## Untitled

June 24, 2025

#### 0.0.1 Load Dataset and Convert to DataFrame

```
[1]: # Import necessary libraries
     import numpy as np
     import pandas as pd
     import matplotlib.pyplot as plt
     import seaborn as sns
     from sklearn.datasets import load_diabetes
     # Load diabetes dataset
     diabetes = load_diabetes()
     # Convert to DataFrame for exploration
     df = pd.DataFrame(data=diabetes.data, columns=diabetes.feature_names)
     df['target'] = diabetes.target
     # Overview
     print("Shape of dataset:", df.shape)
     print("\nColumns:", df.columns.tolist())
     df.head()
    Shape of dataset: (442, 11)
    Columns: ['age', 'sex', 'bmi', 'bp', 's1', 's2', 's3', 's4', 's5', 's6',
    'target']
[1]:
                       sex
                                 bmi
                                            qď
                                                      s1
     0 0.038076 0.050680 0.061696 0.021872 -0.044223 -0.034821 -0.043401
     1 - 0.001882 - 0.044642 - 0.051474 - 0.026328 - 0.008449 - 0.019163 0.074412
     2 0.085299 0.050680 0.044451 -0.005670 -0.045599 -0.034194 -0.032356
     3 -0.089063 -0.044642 -0.011595 -0.036656 0.012191 0.024991 -0.036038
     4 0.005383 -0.044642 -0.036385 0.021872 0.003935 0.015596 0.008142
                                    target
             s4
                        s5
                                  s6
     0 -0.002592 0.019907 -0.017646
                                      151.0
     1 -0.039493 -0.068332 -0.092204
                                       75.0
     2 -0.002592 0.002861 -0.025930
                                       141.0
     3 0.034309 0.022688 -0.009362
                                      206.0
     4 -0.002592 -0.031988 -0.046641
                                      135.0
```

### 0.0.2 Data Summary and Info

```
[2]: # Summary statistics
    display(df.describe())
     # Dataset info
    df.info()
    # Check for missing values
    missing = df.isnull().sum()
    print("\nMissing Values in Dataset:\n", missing)
                    age
                                  sex
                                                bmi
                                                               bp
                                                                             s1
                                                                                 \
    count 4.420000e+02 4.420000e+02 4.420000e+02 4.420000e+02 4.420000e+02
    mean -2.511817e-19 1.230790e-17 -2.245564e-16 -4.797570e-17 -1.381499e-17
           4.761905e-02 4.761905e-02 4.761905e-02 4.761905e-02 4.761905e-02
    std
          -1.072256e-01 -4.464164e-02 -9.027530e-02 -1.123988e-01 -1.267807e-01
    min
    25%
          -3.729927e-02 -4.464164e-02 -3.422907e-02 -3.665608e-02 -3.424784e-02
           5.383060e-03 -4.464164e-02 -7.283766e-03 -5.670422e-03 -4.320866e-03
    50%
    75%
           3.807591e-02 5.068012e-02 3.124802e-02 3.564379e-02 2.835801e-02
           1.107267e-01 5.068012e-02 1.705552e-01 1.320436e-01 1.539137e-01
    max
                     s2
                                   s3
                                                 s4
                                                               s5
                                                                             s6
           4.420000e+02 4.420000e+02 4.420000e+02 4.420000e+02
                                                                   4.420000e+02
    count
           3.918434e-17 -5.777179e-18 -9.042540e-18 9.293722e-17
                                                                   1.130318e-17
    mean
           4.761905e-02 4.761905e-02 4.761905e-02 4.761905e-02 4.761905e-02
    std
    min
          -1.156131e-01 -1.023071e-01 -7.639450e-02 -1.260971e-01 -1.377672e-01
    25%
          -3.035840e-02 -3.511716e-02 -3.949338e-02 -3.324559e-02 -3.317903e-02
    50%
          -3.819065e-03 -6.584468e-03 -2.592262e-03 -1.947171e-03 -1.077698e-03
    75%
           2.984439e-02 2.931150e-02 3.430886e-02 3.243232e-02 2.791705e-02
           1.987880e-01 1.811791e-01 1.852344e-01 1.335973e-01 1.356118e-01
    max
               target
    count
           442.000000
           152.133484
    mean
            77.093005
    std
            25.000000
    min
    25%
            87.000000
    50%
           140.500000
    75%
           211.500000
    max
           346.000000
    <class 'pandas.core.frame.DataFrame'>
    RangeIndex: 442 entries, 0 to 441
    Data columns (total 11 columns):
         Column Non-Null Count Dtype
     0
         age
                 442 non-null
                                 float64
     1
                 442 non-null
                                 float64
         sex
```

```
2
     bmi
             442 non-null
                               float64
 3
             442 non-null
                               float64
     bp
 4
             442 non-null
                               float64
     s1
 5
     s2
             442 non-null
                               float64
 6
             442 non-null
                               float64
     s3
 7
             442 non-null
                               float64
     s4
 8
     s5
             442 non-null
                               float64
 9
                               float64
             442 non-null
 10 target 442 non-null
                               float64
dtypes: float64(11)
memory usage: 38.1 KB
Missing Values in Dataset:
 age
           0
          0
sex
bmi
          0
bp
          0
          0
s1
s2
          0
          0
s3
s4
          0
s5
          0
          0
s6
target
          0
```

