

Artificial Intelligence

Introduction

- one of the fascinating and universal field in computer science which has a greatest scope in the future
- It has a tendency to cause a machine to work as human.
- At present, AI is working with a variety of sub-fields, e.g., whatever gadgets we are using nowadays are based on AI like ranging from general to specific - e.g. Self driving car, playing chess in the mobile phone, playing music, video, everything is related to AI

what is Artificial Intelligence?

"[↙] man made" + "[↑] thinking power"

"It is branch of computer science by which we can create an intelligent machine which can behave like a human, think like human & able to make decisions"

→ we do not need to pre-program the machine. e.g. if we are talking about an gadget, computer, mobile phone etc, they are programmed to perform a specific task

- In AI, we do not need to preprogram machine to do some work.
- we have to create a machine with programmed algorithm which can work with own intelligence i.e. it can take its own decision with its own intelligence (man-made intelligence)

Reas of Boost in AI

- 1) Smart device can be made to solve real time problems.
- 2) Creation of virtual assistant [SIRI, CORTANA]
to help/assist humans
- 3) Robots development
[Helps in dangerous environment condition]
(e.g. nuclear affected, land mine, diffusion of bomb, disaster prone area]
- 4) New job opportunities

Applications of AI :-

- 1) AI in Gaming: Chess, Poker, tic-tac

2. Artificial Intelligence
Date : 21/10/2021

What is Artificial Intelligence?

- with the help of AI, we can predict the happenings and take steps soon before anything starts very early and take necessary steps to reduce losses, maintaining healthy income.
- with the help of AI, you can create your business without any investment or cost.
- with the help of AI, you can build such tools which can work for an environment where human can be at risk for health issues.
- It gives a path for new technologies, new devices and new opportunities.

Goals of Artificial Intelligence

- ① Duplicate human intelligence
- ② have knowledge-based system
- ③ be intelligent correction of equipments used
- ④ building a machine which can interpret the inputs by an intelligent but non-thinking human
- ⑤ Playing chess
- ⑥ Non-human based system
- ⑦ having a car to fully depend on the vehicle and running with it

Linguistic intelligence → It refers to ability to use language effectively both in written and oral form. It involves capacity to understand and use words effectively. People with good linguistic intelligence can learn new language easily.

(5) Creating some systems which can exhibit intelligent behaviour, learn new things by itself, demonstrate, explain and can advise to its user.

(6) Intelligent communication between Perception & action

What is Intelligence composed of?

Artificial - man made

Intelligence - thinking power

judgment, making decisions
prediction

Reasoning

Intelligence

Linguistic Intelligence

(Important in
interpersonal
communication)

Learning

activity of gaining knowledge

Perception

process of acquiring, gathering, interpreting, selecting, organizing sensor information

Problem Solving

process of working through details of a problem to reach the solution (decision making)

Perception is a mechanism that puts data acquired by the sensor together in a meaningful manner.

Applications of AI

(1) AI in Gaming: e.g. chess, poker, tic-tac-toe
Machines can think large number of possible moves

Robotic surgery It is also known as robot-assisted surgery, is a type of minimally invasive surgery that uses robotic systems to perform surgical procedures. The robotic system is operated by a trained surgeon who controls the robot through a console.

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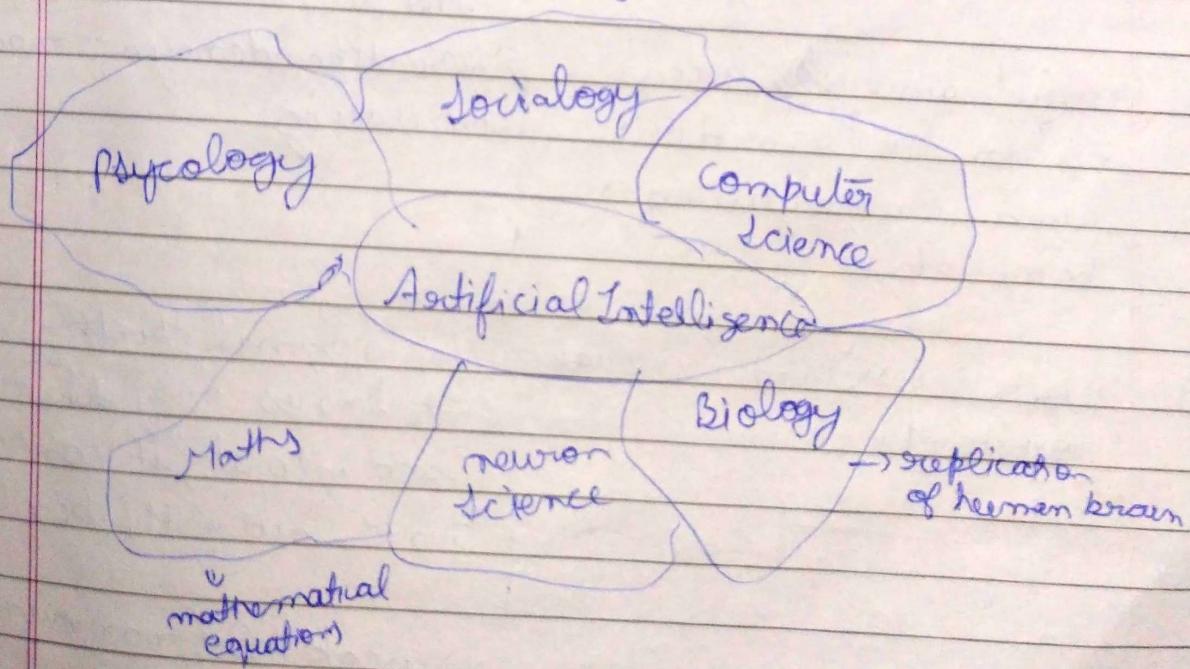
- ① **AI in NLP**: Natural language processing
↳ Machine can understand human language
- ② **AI in Healthcare**: Fast diagnosis of disease so timely
↳ Robotic surgery treatment can be provided
- ③ **AI in Finance**: Adaptive intelligence
↳ automatic chatbots, algorithm trading (algo. is deciding suggesting that ^{which} share to buy, M&A is widely being used in this domain)
- ④ **AI in Data Security**: helps in making data / application more secure.
e.g. AI bot, AI2 platform
They can detect bug in the software efficiently & prevent cyber attack efficiently in a more effective manner.
- ⑤ **Expert Systems**:- It is an integration of Software, machine and Special information to provide reasoning and advice.
e.g. If we are ~~not~~ stuck in some problem, we usually consult an expert that can give wise suggestion to deal with the problem.
^{through its extensive knowledge} Likewise we can make expert system in the machine
- ⑥ **Computer vision**:- To understand the visual automatically by machine (e.g. image / video recognition)

The robotic system consists of surgeon's console, robotic arms and camera arm. The surgeon sits at the console and control the robot arms, which are ~~equipped with~~
<sup>Evergreen
Page No.</sup> surgical instruments. The camera arm ~~provides 3D~~
^{Provides} view of surgical site allowing surgeon to see ~~area in~~
^{greater detail} speech recognition; it helps in extracting the meaning of the sentence by human talk & slangs removal, noise removal etc.]

(8) Robotics: ^{host} Intelligent ~~Robot~~ humanoid robots \rightarrow Erica and Sophia (they can talk & behave like humans)

(9) AI in e-commerce: Automatic recommendation of products, handling service requests through chatbots etc.

AI is comprised of:-



- ↳ Reasoning
→ Learning
→ Problem solving
→ Language understanding

Advantages of AI

① Accuracy ↑ & Error ↓



② High Speed / Fast decision making (e.g. AI system that dominated chess champion in chess game)

③ Reliability is more

④ Useful in risky areas (e.g. in hazardous areas, or diffusing a bomb etc.)

⑤ Digital Assistant (virtual assistant)

Disadvantages of AI

cost ↑ (as more S/w & H/w components will be used to increase the accuracy & reduce the error)

it can't think beyond its limits (e.g. system trained to play chess cannot play ludo)

No feeling and emotions (e.g. replacing nurse with a robot)

More dependency on machine increasing

No original thinking (It knows only the method feed into it, it can't think out of the box)

Classification of AI

weak AI (narrow AI)

Only trained for one specific task (General AI)

- i) Weak AI (also known as Narrow AI) (dedicated for one task)
- It is able to perform dedicated tasks with intelligence
 - It can't perform beyond its field or limitations
 - It is not concerned with how the task is being performed but is affected by the efficiency of the task

Evolutionary algo. solves problem by employing processes that mimic the behaviors of living things. As such, it uses mechanisms that are typically associated with biological evolution, such as reproduction, mutation and recombination. Weakest solutions are eliminated while stronger, more viable ones are retained and re-evaluated in the next evolution.

Example

All the goal being to arrive at optimal actors to achieve the desired outcome.

Flying machine

using logics

Mobile SIRI (will be able to perform only the tasks for which it is trained)

Playing chess

Self driving car, speech recognition, image recognition

perform like human

i) Strong AI (also known as General AI)

(could perform) It is the study and design of machines that simulate human mind to perform intelligent tasks. (which can think & perform tasks like humans, currently no such system exists.)

The idea behind general AI is to make such a system which could be smarter and think like a human by its own.

1) Borrowing ideas from physiology and neuroscience

ii) forgetting things, genetics, language understanding

Evolutionary AI

It is the study and design of machines that simulate simple creatures and attempt to evolve. e.g. Ants, bees etc.

Super AI (Intelligent than human hypothetical concept)

↳ Design under thought process
Seeks to create machines better than humans

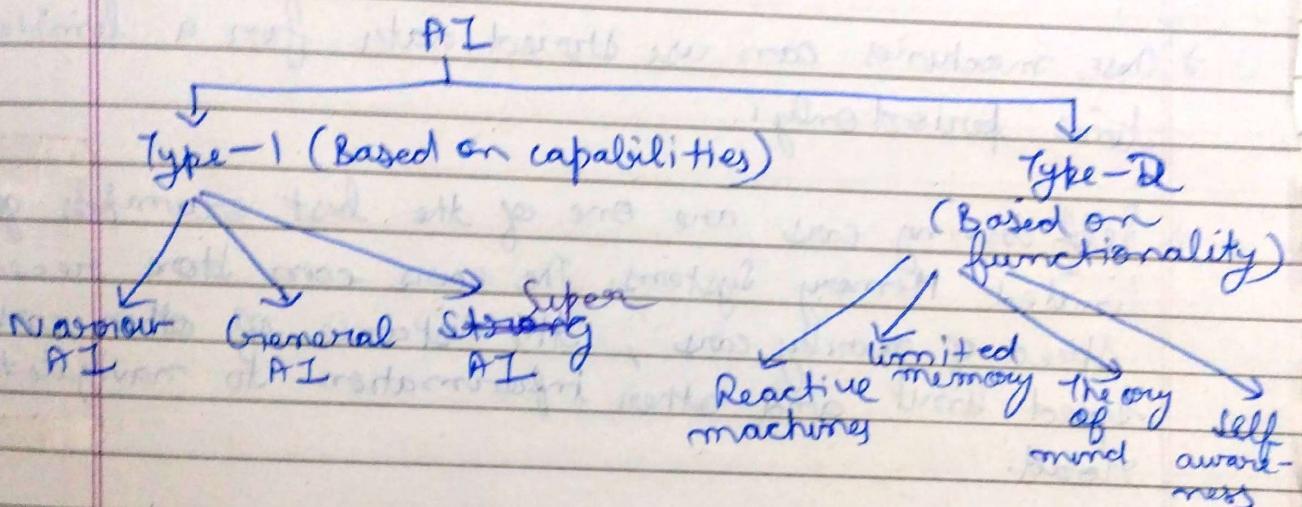
↳ [Machine communication machine]
machine could surpass human intelligence. It is an outcome of general AI.

Super AI: continued

Some key characteristics may include the ability to think, to reason, solve the puzzle, make judgements, plan, learn and communicate by its own.

Classification of AI

AI can be classified as



Type-1 has been discussed above.

Type-2

① Reactive machines

- Purely reactive machines are the most basic types of AI
- Such AI systems do not store memories or past experiences for future actions.
- These machines only focus on current decisioning

and react on it as per possible best action.

- IBM's Deep Blue system is an example of reactive machine
- Google AlphaGo

② Limited Memory

- Limited memory machines can store past experiences or some data from a short period of time.
- These machines can use stored data for a limited time period only.
- Self-driving cars are one of the best examples of limited memory systems. The cars can store recent speed of nearby cars, the distance of other cars, speed limit and other information to navigate the road.

③ Theory of mind

- Theory of mind should understand human emotions, people beliefs and be able to interact socially like humans.
- This type of AI machines are still not developed, but researchers are making lots of efforts and improvement for developing such AI machines.

④ Self-Awareness

- Self-awareness AI is the future of AI. These

machines will be super intelligent, and will have their own consciousness, sentiments and self-awareness.

- These machines will be smarter than human mind.
- Self-Awareness AI does not exist in reality still and it is a hypothetical concept.

AI Agents [Responsible for any work output obtained from the system]

AI is defined as a study of rational agents.

- It is main component of AI
- It is an intelligent component of the system that needs to be developed

Agent → gather¹⁵ information from the environment
→ perform action accordingly

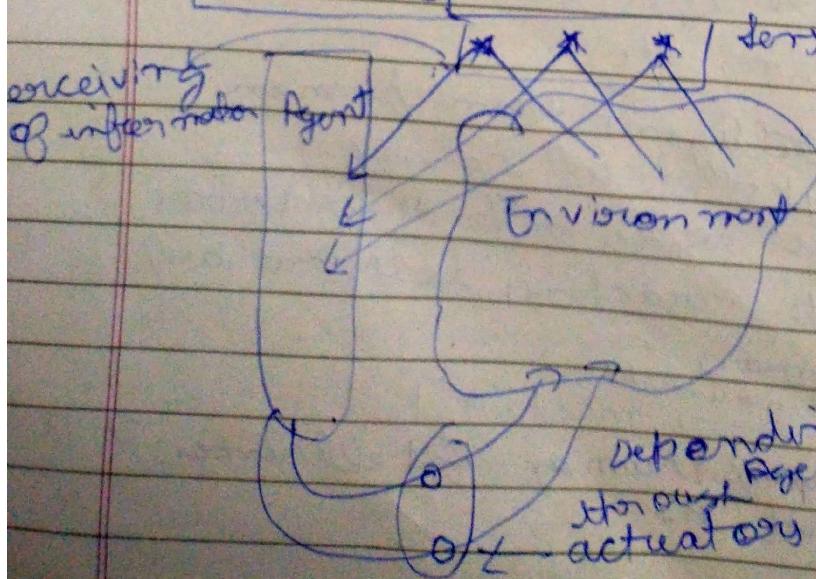
Agents → Person
→ Firm
→ Machine / Software

rational agent
the one that
can make
decisions

AI system is composed of → Agent
→ environment

Agent is anything like :-

- i) Receiving ^{sense} information through [sensors]
- ii) Acting upon that environment through [actuators].



Actuators - These are the devices that convert AI agent's decisions into actions

depending upon the info received
Agent acts on the environment
through actuators (action on the environment)

Agent perceives info about the environment through the sensory

→ Depending upon the info received, agent acts upon the environment

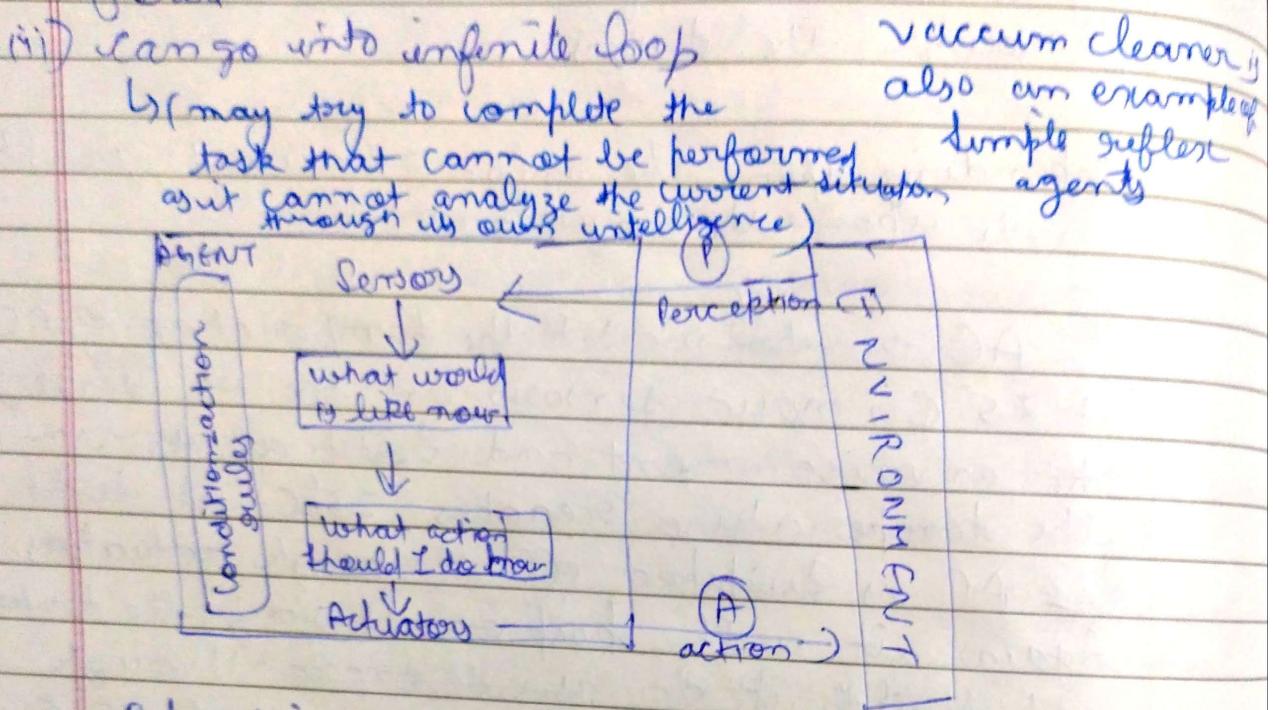
e.g. AC → If we set the temperature of AC at 25°C , now sensors in the AC keep on sensing the environment and switch off as soon as the temperature reaches 25°C . It switch off AC is switched off through actuators. Again it will keep on sensing the temperature and switch it on as it exceeds through actuators as temperature exceeds 25°C

∴ Through sensors and actuators, agents act upon the environment.

Types of AI Agents

- ① Simple Reflex Agents → (works only on limited domain)
 - Works only on current situation / perception
 - and ignores the history of previous state.
 - follows [Condition - Action] Rule
 - ↳ If condition true :- do this
 - If condition is true then take some action
 - Limitations :-
 -) Very limited intelligence (can perform only the work that is stated in it)
 -) No knowledge about non perceptual parts
 -) No knowledge about situations it will have (if some issue arises for which it is unknown then it will have no knowledge regarding what to do)

- Q.2 of Simple reflex agent
- AI enabled camera that clicks photographs and performs auto focus or performs ~~apply filters~~^{Page No.} based on current scenario. It does ~~not~~^{not} depend upon the previous photograph taken of state



Depending upon the action, agent will attempt to perform some action on the environment through actuators.

- ② Model based reflex agents Knowledge
- By analyzing the current situation, works by finding the rule whose condition matches current situation.
 - can work in partially observable environment and track situation.
 - Agent keeps track of internal state which is adjusted by each percept and that depends on percept history.
 - ↳ Model → how things happen in the world
 - Agent State update required information:
 - ① how world is evolving
 - ② how an agent's action affects the world.

present state
update required
situation decision

- (1) - ①
- (2) - ②
- (3) - ③

how the world evolves

what my action do

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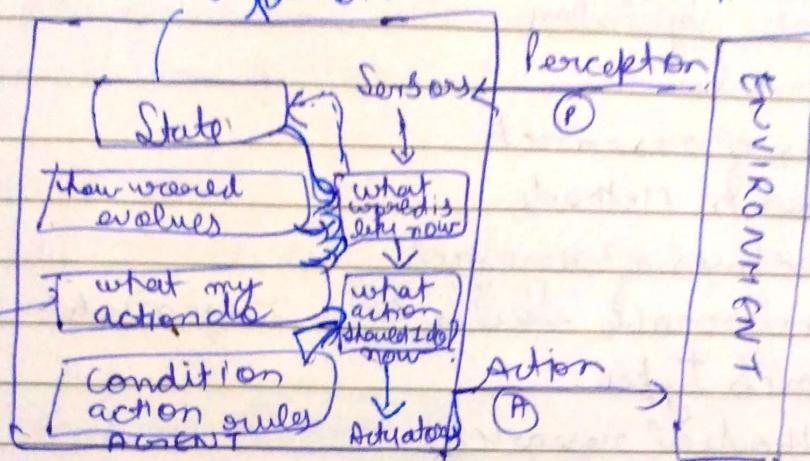
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Date _____ - defines the environment

Actuator - performing the action

cleaner
e.g.
vacuum
environment house
(env) floor)

what is the
result
of action



→ It stores the previous experience also (in the form of state) which is used for examining the current state

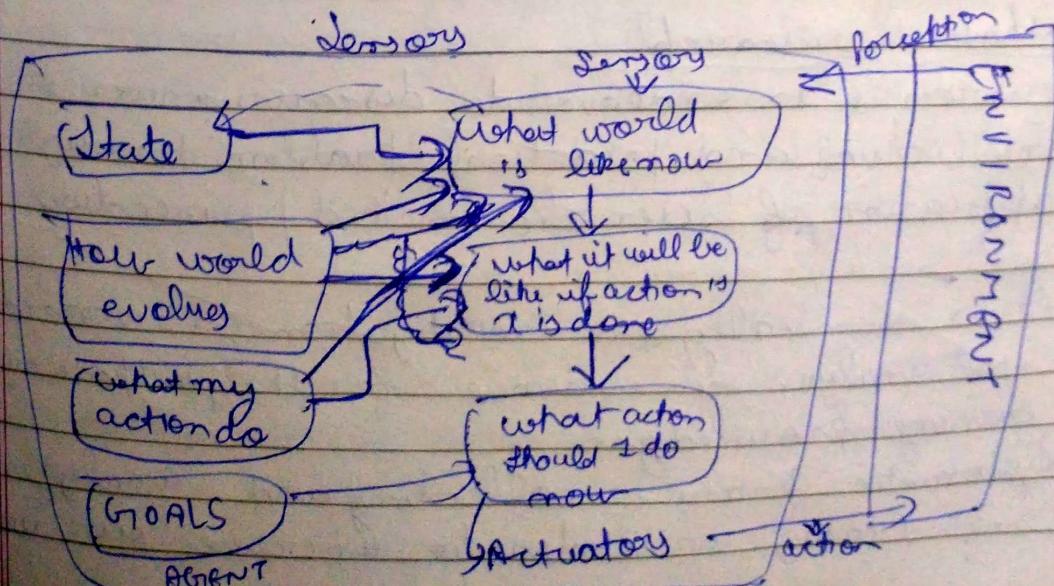
③ Goal based Agent

→ focuses only on reaching the goal set

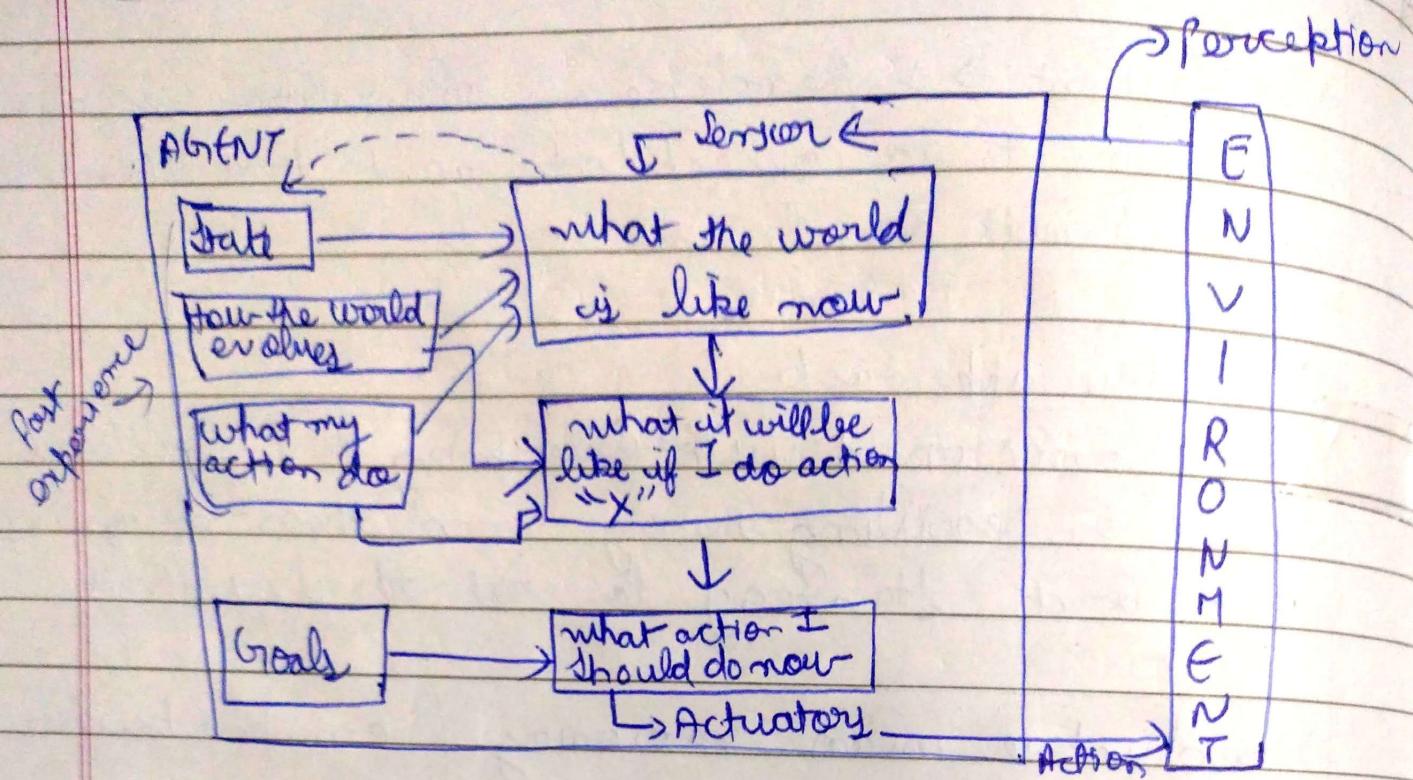
→ Agent takes decision based on how far it is currently from the goal state.

