

1.

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$2. L = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 7 & 1 & 0 & 0 \\ -6 & -\frac{7}{5} & 1 & 0 \\ 8 & \frac{26}{15} & -\frac{20}{21} & 1 \end{bmatrix}, U = \begin{bmatrix} -1 & 3 & -1 & 2 \\ 0 & -15 & 5 & -12 \\ 0 & 0 & 7 & -\frac{74}{5} \\ 0 & 0 & 0 & -\frac{346}{105} \end{bmatrix}$$

3.

$$\begin{pmatrix} -16 & -19 & 15 \\ 19 & -3 & 5 \\ -10 & 9 & 2 \end{pmatrix}$$

4.

$$\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 1 & 4 & 3 & 6 & 5 & 2 \end{pmatrix}$$

5.

$$\sigma = (1, 5, 8, 7, 3, 6, 2)(4, 9), \text{ord} = 14, \sigma^{-821} = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ 6 & 3 & 8 & 9 & 2 & 7 & 5 & 1 & 4 \end{pmatrix} = (1, 6, 7, 5, 2, 3, 8)(4, 9)$$

6. Id; (2, 6); (1, 3, 4, 7, 5); (1, 3, 4, 7, 5) (2, 6);

(1, 4, 5, 3, 7); (1, 4, 5, 3, 7) (2, 6); (1, 5, 7, 4, 3); (1, 5, 7, 4, 3) (2, 6); (1, 7, 3, 5, 4);

(1, 7, 3, 5, 4) (2, 6);

$$7. \frac{10(-20)^n}{37} + \frac{27 \cdot 54^n}{37}$$

$$8. 4 + 0 * x + 1 * x^2 + 1 * x^3 + 3 * x^4$$

9. При $\lambda = 8$

10. Определитель: $278 - 139\lambda$, при $\lambda = [2]$ ранг равен 3, иначе 4