> \textbf{()} \  \, \{
       int i; // careful: i becomes 2^l.size()
       public boolean hasNext() {
         return i < (1 << l.size());
6
       public List<T> next() {
         Vector<T> temp = new Vector<T>();
8
         for (int j = 0; j < l.size(); j++)
10
            if (((i >>> j) & 1) == 1)
              temp.add(l.get(j));
11
12
         i++:
13
         return temp;
       }
14
15
       public void remove() {}
16
       };
    }
17
```

5.2 Longest Common Subsequence

```
#include <stdio.h>
2 #include <stdlib.h>
3 #include <string.h>
6 int lcs( char *a, char *b){
      int len = strlen( a);
      int lenb =strlen(b);
      int *zeile = malloc( (len+1) * sizeof(int)), *temp,
10
          *neue = malloc( (len+1) * sizeof(int)), i, j;
11
12
13
      for(i=0; i<len+1; i++){
          zeile[i] = neue[i] = 0;
14
15
16
      for(j=0; j<lenb; j++){
17
18
           for(i=0; i<len; i++){
               if( a[i] == b[j]){
19
                   neue[i+1] = zeile[i] + 1;
20
               } else {
21
                   neue[i+1] = neue[i] > zeile[i+1] ? neue[i] : zeile[i+1];
22
23
25
          temp = zeile;
26
          zeile = neue;
          neue = temp;
27
      }
28
29
      int res = zeile[len];
30
31
      free( zeile);
32
      free( neue);
      return res;
33
34 }
```

5.3 Longest Increasing Subsequence

```
#include <stdio.h>
2 #include <stdlib.h>
4 int lis( int *list, int n){
      int *sorted = malloc( n*sizeof(int)), sorted_n;
      int i, *lower, *upper, *mid, *pos;
      if( n == 0) return 0;
      sorted[0] = list[0];
10
      sorted_n = 1;
11
12
      for( i=1; i<n; i++){</pre>
13
           /* binaere Suche */
           lower = list;
15
           upper = list + sorted_n;
16
           mid = list + sorted_n / 2;
18
19
           while( lower < upper-1){</pre>
20
               if( list[i] < *mid){</pre>
21
22
                    upper = mid;
               } else {
23
                    lower = mid;
24
26
27
               mid = lower + (upper-lower) / 2;
28
29
    if( mid == list + sorted_n -1 \&\& *mid < list[i]){
31
               *mid = list[i];
               sorted_n++;
32
           }
34
           if( list[i] < *mid){
35
               *mid = list[i];
36
           }
37
38
      }
39
      free( sorted);
40
41
      return sorted_n;
42
43 }
```

6 Eine kleine C-Referenz

C Reference Card (ANSI)

Program Structure/Functions

Taircolons	function declarations	external variable declarations	main routine	local variable declarations			function definition	local variable declarations				comments	main with args	terminate execution
T TOPICHI DOLACOALO, T ATTICOLOGIS	$type\ fnc(type_1,)$	type $name$	main() {	declarations	statements	~	$type\ fnc(arg_1,)$ {	declarations	statements	return value;	~	/* */	main(int argc, char *argv[])	exit(arg)

C Preprocessor

#include <flename></flename>	#include "flename"	#define name text	#define name(var) text	Example. #define max(A,B) ((A)>(B) ? (A) : (B))	+undef $name$	#	##	#if, #else, #elif, #endif	#ifdef, #ifndef	defined(name)	_
include library file	include user file	replacement text	replacement macro	Example. #define max(A,	undefine	quoted string in replace	concatenate args and rescan	conditional execution	is name defined, not defined?	name defined?	line continuation char

Data Types/Declarations

char	int	float	double	short	long	signed	unsigned	*int, *float,	ennm	const	extern	register	static	void	struct	typedef typename	$\mathbf{t_{-t}}$) sizeof $object$	<pre>ze_t) sizeof(type name)</pre>	
 character (1 byte)	integer	float (single precision)	float (double precision)	short (16 bit integer)	long (32 bit integer)	positive and negative	only positive	pointer to int, float,	enumeration constant	constant (unchanging) value	declare external variable	register variable	local to source file	no value	structure	create name by data type	size of an object (type is size_t)	size of a data type (type is size_t)	

Initialization

$type\ name=value$	$type name []=\{value_1, \ldots\}$	char name[] = "string"
initialize variable	initialize array	initialize char string

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Constants

L or l F or f	0 O	0x or 0X	\(\frac{\pi}{\pi}\fra	"abcde"
long (suffix) float (suffix)	exponential form octal (prefix zero)	hexadecimal (prefix zero-ex)	newline, cr. tab, backspace special characters	string constant (ends with '\0')

Pointers, Arrays & Structures

declare pointer to type $*name$ declare function returning pointer to type $*f()$	declare pointer to function returning $type\ type\ (*pf)$ () generic pointer type void *	inter J	object pointed to by pointer *pointer	address of object name	name [dim]	im array $name [dim_1][dim_2]$	ures
declare point declare funct	declare point generic point	null pointer	object pointe	address of ob	array	multi-dim array	Structures

rructures struct tag { structure template declarations declaration of members

:-	
create structure	struct tag name
member of structure from template	name $.$ $member$
member of pointed to structure	pointer -> member
Example. $(*p).x$ and $p->x$ are the same	same
single value, multiple type structure	union
bit field with b bits	member: b

Operators (grouped by precedence)

structure member operator	name $.$ $member$
structure pointer	pointer->member
increment, decrement	'++
plus, minus, logical not, bitwise not	· '- '- '+
indirection via pointer, address of object	
cast expression to type	(type) expr
size of an object	sizeof
multiply, divide, modulus (remainder)	*, /, *
add, subtract	- '+
left, right shift [bit ops]	<<, >>
comparisons	>, >=, <, <=
comparisons	=; '==
bitwise and	8
bitwise exclusive or	•
bitwise or (incl)	_
logical and	28
logical or	
conditional expression ex	expr ₁ ? expr ₂ : expr ₃
assignment operators	+=, -=, *=,
expression evaluation separator	•

expression evaluation separator

Unary operators, conditional expression and assignment operators group right to left, all others group left to right.