→ Every action is taken to minimize the distance to goal state

→ more flexible agent (know the goal)



Goal based agents (continued)



Ex. Rubik's cube

Environment - Rubik's cube

Sensors are perceiving Rubik's cube (current condition)

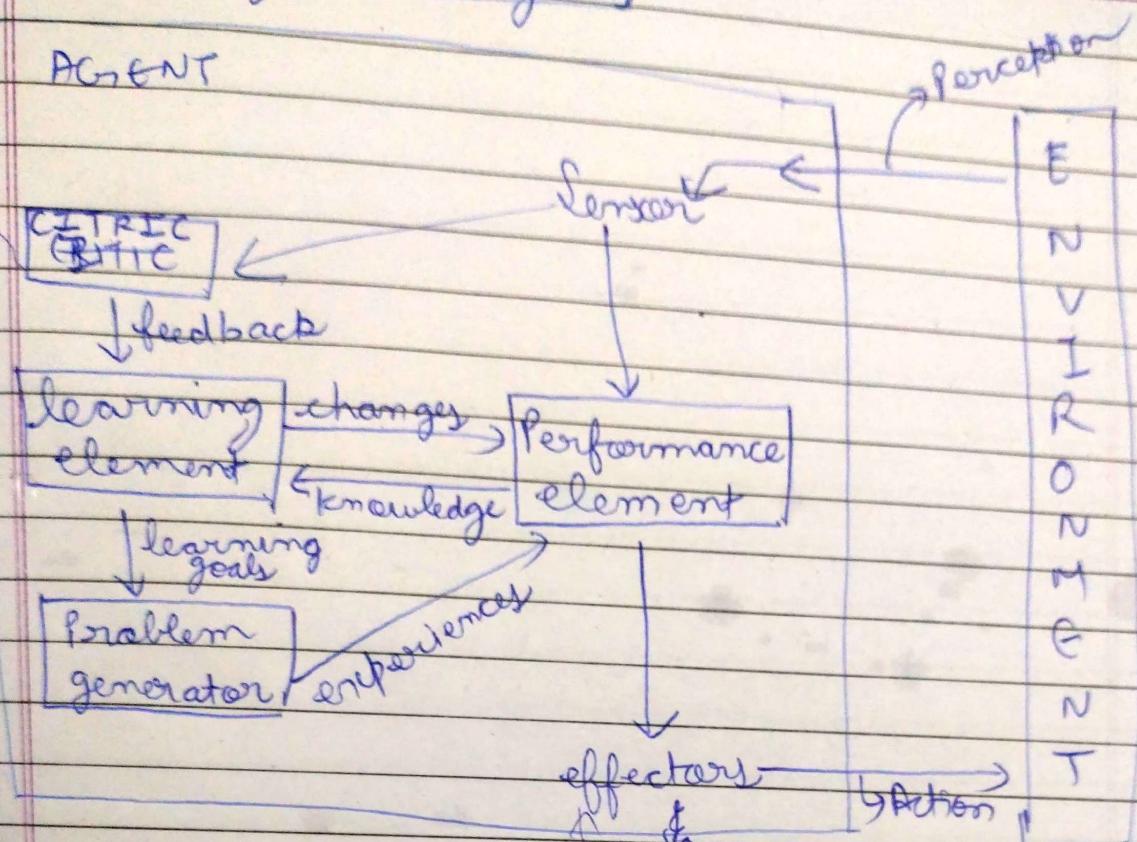
"then" agent will see that how much it becomes nearer to the goal (ie. solving) i.e. how much is the rubik's cube solved in order to if it takes action x

State - Stores the previous actions taken by the agent.

∴ Agent also checks if that specific state is previously encountered by consulting the state. If it similar/same scenario is encountered before also, it will take the action

⑤ Learning based agents

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- Learn from its past experiences
 - Start to act with basic knowledge and then able to act by adapting learning. (Learning enablers keeps on enhancing with past experiences)
- Components:-

learning element : - Improve system by learning from environment. (It suggests the learning goals to the problem generator)

Critic → checks agent working and gives feedback.
(check the performance & gives feedback accordingly)

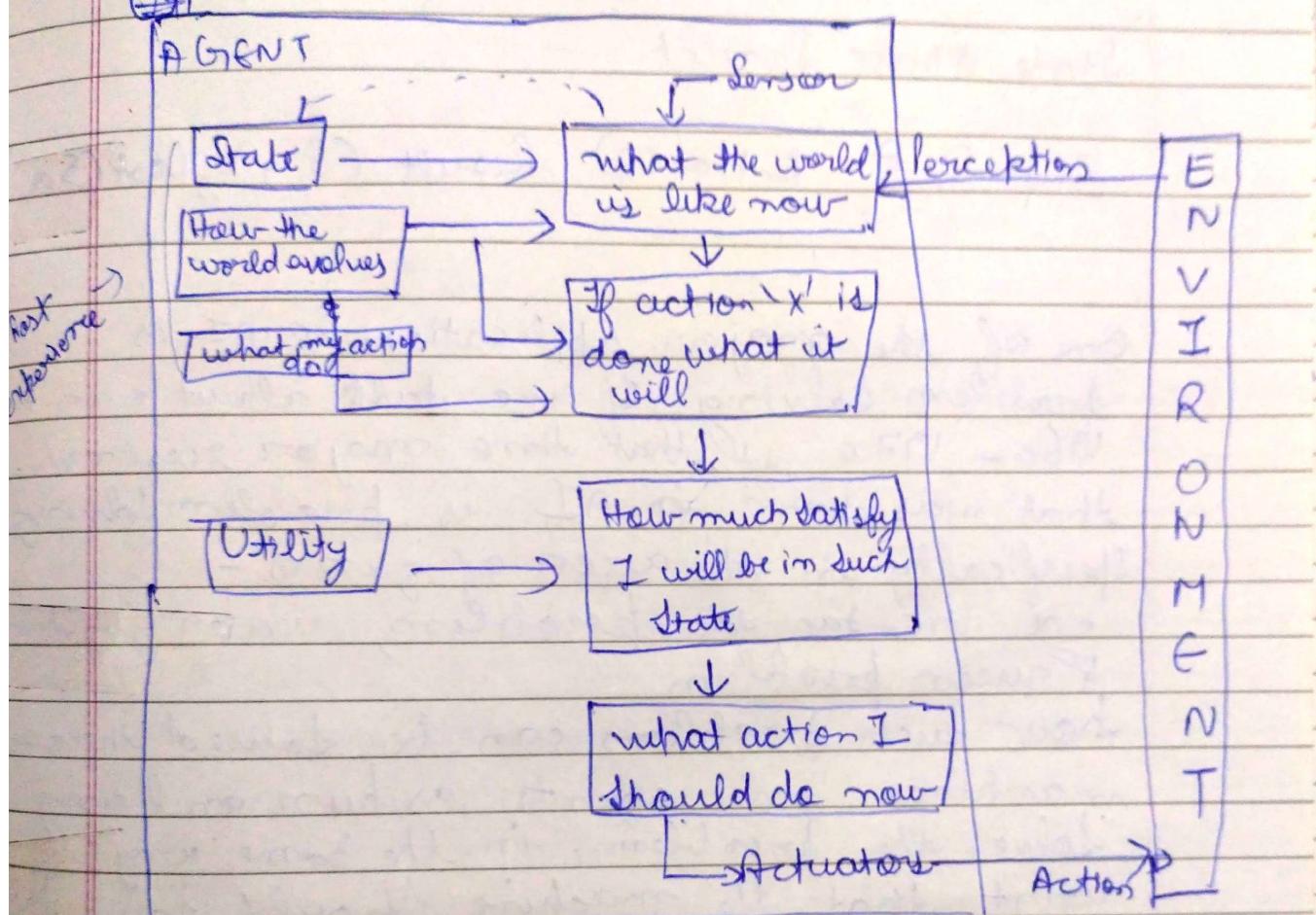
Problem generator : - Suggest the actions to be taken and gain information.

Robot Sofia → Talks to people, reply to them and stores the experience/knowledge gained & use it for future

accordingly. Then actions are performed through actuators. Besides, it also keeps on comparing the current state with the goal state in order to check to what extent current state is near to the goal state.

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(c) Utility based agents



(with Utility, it checks how much it is fulfilled)

- Agents are more focussed towards the preference of each state.
- Act based not only on goals but also the best way to achieve goals
- May be there are many alternatives for one state but agent choose best action to perform that task.

Let's say a task has many subtasks too. Then utility based agent focusses on each subtask too. They try to find the best way to achieve the solution so that task can be performed efficiently.

ex
google maps

AI

Problem Solving

"State Space Search"

$S: \{ S, A, \text{Actions}, \text{Result}(S, a), \text{Cost}(S, a) \}$

One of the major application of AI is problem solving, if we talk about era of 1960 - 1970, at that time major research that was done in AI is problem solving specifically in the area of games:-

tic tac toe problem, water jug problem
8 queen problem

how such problems can be solved through machines and agents, as human being solves the problem, in the same way we want that the machine should solve the problem. That is called problem solving area.

→ In problem solving area, State Space search is very important.

What is State Space Search over here?

↳ No. of States in which a problem can go i.e All the different states in which a problem can go starting from initial state to goal state.

e.g. let say, we have research on a topic, then obviously we will not search at all the places in one time & we start with a start

State, we have a goal State, now in between start and goal State, there may be many intermediate States, we go level by level in order to achieve the goal State.

So all set of States, we use them in the form of representation.

In AI, we mostly talk that how to represent the problem

→ precisely

→ analyze

Because representing the problem is a major task because if you are giving this problem to your machine or to your agent then you cannot tell it verbally, that this is the problem, if you start playing any new game; you do not know anything about that game, you want someone to tell you that how to play that game, all the rules, what are the set of States in it, All these points are necessary for us to solve the problem precisely.

If we precisely represent the problem, we can easily analyze it also

→ how to play the game, how different steps can be taken

→ If we want the problem to represent in all set of states, then we use State Space Search

S: $\{S\}$, A, Action(S), Result(S, a), Cost(S, a)

where S represents the total no. of states
major states in S could be start states, goal,
intermediate

S = start, intermediate, goal

A → Set of actions

e.g. 8 puzzle problem

very first requirement is → to tell the machine or agent, the problem very clearly

2	3	4
5		1
8	7	6

↓
start state

3 * 3 board with 9 spaces
in which we have 8 tiles
which are numbered
& one empty space

→ Represent the problem precisely

→ board of 3 * 3

→ we must also know goal state

S

2	3	4
5		1
8	7	6

3 * 3

Start State

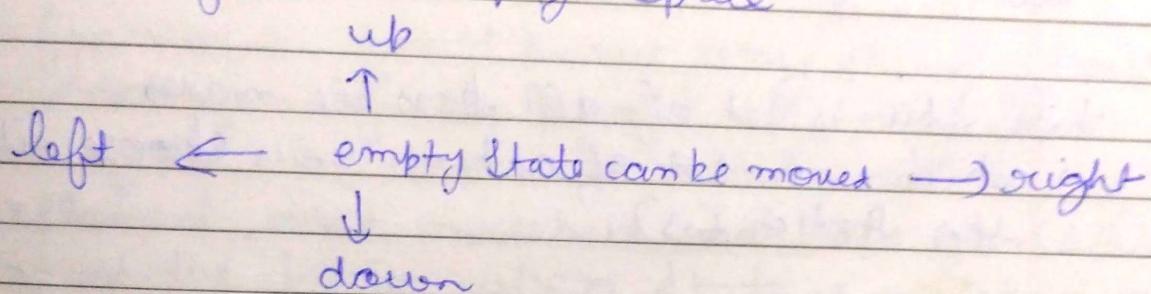
G

1	2	3
8		4
7	6	5

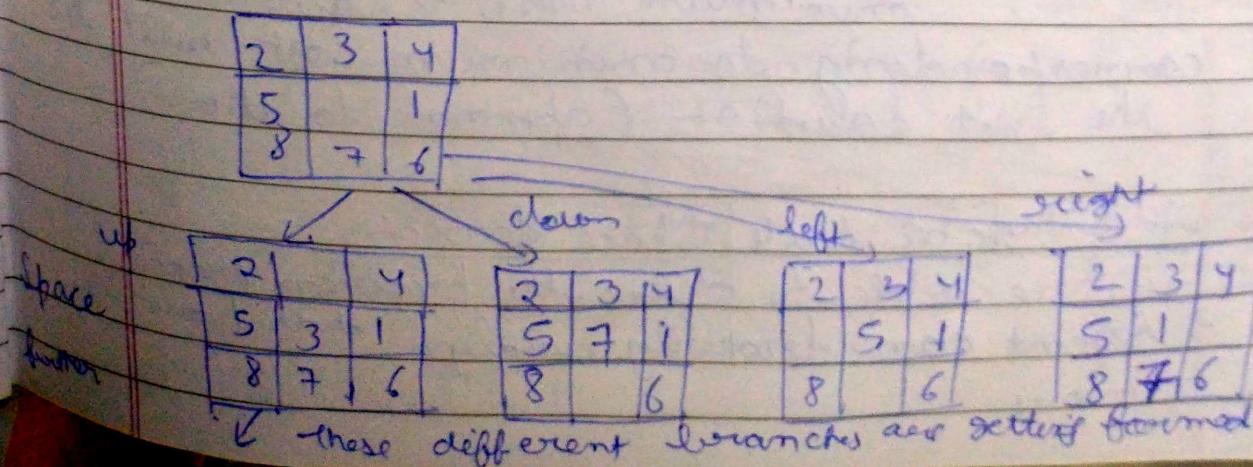
Goal State

Now when we start exploring start state in order to reach the goal state, many intermediate states will start forming. Each intermediate state will be compared with the goal state to check, if it is a goal state or not, if goal state is found then searching will stop at that point.

Action \rightarrow Set of all possible actions considering the empty space



- \rightarrow There can be four possibilities (up, down, left, right)
- \rightarrow we should know about legal and illegal states
- \rightarrow All such conditions must be predefined
(ie empty space can be replaced by left, right, up or down)
- \rightarrow Now one action will be chosen out of these actions



upward

2	3	4
5	3	1
8	7	6

2	3	4
5	7	1
8		6

2	3	4	2
5	1		5
8	7	6	8

state can be moved in
left, right & down
position, up is invalid

legal - left, right, up
illegal - down

legal \Rightarrow right,
up, down
Illegal \Rightarrow left

\rightarrow So this is set of all possible moves

\rightarrow whichever set of action you choose, it will be
the Action(s),

Result \rightarrow the above all are resultant states

(cost) \rightarrow It is any constant value (e.g. in case
of graphs, moving from one edge to another
and in case of trees, moving from one
node to another)

\rightarrow objective \rightarrow searching should be done in
minimum cost \rightarrow Solution corresponding
corresponding to minimum cost will be
the best solution (optimal solution)

Advantage of State Space Search

- \rightarrow we are able to define the problem precisely
- \rightarrow Agent can properly analyze that how to
move

In AI whenever we talk about any searching problem we have started exploring states which will lead to more no. of states in order to reach the goal state.

Searching can be done in 2 ways:-

uninformed
(blind search)

informed
(heuristic search)

uninformed → don't know anything about the domain of the problem, only start and goal is known, states are being explored and matched with the goal state. Stop at the point when state is matched with the goal state.

informed search - concept of heuristic is used in order to solve the problem quickly we go toward the local benefit so that problem can be solved quickly.

uninformed search takes exponential time
→ $O(b^d)$ (non-polynomial)

where b is the branching factor



In the problem discussed can go until $3^{20} \rightarrow$ 3.5 billions states can be covered

That's why informed search is more preferable than uninformed search

Uninformed Searching vs Informed Search

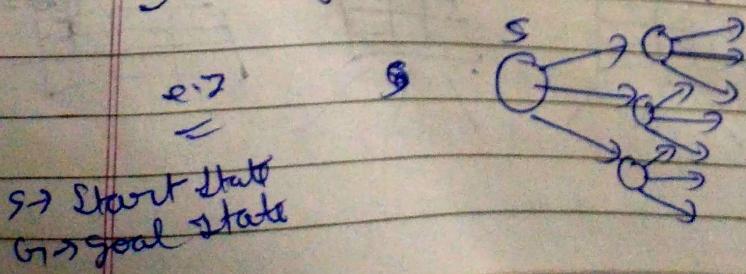
Uninformed Searching

- 1) Search without information
- 2) No knowledge
- 3) Time consuming
- 4) More complexity
(Time, Space)
- 5) DFS, BFS etc.
depth first search breadth first search

Informed Searching

- 1) Search with information
- 2) Use knowledge to find steps to solution
- 3) Quick solution
- 4) less complexity
(Time, Space)
- 5) A*, ~~Hill Climbing~~,
Best first search,
Hill climbing

Uninformed Searching \rightarrow It is also known as
brute force method or blind searching



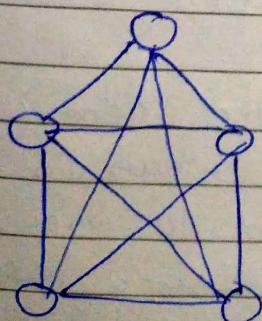
i.e we will start from start state and explore all the possible states in order to find the goal state. If goal state is not found, then exploration will continue on the next ~~step~~ state too Step too, in order to look for goal state.

In this way, after searching all the states, finally we will be able to reach the goal state (we are checking again & again if the intermediate state is the goal state)

- only knowledge of start and goal state
- no knowledge about the domain or problem
- no knowledge about how to reach ~~the~~ the goal
- no guide is there that can guide about the path to be followed

Informed Searching → we are using information. This information is known as heuristics

∴ Eg: Travelling Salesman Problem (TSP)



There are 5 cities connected in this way

problem statement

→ We have to start at one city, cover all the other cities with such that distance covered is minimum then have to reach again at the same city.

In case of 5 cities, if we apply ~~worst~~ uninformed search ie brute force method (ie cover all the possibilities)

Then acc to TSP no. of possibilities (Search space) = $(n-1)!$

In this case, it would be $(5-1)! = 4! = 24$ states
i.e 24 possibilities needs to be explored

After covering all the 24 possibilities, we will get a final optimal solution. It is guaranteed to provide an optimal solution.

→ exponential time is required

If no. of cities = 100

then 99! search space, that is a very large no. which will be very time consuming.

Informed Search

How we use heuristic method

→ Heuristic means assumption

When do we use heuristic search?

→ When search spaces grows in exponential power then we need to use heuristic search

→ Time complexity is very high which we generally call as NP (Non polynomial) problem which can't be solved in polynomial time

- To solve non polynomial time problem, cost is very high (as time & space complexity is very high)
- If we want to solve non polynomial problem in polynomial time then we can use heuristic
- We need to take knowledge of the domain that will help to reduce the searching time
- Time required for the search will be reduced but we may not get an optimal solution

Let's take 24 puzzle problem

In case of uninformed search, we may have to search 10^{24} states, which is practically not possible.

- (a) depth
- (b) branch factor

- Informed search may or may not give an optimal solution.
- Uninformed search is guaranteed to give an optimal solution.

Search Algo.

Breadth First Search

↓
uninformed

- ↳ Breadth First Search
- ↳ Uniform cost Search
- ↳ Depth First Search
- ↳ Depth limited Search
- ↳ Iterative deepening depth first search (IDFS)
- ↳ Bidirectional Search

↓
informed

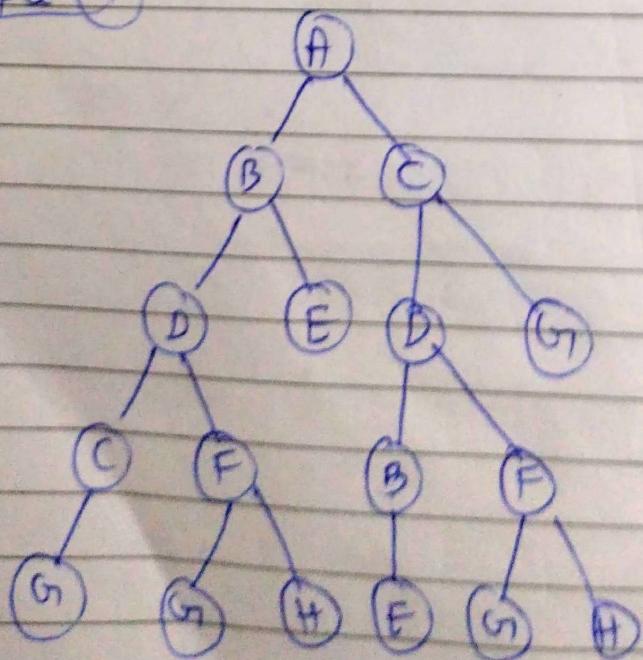
- ↳ Best first search
- ↳ A* search
- ↳ A^{0.4} algorithm
- ↳ Hill climbing

Uninformed Search

(I) Breadth First Search

1. Create a variable called Node-list and set it to the initial state.
2. Until a goal state is found, or Node-list is empty:
 - a) Remove the first element from Node-list and call it E. If Node-list was empty, then quit.
 - b) For element E do the following:-
 - i) Apply the rule to generate a new state;
 - ii) if the new state is a goal state, quit and return this state.
 - iii) otherwise, add the new state to the end of Node-list.

Example ①



(In this case, there are multiple goal nodes)

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Step 1: Initially Node-list contains only one node corresponding to the source state A

Node-list : A

Step 2: A is removed from Node-list. The node is expanded, but [Now remove A from the Node-list (since it's not the goal state) and add its successors] children B and C are generated. They are placed at the back of Node-list.
Node-list : B C

Step 3: Node B is removed from Node-list and is expanded. Its children D and E are generated and put at the back of Node-list.

Node-list : C D E

Step 4: Node C is removed from Node-list and is expanded. Its children D and G are added to the back of Node-list.