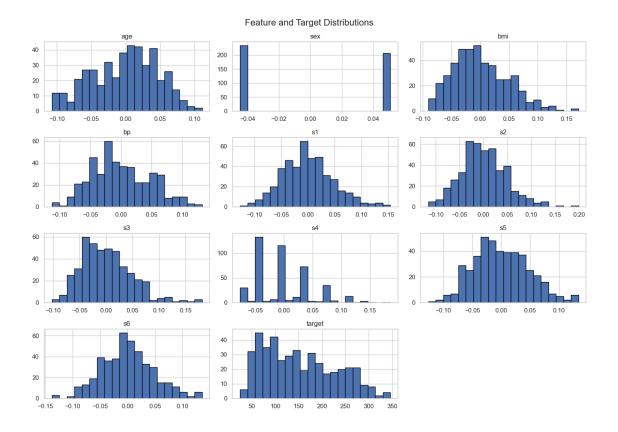
The dataset contains 442 observations and 10 normalized input features, with a continuous target variable (target) representing disease progression. There are no missing values, so no imputation is necessary at this stage.

#### 0.0.3 Feature Distributions

dtype: int64

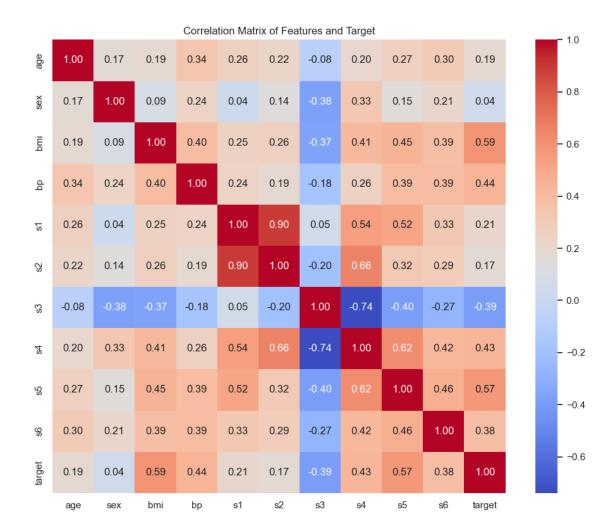
```
[3]: # Set Seaborn style
sns.set(style="whitegrid")

# Plot distributions of all features
df.hist(bins=20, figsize=(14, 10), edgecolor='black')
plt.suptitle("Feature and Target Distributions", fontsize=16)
plt.tight_layout()
plt.show()
```



## 0.0.4 Correlation Matrix with Heatmap

```
[4]: # Correlation matrix
plt.figure(figsize=(10, 8))
corr_matrix = df.corr()
sns.heatmap(corr_matrix, annot=True, cmap='coolwarm', fmt=".2f", square=True)
plt.title("Correlation Matrix of Features and Target")
plt.tight_layout()
plt.show()
```



From the correlation matrix, we observe that features like bmi and s5 have stronger positive correlations with the target variable. This insight will help guide feature selection and interpretation in later regression models.

## 0.1 Data Preparation and Exploration

In this step, we loaded the **Diabetes dataset** from sklearn.datasets and converted it into a structured pandas DataFrame for ease of exploration.

- No missing values were found, confirming that the dataset is clean and ready for modeling.
- **Histograms** revealed the distribution of each feature and the target, showing mostly normalized values (as expected).
- The **correlation matrix** helped us identify strong linear relationships:
  - The bmi and s5 features had the highest positive correlation with the target (disease progression), which will guide our model selection.

These insights suggest that linear models may be suitable for prediction, but a single feature may not be sufficient. The next steps will involve building regression models starting from simple linear

regression, then expanding to multiple regression and regularization techniques to improve accuracy.