Flow of Control

; { } break continue	goto label label: return expr	<pre>if (expr) statement else if (expr) statement else statement</pre>	pr) nt	<pre>for (expr1; expr2; expr3) statement</pre>	statement (expr);	<pre>tch (expr) { case const₁: statement₁ break; case const₂: statement₂ break; default: statement</pre>
statement terminator block delimeters exit from switch, while, do, for next iteration of while, do, for	go to label return value from function Flow Constructions		while statement while (expr)	for statement for (expr1; statement	<pre>do statement do statemer while(expr);</pre>	<pre>switch statement switch (expr) { case const; case const; default: stat }</pre>

ANSI Standard Libraries

<pre><float.h> <linits.h> <signal.h> <stdarg.h> <string.h> <time.h></time.h></string.h></stdarg.h></signal.h></linits.h></float.h></pre>	<ctype.h></ctype.h>	isalnum(c)	isalpha(c)	iscntrl(c)	isdigit(c)	isgraph(c)	islower(c)	isprint(c)	ispunct(c)	isspace(c)	isupper(c)	isxdigit(c)	tolower(c)	toupper(c)
<pre><errno.h> <setjmp.h> <stdlib.h></stdlib.h></setjmp.h></errno.h></pre>		įį	įį	i:	i		įį				żi	żi	ţ	ţ
<pre><assert.h> <ctype.h> <locale.h> <math.h> <stdddf.h> <stdio.h></stdio.h></stdddf.h></math.h></locale.h></ctype.h></assert.h></pre>	Character Class Tests	alphanumeric?	alphabetic?	control character?	decimal digit?	printing character (not incl space)?	lower case letter?	printing character (incl space)?	printing char except space, letter, digit?	space, formfeed, newline, cr, tab, vtab?	upper case letter?	hexadecimal digit?	convert to lower case?	convert to upper case?

String Operations <string.h>

s,t are strings, cs,ct are constant strings	gs
length of s	strlen(s)
copy ct to s	strcpy(s,ct)
up to n chars	strncpy(s,ct,n)
concatenate ct after s	strcat(s,ct)
up to n chars	strncat(s,ct,n)
compare cs to ct	strcmp(cs,ct)
only first n chars	strncmp(cs,ct,n
pointer to first c in cs	strchr(cs,c)
pointer to last c in cs	strrchr(cs,c)
copy n chars from ct to s	memcpy(s,ct,n)
copy n chars from ct to s (may overlap)	memmove(s,ct,n)
compare n chars of cs with ct	memcmp(cs,ct,n)
pointer to first c in first n chars of cs	memchr(cs,c,n)
put c into first n chars of cs	memset(s,c,n)

(4,294,967,295)(65,536)

 (10^{37}) (10^{-37})

> maximum floating point number minimum floating point number

maximum exponent

FLT_MAX_EXP

FLT_MAX FLT_MIN

number of digits in mantissa smallest $x \text{ so } 1.0 + x \neq 1.0$

FLT_MANT_DIG

FLT_EPSILON

FLT_ROUNDS

FLT_RADIX FLT_DIG

 (10^{-5})

floating point rounding mode

radix of exponent rep

decimal digits of precision

Float Type Limits <float.h>

max value of unsigned short

 (10^{-9})

(10)

 (10^{37}) (10^{-37})

max double floating point number min double floating point number

maximum exponent

minimum exponent

DBL MIN EXP

number of digits in mantissa

smallest $x \text{ so } 1.0 + x \neq 1.0$

DBL_EPSILON DBL_MANT_DIG

DBL_MAX DBL_MAX_EXP

decimal digits of precision

minimum exponent

FLT_MIN_EXP DBL_DIG

(+32,767)(-32,768)

(255)(65,535)

max value of unsigned char max value of unsigned long max value of unsigned int

(-128)

(+127)

max value of signed char min value of signed char

max value of long

INT_MIN LONG_MAX

min value of long

LONG_MIN SCHAR_MIN

SCHAR_MAX

max value of short min value of short

SHRT_MAX SHRT_MIN UCHAR_MAX

UINT_MAX ULONG_MAX

USHRT_MAX

C Reference Card (ANSI)

Input/Output <stdio.h> Standard I/O

stendard input streem	\$
standard input stream	TTDOG
standard output stream	stdout
standard error stream	stderr
end of file	EOF
get a character	getchar()
print a character	putchar(chr)
print formatted data	printf("format", arg1,
print to string s	sprintf(s, "format", arg1,
read formatted data	scanf("format", &name1,
read from string s	sscanf(s, "format", &name1,
read line to string s (< max chars)	x chars) gets(s,max)
print string s	puts(s)
File I/O	
declare file pointer	FILE * fp
pointer to named file	fopen("name","mode