Node-list : D E D G

Step 5: Node D is removed from Node-list. Its children C & F are generated and added to the back of Node-list.

Node-list : E D G C F

Step 6: Node E is removed from the node-list. It has no children

Node-list : D G C F

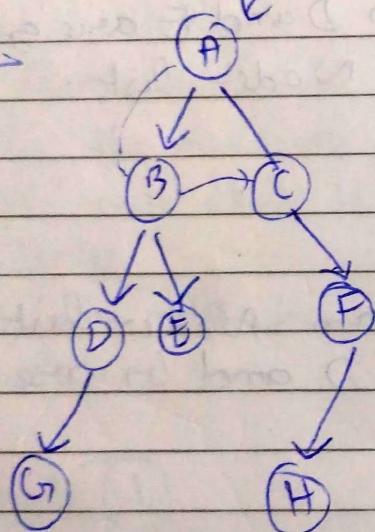
Step 7: D is expanded, B and F are added to the Node-list
 removed from the Node-list ~~its children~~

Node-list: B C F B F

Step 8: G is selected for expansion. It is found to be goal node.

Hence algorithm returns the path A-C-G by following the parent pointers of the node corresponding to G.

Example(2)



Start mode - A

start node

Node-list of A }

Node-list: { B, C }

Node-list: { C, D, E }

Node-list: { D, E, F }

Node-list: { E, F, G }

can also
be called
as queue

{ A }
 { B, C }
 { C, D, E }
 { D, E, F, G }
 { E, F, G, H }
 { F, G, H, I }
 { G, H, I, J }
 { H, I, J }
 { I, J, K }
 { J, K }
 { K }
 { } C

route
 A → B → C → D → E → F → G
 K ← J ← I ← H ←

Node-list : { F, G }

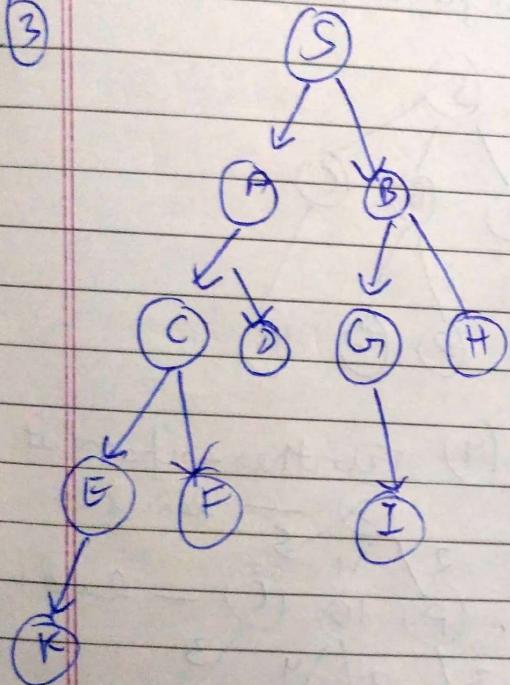
Node-list : { G, H }

Node-list : { H }

Path

A → B → C → D → E → F → G → H

n(3)



PSG

↳ { A, B }

↳ { B, C, D }

↳ { C, D, G, H, I }

↳ { D, G, H, I, E, F }

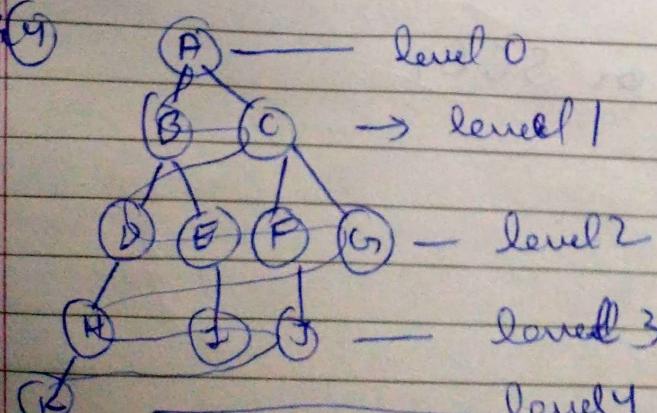
↳ { H, E, F, I, G }

↳ { F, I, K }

↳

S → A → B → C → D → G → H → E → F → I → K

GOAL



Source node - A
Goal node - K

Path:

↳ { B, C }

↳ { A, B, C }

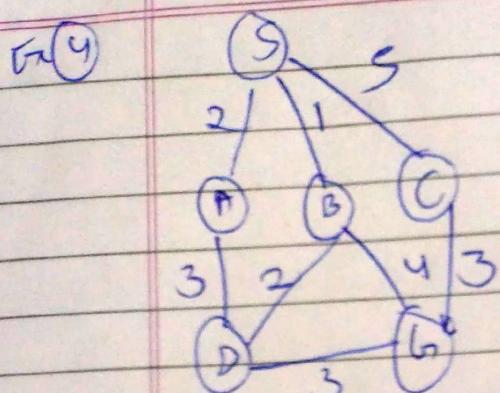
↳ { E, F, G }

↳ { H, I, J }

↳ { K }

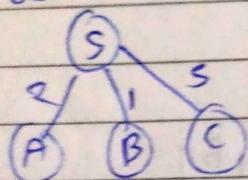
↳ { H, I, J, K }

Find route from S to G using
BFS

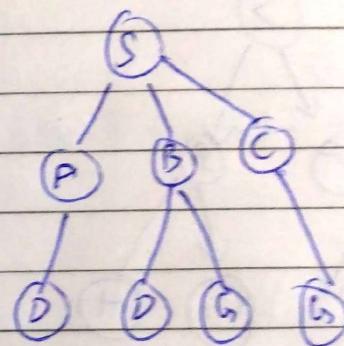


Set (1) {S}

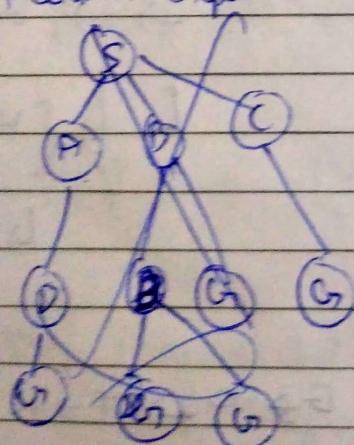
Step (2) Expand



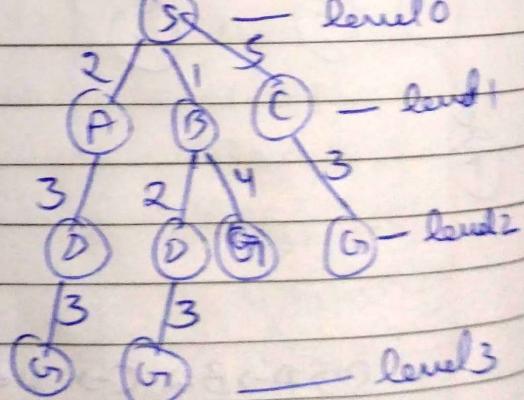
Step (3) Expand further



Step (4) Further expand it



Step (5) Further expand it

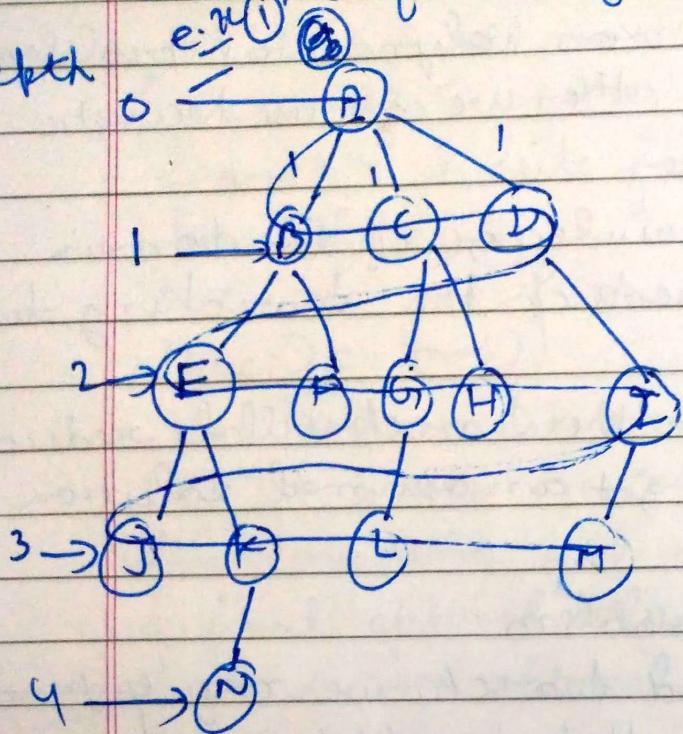


path \Rightarrow S-B-G or S-C-G

Example of depth first

Example of Uninformed Search ① Breadth first search

Depth



'Assuming cost = 1'

→ usually when cost of all the edges are same, if cost is different then heuristic is used

uninformed search technique (brute force)

→ It follows FIFO principle. Data structure used - Queue

- It explores shallowest node first (it goes level by level, covering all the nodes at a particular level then moving onto the next level).
- optimal for unweighted graph and is particularly suitable when all the actions have the same cost.
- It is complete
- It gives optimal solution
- Time complexity, $O(V+E)$

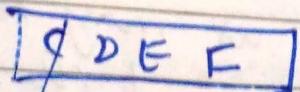
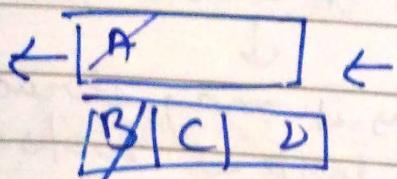
In AI it is represented as $O(b^d)$

→ BFS is also known as

\downarrow
FIFO factor
(max no. of children
a node can have)

~~b3~~
Considering ex ①

Traversing this tree using BFS
using Queue DS



B E F G H

F G H I

G H I J K

H I J K

I J K L

J K L

K L M

L M N

M N

N

let us assume goal state to be G^x , then complexity = $O(b^d)$ it is to be searched

Path from root to goal
A B C H

$b=3$, $d=2$ (in this case)

(maximise value)

assuming branch factor = 3

then OOF complexity = $b^d = 3^2 = 9$
max no. search required = 9

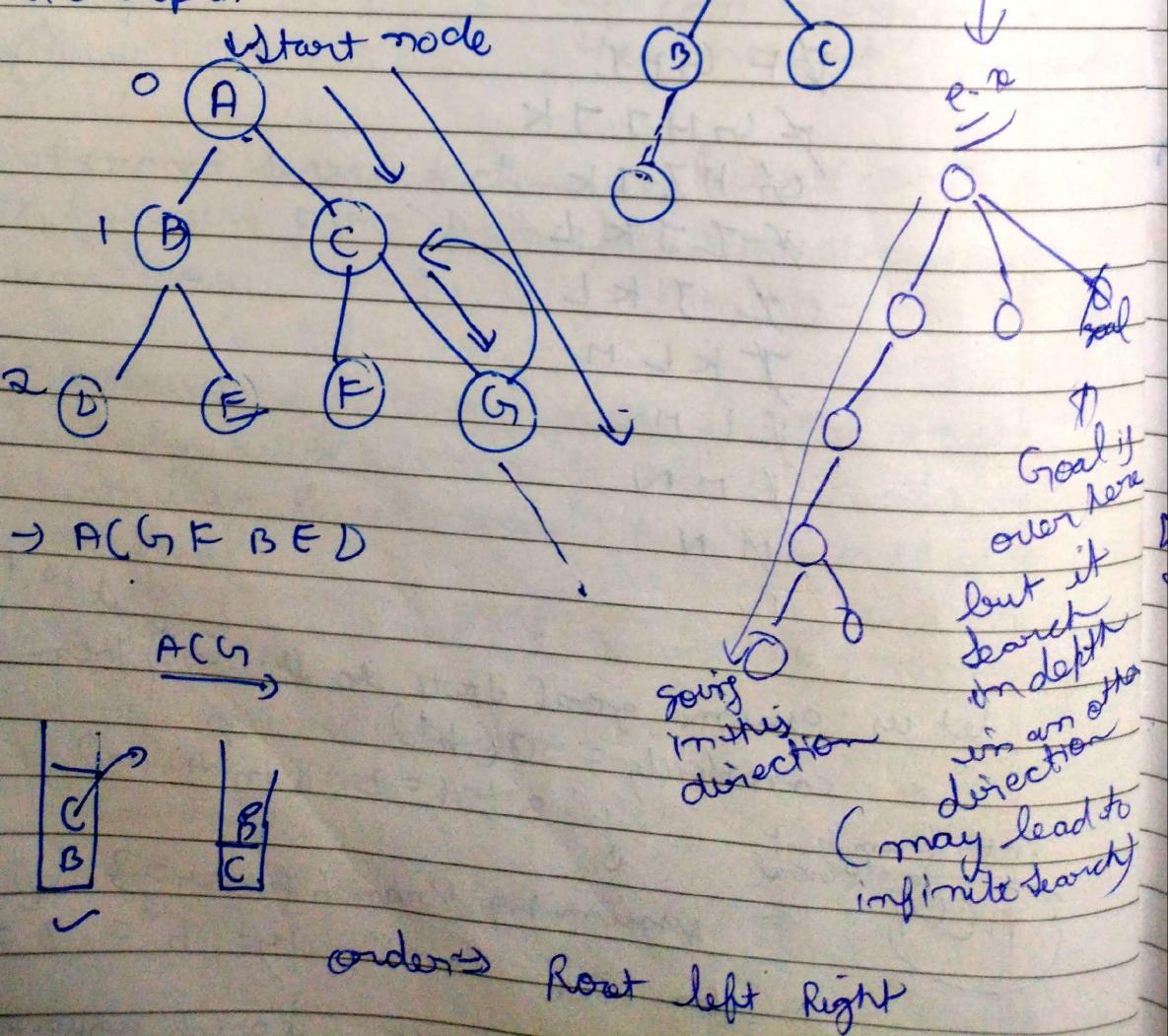
Depth Search

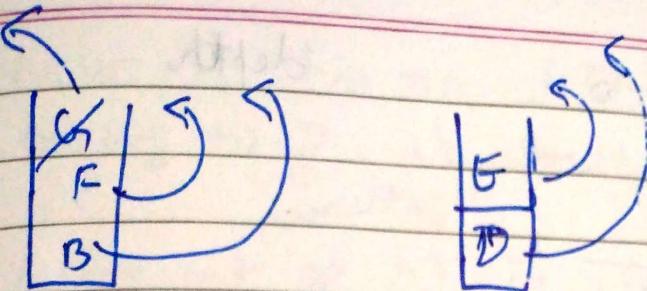
- ② Depth first search \rightarrow works in a horee for manner with present knowledge (does not work on heuristic)
- \rightarrow uninformed search technique
 - \rightarrow Stuck [LIFO]
 - Deepert Node
 - Incomplete (may not give the solution)
 - Non optimal
 - Time complexity
 $O(V+E)$
 $O(b^d)$

as it may stuck into a loop if loops are present,
or it may have to go to infinite (long) depth
search space is infinite

b = branching factor

d = depth





let G be the goal state to be searched

$$\text{Complexity} = O(b^d)$$

let us assume a binary tree with branching factor = 2

no of children possible

$$\text{Complexity} = 2^2 = 4 \quad (\text{max 4 search operations are required})$$

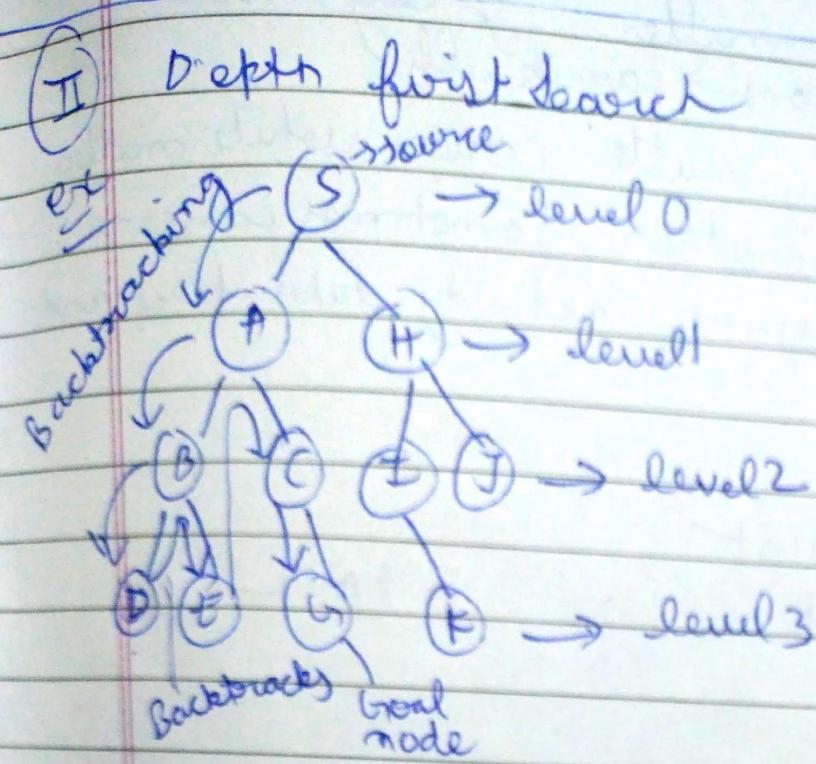
Deepest Node \rightarrow It will go deep in one direction in order to find the goal state. If it does not find the goal state, it backtracks in order to another direction to search for the goal state

With First Iterative Deepening (DFID)

To know about DFID, we should be clear about the concepts of Depth first search (DFS) and Depth limited search (DLS)

Considering the example

S



After searching at (G), it will terminate as goal node is found.

Time Complexity $T(n) = 1 + n^2 + n^3 + \dots + n^m$
 $\approx O(n^m)$

$m = \text{max depth of any node}$

Space complexity $S(C) = O(bm)$
 $b = \text{level}$

→ is non-optimal as it may go to infinite loop
or may generate large no. of steps

→ Similar to DFS with a predefined / predetermined limit. It can solve the drawback of the infinite path in DFS. In this algo, the node at the depth limit ^{Ex: 3rd level} has no successors & nodes further.

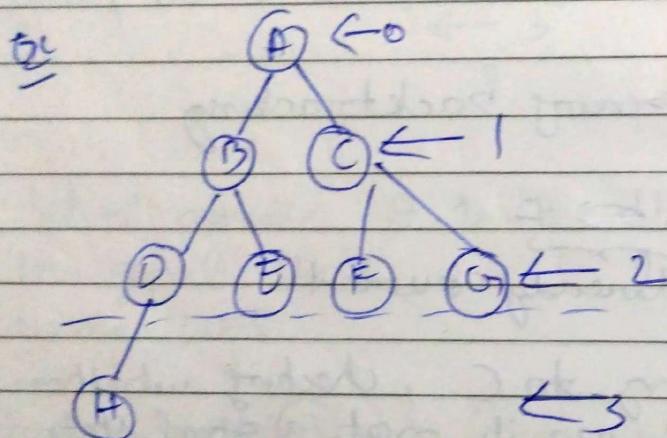
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(3)

Depth Limited Search

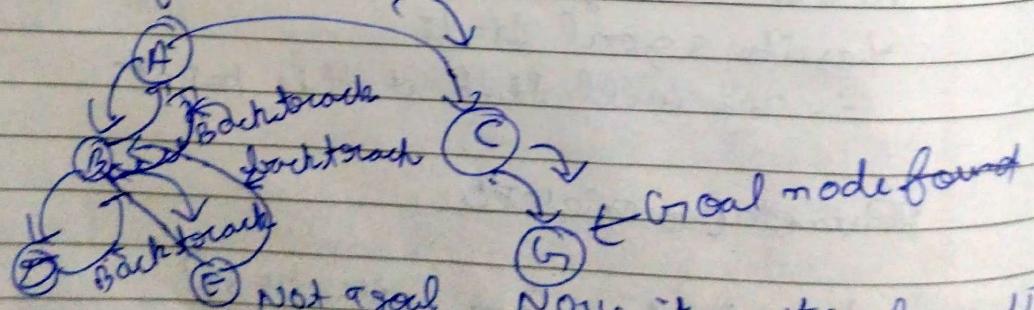
Used to remove the problem associated with depth limited search

→ DLS works like DFS but it imposes a limit on depth to be searched



Let's assume limit = 2 (l=2)
ie we can search upto second limit
we can't go beyond this limit.

It doesn't matter how many states are there after this limit



Now it can't go beyond D
so it will backtrack

DLS can be terminated with two conditions of failure -
Standard failure value: It indicates that problem does not have any solution.

Cutoff failure value. It defines a solution for the problem within the given depth ~~val~~ limit.

