

1.

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$2. L = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ \frac{8}{7} & \frac{47}{35} & 1 & 0 \\ \frac{5}{7} & -\frac{9}{7} & \frac{5}{8} & 1 \end{bmatrix}, U = \begin{bmatrix} 7 & -2 & 2 & 9 \\ 0 & -5 & 2 & 4 \\ 0 & 0 & -\frac{104}{35} & -\frac{408}{35} \\ 0 & 0 & 0 & -2 \end{bmatrix}$$

3.

$$\begin{pmatrix} -11 & -4 & -1 \\ -9 & -3 & -4 \\ 3 & -18 & -12 \end{pmatrix}$$

4.

$$\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 6 & 5 & 2 & 4 & 1 & 3 \end{pmatrix}; \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 5 & 1 & 3 & 2 & 6 & 4 \end{pmatrix}$$

5.

$$\sigma = (1, 7, 8, 4, 9, 3)(2, 6, 5), \text{ord} = 6, \sigma^{-821} = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ 7 & 6 & 1 & 9 & 2 & 5 & 8 & 4 & 3 \end{pmatrix} = (1, 7, 8, 4, 9, 3)(2, 6, 5)$$

6. Id; (1, 2, 5, 7, 6, 4, 3); (1, 3, 4, 6, 7, 5, 2); (1, 4, 7, 2, 3, 6, 5);
(1, 5, 6, 3, 2, 7, 4); (1, 6, 2, 4, 5, 3, 7); (1, 7, 3, 5, 4, 2, 6);

$$7. -\frac{3 \cdot 18^n}{5} + \frac{8 \cdot 48^n}{5}$$

$$8. -2 + 1 * x + 2 * x^2 + -2 * x^3 + -3 * x^4$$

9. При $\lambda = -1$

10. Определитель: $15 - 78\lambda$, при $\lambda = [5/26]$ ранг равен 3, иначе 4