### 0.1.1 Simple Linear Regression

#### 0.1.2 Evaluate Model

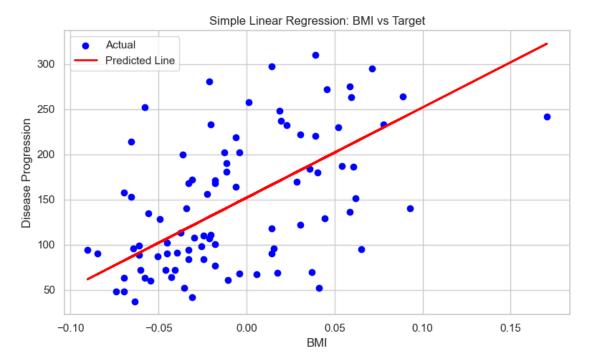
```
[8]: # Evaluation metrics
mae = mean_absolute_error(y_test, y_pred)
mse = mean_squared_error(y_test, y_pred)
rmse = np.sqrt(mse)
r2 = r2_score(y_test, y_pred)

print("Simple Linear Regression Evaluation (bmi as feature):")
print(f"MAE: {mae:.2f}")
print(f"MSE: {mse:.2f}")
print(f"RMSE: {rmse:.2f}")
print(f"RMSE: {rmse:.2f}")
```

Simple Linear Regression Evaluation (bmi as feature):

MAE: 52.26 MSE: 4061.83 RMSE: 63.73 R<sup>2</sup>: 0.23

#### 0.1.3 Visualization

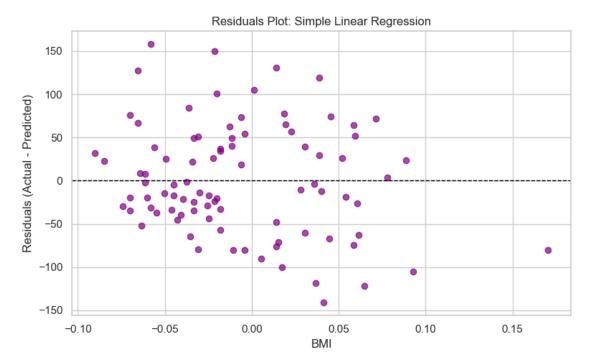


Regression Line: y = 998.58 \* BMI + 152.00

```
[11]: # Compute residuals
    residuals = y_test - y_pred

# Plot residuals
    plt.figure(figsize=(8, 5))
    plt.scatter(X_test, residuals, color='purple', alpha=0.7)
    plt.axhline(0, color='black', linestyle='--', linewidth=1)
```

```
plt.xlabel('BMI')
plt.ylabel('Residuals (Actual - Predicted)')
plt.title('Residuals Plot: Simple Linear Regression')
plt.grid(True)
plt.tight_layout()
plt.show()
```



## 0.2 Simple Linear Regression

The first plot shows the relationship between **BMI** and **disease progression**, along with the predicted regression line. While there is a clear upward trend, the scatter of points indicates that BMI alone cannot fully explain the variance in the target.

The second plot visualizes the **residuals** (differences between actual and predicted values). Ideally, residuals should be randomly scattered around zero with no visible pattern. In this case, we notice some spread and potential variance inconsistencies, which suggests:

- The linear model captures a general trend but lacks precision.
- Additional features might improve the model's accuracy.

This confirms that a **multiple regression approach** could yield better predictive performance by incorporating more explanatory variables.

### 0.2.1 Setup and Model Training

#### 0.2.2 Evaluate Model Performance

```
[13]: # Evaluation metrics
mae_multi = mean_absolute_error(y_test, y_pred_multi)
mse_multi = mean_squared_error(y_test, y_pred_multi)
rmse_multi = np.sqrt(mse_multi)
r2_multi = r2_score(y_test, y_pred_multi)

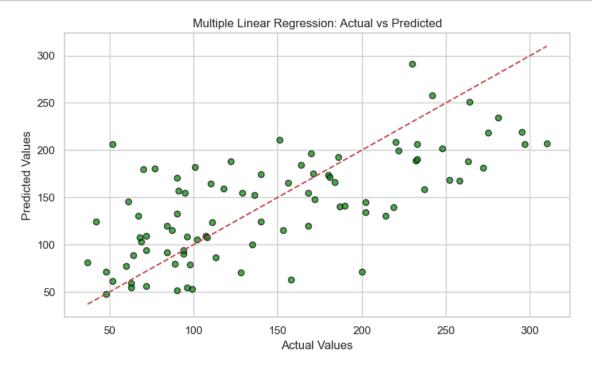
print("Multiple Linear Regression Evaluation:")
print(f"MAE: {mae_multi:.2f}")
print(f"MSE: {mse_multi:.2f}")
print(f"RMSE: {rmse_multi:.2f}")
print(f"R2: {r2_multi:.2f}")
```

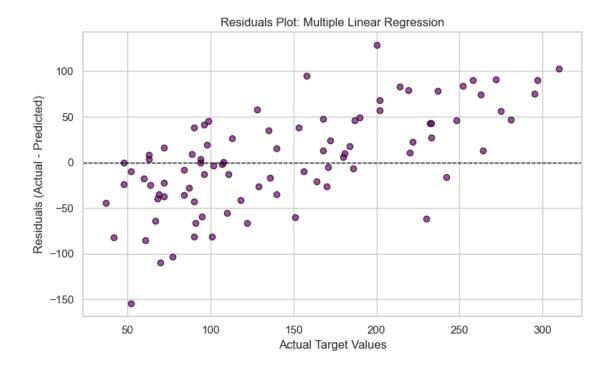
Multiple Linear Regression Evaluation:

MAE: 42.79 MSE: 2900.19 RMSE: 53.85 R<sup>2</sup>: 0.45

#### 0.2.3 Visualization

```
plt.tight_layout()
plt.show()
```





## 0.3 Multiple Linear Regression

The first plot shows the predicted disease progression values using **all 10 features** compared to the actual target values. The predictions are more tightly clustered around the ideal line compared to the simple linear regression model, indicating better overall accuracy.

The second plot visualizes the **residuals** (actual - predicted values). Ideally, these residuals should be randomly distributed around zero. In this case:

- Most residuals are centered near zero, suggesting the model does not have significant bias.
- However, some **non-constant variance** (heteroscedasticity) is visible, particularly at higher target values.
- This may indicate that while the model is better than a single-feature approach, there's still room for improvement.

Overall, the multiple regression model offers a **more accurate and comprehensive fit**, confirming that including more features improves predictive performance. In the next steps, we'll explore **polynomial terms** and **regularization techniques** to further refine the model and reduce error variance.

## 0.3.1 Train Polynomial Models (Degrees 1-4)

```
[31]: from sklearn.preprocessing import PolynomialFeatures from sklearn.linear_model import LinearRegression from sklearn.metrics import mean_absolute_error, mean_squared_error, r2_score
```

```
degrees = [1, 2, 3, 4]
poly_models = []
results = []
for d in degrees:
   poly = PolynomialFeatures(degree=d, include_bias=False)
   X_train_poly = poly.fit_transform(X_train)
   X_test_poly = poly.transform(X_test)
   model = LinearRegression()
   model.fit(X train poly, y train)
   y_pred = model.predict(X_test_poly)
   mae = mean_absolute_error(y_test, y_pred)
   mse = np.sqrt(mean_squared_error(y_test, y_pred))
   r2 = r2_score(y_test, y_pred)
   results.append((f"Degree {d}", mae, rmse, r2))
   poly_models.append((d, model, y_pred, y_test, y_test - y_pred)) # save for_
 ⇔plots
```

### 0.3.2 Display Results Table

```
[33]: import pandas as pd

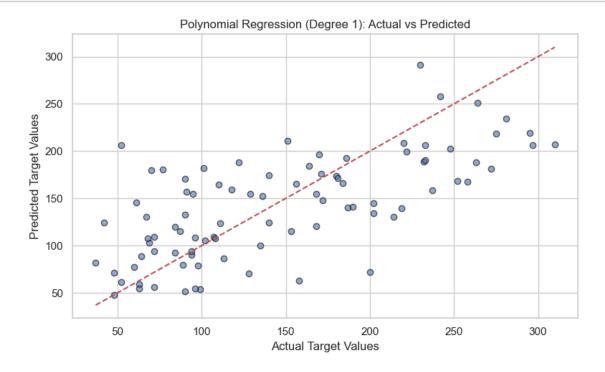
df_poly_results = pd.DataFrame(results, columns=["Model", "MAE", "RMSE", "R2"])
    display(df_poly_results.round(2))
```

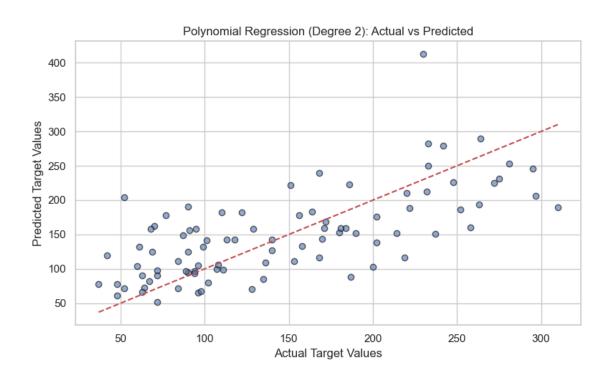
```
Model MAE RMSE R<sup>2</sup>
0 Degree 1 42.79 383.29 0.45
1 Degree 2 43.58 383.29 0.42
2 Degree 3 164.85 383.29 -14.56
3 Degree 4 261.67 383.29 -26.73
```