Advantages: - It is memory efficient

Disadvantages: - \rightarrow incompleteness (can move only upto ~~specified~~ limit even if the goal is not found, cant go further) Date: / /20
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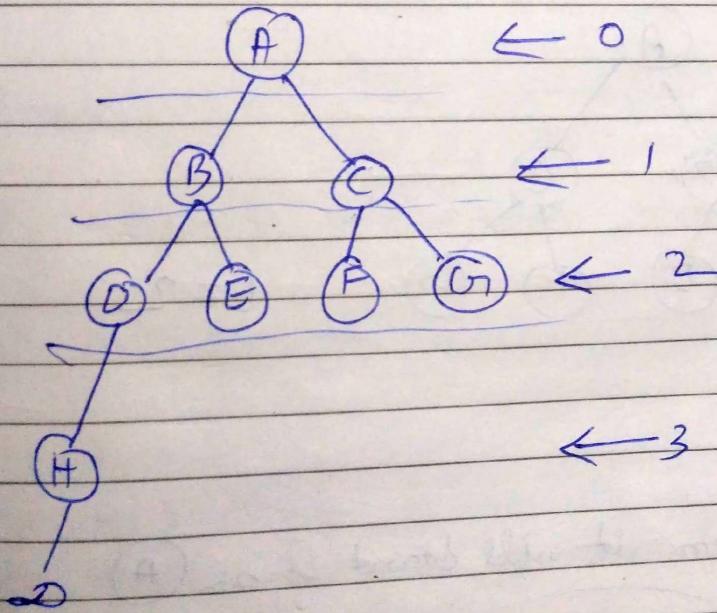
Problems

If Goal State = H & depth limit = 2
In this case we will never be able to reach the goal state

Now to overcome this drawback of depth limited search (DLS)

(Y) \rightarrow Depth First Iterative Deepening is used (DFID)

Let us understand through an example

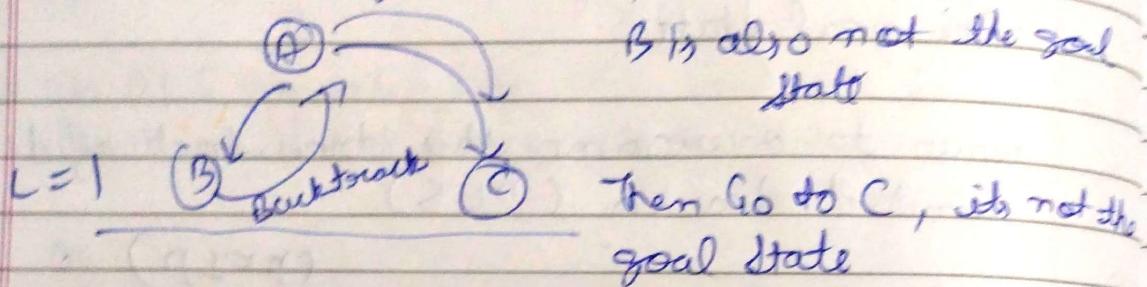


Let us assume goal state = H & start state = A
limit will always start with 0, $L=0$

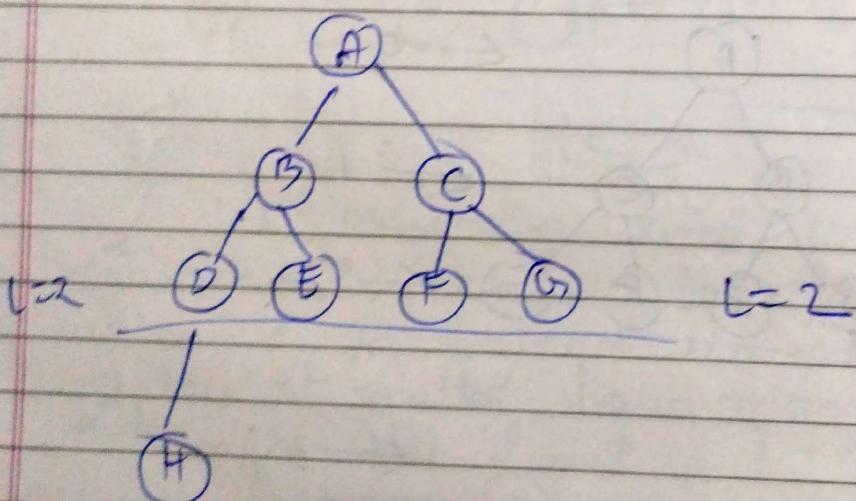
Now it checks if A is the goal state, no it is not
so depth limit, L will be increased by 1
 $\therefore L=1$

Now it will again start searching from A

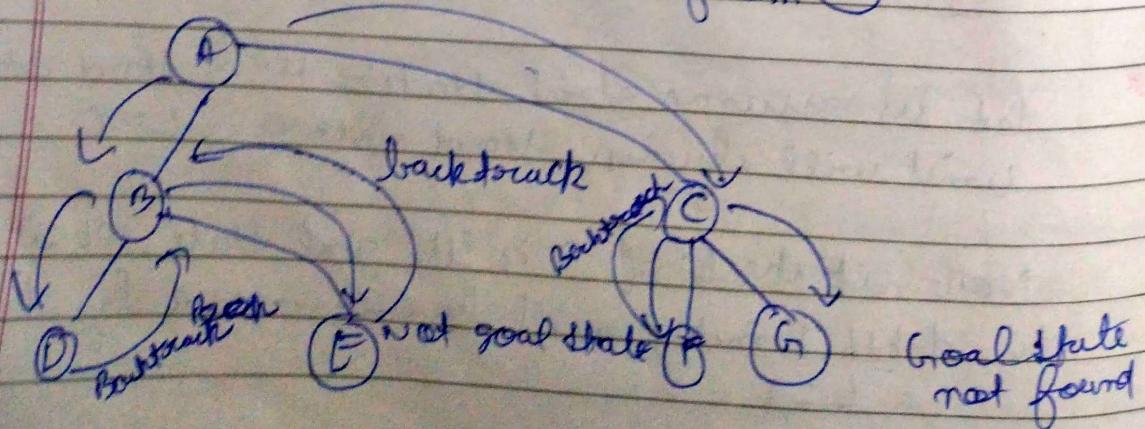
A is not the goal state, it goes to B



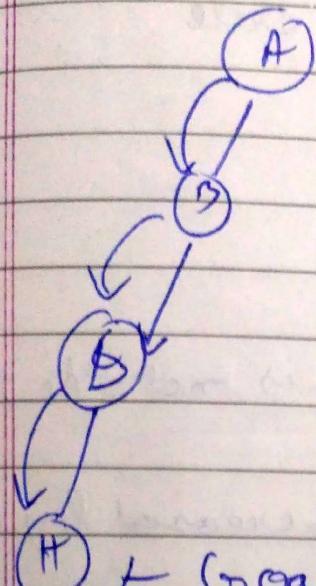
Now again it will increase the depth limit by 1 $\therefore L = 1 + 1 = 2$



Now again it will start from A



Again Goal State not found
So L is increased by 1 again
 $L = 2 + 1 = 3$



$L=3$ & Goal State found

Advantages

1) It inherits advantages of both depth first

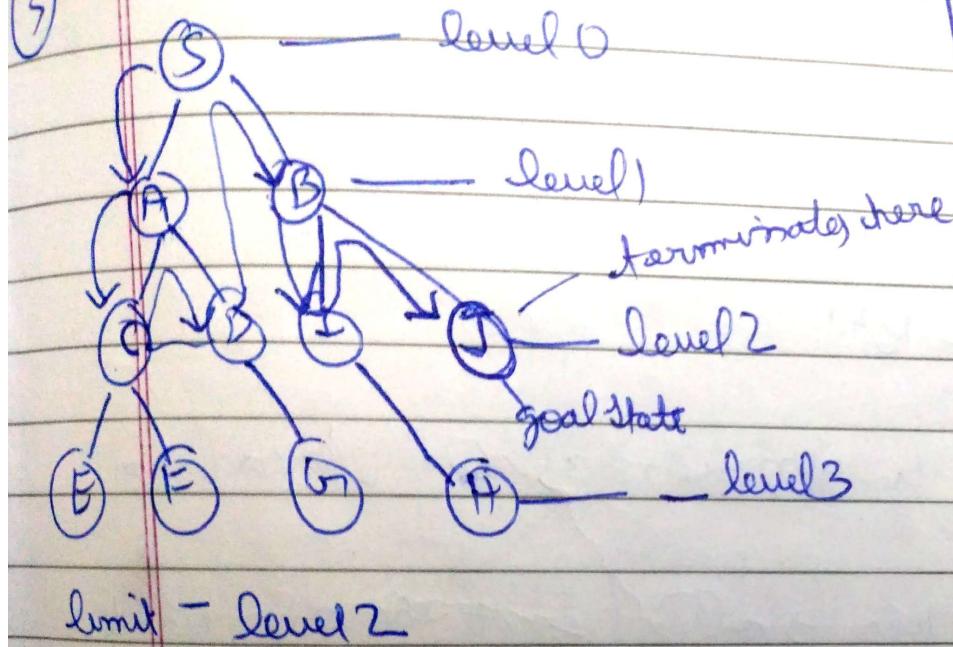
DFS & DLS

Fast searching

2) Disadvantages

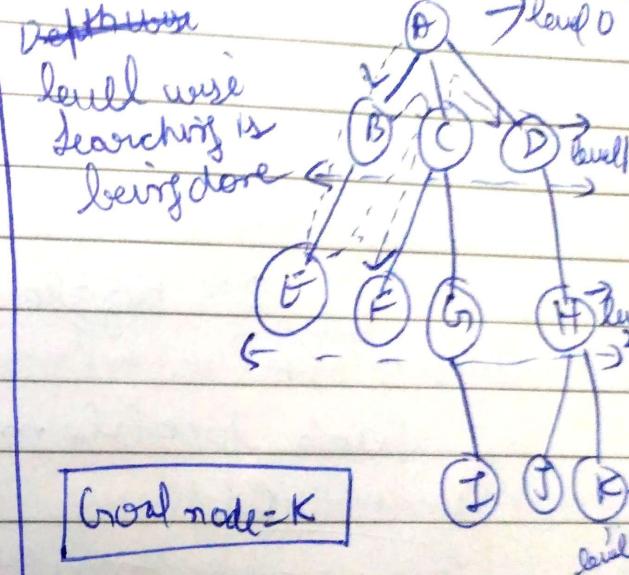
1) Keeps repeating process of previous phase
It has to start again from the starting point
in every iteration.

③ DLS (Example)



DLS searches at a particular level until the goal node is found. If the goal node is found, it stops otherwise the level is increased by 1 & search again begins from the source.

④ DFID example



Depth/ Level	Iterative deepening search
0	A
1	ABC
2	ABCE (FGDH) (up to level 2)
3	ABE C FG I DH JK (up to level 3) Goal node

State Space Search

(4) Uniform cost search algorithm:-

- It is used for traversing weighted tree or graph.
- It comes into play when different cost is available for each edge.
- The goal of UCS is to find a path to the goal node which has the lowest cumulative cost.
- It expands the nodes according to their path cost from the root.
- It can be used to solve any graph/tree where the optimal cost is in demand.
- A UCS algo. is implemented by the priority queue.
- It gives maximum priority to the lowest cumulative cost.
- It is equivalent to BFS if the path cost of all the edges is same.

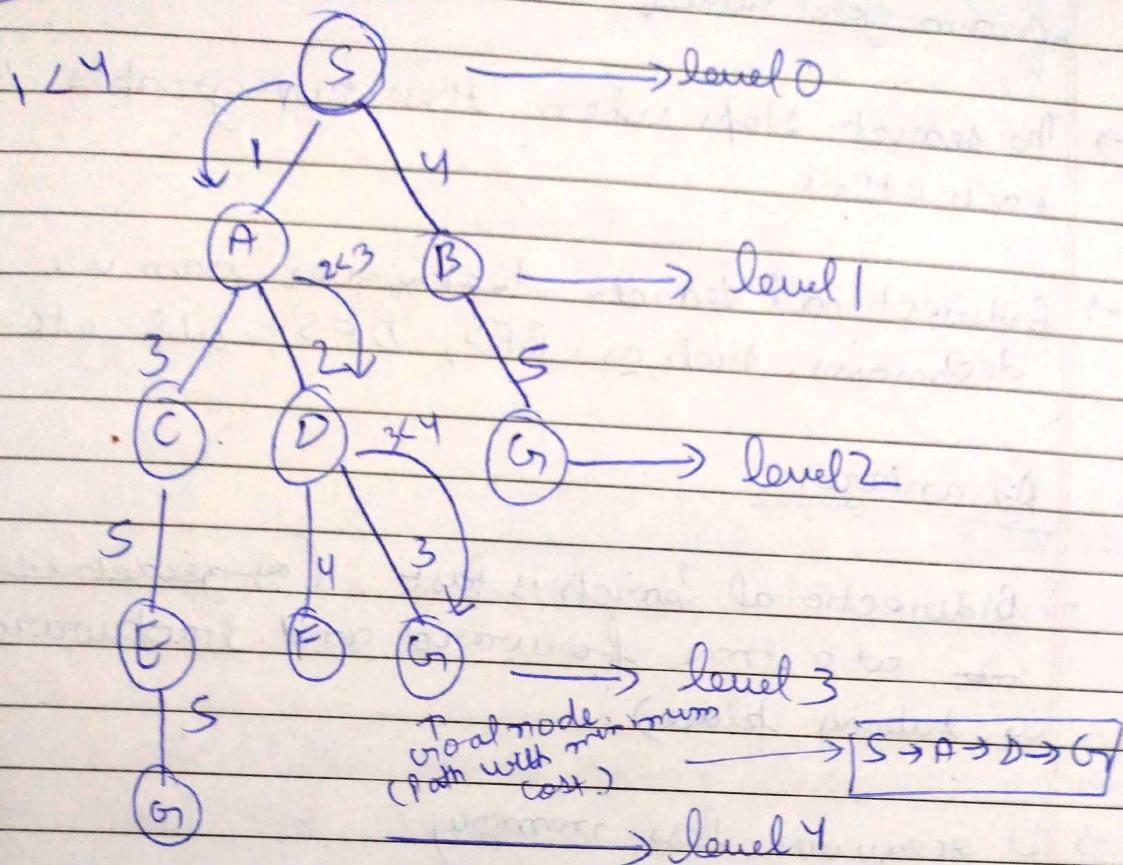
Advantages

- UCS is optimal because at every state the path with the least cost is chosen.

Disadvantages

- It does not care about the no. of steps involved in searching and only concerned about the path cost. Due to this reason, this algo. may be stuck in an infinite loop.

Example



G \rightarrow Goal node

(There are many G nodes, but which G to search, it depends upon the cost of path involved)

⑥ Bidirectional Search

→ It runs two simultaneous searches, one from initial state called as forward search and other from goal node called backward search to find goal node.

→ It replaces one single search graph with two small sub-graphs in which one starts the search from initial vertex and other starts

from goal vertex)

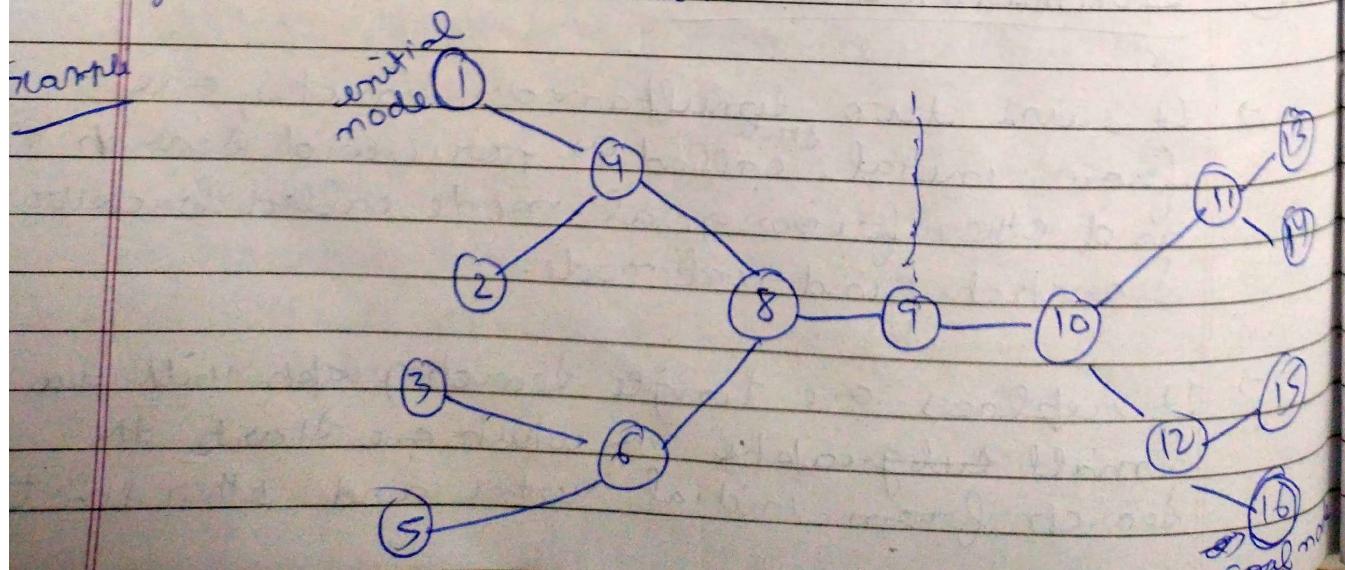
- The search stops when these two graphs intersect each other.
- Bidirectional Search techniques can use search techniques such as BFS, DFS, DLS etc.

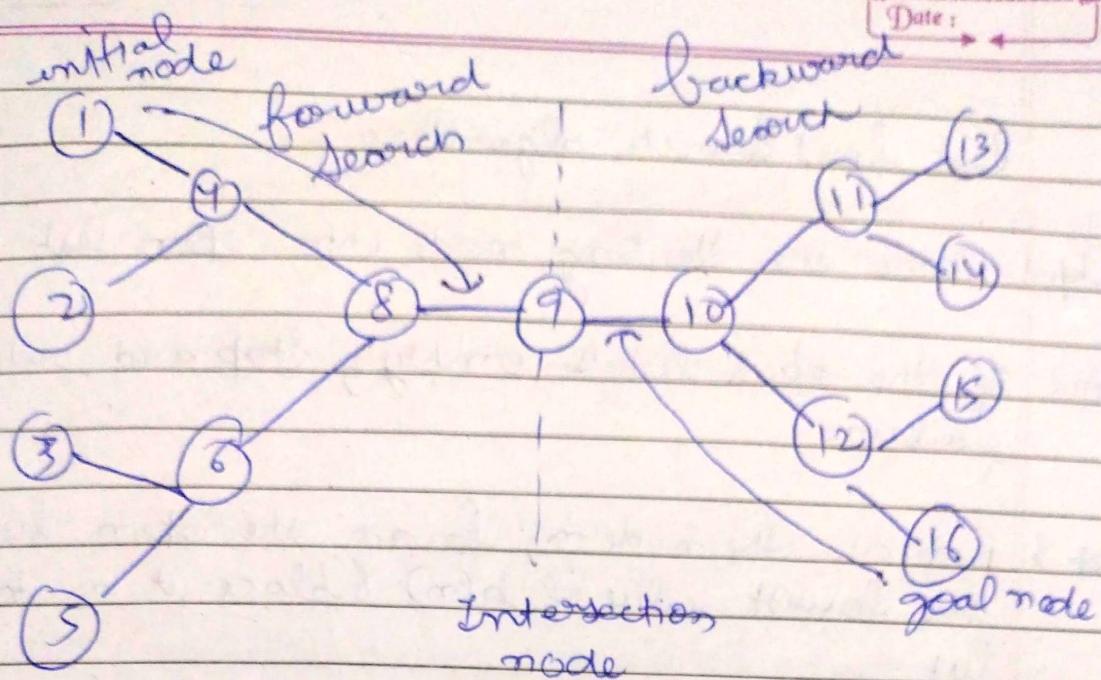
Advantages

- Bidirectional search is fast (as graph is divided into at a time forward and backward search is taking place)
- It requires less memory.

Disadvantages

- Implementation of the bidirectional search tree is difficult.
- In bidirectional search, one should know the goal state in advance.





- It is complete (If we use BFS in both searches)
- It is optimal

Informed Search algorithm

① Best - first search (Greedy search) $h(n)$

→ It always selects the path which appears best at that moment.

→ It is a combination of depth first search (DFS) and Breadth first search (BFS)

→ It uses the heuristic function $h(n) \leq h^*(n)$

$h(n)$ = heuristic cost

$h^*(n)$ = estimated cost

→ The greedy ~~loses~~ best first algorithm is implemented by priority queue.

Best first Search algorithm :-

Step 1: Place the starting node into open list

Step 2: If the open list is empty, stop and return failure.

Step 3: Remove the node n_g from the open list which has lowest value of $h(n_g)$ & place it in the closed list.

Step 4: Expand the node n_g and generate the successors of node n_g .

Step 5: Check each successor of node n_g and find whether node is a goal node or not. If any successor is a goal node, then return success & terminate the search, else proceed to Step 6

Step 6: For each successor node, algorithm checks for evaluation function $F(n)$, & then check if node has been in either Open or Closed list. If the node has not been in both lists, then add it to the OPEN list.

Step 7: Return to Step 2

Advantages

- Best first search can switch between BFS & DFS by gaining advantages of both the algorithm.
- This algorithm is more efficient than BFS and DFS algorithm.

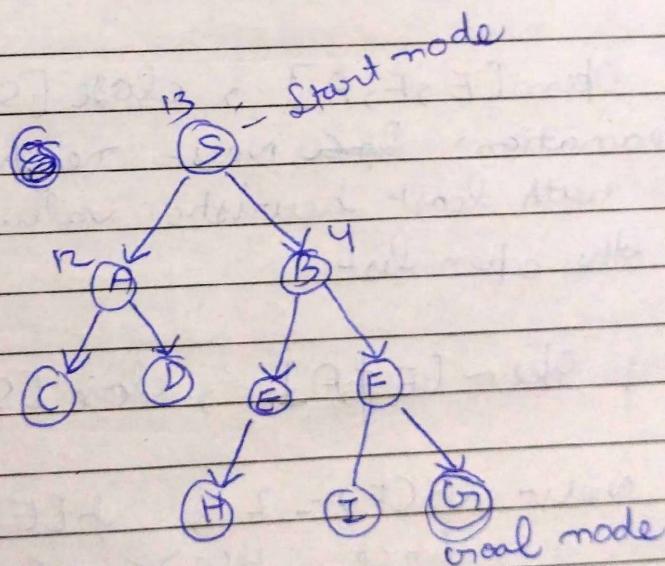
Disadvantages

- It can behave as an unguided depth-first search in the worst case scenario.
- It can get stuck in a loop as DFS.
- This algorithm is not optimal.

Example

Heuristics given

node	$f(n)$
S	13
A	12
B	4
C	7
D	3
E	8
F	2
H	4
I	9
G	0



Note: Final notes should be placed in closed list

(The node with least ^{Date} value will be placed in closed list)

open, close

S → Initialization

open [A, B], close [S]

check with A

(1) open [A]

S → Initialization

open [A, B], close [S]

(1) open [A, B], close [S, B]

$$h(A) = 12, h(B) = 4$$

Explanation: Since $h(B) < h(A)$ i.e. $4 < 12$

Remove B from the open list and place it in the closed list.

(2) Open [E, F, A] → close [S, B]

Explanation: Since now neighbours of B (the node with least heuristic value) will be added to the open list.

Open [E, A] → close [S, B, F]

$$\text{Now } h(F) = 2, h(E) = 8$$

Since $h(F) < h(E)$ i.e. $2 < 8$

Remove F from the open list and add it to the closed list.

(3) Open [E, A, I, G] → close [S, B, F]

Explanation: Now add successors of F i.e. I and G

Open [E, A, I, h], Closed [S, B, F, G]

Next node $h(I) = 9$, $h(G) = 0$

Since $h(G) < h(I)$ i.e. $0 < 9$

∴ add Remove G from the open list and add it to the closed list

∴ Path will be

$S \rightarrow B \rightarrow F \rightarrow G$

→ Time complexity $\Rightarrow T(n) = O(b^m)$
 $s(C) = O(b^m)$

where m is max depth of search space

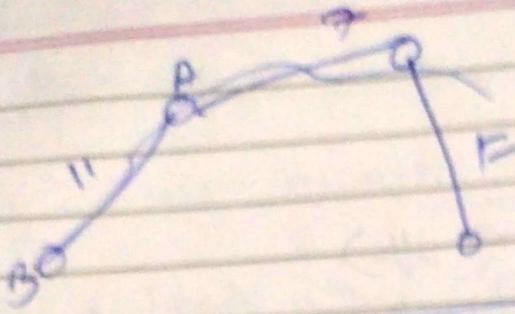
→ Best first search is incomplete & not optimal

② A* Search Algorithm

→ A* search algorithm finds the shortest path through the search space using the heuristic function.

→ It uses $h(n)$ and cost to reach the node n from the start state $g(n)$
 $f(n) = g(n) + h(n)$

→ This algo. expands less search time and provides optimal results faster.



Best Informed Search Algorithm.

- ① Best First Search (Informed, Heuristic)

Algorithm

→ let OPEN be a priority queue containing initial state

loop

if OPEN is empty return failure

Node \leftarrow Remove - First (OPEN)

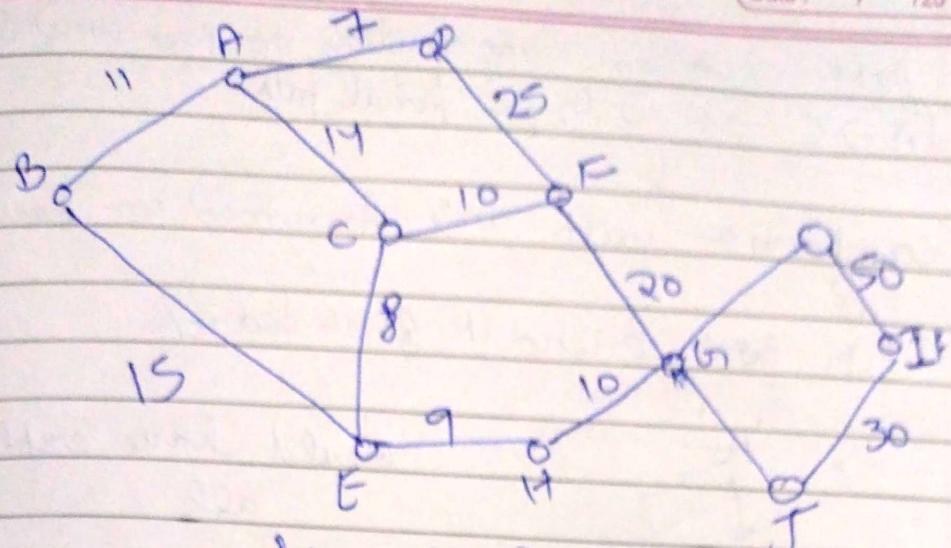
if Node is a goal

then return the path from initial to Node

else generate all successors of Node and

put the newly generated node into OPEN
according to their f values

End loop



straight line distance.

$$A \rightarrow G = 40$$

$$B \rightarrow G = 32$$

$$C \rightarrow G = 25$$

$$D \rightarrow G = 35$$

$$E \rightarrow G = 19$$

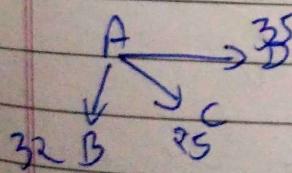
$$F \rightarrow G = 17$$

$$H \rightarrow G = 10$$

$$G \rightarrow G = 0$$

(Already
given in question)

A Priority \rightarrow the one with least heuristic value is the best and explore that node

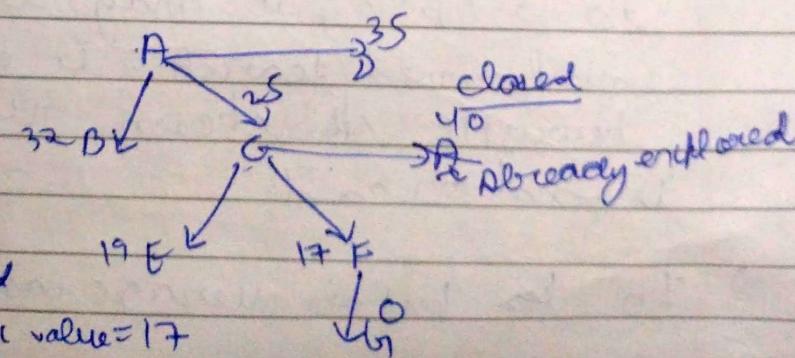


Successors of $A \rightarrow B, C, D$
Put B, C & D in queue
based on heuristic value

A, F, B, D
* need to explore C

Now Successor of C
 \rightarrow E, F, (A) already explored

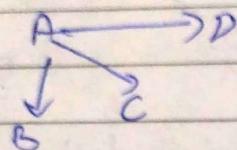
Pick F with heuristic value = 17



- Path chosen according to Best First Search
- $A \rightarrow C \rightarrow F \rightarrow G$] ← final path

Comparison with uninformed or heuristic

like ~~BFS~~ Breadth First Search



would have explored B, C, D all

~~Complexity~~ complexity $O(b^d)$

- Best first search - uses greedy method based on heuristic value
- Time complexity is reduced
- It always gives the good solution
- It may or may not give an optimal solution
- Much better than uninformed method with polynomial time complexity
- In worst case, complexity can be equal to $O(b^d)$, it may behave as ~~worst~~ + uninformed search. It depends upon the heuristic chosen, whether heuristic chosen is good or bad
- In ~~best~~ average case, its complexity is

②

A* Search Algorithm

→ A* search algorithm finds the shortest path through the search space using the heuristic function.

