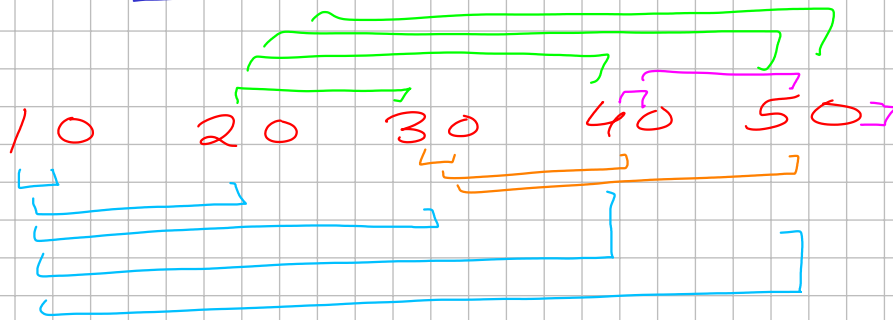


Generate Subarray

Theory:- Subarray of an array is a contiguous part of an given array.

eg:-

0	1	2	3	4
10	20	30	40	50



all subarrays.

let i be start of the subarray and j be the end of the subarray.

We can say,

$$0 \leq i \leq n-1$$

$$i \leq j \leq n-1$$

no of possible subarrays for n size

i	j	# Sub-arrays
0	0 to $n-1$	n
1	1 to $n-1$	$n-1$
2	2 to $n-1$	$n-2$
\vdots	\vdots	\vdots
$n-1$	$n-1$ to $n-1$	1

$$\Sigma = \frac{n(n+1)}{2}$$

$$\approx n^2$$

$$\boxed{\frac{n(n+1)}{2}} \rightarrow \text{no of subarray}$$

Code:-

```
CB > LEC11 > 1_generate_subarray.cpp > ...
1  #include <iostream>
2
3  using namespace std;
4
5  void generateSubArray(int arr[], int n)
6  {
7      for(int i = 0; i <= n-1; i++)
8      {
9          for(int j = i; j <= n-1; j++)
10         {
11             cout << i << j << ":";
12             for(int k = i; k <= j; k++)
13             {
14                 cout << arr[k] << " ";
15             }
16             cout << endl;
17         }
18         cout << endl;
19     }
20 }
21
22 int main()
23 {
24     int arr[] = {10,20,30,40,50};
25     int n = 5;
26
27     generateSubArray(arr,n);
28 }
```

Output

```
00:10
01:10 20
02:10 20 30
03:10 20 30 40
04:10 20 30 40 50

11:20
12:20 30
13:20 30 40
14:20 30 40 50

22:30
23:30 40
24:30 40 50

33:40
34:40 50

44:50
```

Maximum Subarray Sum

↳ To find the maximum subarray sum

Theory:-

Cumulative Sum / Prefix Sum

↳ eg:- 10 20 30 40 50

10 → 10
10 20 → 30
10 20 30 → 60
10 20 30 40 → 100
10 20 30 40 50 → 150



Prefix
sum

Method - I

Brute force method :-

can be implemented from the above code.

Time complexity :- $O(n^3)$

Space complexity :- $O(1)$

Method - II

Optimizing the above method.

by computing the prefix sum of the array.

eg :-

S_{16}

-	0	1	2	3	4	5	6	7	8
	-2	1	-3	4	-1	2	1	-5	4

0	1	2	3	4	5	6	7	8	9
	-2	-1	-4	0	-1	1	2	-3	1

arr

prefix sum
arr.

① $\rightarrow S_{16}$

formula :- $[pSum[j+1] - pSum[i]] = S_{ij}$

0		$i-1$	i		4
	...	j		...	

for finding
the subarray sum

$$\textcircled{2} [pSum[i] = pSum[i-1] + arr[i-1]]$$

for computing the prefix sum
arr

	$i-1$	i	

prefix sum
array
array

don't have to iter
over these values

Code:-



```
CB > LEC11 > 2_maximum_subarray_sum.cpp > ...
1  #include <iostream>
2  #include <climits>
3  using namespace std;
4  int maxSubArraySum(int arr[], int n)
5  {
6      int maxSoFar = INT_MIN;
7      int psum[101] = {};
8      psum[0] = 0; // Initialize the first prefix sum to 0
9      for(int i = 1; i <= n; i++)
10     {
11         psum[i] = psum[i-1] + arr[i-1];
12     }
13
14     for(int i = 0; i <= n-1; i++)
15     {
16         for(int j = i; j <= n-1; j++)
17         {
18             int sum = psum[j+1] - psum[i];
19             maxSoFar = max(maxSoFar, sum);
20         }
21     }
22     return maxSoFar;
23 }
24 int main()
25 {
26     int arr[] = {10,20,30,40,-100};
27     int n = 5;
28     cout << maxSubArraySum(arr,n);
29 }
30
31
```

100:- constraint

(2)

Computing prefix

checking subarray sum (1)

Output:- 100

Time Complexity :- $O(n^2)$

Space Complexity :- $O(n)$

Method-III (Kadane Method)

Best Method for finding subarray sum.