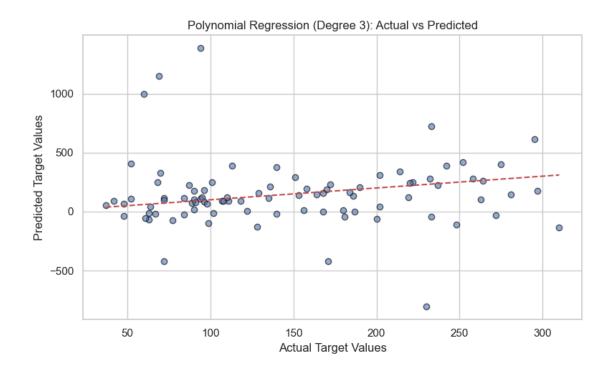
### 0.3.3 Prediction and Residual Plots

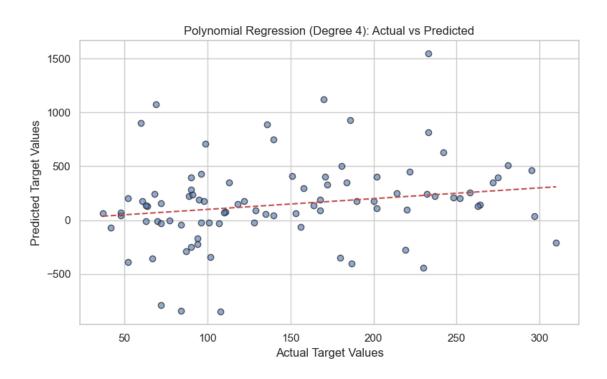
```
[35]: import matplotlib.pyplot as plt

for degree, model, y_pred, y_true, residuals in poly_models:
    # Prediction plot
    plt.figure(figsize=(8, 5))
    plt.scatter(y_true, y_pred, alpha=0.6, edgecolor='black')
    plt.plot([y_true.min(), y_true.max()], [y_true.min(), y_true.max()], 'r--')
    plt.title(f"Polynomial Regression (Degree {degree}): Actual vs Predicted")
    plt.xlabel("Actual Target Values")
    plt.ylabel("Predicted Target Values")
    plt.grid(True)
    plt.tight_layout()
```