→ It uses $h(n)$ and cost to reach the node n from the start state $g(n)$

$$f(n) = g(n) + h(n)$$

→ This algo. expands less search time and provides optimal results faster.

- It is similar to UCS except that it uses $g(n) + h(n)$ instead of $g(n)$
- $f(n)$ uses search heuristic as well as the cost to reach the node. Hence we combine both costs.

$$f(n) = g(n) + h(n)$$
 (fitness number)
cost from source node to a particular node
- 3 $f(n)$ = Estimated cost of the cheapest solution.

$g(n)$ = cost to reach node n from start state

$h(n)$ = cost to reach from node n to goal node

Algorithm of A* Search

- Step ① Place the starting node in OPEN list.
- Step ② Check if the OPEN list is empty or not, if the list is empty, return failure and stop.
- Step ③ Select the node from OPEN list which has the smallest value of evaluation function ($g + h$). If node n is a goal node, then return success & stop. Otherwise,
- Step ④ Expand node n and generate all of its successors and put n in the CLOSED list.
 - For each successor ' n' , check whether n is already in the OPEN and CLOSED list.
 - If not then compute evaluation function for n and place it in OPEN list.

Date: _____
Time: _____

Step 5:

Else if node 'n' is already in open and closed then it should be attached to the back pointer which replaces the lowest $g(n)$ value.

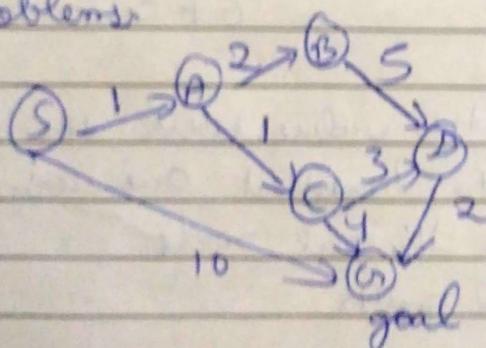
Step 6: Return to Step 2.

Advantages

- (1) It is best algorithm than other search algorithms
- (2) It is optimal & complete.
- (3) It can solve very complex problems.

Disadvantages

- It does not always produce shortest paths.
- It is not practical for various large-scale problems.



Current State	$h(n)$
S	5
A	3
B	4
C	2
D	6
goal	0

① $S \rightarrow A \Rightarrow F(n) = g(n) + h(n) \Rightarrow g(n) + h(n)$
 $= 1+3 = 4$
 $\downarrow g(n) \quad \downarrow h(n)$

$S \rightarrow G \Rightarrow F(n) = g(n) + h(n) \Rightarrow g(n) + h(G)$
 $= 10 + 0 = 10 \quad (\text{hold}) \quad X$

② $S \rightarrow A \rightarrow B \Rightarrow F(n) = 1+2 g(n) + h(n)$
 $= (1+2) + g(B)$
 $\Rightarrow 3+4 = 7 \quad (\text{hold}) \quad X$

$S \rightarrow A \rightarrow C \Rightarrow F(n) = g(n) + h(n)$
 $= (1+1) + h(C)$
 $\Rightarrow 2+2 = 4 \quad \checkmark$

③ $S \rightarrow A \rightarrow C \rightarrow D \Rightarrow F(n) = 1+1+3 + h(D)$
 $= 5+6 = 11 \quad \text{hold} \quad X$

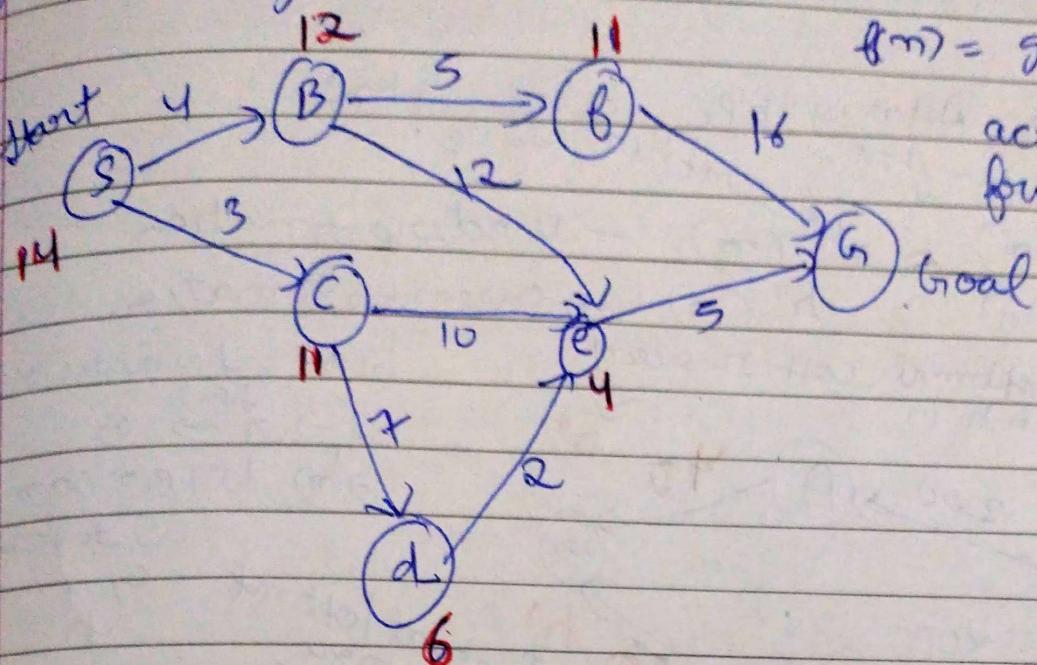
$S \rightarrow A \rightarrow C \rightarrow G \Rightarrow F(n) = 1+1+4 + h(G)$
 $= 6+0 = 6 \quad \checkmark$

Now compare this value with the values on hold
 Since this is the smallest one among other
 and also contains the goal node.
 \therefore It is the final path

$S \rightarrow A \rightarrow C \rightarrow G$
 $\text{cost} = 6$

④ A* algorithm is a heuristic search algorithm
 uses the concept of AND-OR graph to decompose any
 complex problem given into smaller set of problems
 which are further solved.

A* Algorithm



↑ mode

$$f(n) = g(n) + h(n)$$

↓ actual cost
from start node to n

Note we have to reach from S to G

$$\begin{aligned} f(S) &= 0 + 14 \quad (g(n) + h(n)) = \\ &= 14 \end{aligned}$$

$$\begin{aligned} S \rightarrow B \\ = 4 + 12 \\ = 16 \end{aligned}$$

$$\begin{aligned} S \rightarrow C \\ = 3 + 11 \\ = 14 \end{aligned}$$

(choose the one with minimum cost)

$$\begin{aligned} S \rightarrow B \rightarrow F &= 4 + 5 + 11 = 20 \\ S \rightarrow B \rightarrow E &= 4 + 12 + 4 = 20 \\ S \rightarrow B \rightarrow G &= 4 + 5 + 16 + 6 \\ &= 25 \end{aligned}$$

$$\begin{aligned} S \rightarrow C \rightarrow E &= 3 + 10 + 4 = 17 \\ S \rightarrow C \rightarrow D &= 3 + 7 + 6 = 16 \\ S \rightarrow C \rightarrow D \rightarrow E &= 3 + 7 + 2 + 4 \\ &= 16 \\ S \rightarrow C \rightarrow D \rightarrow E \rightarrow G &= 3 + 7 + 2 + 10 + 5 = 25 \\ \hline &= 17 \end{aligned}$$

choose the minimum. Goal State

Time complexity = $O(b^d)$

\hookrightarrow branch factor

(\downarrow no. of children of particular node)

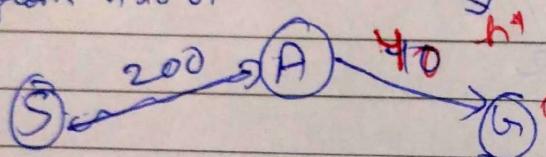
Space complexity = $O(b^d)$

$\Rightarrow A^*$ is Admissible algorithm

$h(n) \leq h^*(n)$ — underestimation

$h(n) \geq h^*(n)$ — overestimation

actual / optimal cost to reach
from A to G



$h(n)$ = heuristic value

$S \xrightarrow{g(n)} n \xrightarrow{h(n)} G$

$g(n)$ b.e. n can take
S to goal state

g , in cost
 h

actual / optimal
cost to go
from B to G

$S \rightarrow$ Start State $G \rightarrow$ Goal State

A & B \rightarrow intermediate node

$$h(A) = 100$$

$$g(A) = 200$$

$$g(B) = 200$$

case I overestimation actual value
est. value $\left[\begin{array}{l} h(A) = 80 \\ h(B) = 70 \end{array} \right] > f(A)$ $f(n) = g(n) + h(n)$
 $f(A) = 200 + 80 = 280$ $f(A) = 200 + 70 = 270$ ($\text{In this case } h^*(A) = 40$)
 $f^*(A) = 40$ $h^*(B) = 50$

$$f(A) = 200 + 80 = 280 \quad ; \quad f(B) = 200 + 70 = 270$$

$$f(B) = 200 + 70 = 270 \quad (\text{Minimum})$$

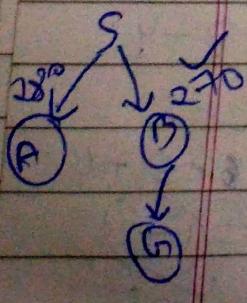
$$f(G) = g(G) + h(G)$$

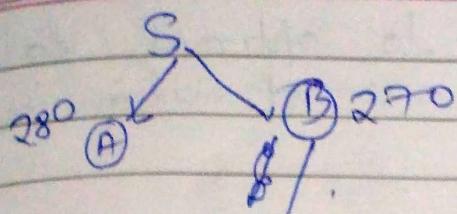
$$= 250 + 0$$

$\because h(G) = 0$ heuristic
to search goal is to be 0

$$g(G) = 200 + 50 = 250$$

(via B)





$\text{G}(B) = 250 \rightarrow$ this is the minimum cost, so it will stop here.

$$\begin{aligned} f(G) &= g(G) + h(G) \\ &= 200 + 50 = 250 \end{aligned}$$

case 2 underestimation

$$h(A) = 30$$

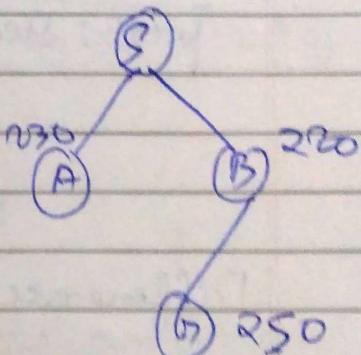
$$h(B) = 20$$

$$f(A) = g(A) + h(A)$$

$$f(A) = 200 + 30 = 230$$

$$f(B) = g(B) + h(B) \quad f(B) = 200 + 20 = 220 \checkmark$$

$$\begin{aligned} f(G) &= g(G) + h(G) \\ &= 250 + 0 = 250 \end{aligned}$$



Now it will not stop as state \textcircled{A} has value lesser than 250

Now $f(\textcircled{B})$ will be computed again via A

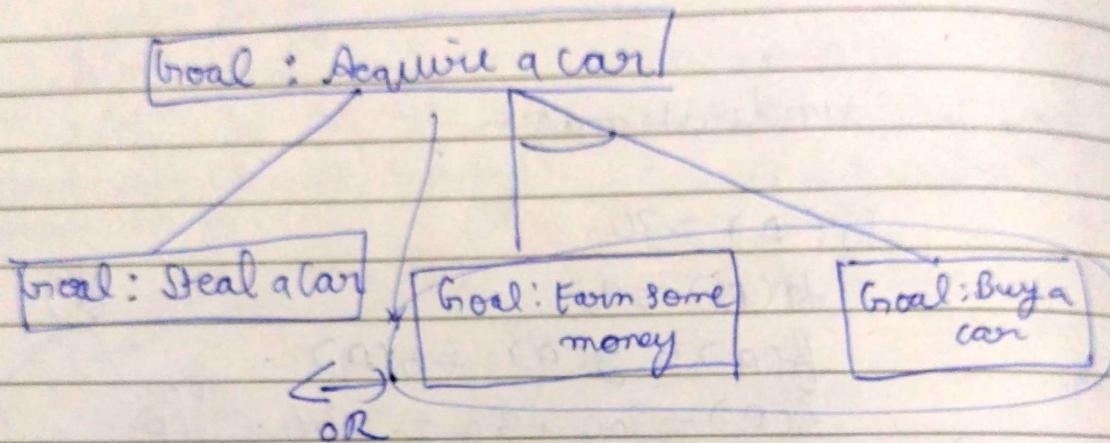
$$\begin{aligned} f(G) &= g(G) + h(G) \\ &= (200 + 40) + 0 \end{aligned}$$

$$f(G) = 240$$

$f(\textcircled{B}) = 240$ This is the optimal value to reach the goal state

underestimation leads to optimal solution
always but overestimation may not

- ③ A* (And OR) \rightarrow Problem decomposition
(And-OR graphs) (Breakdown into small pieces)



Difference between A* & A*^{*}

Similarly

strategy of

\rightarrow Both work on Best First Search

\rightarrow Both are informed search techniques
and work on the basis of heuristic value

Difference

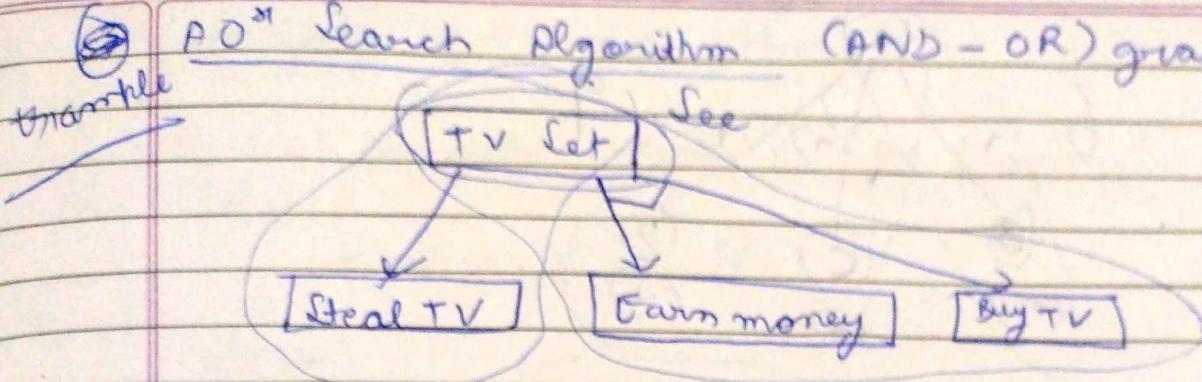
\rightarrow A* always give the optimal solution

* ~~iff~~ \rightarrow A* is not guaranteed to give an
admissible optimal solution

\rightarrow A* does not explore all the solution paths
once it got a solution.

\rightarrow A* always gives an optimal solution

AO* Search Algorithm (AND - OR) graph



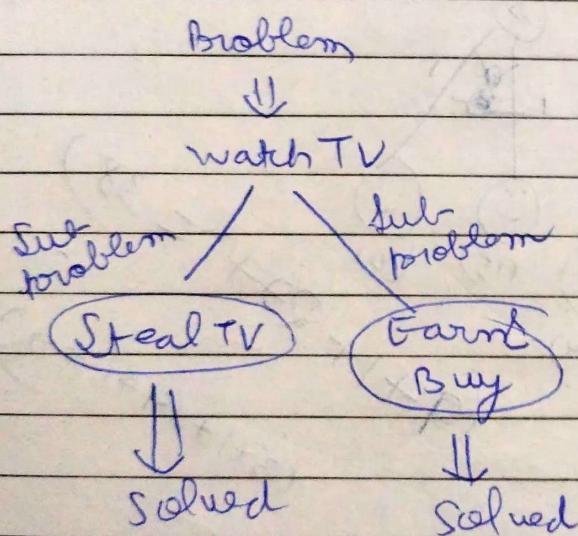
Earn money + Buy TV \Rightarrow watch TV

AND is
represented
by +

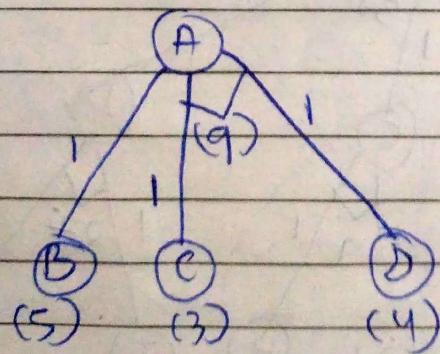
And /
OR

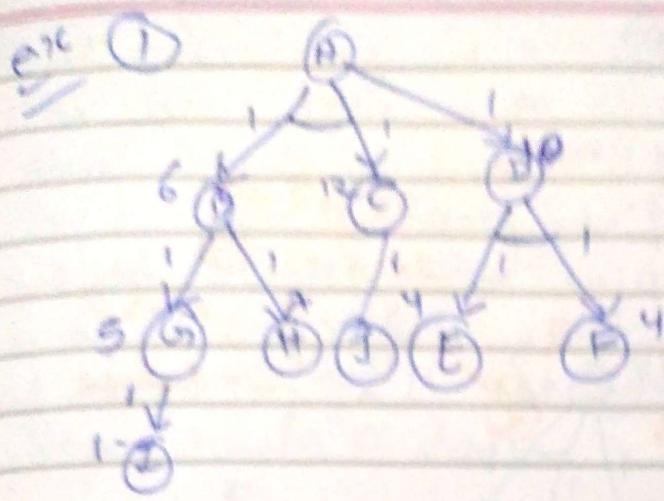
or

Steal the TV \Rightarrow watch TV

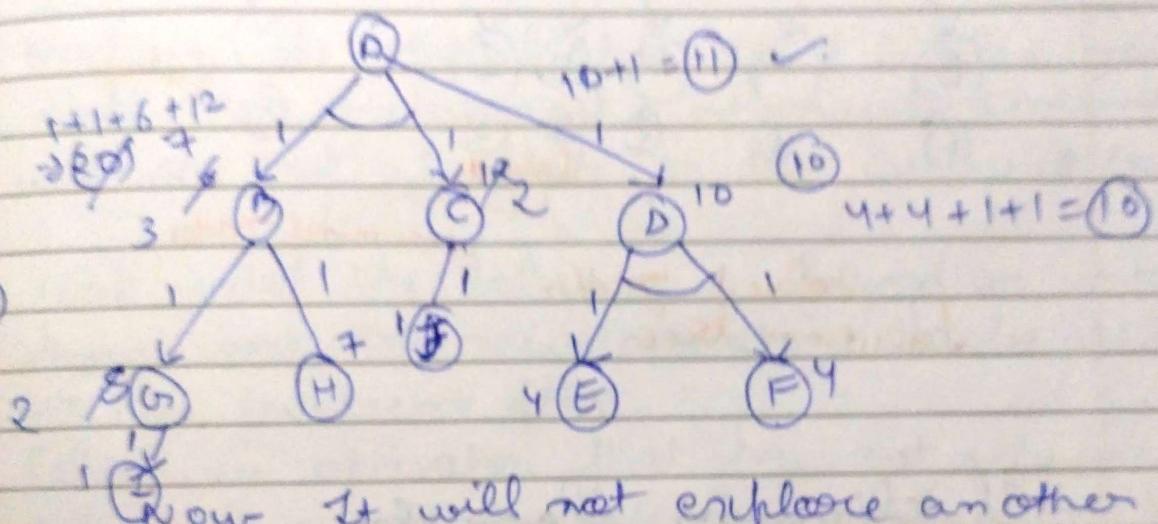


Example





cost of all edges = 1

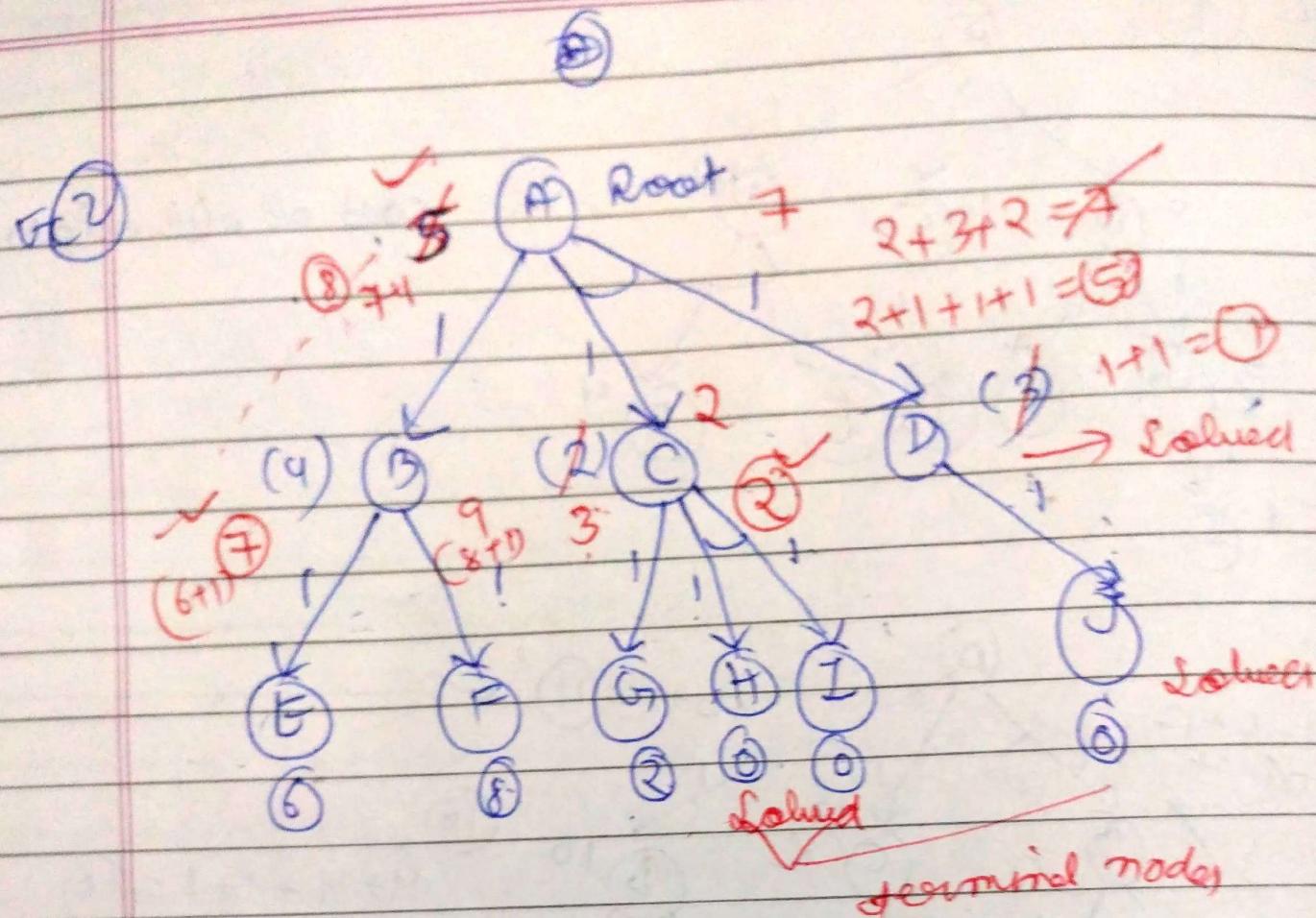


Now it will not explore another path.