modes: r (read), w (write), a (append)	rite), a (append)
get a character	getc(fp)
write a character	putc(chr,fp)
write to file	fprintf(fp ," $format$ ", arg_1 ,
read from file	$fscanf(fp,"format", arg_1,$
close file	fclose (fp)
non-zero if error	ferror(fp)
non-zero if EOF	
read line to string s (< max chars)	x chars) fgets(s,max, fp)
write string s	
Codes for Formatted I/O: " $\%$ -+ 0 w .pmc"	'O: "%-+ 0w.pmc"
- loft instify	•

<u>-</u>

pad with leading zeros space print space if no sign print with sign left justify ı + 0 8

L long double 1 long, conversion character: conversion character: h short, min field width precision p

n number of chars written p pointer n number of chars writt g,G same as f or e,E depending on exponent x,X hexadecimal e, E exponential char string u unsigned d,i integerc single charf double o octal c

Variable Argument Lists <stdarg.h>

va_list name;

declaration of pointer to arguments

initialization of argument pointer va_start(name, lastarg) access next unamed arg, update pointer va_arg(name,type) $\mathtt{va_end}(name)$ lastarg is last named parameter of the function call before exiting function

Standard Utility Functions <stdlib.h>

 $\begin{array}{c}
(8) \\
(127 \text{ or } 255) \\
(-128 \text{ or } 0)
\end{array}$

The numbers given in parentheses are typical values for the constants on a 32-bit Unix system.

CHAR_BIT bits in char (8

max value of char

min value of char

CHAR_MIN CHAR_MAX INT_MAX

max value of int min value of int

Integer Type Limits inits.h>

(-32,768)(+2,147,483,647)(-2,147,483,648)

(+32,767)

abs(n)	labs(n)	div(n,d)	and div_t.rem	ldiv(n,d)	and ldiv_t.rem	rand()	srand(n)	exit(status)	system(s)		atof(s)	atoi(s)	atol(s)	strtod(s,endp)	strtol(s,endp,b)	strtoul(s,endp,b)		malloc(size) calloc(nobi size)
absolute value of int n	absolute value of long n	quotient and remainder of ints n,d	retursn structure with div_t.quot and div_t.rem	quotient and remainder of longs n,d	returns structure with ldiv_t.quot and ldiv_t.rem	pseudo-random integer [0, RAND_MAX]	set random seed to n	terminate program execution	pass string s to system for execution	Conversions	convert string s to double	convert string s to integer	convert string s to long	convert prefix of s to double	convert prefix of s (base b) to long	same, but unsigned long	Storage Allocation	allocate storage malloc(size)

malloc(size), calloc(nobj,size) realloc(pts,size) allocate storage change size of object

bsearch(key, array, n, size, cmp()) qsort(array,n,size,cmp()) free(ptr) sort array ascending order search array for key Array Functions deallocate space

Time and Date Functions <time.h>

difftime(time2,time1) processor time used by program clock() Example. clock()/GLOCKS_PER_SEC is time in seconds clock_t,time_t time() months since January structure type for calendar time comps seconds after minute hours since midnight minutes after hour days since Sunday arithmetic types representing times years since 1900 time2-time1 in seconds (double) day of month current calendar time tm_hour tm_mday tm_year tm_wday tm_sec tm_min tm_mon

asctime(tp) mktime(tp) Daylight Savings Time flag days since January 1 convert local time to calendar time convert time in tp to string tm_isdst tm_yday

strftime(s,smax,"format",tp) localtime(tp) gmtime(tp) convert calendar time in tp to local time ctime(tp) convert calendar time to GMT gmtime(tp tp is a pointer to a structure of type tm convert calendar time to local time format date and time info

Mathematical Functions <math.h>

Arguments and returned values are double

asin(x), acos(x), atan(x)
atan2(y,x) sinh(x), cosh(x), tanh(x)
exp(x), log(x), log10(x) sin(x), cos(x), tan(x)ldexp(x,n), frexp(x,*e) modf(x,*ip), fmod(x,y) pow(x,y), sqrt(x)
ceil(x), floor(x), fabs(x) exponentials & logs (2 power) hyperbolic trig functions inverse trig functions division & remainder exponentials & logs trig functions arctan(y/x)rounding

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