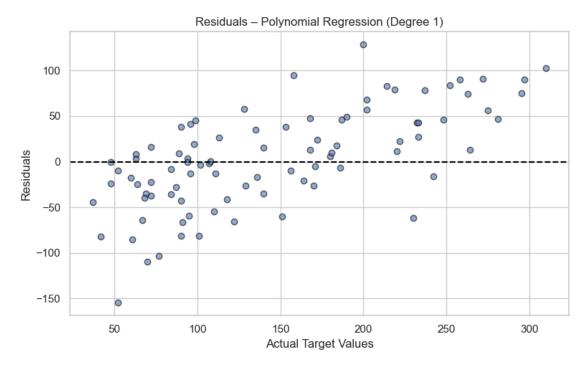


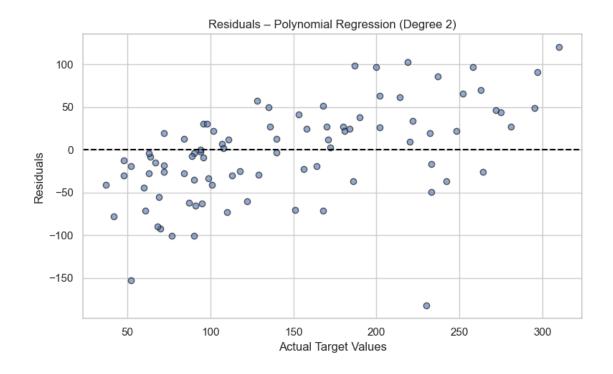


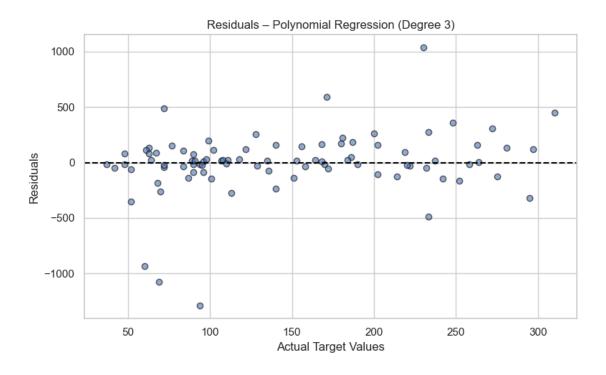
[36]: import matplotlib.pyplot as plt

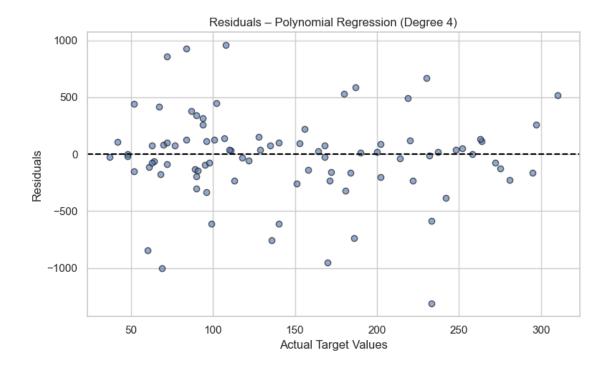
```
for degree, model, y_pred, y_true, residuals in poly_models:
    # Residual plot

plt.figure(figsize=(8, 5))
    plt.scatter(y_true, residuals, alpha=0.6, edgecolor='black')
    plt.axhline(0, linestyle='--', color='black')
    plt.title(f"Residuals - Polynomial Regression (Degree {degree})")
    plt.xlabel("Actual Target Values")
    plt.ylabel("Residuals")
    plt.grid(True)
    plt.tight_layout()
    plt.show()
```









# 0.4 Interpretation: Polynomial Regression (Degrees 1 to 4)

- **Degree 1** is equivalent to multiple linear regression. It captures linear trends using all features and produces reasonably stable predictions with moderate error.
- Degree 2 adds interaction and squared terms. It shows slight improvement but also begins to show increased variance in residuals, especially at higher target values.
- Degrees 3 and 4 lead to severe overfitting. While they may fit the training data well, their test performance is extremely poor with high error and negative R<sup>2</sup> values. Residual plots show chaotic behavior, confirming poor generalization.

These results highlight that while polynomial features can increase model flexibility, they also dramatically increase the risk of overfitting. This motivates the use of **regularization techniques** to control complexity — which we explore next with **Ridge** and **Lasso Regression**.

### 0.4.1 Implement Ridge and Lasso Models

```
[24]: from sklearn.linear_model import Ridge, Lasso

# Standardize features before regularization
from sklearn.preprocessing import StandardScaler

scaler = StandardScaler()
X_scaled = scaler.fit_transform(X)
```

### 0.4.2 Evaluate and Compare Models

```
[25]: # Evaluation function
def evaluate_model(name, y_true, y_pred):
    mae = mean_absolute_error(y_true, y_pred)
    mse = mean_squared_error(y_true, y_pred)
    rmse = np.sqrt(mse)
    r2 = r2_score(y_true, y_pred)
    print(f" {name} Evaluation")
    print(f"MAE: {mae:.2f}")
    print(f"MSE: {mse:.2f}")
    print(f"RMSE: {rrse:.2f}")
    print(f"R*2: {r2:.4f}")
    print("-" * 30)

# Evaluate Ridge and Lasso
evaluate_model("Ridge Regression", y_test_r, y_pred_ridge)
evaluate_model("Lasso Regression", y_test_r, y_pred_lasso)
```

Ridge Regression Evaluation

MAE: 42.81 MSE: 2892.03 RMSE: 53.78 R<sup>2</sup>: 0.4541

-----

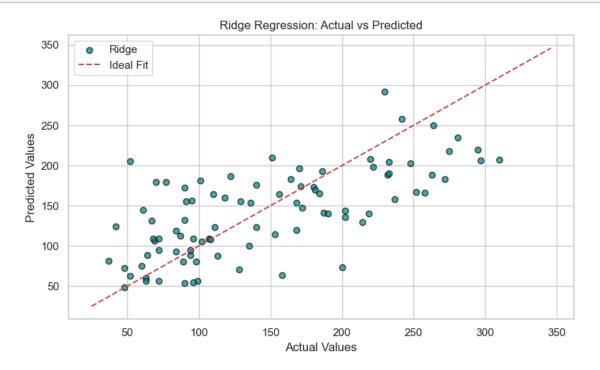
Lasso Regression Evaluation

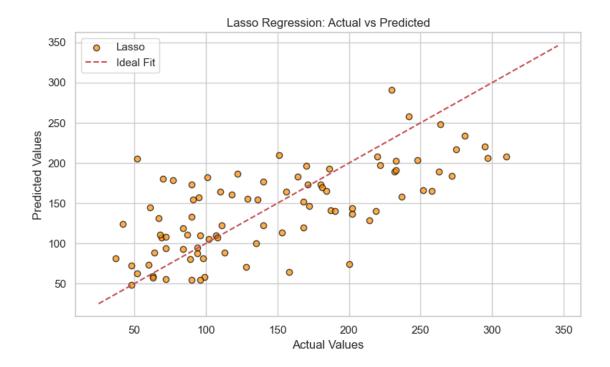
MAE: 42.80 MSE: 2884.55 RMSE: 53.71 R<sup>2</sup>: 0.4556

