

1.

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$2. L = \begin{bmatrix} 1 & 0 & 0 & 0 \\ -6 & 1 & 0 & 0 \\ -8 & \frac{21}{20} & 1 & 0 \\ 9 & -\frac{13}{10} & -\frac{22}{37} & 1 \end{bmatrix}, U = \begin{bmatrix} -1 & 2 & -5 & -9 \\ 0 & 20 & -37 & -61 \\ 0 & 0 & \frac{37}{20} & -\frac{119}{20} \\ 0 & 0 & 0 & -\frac{216}{37} \end{bmatrix}$$

3.

$$\begin{pmatrix} -8 & -15 & -13 \\ -3 & 2 & -5 \\ 18 & 9 & 12 \end{pmatrix}$$

4.

$$\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 2 & 1 & 3 & 6 & 4 & 5 \end{pmatrix}$$

5.

$$\sigma = (1, 9)(2, 6, 4)(3, 7, 5, 8), \text{ord} = 12, \sigma^{-823} = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ 9 & 4 & 7 & 6 & 8 & 2 & 5 & 3 & 1 \end{pmatrix} = (1, 9)(2, 4, 6)(3, 7, 5, 8)$$

6. Id; (1, 2, 4, 7, 6, 5, 3); (1, 3, 5, 6, 7, 4, 2); (1, 4, 6, 3, 2, 7, 5);
(1, 5, 7, 2, 3, 6, 4); (1, 6, 2, 5, 4, 3, 7); (1, 7, 3, 4, 5, 2, 6);

$$7. \frac{8(-64)^n}{15} + \frac{7 \cdot 56^n}{15}$$

$$8. -1 + 1 * x + 3 * x^2 + 1 * x^3 + 3 * x^4$$

9. При $\lambda = -1$

10. Определитель: $374 - 96\lambda$, при $\lambda = [187/48]$ ранг равен 3, иначе 4