

1.

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$2. L = \begin{bmatrix} 1 & 0 & 0 & 0 \\ \frac{4}{5} & 1 & 0 & 0 \\ -\frac{3}{5} & 0 & 1 & 0 \\ 1 & \frac{2}{3} & -\frac{41}{57} & 1 \end{bmatrix}, U = \begin{bmatrix} -5 & -5 & -3 & -9 \\ 0 & 12 & -\frac{13}{5} & -\frac{4}{5} \\ 0 & 0 & -\frac{19}{5} & -\frac{27}{5} \\ 0 & 0 & 0 & \frac{721}{57} \end{bmatrix}$$

3.

$$\begin{pmatrix} -10 & 0 & -9 \\ 2 & -10 & -9 \\ 16 & -5 & 13 \end{pmatrix}$$

4.

$$\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 1 & 2 & 6 & 5 & 3 & 4 \end{pmatrix}$$

5.

$$\sigma = (1, 4, 8, 6, 3, 9, 7)(2, 5), \text{ord} = 14, \sigma^{-727} = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ 4 & 5 & 9 & 8 & 2 & 3 & 1 & 6 & 7 \end{pmatrix} = (1, 4, 8, 6, 3, 9, 7)(2, 5)$$

6. Id; (1, 2, 3, 4, 7, 6, 5); (1, 3, 7, 5, 2, 4, 6); (1, 4, 5, 3, 6, 2, 7);
(1, 5, 6, 7, 4, 3, 2); (1, 6, 4, 2, 5, 7, 3); (1, 7, 2, 6, 3, 5, 4);

7. брак

$$8. -1 + -1 * x + 0 * x^2 + 0 * x^3 + 4 * x^4$$

9. При $\lambda = -1$

10. Определитель: $483 - 9\lambda$, при $\lambda = [161/3]$ ранг равен 3, иначе 4