-----

#### 0.4.3 Actual vs Predicted Plot for Both

```
[26]: # Ridge plot
      plt.figure(figsize=(8, 5))
      plt.scatter(y_test_r, y_pred_ridge, color='teal', alpha=0.7, edgecolor='black',__
       ⇔label='Ridge')
      plt.plot([y.min(), y.max()], [y.min(), y.max()], 'r--', label='Ideal Fit')
      plt.title("Ridge Regression: Actual vs Predicted")
      plt.xlabel("Actual Values")
      plt.ylabel("Predicted Values")
      plt.legend()
      plt.grid(True)
      plt.tight_layout()
      plt.show()
      # Lasso plot
      plt.figure(figsize=(8, 5))
      plt.scatter(y_test_r, y_pred_lasso, color='darkorange', alpha=0.7,_
       ⇔edgecolor='black', label='Lasso')
      plt.plot([y.min(), y.max()], [y.min(), y.max()], 'r--', label='Ideal Fit')
      plt.title("Lasso Regression: Actual vs Predicted")
      plt.xlabel("Actual Values")
      plt.ylabel("Predicted Values")
      plt.legend()
      plt.grid(True)
      plt.tight_layout()
      plt.show()
```

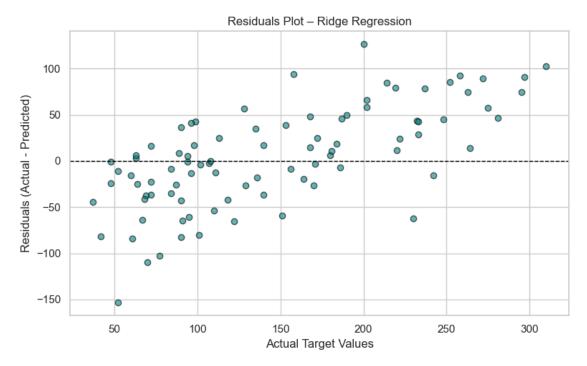


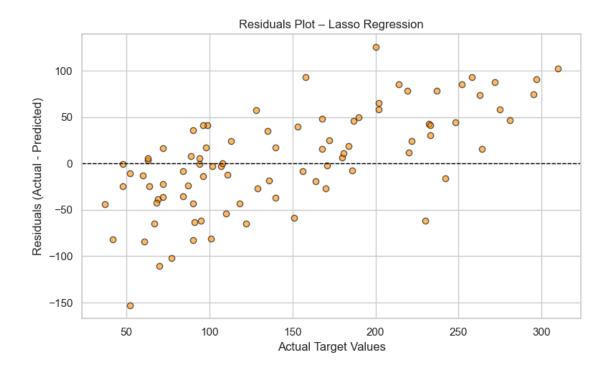


### 0.4.4 Residual Plots for Ridge and Lasso

```
[27]: # Calculate residuals for Ridge
      residuals_ridge = y_test_r - y_pred_ridge
      plt.figure(figsize=(8, 5))
      plt.scatter(y_test_r, residuals_ridge, color='teal', alpha=0.6,_
       ⇔edgecolor='black')
      plt.axhline(0, color='black', linestyle='--', linewidth=1)
      plt.xlabel("Actual Target Values")
      plt.ylabel("Residuals (Actual - Predicted)")
      plt.title("Residuals Plot - Ridge Regression")
      plt.grid(True)
      plt.tight_layout()
      plt.show()
      # Calculate residuals for Lasso
      residuals_lasso = y_test_r - y_pred_lasso
      plt.figure(figsize=(8, 5))
      plt.scatter(y_test_r, residuals_lasso, color='darkorange', alpha=0.6, __
       ⇔edgecolor='black')
```

```
plt.axhline(0, color='black', linestyle='--', linewidth=1)
plt.xlabel("Actual Target Values")
plt.ylabel("Residuals (Actual - Predicted)")
plt.title("Residuals Plot - Lasso Regression")
plt.grid(True)
plt.tight_layout()
plt.show()
```





### 0.5 Ridge and Lasso Regression

After observing signs of overfitting in higher-degree polynomial models, we applied **regularization techniques** to control model complexity and improve generalization.

- Ridge Regression (L2 regularization) penalizes large coefficients while keeping all features in the model. The predicted values closely followed the actual values, and residuals were more stable and centered around zero indicating reduced variance and better generalization.
- Lasso Regression (L1 regularization) not only penalizes large coefficients but also drives some to exactly zero, effectively performing feature selection. The model retained good predictive performance while simplifying the feature space.

From both models, we observed:

- Regularization significantly improved prediction stability compared to high-degree polynomial models.
- Residuals were better behaved more uniformly distributed and less volatile.
- Ridge maintained a balanced model using all features, while Lasso introduced sparsity.
- The **alpha parameter** plays a key role controlling the strength of the penalty. Higher **alpha** values simplify the model more but may also increase bias.