Theory

Assume :-

arr,

0	1	2	3	4
-3	2	-1	4	-5

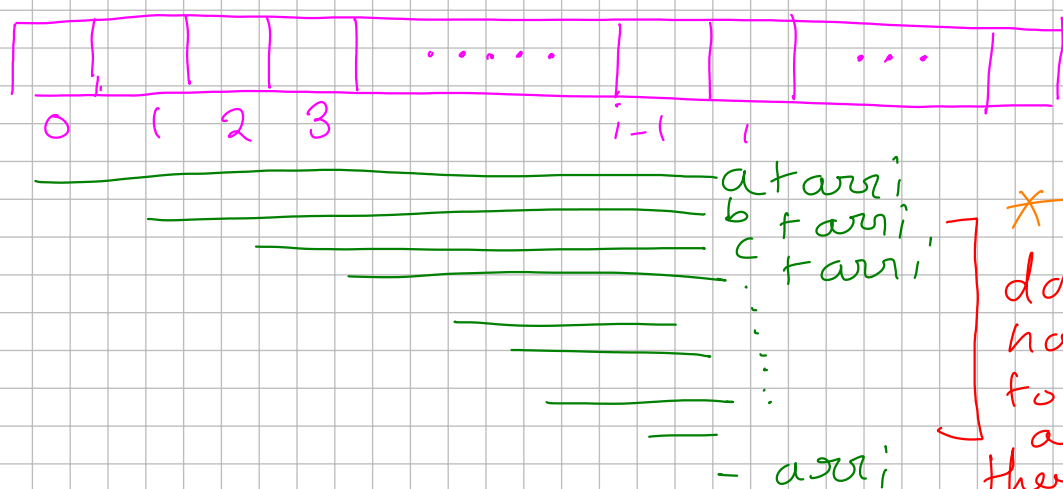
arr

-3	2	1	5	0
----	---	---	---	---

x

$x_0 \quad x_1 \quad x_2 \quad x_3 \quad x_4$

$x_i \rightarrow \text{Max}(\text{sum of elements which end at } i) (\text{contiguous of } arr)$



*
don't have to check as they are $< a + arr_i$

\therefore if we have, x_{i-1} and arr_i ,

we can find x_i by

$$x_i \rightarrow \max(x_{i-1} + arr_i, arr_i)$$

Calculating values of x ,

$$\begin{aligned}
 x_1 &= \max(x_0 + arr_1, arr_1) \\
 &= \max(-3 + 2, 2) \\
 &= \max(-1, 2) = 2
 \end{aligned}$$

$$\begin{aligned}
 x_2 &= \max(x_1 + arr_2, arr_2) \\
 &= \max(2 + (-1), -1) \\
 &= \max(1, -1) = 1
 \end{aligned}$$

$$x_3 = \max(x_2 + arr_2, arr_2) \\ = \max(1 + 4, 4) = 5$$

$$x_4 = \max(x_3 + arr_3, arr_3) \\ = \max(5 + -5, -5) \\ = \max(0, -5) = 0 //$$

$$x_0 \text{ is } arr_0 = \underline{\underline{-3}}$$

Code:-

```
CB > LEC11 > 4_maximum_subarray_kadane_algo_space_optimized.cpp > ...
1  #include <iostream>
2  #include <climits>
3  using namespace std;
4
5  int maxSubArraySumUsingKadane(int arr[], int n){
6      int x; ← Space optimized
7      x = arr[0];
8      int maxSoFar = x; → xi-1
9
10     for(int i = 0; i <= n-1; i++)
11     {
12         x = max(x+arr[i], arr[i]);
13         maxSoFar = max(maxSoFar, x);
14     }
15     return maxSoFar;
16 }
17
18 int main()
19 {
20     int arr[] = {1};
21     int n = 1;
22     cout << maxSubArraySumUsingKadane(arr, n);
23 }
24
25
```

calc
x_{i-1}
and
finding the
max sum.

Time Complexity → $O(n)$

Space Complexity → $O(1)$, if arr of x
is maintained
then, $O(n)$