Had it explored other path, it could provide better solution

let's explore For example

In A*, we need to calculate new estimation value at every step and estimate the move towards root

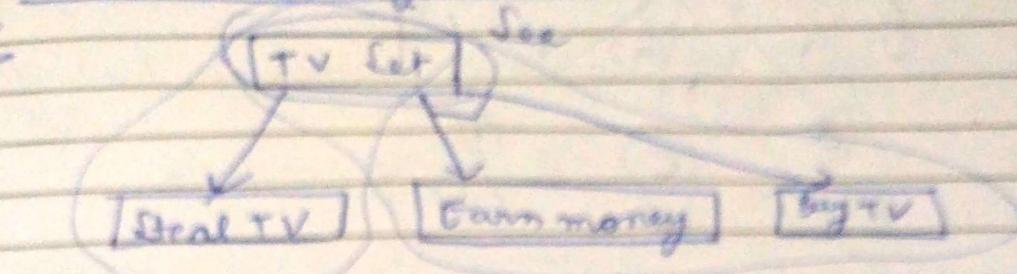


Solved graph
Solution tree

A* Search Algorithm (AND-OR) graph

Branch & Bound

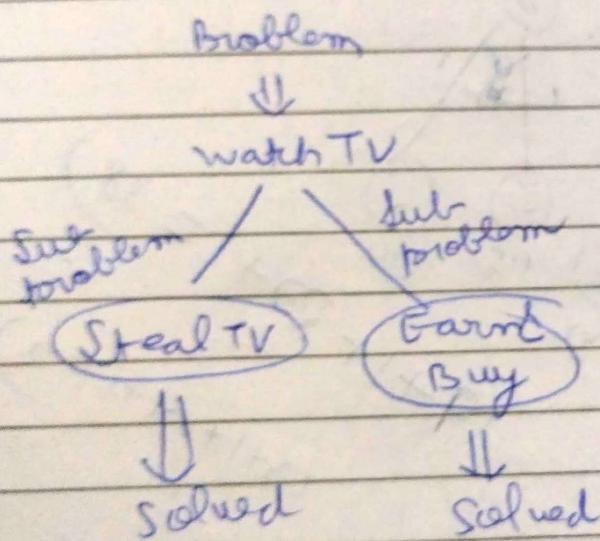
A* Search Algorithm (AND-OR) graph



Earn money + Buy TV \Rightarrow watch TV
AND is represented by +
and OR

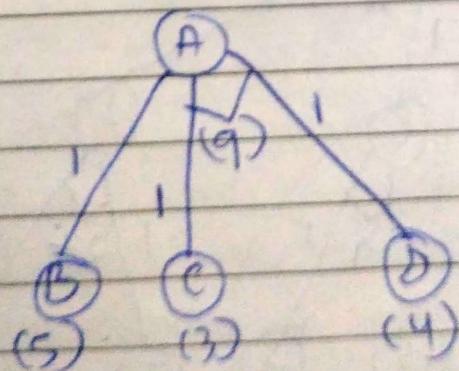
OR

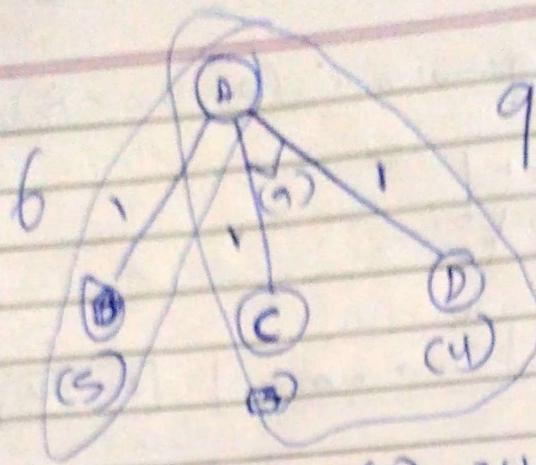
Steal the TV \Rightarrow watch TV



Each subproblem is solved separately

Example

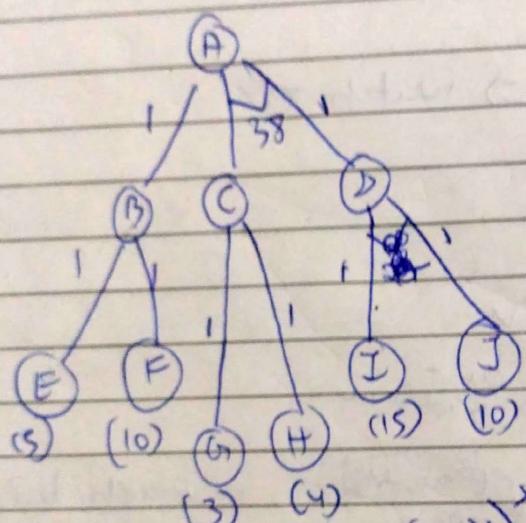




$$F(n) = 5 + 1 \\ = 6$$

$$F(n) = 3 + 1 + 4 + 1 \\ = 9$$

Q1

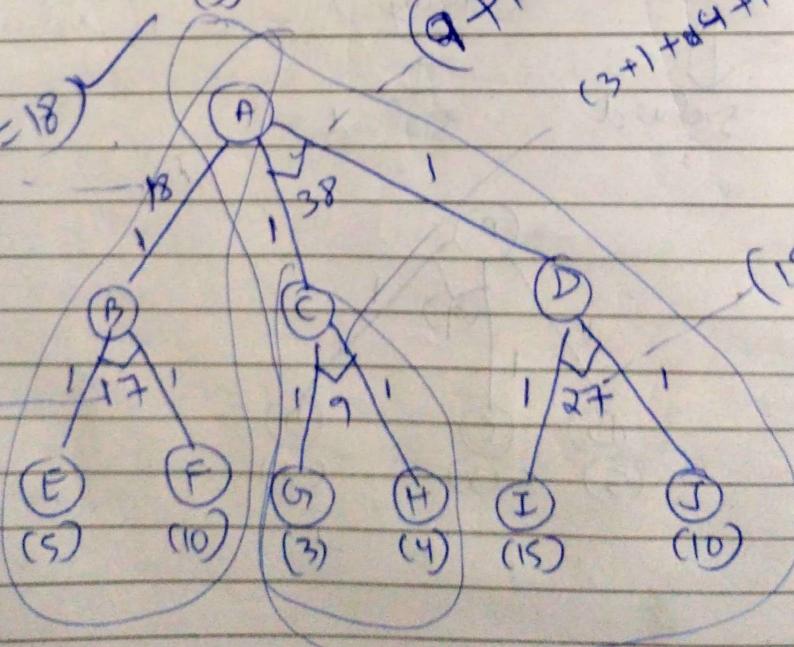


38
30 this will
be chosen
 $(2+1=18)$

$$(9+1+27+1 = 38)$$

$$(3+1+4+1 = 9)$$

$$(5 \times 1 \times 10 \times 1) \\ = 50$$



$$(5+1+10+1 = 27)$$

Working of A* algorithm

→ The A* algorithm works on the formula given below:

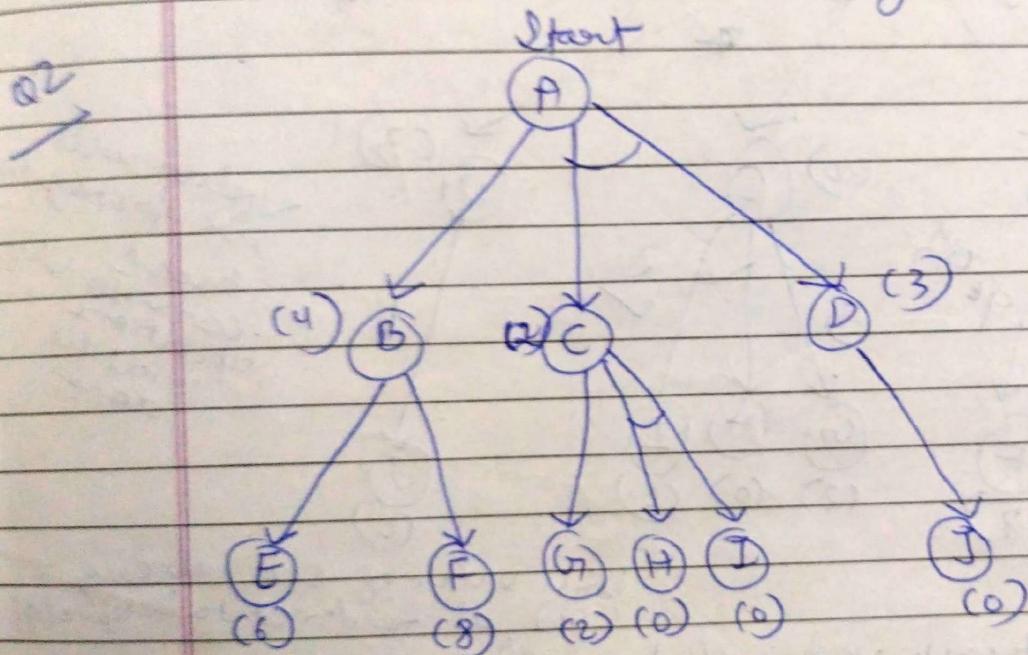
$$f(n) = g(n) + h(n)$$

where

$g(n)$ - The actual cost of traversal from initial state to the current state.

$h(n)$ - The estimated cost of traversal from the current state to the goal state.

$f(n)$ - The actual cost of traversal from initial state to the goal state.



→ Here, in the above example, all the numbers in brackets are the heuristic values i.e. $h(n)$

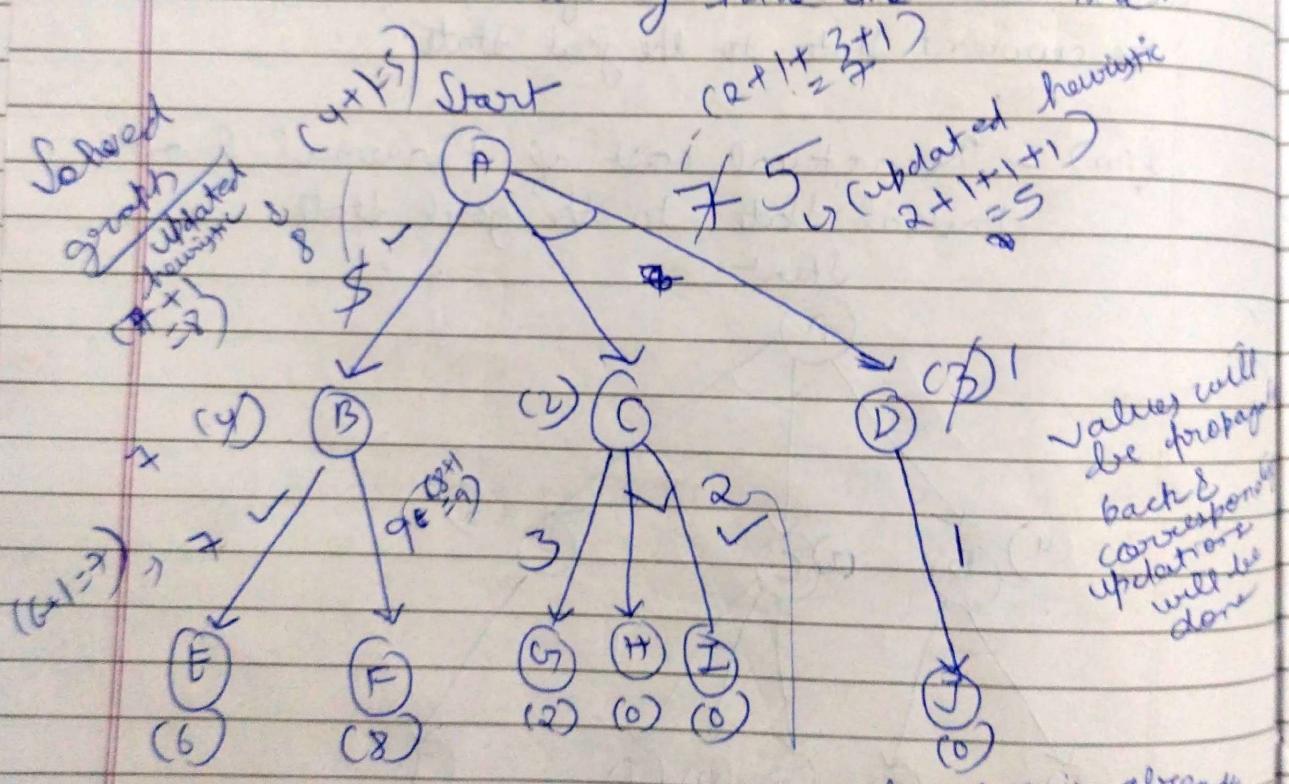
→ Each edge is considered to have a value of 1 by default.

Step 1 : Starting from node A, we first calculate best path.

$f(A-B) = g(B) + h(B) = 1 + 4 = 5$, where 1 is the default cost value of travelling from A to B and 4 is the estimated cost from B to Goal state.

$$f(A-C-D) = g(C) + h(C) + g(D) + h(D) \\ = 1 + 2 + 1 + 3 = 7$$

here, we are calculating the path cost as both C and D because they have the AND-Arc.



Since value of C is already 2, it need not to be updated.

The default cost value of travelling from A-C is 1 and from A-D is 1 but the heuristic value given for C & D are 2 and 3 respectively hence making the cost as 7.

Step 2

Now cost of path A-B is lesser (i.e 5) than cost of Path A-C-D (i.e 7) hence this path will be chosen

from the B node,

$$f(B-E) = 1+6=7$$

$$f(B-F) = 1+8=9$$

- Hence B-E path has lesser cost. Now the heuristics have to be updated since there is a difference between actual and heuristic value of B.
- The minimum f-value path is chosen and is updated as the heuristic, in our case the value is 7.
- And because of change in heuristic of B there is also change in heuristic of A, which is to be calculated again.

$$f(A-B) = g(B) + \text{updated}(h(B)) = 1+7=8$$

Step 3: Now the current node becomes C node & the cost of the path is calculated.

$$f(C-G) = 1+2=3$$

$$f(C-H-I) = 1+0+1+0=2$$

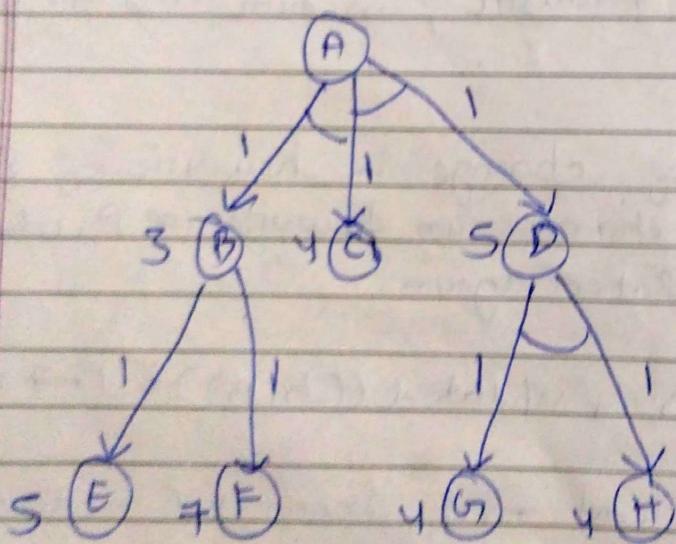
$f(C-H-I)$ is chosen as minimum cost path

- Heuristic of paths H and I are 0 which hence H & I are solved.
- But path A-D also needs to be calculated, hence it has an FND arc.
- $f(D-J) = 1+0 = 1$, hence heuristic of D needs to be updated to 1
- finally, $f(A-C-D)$ needs to be updated.

$$f(A-C-D) = g(C) + h(C) + g(D) + \text{updated}(h(D))$$

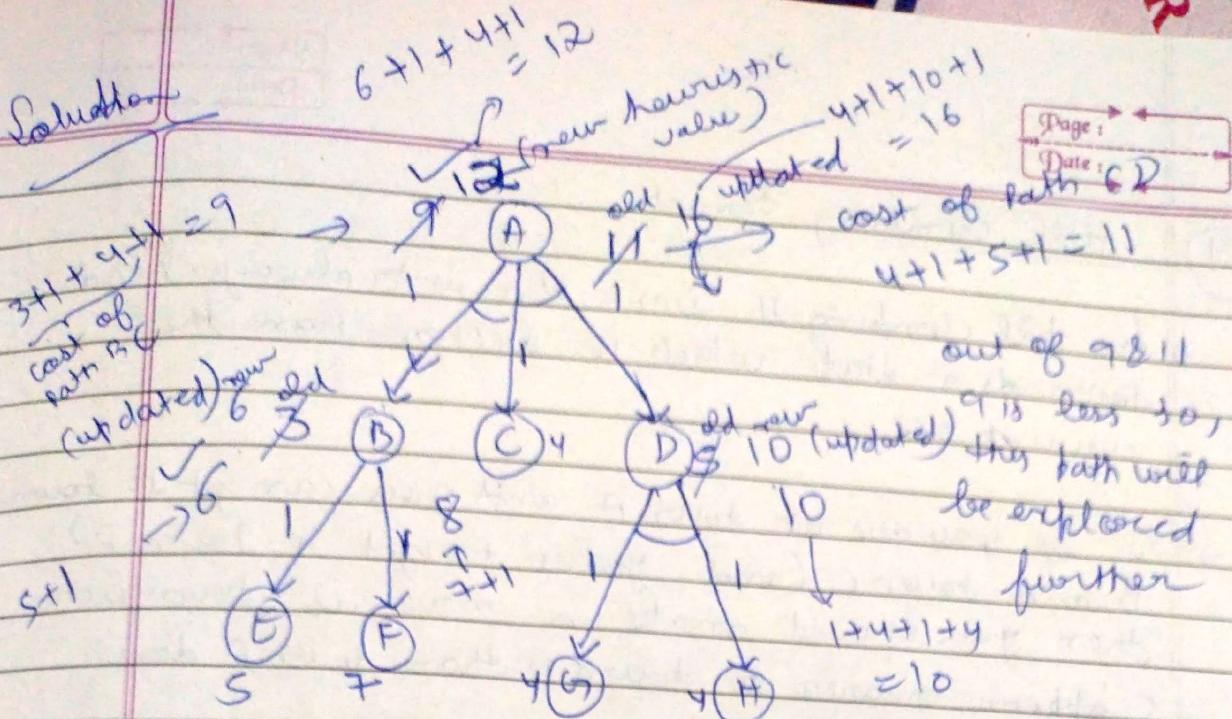
$$= 1+2+1+1=5$$

93.



In order to solve A, solve B and C or
Solve C & D

Solution



Now in order to solve B either path BE or BF can be considered as they are not connected through AND.

Now after updation of heuristic value as 12 of Path A-B-C, heuristic value of Path A-C-D seems to be less (i.e 11) so it will be explored further

After solving this graph
Cost of Path A-B-C = 12 ✓
Cost of Path A-C-D = 16

Optimal value will be lesser one i.e with Path A-B-C = 12 (so it will be chosen)

A
B C
E

(optimal path)

(4)

Hill climbing search

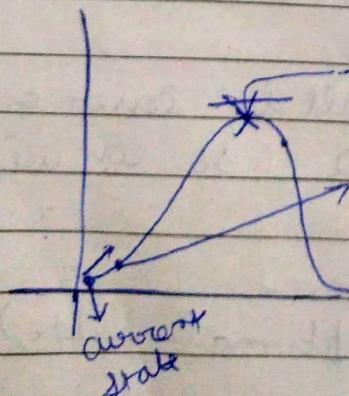
- In hill climbing the basic idea is to always head towards a state which is better than the current one.
- So, if you are at town A and you can get to town B and town C (and your target is town D) then you should make a move if town B or C appear nearer to town D than town A does.

two possibilities i.e
 $A \rightarrow B \rightarrow D$ choose the path
 or
 $A \rightarrow C \rightarrow D$ which appears better than the
 current state

Hill climbing search (key points)

- Local search algorithm → always moves in a single direction
- Greedy approach
- No backtracking

If a node is selected during the searching process, the same node will expanded further. We can't do backtracking and cannot select any other node in between.



