

1.

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$2. L = \begin{bmatrix} 1 & 0 & 0 & 0 \\ -\frac{10}{9} & 1 & 0 & 0 \\ \frac{1}{9} & -\frac{14}{5} & 1 & 0 \\ -\frac{7}{9} & \frac{22}{25} & -\frac{337}{670} & 1 \end{bmatrix}, U = \begin{bmatrix} 9 & -2 & -6 & 4 \\ 0 & \frac{25}{9} & -\frac{38}{9} & \frac{58}{9} \\ 0 & 0 & -\frac{134}{5} & \frac{63}{5} \\ 0 & 0 & 0 & -\frac{1489}{670} \end{bmatrix}$$

3.

$$\begin{pmatrix} -15 & 19 & -15 \\ 17 & -13 & 2 \\ -12 & 6 & 13 \end{pmatrix}$$

4.

$$\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 6 & 2 & 5 & 4 & 1 & 3 \end{pmatrix}$$

5.

$$\sigma = (1, 7, 3)(2, 6, 5, 4, 8, 9), \text{ord} = 6, \sigma^{-733} = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ 3 & 9 & 7 & 5 & 6 & 2 & 1 & 4 & 8 \end{pmatrix} = (1, 3, 7)(2, 9, 8, 4, 5, 6)$$

6. Id; (5, 6); (2, 3, 4); (2, 3, 4) (5, 6);

(2, 4, 3); (2, 4, 3) (5, 6); (1, 5) (6, 7); (1, 5, 7, 6); (1, 5) (2, 3, 4) (6, 7);

(1, 5, 7, 6) (2, 3, 4); (1, 5) (2, 4, 3) (6, 7); (1, 5, 7, 6) (2, 4, 3); (1, 6, 7, 5); (1, 6) (5, 7);

(1, 6, 7, 5) (2, 3, 4); (1, 6) (2, 3, 4) (5, 7); (1, 6, 7, 5) (2, 4, 3); (1, 6) (2, 4, 3) (5, 7); (1, 7);

(1, 7) (5, 6); (1, 7) (2, 3, 4); (1, 7) (2, 3, 4) (5, 6); (1, 7) (2, 4, 3); (1, 7) (2, 4, 3) (5, 6);

7. $-6 \cdot 54^n + 7 \cdot 63^n$

8. $0 + 1 * x + 2 * x^2 + -2 * x^3 + 2 * x^4$

9. При $\lambda = 9$

10. Определитель: $298 - 47\lambda$, при $\lambda = [298/47]$ ранг равен 3, иначе 4