

1.

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$2. L = \begin{bmatrix} 1 & 0 & 0 & 0 \\ \frac{3}{5} & 1 & 0 & 0 \\ \frac{3}{5} & -\frac{34}{31} & 1 & 0 \\ -\frac{1}{5} & -\frac{7}{31} & \frac{28}{43} & 1 \end{bmatrix}, U = \begin{bmatrix} -5 & 3 & 1 & -5 \\ 0 & \frac{31}{5} & \frac{42}{5} & -2 \\ 0 & 0 & -\frac{43}{31} & \frac{56}{31} \\ 0 & 0 & 0 & \frac{145}{43} \end{bmatrix}$$

3.

$$\begin{pmatrix} 4 & -10 & 0 \\ -20 & -14 & -18 \\ -3 & 1 & 11 \end{pmatrix}$$

4.

$$\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 6 & 4 & 5 & 2 & 1 & 3 \end{pmatrix}$$

5.

$$\sigma = (1, 5, 2, 3, 6, 7, 9)(4, 8), \text{ord} = 14, \sigma^{-827} = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ 9 & 5 & 2 & 8 & 1 & 3 & 6 & 4 & 7 \end{pmatrix} = (1, 9, 7, 6, 3, 2, 5)(4, 8)$$

6. Id; (1, 2, 7, 5, 4, 6, 3); (1, 3, 6, 4, 5, 7, 2); (1, 4, 2, 6, 7, 3, 5);  
(1, 5, 3, 7, 6, 2, 4); (1, 6, 5, 2, 3, 4, 7); (1, 7, 4, 3, 2, 5, 6);

$$7. -\frac{5 \cdot 35^n}{4} + \frac{9 \cdot 63^n}{4}$$

$$8. 4 + 4 * x - 2 * x^2 + 4 * x^3 + 4 * x^4$$

9. При  $\lambda = 8$

10. Определитель:  $52\lambda + 94$ , при  $\lambda = [-47/26]$  ранг равен 3, иначе 4