

1.

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$2. L = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ 1 & -\frac{1}{8} & 1 & 0 \\ \frac{2}{3} & \frac{17}{24} & \frac{101}{81} & 1 \end{bmatrix}, U = \begin{bmatrix} -9 & 4 & -5 & -6 \\ 0 & -8 & 3 & 4 \\ 0 & 0 & \frac{27}{8} & \frac{9}{2} \\ 0 & 0 & 0 & -\frac{112}{9} \end{bmatrix}$$

3.

$$\begin{pmatrix} 0 & 18 & 15 \\ -18 & -17 & -7 \\ -8 & -2 & 15 \end{pmatrix}$$

4.

$$\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 1 & 6 & 2 & 3 & 4 & 5 \end{pmatrix}$$

5.

$$\sigma = (1, 2, 7, 5, 8, 3)(4, 6, 9), \text{ord} = 6, \sigma^{-821} = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ 2 & 7 & 1 & 6 & 8 & 9 & 5 & 3 & 4 \end{pmatrix} = (1, 2, 7, 5, 8, 3)(4, 6, 9)$$

$$6. \text{Id}; (1, 2, 7, 6, 5, 3, 4); (1, 3, 6, 2, 4, 5, 7); (1, 4, 3, 5, 6, 7, 2); \\ (1, 5, 2, 3, 7, 4, 6); (1, 6, 4, 7, 3, 2, 5); (1, 7, 5, 4, 2, 6, 3);$$

$$7. \frac{9(-9)^n}{41} + \frac{32 \cdot 32^n}{41}$$

$$8. -1 + 0 * x + 2 * x^2 + 0 * x^3 + -1 * x^4$$

$$9. \text{При } \lambda = 4$$

$$10. \text{Определитель: } 100 - 10\lambda, \text{ при } \lambda = [10] \text{ ранг равен } 3, \text{ иначе } 4$$