If we are climbing over a hill, upward state is considered better than the current state.
(as the next state will not be better than the current state)

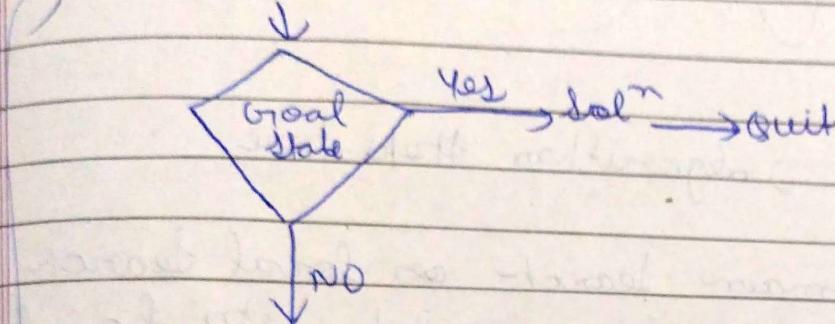
If new state is better than current state,

then

$\text{new state} = \text{current state}$

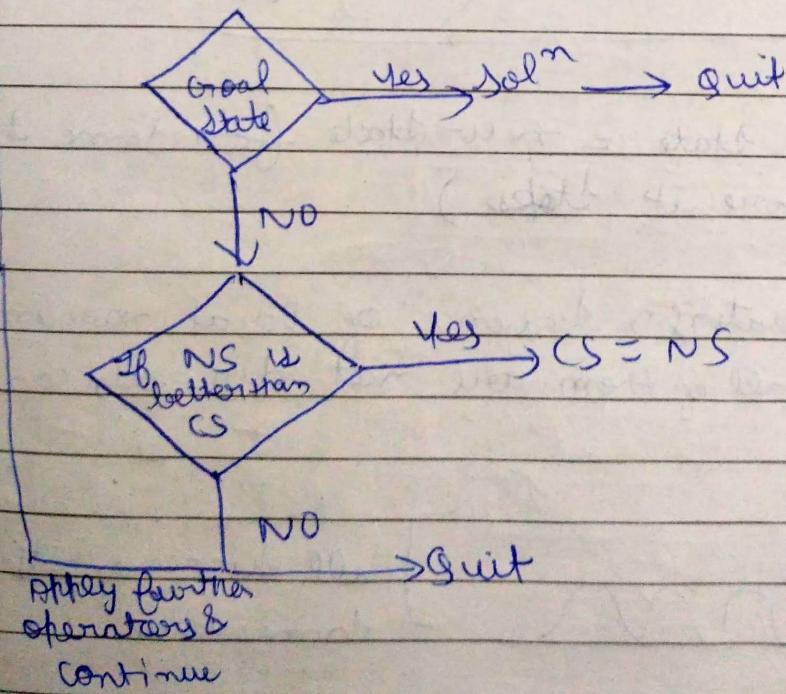
If new state is not better than the current state,
then stop

Evaluate initial state



current state = initial state
(CS)

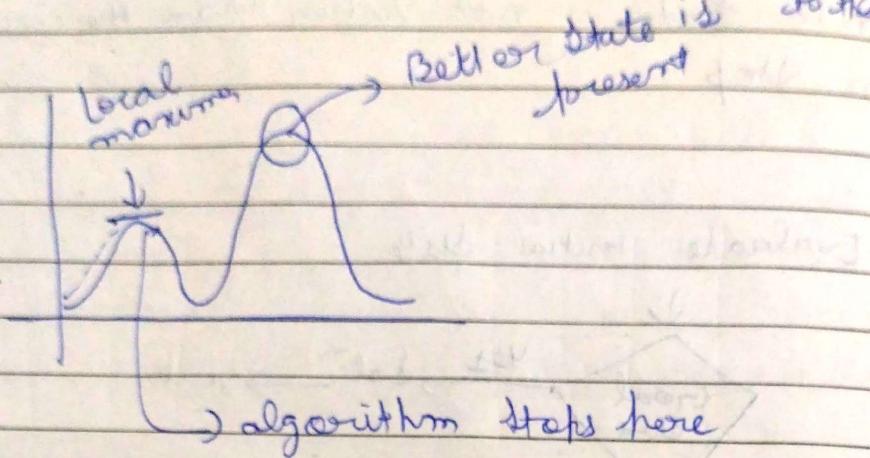
Apply operator 'o' and get new state
(NS)



Limitations of hill climbing

① local maxima

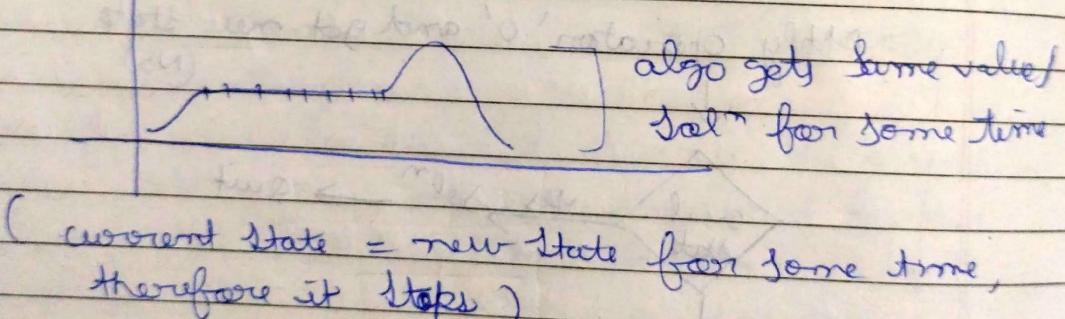
→ State which is better than all of its neighbours but not better than some other state which is not directly connected to that state.



also known as local domain search or local search as it has information related to local domain only.

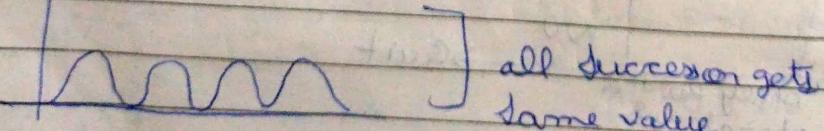
② Plateau / Flat maximum

→ A flat area of the search space in which all the neighbouring states have same values.

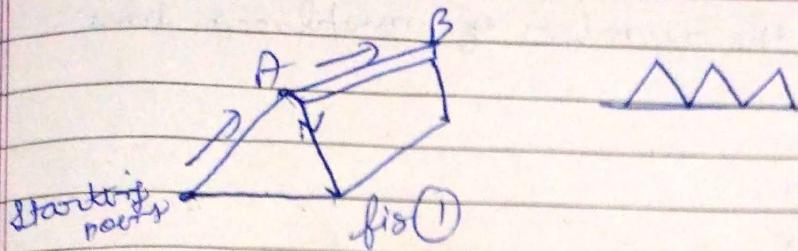


③ Ridge

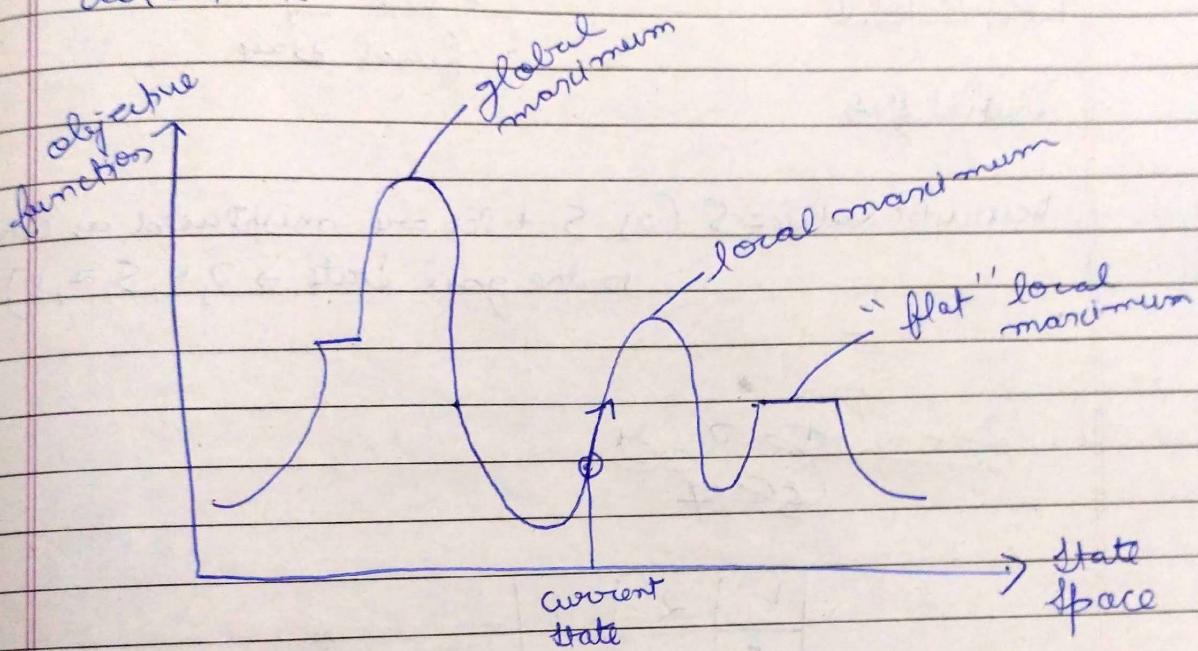
Creating a sequence of local maxima but all of them are not directly connected



instead of path cost



e.g. In this fig ①, it is moving in upward direction towards B but after reaching at A, it has to stop. Although Point B is above A, it cannot go further because it can not change its direction.



Example Solve 8 puzzle problem using Hill climbing search

1	2	4
5		7
3	6	8

Initial State

1	4	7
2	5	8
3	6	

final State

using backtracking hill climbing algorithm

[Any heuristic value which is less than or equal to the actual value is said to be admissible]

Page: _____
Date: _____

$H=$ the number of misplaced tiles

5 2 9 4
6 3 7 8

Tens with Red is representing the misplaced tiles

1	2	4
5		7
3	6	8

1	4	7
2	5	8
3	6	

final state

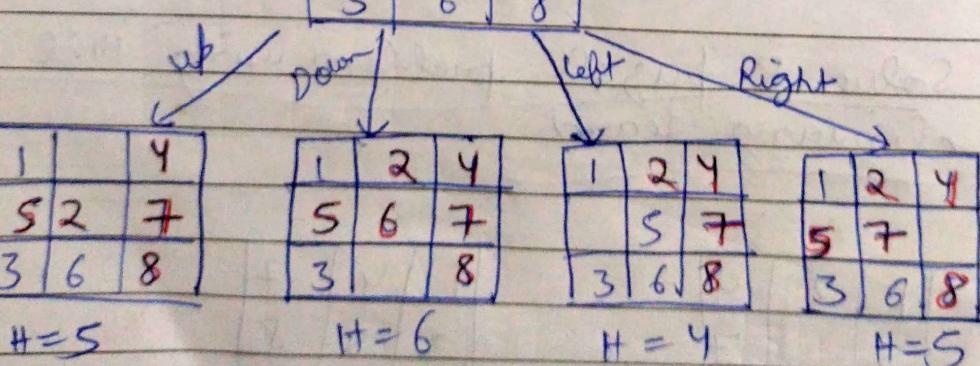
Initial State

a) Heuristic value = 5 (as 5 tiles are misplaced as compared to the goal state $\rightarrow 1, 4, 5, 7, 8$)

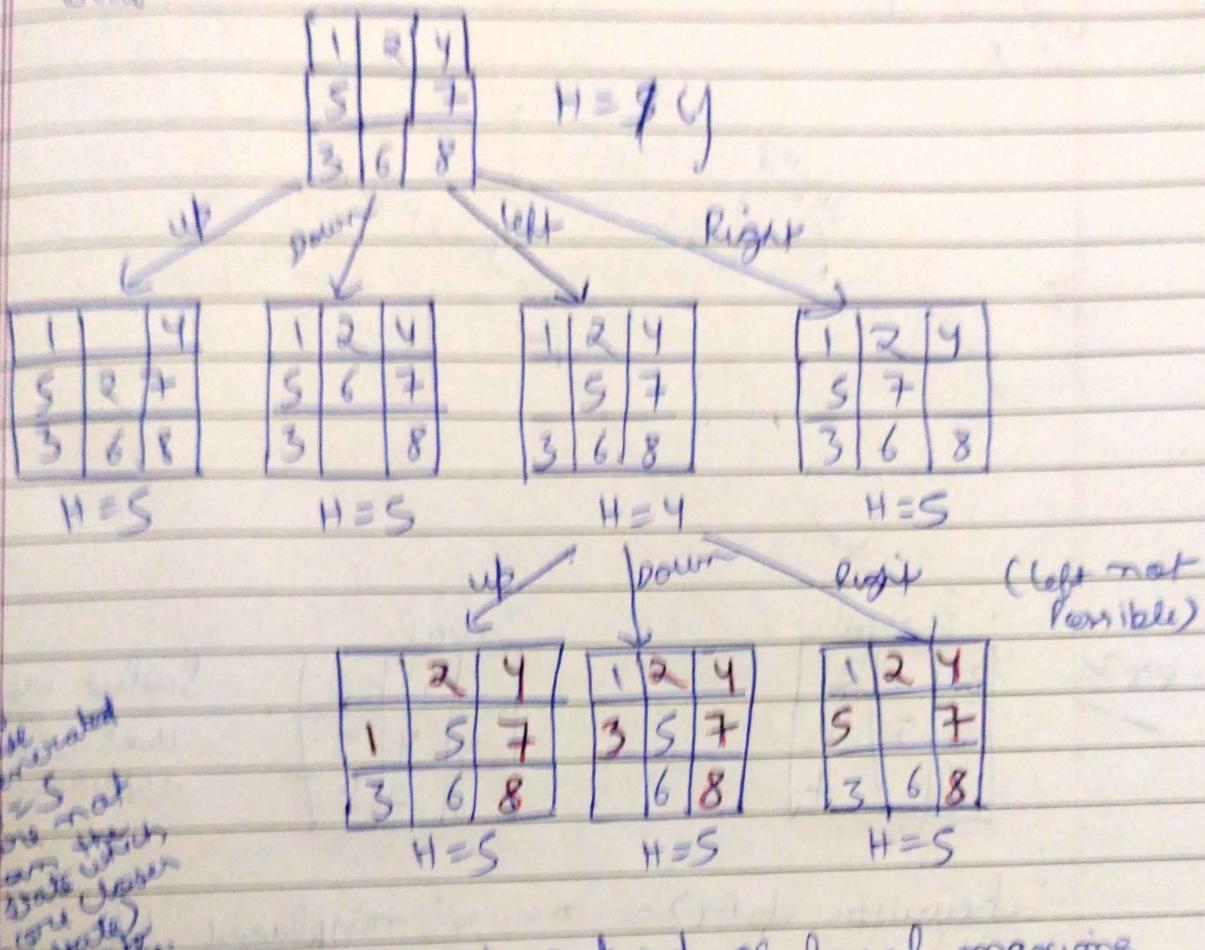
5 2 9 4
6 3 7 8

1	2	4
5		7
3	6	8

Red color represents heuristic value (no. of misplaced tiles)



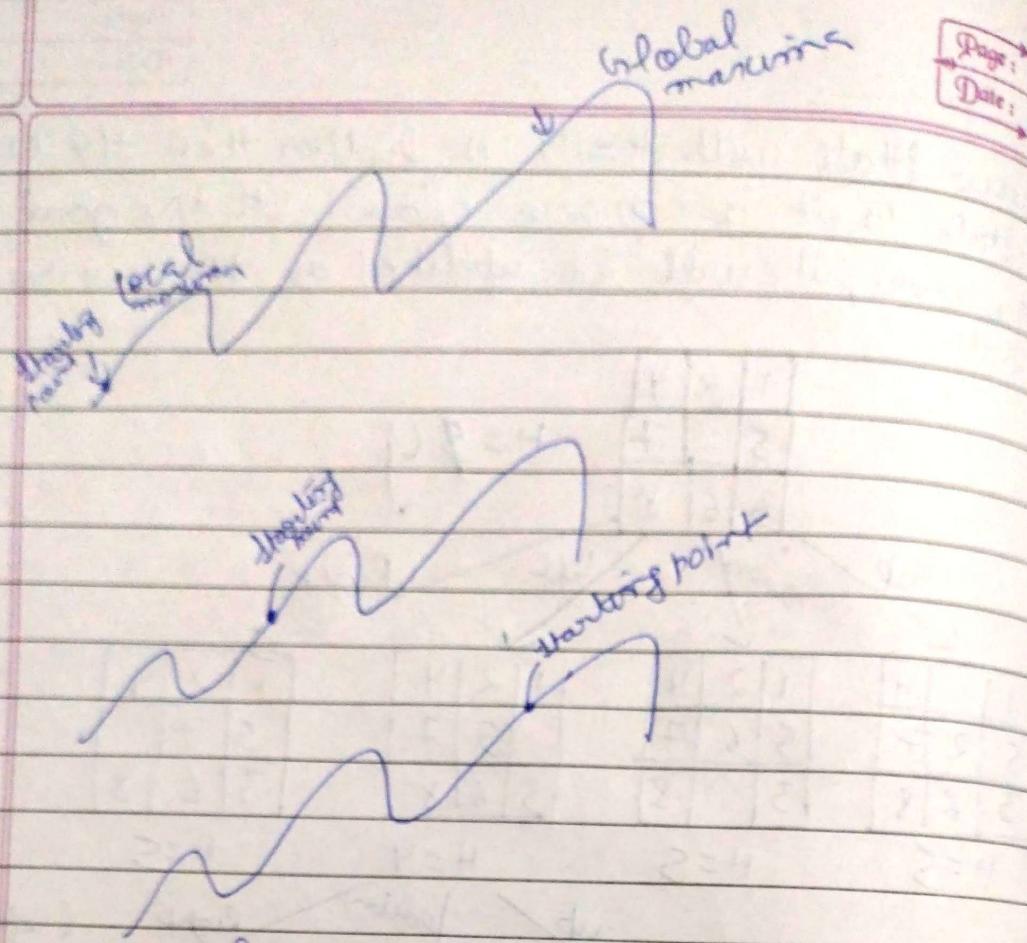
Now State with $H=4$ is better than the current state so it is more closer to the goal state therefore, it will be updated as the current state.



\therefore This is a kind of local maxima
i.e. in every direction the solution
generated is inferior than the current
solution

Solutions of hill climbing weaknesses

- Random initialization of starting state
- Jump



Initial

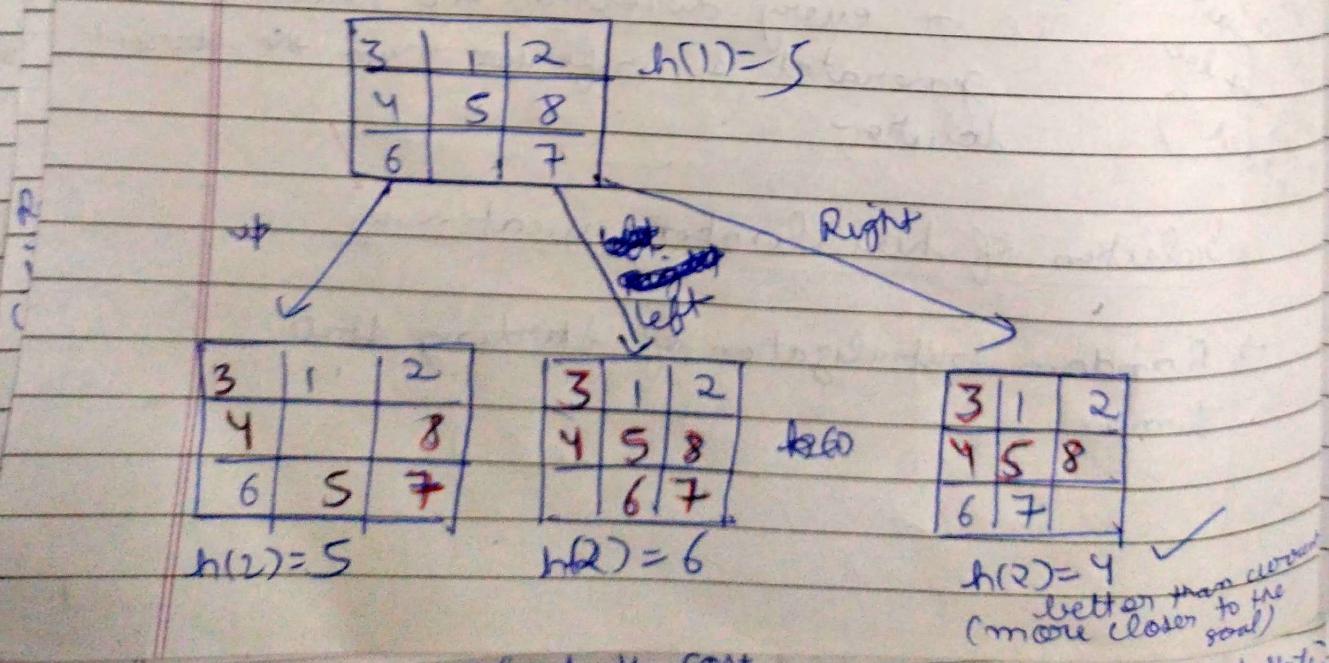
3	1	2
4	5	8
6		7

Goal

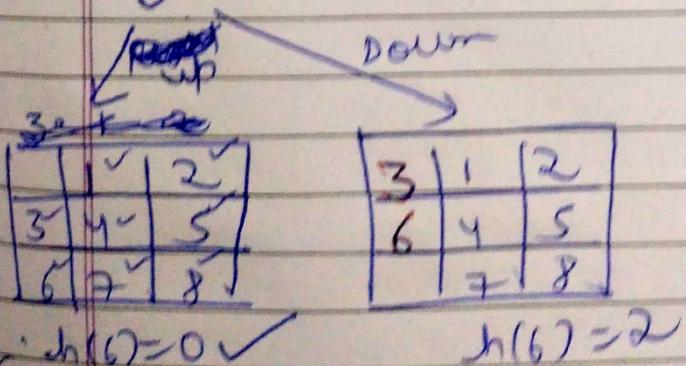
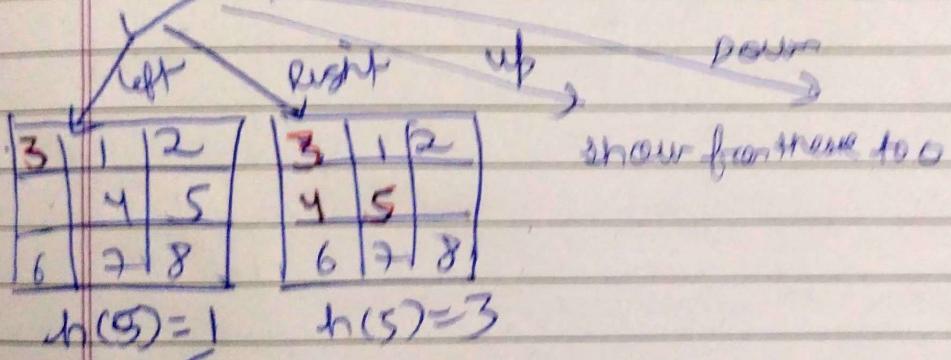
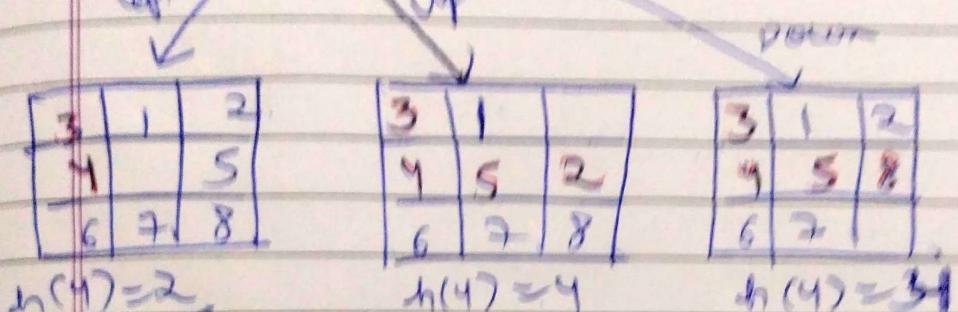
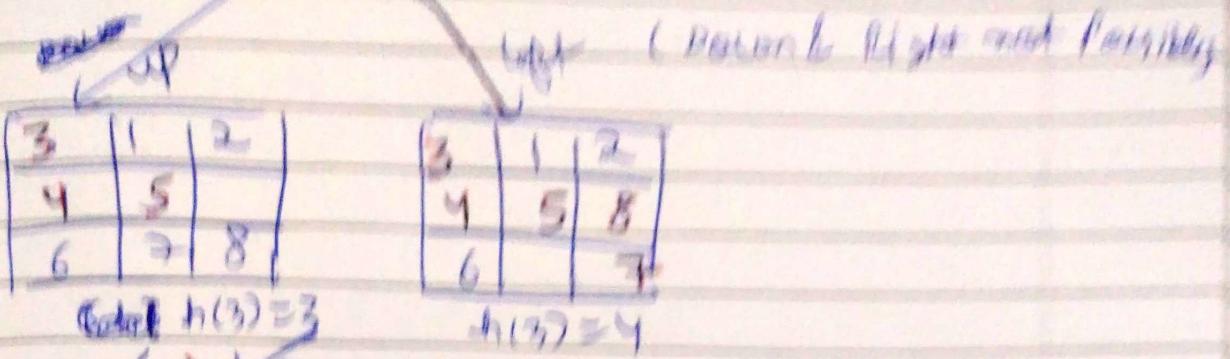
1	2	
3	4	5
6	7	8

Solve using
Hill climb
approach

heuristic $h(r) = \text{no. of misplaced tiles}$, we
have to minimize the value of $h(r)$

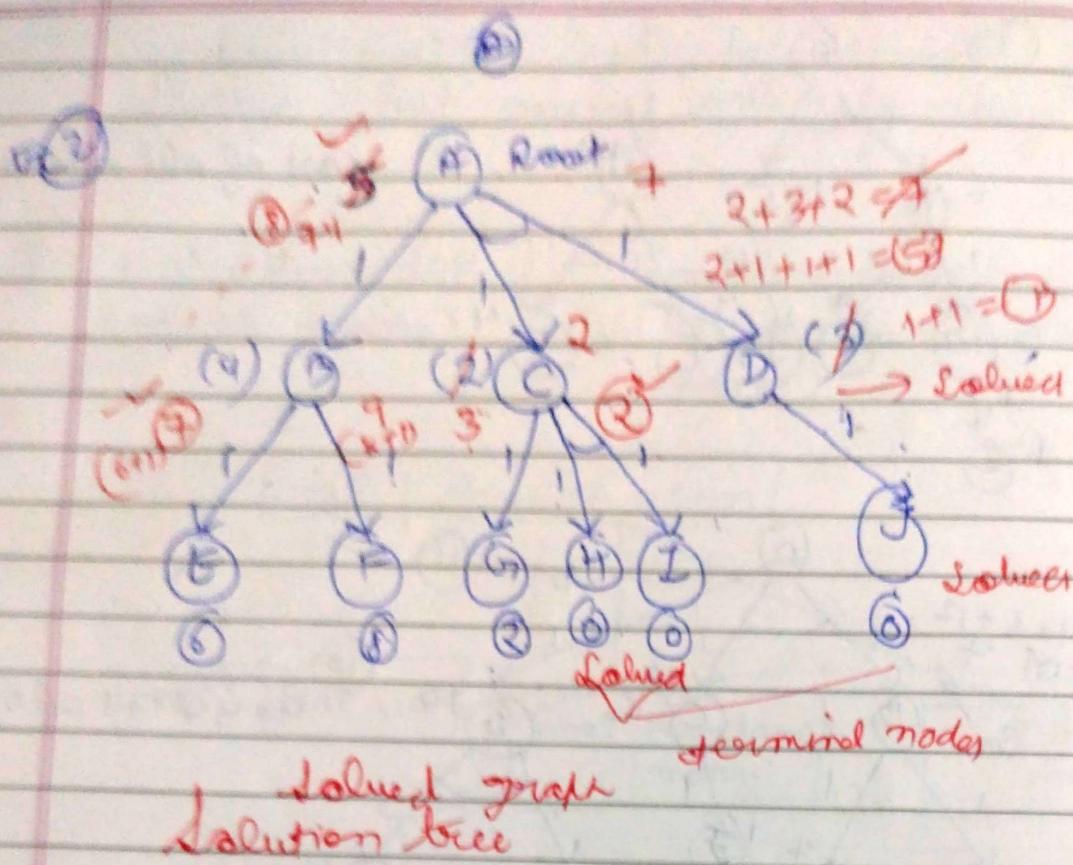


3	1	2
4	5	8
6	7	



all tiles are correctly placed now

Answer with $h(6) = 0$



Hill climbing Algorithm

Local search

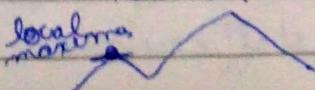
- Evaluate and modifying one or more current states rather than systematically exploring paths from an initial state
- Good for those which requires only solution instead of path cost
 - requires less memory (store only current state)
 - move only to neighbors of that node (current node)

→ Hill climbing is a type of local search
 → the basic idea is to always head towards a state which is better than the current one
 → So, if you are at town A and you can get to town B and town C (and your target is town D) then you should make a move if town B or C appear nearer to town D than town A does.

