

1.

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$2. L = \begin{bmatrix} 1 & 0 & 0 & 0 \\ -\frac{5}{9} & 1 & 0 & 0 \\ -\frac{4}{9} & \frac{3}{2} & 1 & 0 \\ \frac{1}{3} & -3 & -\frac{726}{271} & 1 \end{bmatrix}, U = \begin{bmatrix} -9 & 9 & 4 & -4 \\ 0 & 4 & \frac{101}{9} & \frac{25}{9} \\ 0 & 0 & -\frac{271}{18} & \frac{19}{18} \\ 0 & 0 & 0 & \frac{4199}{271} \end{bmatrix}$$

3.

$$\begin{pmatrix} 5 & -1 & 17 \\ 10 & 10 & -18 \\ 11 & 5 & 19 \end{pmatrix}$$

4.

$$\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 2 & 5 & 6 & 3 & 4 & 1 \end{pmatrix}$$

5.

$$\sigma = (1, 7, 3)(2, 6, 4, 5)(8, 9), \text{ord} = 12, \sigma^{-733} = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ 3 & 5 & 7 & 6 & 4 & 2 & 1 & 9 & 8 \end{pmatrix} = (1, 3, 7)(2, 5, 4, 6)(8, 9)$$

6. Id; (1, 2, 4, 7, 6, 5, 3); (1, 3, 5, 6, 7, 4, 2); (1, 4, 6, 3, 2, 7, 5);
(1, 5, 7, 2, 3, 6, 4); (1, 6, 2, 5, 4, 3, 7); (1, 7, 3, 4, 5, 2, 6);

$$7. \frac{15(-30)^n}{47} + \frac{32 \cdot 64^n}{47}$$

$$8. -4 + 3 * x + 2 * x^2 + -2 * x^3 + -3 * x^4$$

9. При $\lambda = -4$

10. Определитель: $4 - 38\lambda$, при $\lambda = [2/19]$ ранг равен 3, иначе 4