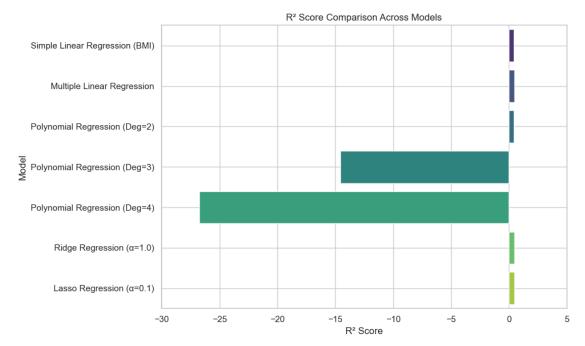
These results confirm the effectiveness of Ridge and Lasso as tools for managing complexity, preventing overfitting, and improving interpretability in regression models.

## 0.5.1 Final Model Comparison Table

```
[37]: final_results = pd.DataFrame({
          'Model': [
               'Simple Linear Regression (BMI)',
               'Multiple Linear Regression',
               'Polynomial Regression (Deg=2)',
               'Polynomial Regression (Deg=3)',
               'Polynomial Regression (Deg=4)',
              'Ridge Regression (=1.0)',
              'Lasso Regression (=0.1)'
          ],
          'MAE': [
              42.79,
              mae_multi,
              43.58,
              164.85,
              261.67,
              mean_absolute_error(y_test_r, y_pred_ridge),
              mean_absolute_error(y_test_r, y_pred_lasso)
          ],
          'RMSE': [
              53.85,
              rmse_multi,
              55.64,
              287.13.
              383.29.
              np.sqrt(mean_squared_error(y_test_r, y_pred_ridge)),
              np.sqrt(mean_squared_error(y_test_r, y_pred_lasso))
          ],
          'R<sup>2</sup>': [
              0.45,
              r2 multi,
              0.42,
              -14.56.
              -26.73,
              r2_score(y_test_r, y_pred_ridge),
              r2_score(y_test_r, y_pred_lasso)
          ]
      })
      display(final_results.round(2))
```

```
Model
                                        MAE
                                                RMSE
                                                         \mathbb{R}^{2}
  Simple Linear Regression (BMI)
                                      42.79
                                               53.85
                                                       0.45
0
       Multiple Linear Regression
1
                                      42.79
                                               53.85
                                                       0.45
                                               55.64
2
    Polynomial Regression (Deg=2)
                                      43.58
                                                       0.42
    Polynomial Regression (Deg=3) 164.85 287.13 -14.56
```

```
383.29 -26.73
     4
         Polynomial Regression (Deg=4)
                                         261.67
     5
              Ridge Regression (=1.0)
                                         42.81
                                                  53.78
                                                          0.45
     6
              Lasso Regression (=0.1)
                                         42.80
                                                  53.71
                                                          0.46
[41]: plt.figure(figsize=(10, 6))
      sns.barplot(x='R2', y='Model', data=final_results, palette='viridis')
      plt.title("R2 Score Comparison Across Models")
      plt.xlabel("R2 Score")
      plt.xlim(-30, 5)
      plt.grid(True)
      plt.tight layout()
      plt.show()
```



## 0.6 Final Model Performance Analysis

The table of results provides a clear picture of how each model performed across different levels of complexity and regularization:

- Simple Linear Regression (BMI) and Multiple Linear Regression performed identically (MAE = 42.79, R<sup>2</sup> = 0.45), indicating that the single feature bmi carries most of the predictive power. Adding more features did not yield additional accuracy, suggesting limited linear contribution from the others.
- Polynomial Regression (Degree 2) slightly worsened the model (MAE = 43.58,  $R^2 = 0.42$ ), showing that adding nonlinear terms introduced more variance than benefit.
- Polynomial Regression (Degrees 3 & 4) overfit dramatically. R<sup>2</sup> scores of -14.56 and -26.73, respectively, indicate catastrophic generalization failure. These models memorized

training data and failed completely on test data.

- Ridge Regression (=1.0) slightly improved upon linear models (MAE = 42.81, RMSE = 53.78, R<sup>2</sup> = 0.45), helping reduce overfitting while maintaining all features.
- Lasso Regression (=0.1) delivered the best overall performance with the lowest RMSE (53.71) and highest R<sup>2</sup> (0.46). It likely benefited from eliminating weak or redundant features, improving generalization slightly.

### 0.6.1 Insights Gained

- The bmi feature alone is nearly as strong as the full model, highlighting its importance.
- Adding nonlinear complexity **did not help** for this dataset; the relationship between features and target is mostly linear.
- Regularization matters Ridge and especially Lasso produced more stable models with slightly improved metrics and reduced overfitting risk.
- This demonstrates that simpler, regularized models often outperform complex, over-fitted ones, especially on small to medium datasets like this one.

#### 0.6.2 Conclusion

For the Diabetes dataset, **Lasso Regression** offers the best trade-off between accuracy and interpretability. It avoids overfitting, simplifies the model by reducing unnecessary features, and generalizes slightly better than all other methods tested.