1. Evaluate the initial state. If it is also goal state then return it, otherwise continue with the initial state as the current state.
2. Loop until the solution is found or until there are no new operators to be applied in the current state.
 - a) Select an operator that has not yet been applied to current state and apply it to produce new state.
 - b) Evaluate the new state
 - i) if it is a goal state, then return it and quit
 - ii) if it is not a goal state but it is better than the current state, then make it as a current state
 - iii) if it is not better than the current state, then continue in the loop.

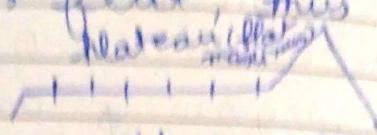
Drawbacks of hill climbing algorithm

- Local Maxima - A local maximum as opposed to global maximum.

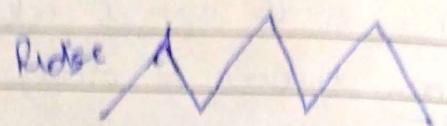


Some answer from all the
possible roads

(ii) Plateau - An area of search space where evaluation function is flat, thus requiring random walk.



(iii) Ridge - where there are steep slopes, and the search direction is not towards top but towards the side



→ In each of the previous cases, (local maxima, plateaus & ridge), the algorithm reaches a point at which no progress is being made.

→ A solution is to do a random-restart hill climbing - where random initial states are generated, running each until it halts or makes no progress. The best result is chosen (the one which gives maximum value).

(Rather than starting at one initial state, start with multiple initial states, then calculate the goal state. Cho then choose the one which gives maximum value of goal state (best value))

→ Hill climbing uses local information: It decides what to do next by looking only at the "immediate" consequences of its choices.

→ will determine when at local optimum and may not be able to reach global optimum. → The order of application of operators can make big difference.

→ Global information might be encoded in heuristic functions → consider future consequences

→ Example of Simple hill climbing

Start	A	Goal	D
	D		C
	C		B
	B		A

Blocks world

Solve this problem using hill climbing algorithm

Sol case 1: using local heuristic (Defining a heuristic function $h(x)$)

$h(x)$ (if correctly positioned)

+1 for each block that is resting on the thing it is supposed to be resting on.

-1 for each block that is resting on a wrong thing.

(if incorrectly placed)

Start

total = 0

A	-1
D	+1
C	+1
B	-1

Goal

D	+1
C	+1
B	+1
A	+1

If we should start with 0 and at the end, should be able to reach at 4.

0

A
D
C
B

2 (+1 -1 +1)

Total

+1	D
-1	C
+1	B

| A | +1

	D	(2)	If D is placed at O							
x1	C		x1	C	D	-1	x1	C	(2)	
x1	B	A	x1	-1	B	A	x1	-1	B	
x1			x1	-1		A	x1	-1	D	

\leftarrow disadvantage of
disadv. being 1

With time
access of local
information is
increasingly plateaued

Mainly happens in case of local transformation

Now for both of these states, we are getting value = 0, so it is a kind of plateau

is a kind of plateau

case 2 using Global heuristic

<u>Start</u>	A
	D
	C
	B

Goal	D
	C
	B
	A

Blocky world

Global heuristic / we do not just consider the blocks below the current block rather we are considering the support structure

- For each block that has the correct support structure : +1 to every block in the support structure
- For each block that has a wrong support structure : -1 to every block in the support structure

Start	A	-3
-6	D	-2
	C	-1
	B	0

Block world

D	3
C	2
B	1
A	0

Note: we are considering global info. over here

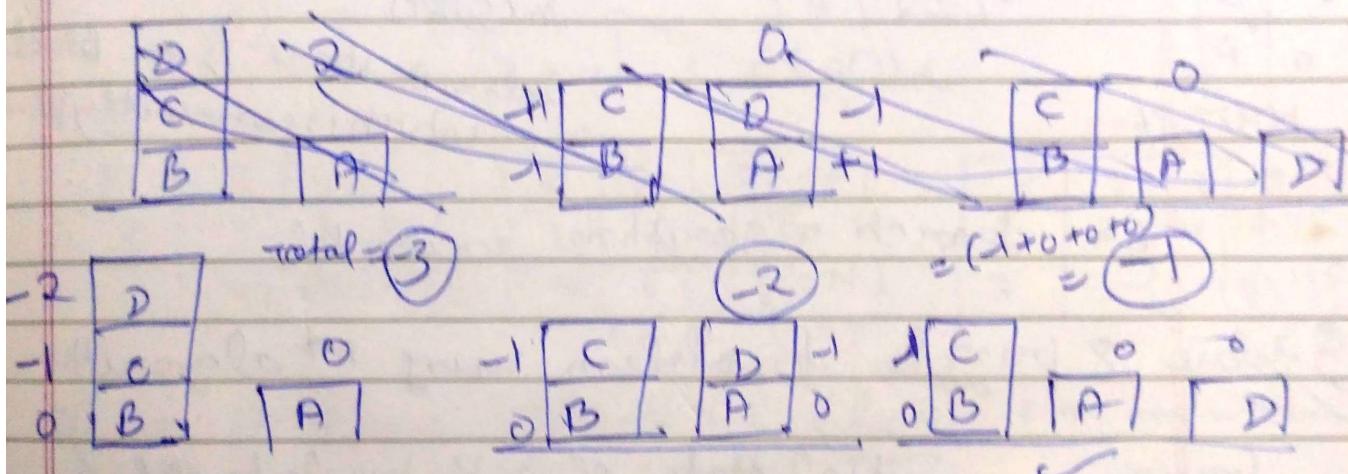
Below B, nothing is placed, so it is 0

Below C, B is incorrectly placed so it is -1

Below D, C & B are incorrectly placed, so it is -2

Below A & D, C, B are incorrectly placed so -3

A	-6
D	
C	
B	



Now comparing the three states, choosing the maximum value i.e. -1, so picking the third state.

C			
B			
A			
D			

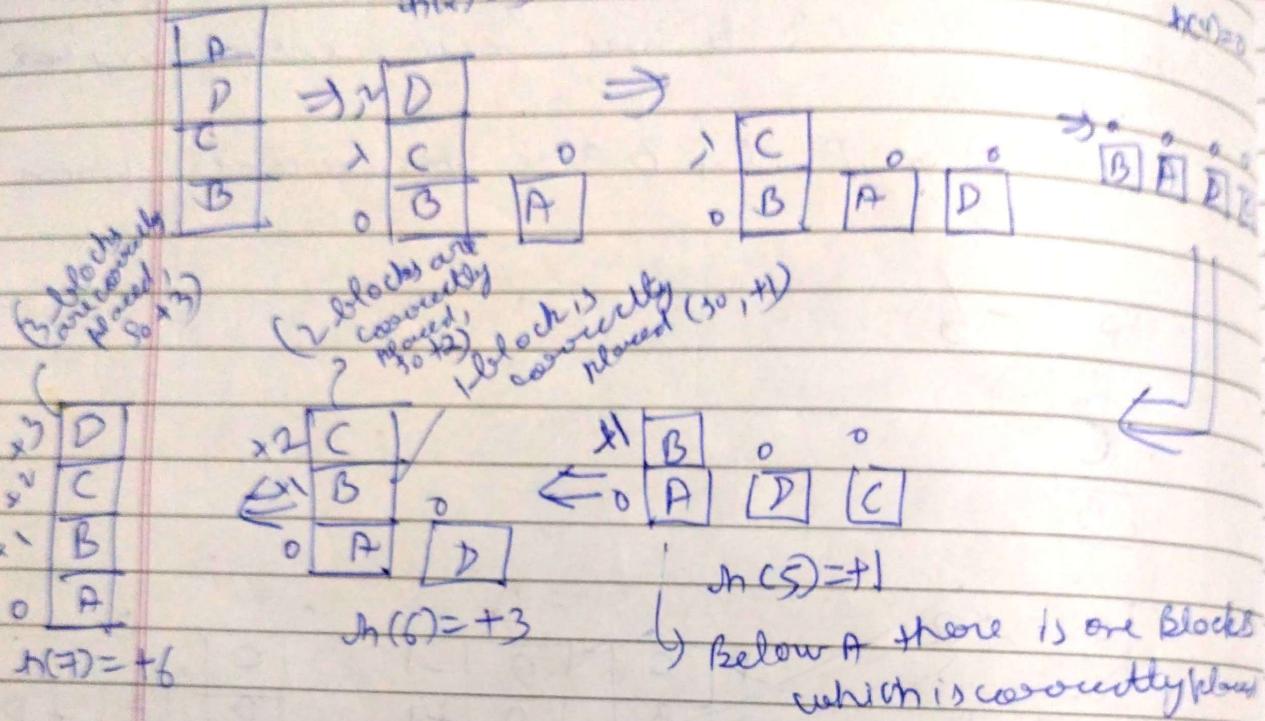
(as compared with the local search, same value was achieved from the 2nd & 3rd alternative possibility)

$$h(1) = -6$$

$$h(2) = -3$$

$$h(3) = -1$$

$$h(4) = 0$$



A* Search algorithm example

Solve 8-puzzle problem using A* algorithm

Given an initial state of a 8-puzzle problem and final state to be searched/reached

2	8	3
1	6	4
7		5

Initial state

1	2	3
8		4
7	6	5

Final state

Find the most cost-effective path to reach the final state from initial state using A* algorithm

$$f(n) = g(n) + h(n)$$

Consider $g(m)$ = depth of node
 $h(m)$ = no. of misplaced tiles

If root level depth = 0 $\therefore g(m) = 0$

$h(m)$ = no. of misplaced tiles = 4

(with respect to final state)

Initial state

2	8	3
1	6	4
7		5

$$\begin{aligned} g &= 0 \\ h &= 4 \\ f &= 0 + 4 = 4 \end{aligned}$$

2	8	3	$g=1$
1	6	4	$h=5$
7	5		$f=1+5=6$

2	8	3	$g=1$
1		4	$h=3$
7	6	5	$f=1+3=4$

2	8	3	$g=1$
1	6	4	$h=5$
7	5		$f=1+5=6$

If we compare all three ($f=4$) is the minimum
 (with least misplaced tiles)

2	8	3	$g=2$
	1	4	$h=3$
7	6	5	$f=2+3=5$

2		3	$g=2$
1	8	4	$h=3$
7	6	5	$f=2+3=5$

2	8	3	$g=2$
1		4	$h=4$
7	6	5	$f=2+4=6$

These will be considered next with $f=5$

Now $f = 5$

Evergreen
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2	1	8	3
7	6	5	
g=2	h=3		$f = 2+3 = 5$

2		3
1	8	4
7	6	5

$$g=2$$

$$h=3$$

$$f = 2+3 = 5$$

2	8	3
3	1	4
7	6	5

$$g=3$$

$$h=3$$

$$f = 3+3 = 6$$

2	8	3
7	1	4
6	5	

$$g=3$$

$$h=4$$

$$f = 3+4 = 7$$

2	3	
1	8	4
7	6	5

$$g=3$$

$$h=2$$

$$f = 3+2 = 5$$

$$f = 5$$

Least value will be considered
 $g=3$
 $h=4$
 $f = 3+4 = 7$

2	3	
1	8	4
7	6	5

$$g=3$$

$$h=2$$

$$f = 3+2 = 5$$

1	2	3
8		4
7	6	5

$$g=4$$

$$h=1$$

$$f = 4+1 = 5$$

1	2	3
8		4
7	6	5

$$g=5$$

$$h=0$$

$$f = 5+0 = 5$$

1	2	3
7	8	4
6	5	

$$g=5$$

$$h=2$$

$$f = 5+2 = 7$$

Final State

8-Puzzle using A*

Complete tree

Every page
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2	8	3	$g=0$
1	6	4	$h=4$
7	5		$f=0+4=4$

2	8	3	$g=1$
1	6	4	$h=5$
7	5		$f=1+5=6$

2	8	3	$g=1$
1		4	$h=3$
7	6	5	$f=1+3=4$

2	8	3	$g=1$
1	6	4	$h=5$
7	5		$f=1+5=6$

2	8	3	$g=2$
4	1	4	$h=2$
7	6	5	$f=2+3=5$

2	8	3	$g=2$
1	8	4	$h=3$
7	6	5	$f=2+3=5$

2	8	3	$g=2$
1	4		$h=4$
7	6	5	$f=2+4=6$

2	8	3	$g=3$
1	4		$h=3$
7	6	5	$f=3+3=6$

2	8	3	$g=3$
7	1	4	$h=4$
6	5		$f=3+4=7$

2	8	3	$g=3$
1	8	4	$h=2$
7	6	5	$f=3+2=5$

2	3		$g=3$
1	8	4	$h=4$
7	6	5	$f=3+4=7$

$$f = g + h = 3+4 = 7$$

1	2	3	$g=4$
	8	4	$h=1$
7	6	5	$f=4+1=5$

1	2	3	$g=5$
8		4	$h=0$
7	6	5	$f=5+0=5$

Final State

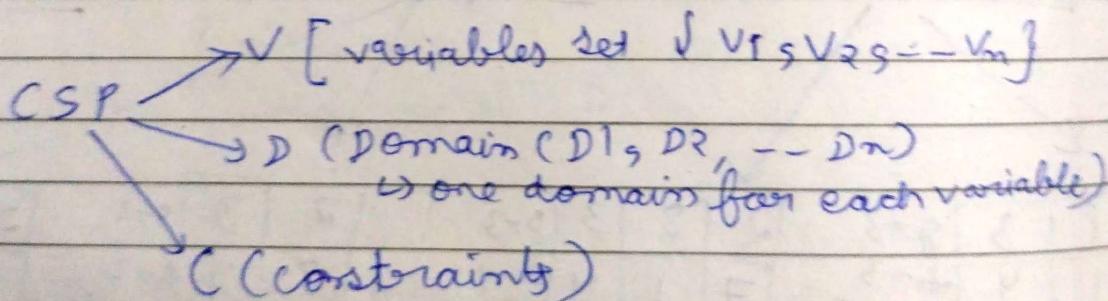
1	2	3	$g=5$
7	8	4	$h=2$
6	3		$f=5+2=7$

Constraint Satisfaction

- ↳ It is search procedure that operates in a space of constraint sets
- Constraint Satisfaction problems in AI have goal of discovering some problem state that satisfies a given set of constraints.

Process:

- i) Constraints are discovered and propagated throughout the system.
- ii) If still there is no solution, search begins
 - Guess is made about something and added as a new constraint



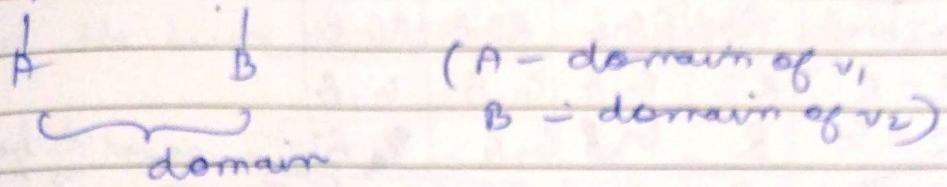
↳ Specify allowable combination of values

$$C_i = (\text{scope}, \text{relation})$$

↓
(Set of variables
that participate
in constraint)

↳ defines values that a
variable can take

v_1 and v_2 (variables)



② constraint

(1) values of v_1 & v_2 can't be same

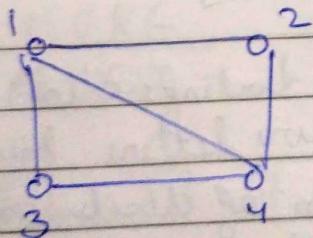
$$C_1 = \{ (v_1, v_2) \mid v_1 \neq v_2 \}$$

scope relation

To solve CSP, we used intelligent backtracking method

intelligent Backtracking \rightarrow only backtrack where conflict occurs

3) node colouring :-



we are given a graph.
constraint is that two
adjacent nodes can't have
the same colour

$$V = \{ 1, 2, 3, 4 \}$$

$$D = \{ R, G, B \}$$

$$V = \{ 1, 2, 3, 4 \}$$

$$D = \{ \text{Red, Green, Blue} \}$$

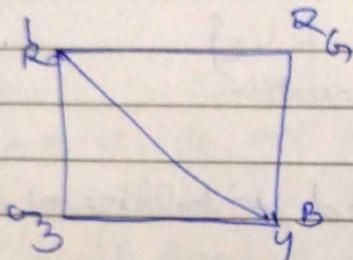
$C = \{ \text{adjacent nodes should not have same colour} \}$

Initial	1	2	3	4
	RGrB	RGrB	RGrB	RGrB
$1=R$	R	G, B	G, B	G, B
$2=G$	R	G,	G, B	B
$3=B$	R	G	B	B
$4=G$	R	G	G	B

count + be full
as no column
left

\therefore To solve this error

we need to backtrace
moving directly to
point that caused
problem



Advantages

- ① It is time efficient

CryptArithmetic Problem

- ↳ Types of constraint satisfaction problem (CSP)
- ↳ constraints
 - \rightarrow No two letters have same value
 - \rightarrow Sum of digits must be as shown in problem

\rightarrow There should be only one carry forward

\rightarrow Digits that can be assigned to a word / alphabet

(0-9)

orange

\rightarrow Numbers must not begin with zero i.e. 0123 (Wrong), 123 (Correct)

9 1

+ 0

+ G 0

—
0 U T

at most

and left most digit
can't be 0

left most digit = ①
(represents carry)

0-9 ($9+8=17$)

\downarrow
most carry = 1

Assign each letter a digit in the range 0-9,
and the sum should be equal to 07 (given)

unique letter	Digit
T	2
O	1
G	8
U	0

$$\boxed{2} \quad \boxed{1}$$

$$\begin{array}{r} \boxed{8} \quad \boxed{1} \\ \hline \boxed{0} \quad \boxed{2} \end{array}$$

$$2 + 6 = 8; 2 + 6 \geq 10$$

$$\begin{aligned} 2 + 9 &= 11 & \times & \text{can't be taken} \\ &&&\text{as it will carry} \\ 2 + 8 &= 10 & \checkmark & \text{0 & 8 both} \\ &&&\text{be 1 that} \\ &&&\text{is not possible} \end{aligned}$$

QR

S END
MORE
M O NEY

C₄ C₃ C₂ C₁
 9_S 5_E 6_N 7_D

$$\begin{array}{r} + \\ \hline \end{array} \quad \begin{array}{r} 1_n \\ 0_o \\ 8_s \\ 5_e \\ \hline 0_o \\ 6_n \\ 5_e \\ 2_1 \end{array}$$

$$S + M, \text{ if } M = 1, S + M \geq 10$$

$$S = 9$$

$$\begin{aligned} E + O = N & \quad \left\{ \begin{array}{l} \text{if } C_2 = 0 \times \\ \hookrightarrow \text{zero}(0) \quad \text{then } E = N \\ \text{which is wrong} \end{array} \right. \\ & \text{every letter} \\ & \text{should be given a} \\ & \text{unique no.} \\ & \therefore bC_2 = 1 \end{aligned}$$

$$\begin{aligned} & \text{let } E = 5 \\ & E + O + C_2 = N \end{aligned}$$

$$\begin{aligned} S + C_2 &= N \\ S + 1 &= N \Rightarrow \cancel{\boxed{S+1}} \Rightarrow \boxed{N=6} \end{aligned}$$

$$N + R = E$$

$$6 + R = 5$$

$$\text{let } R = 9$$

$$6 + 9 = 15$$

$$\downarrow \text{carry}$$

$$E = 5$$

$$\text{out } S = 9 \text{ (already)}$$

$$\therefore R \text{ can't be } 9$$

$$D+E = Y$$

$$D+S = Y$$

we need carry

start is possible only if $D > S$

$$\begin{array}{r} D-S-G \\ -6-N \\ -7-X \\ -8-R \\ -9-S \end{array}$$

$$7+8 = Y$$

$$\boxed{Y=15}$$

carry

$$Y = \begin{array}{r} 0 \\ 5 \\ \downarrow \\ \text{carry} \end{array} \quad \boxed{Y=2}$$

$$\begin{array}{r} \begin{array}{ccccc} C_5 & C_4 & C_3 & C_2 & C_1 \\ \hline C & R & O & S & S \end{array} \\ \begin{array}{ccccc} + & R & O & A & D \\ \hline D & A & N & G & C & R \end{array} \end{array}$$

character	code
D	1
C	
R	
A	
O	
N	
G	
S	
E	

$$\begin{array}{r} \begin{array}{|c|c|c|c|c|} \hline C_5 & C_4 & C_3 & C_2 & C_1 \\ \hline 1 & 0 & 1 & 1 & 0 \\ \hline \end{array} \\ + \begin{array}{|c|c|c|c|c|} \hline C_5 & C_4 & C_3 & C_2 & C_1 \\ \hline 0 & 1 & 0 & 1 & 0 \\ \hline \end{array} \\ \hline \begin{array}{|c|c|c|c|c|} \hline C_5 & C_4 & C_3 & C_2 & C_1 \\ \hline 1 & 1 & 1 & 0 & 0 \\ \hline \end{array} \end{array}$$

$$S+S=R$$

Rule 2: Sum of two same numbers is even

$\therefore S+S=R$, so R is even
(By using Rule 2)

$$C_5 \leftarrow \begin{array}{l} 0 \\ 1 \end{array}$$

Rule 1: Result should not start with 0
 $\therefore C_5 = 1$