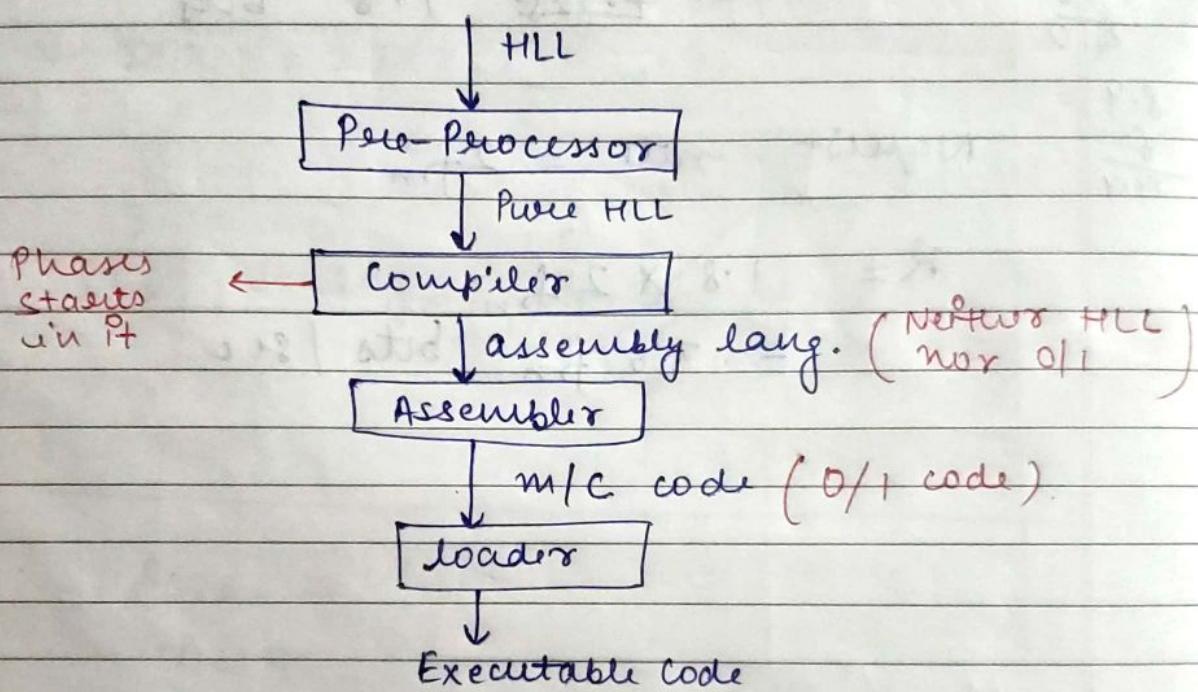


# Compiler Design

## Unit - 1

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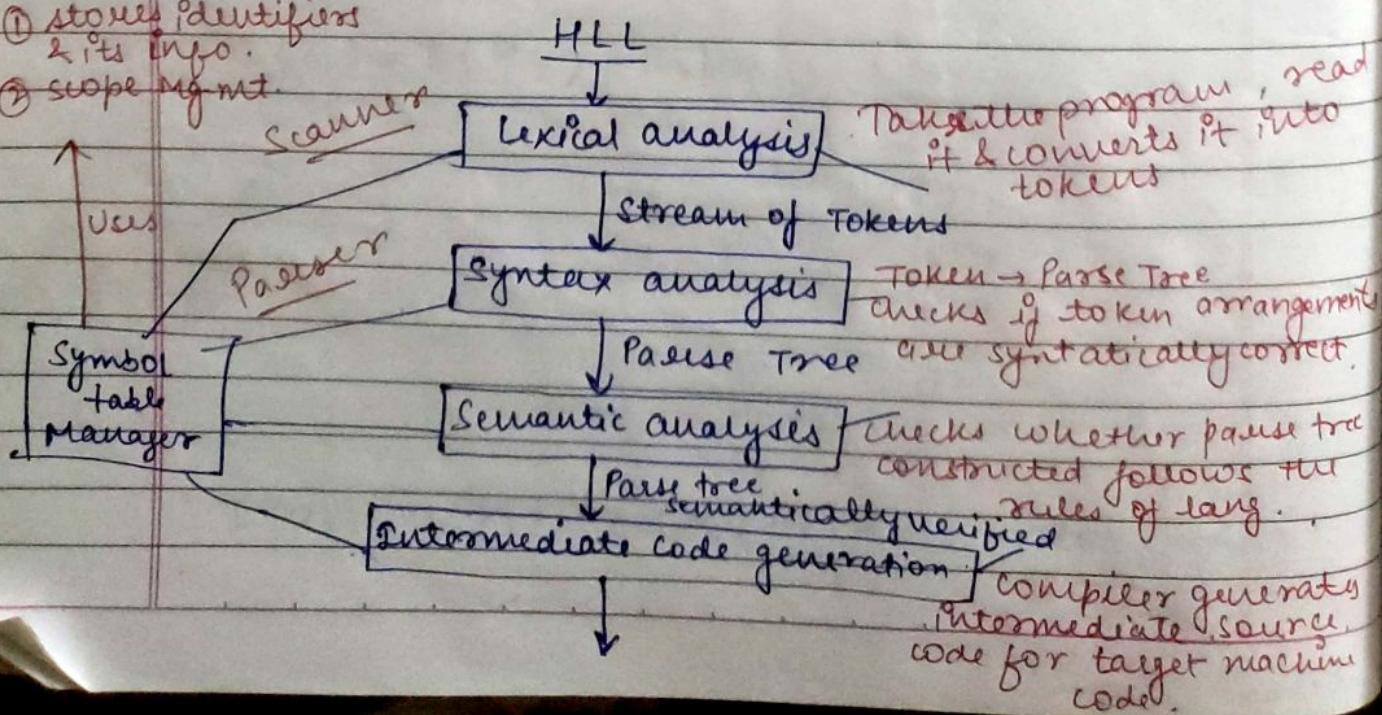
- \* The compilation process is a sequence of various phases. Each phase takes input from previous stage, has its own representation of source program, and feeds its output to next phase of compiler. It also reports errors present in source program as a part of its translation process.



### \* Phases of compiler :-

① stores identifiers & its info.

② scope mgmt.



## Code Optimization

optimization of intermediate code such as removing unnecessary code lines & arranges sequence of stmt. in order etc.

## Code Generation

### Assembly

It translates intermediate code into sequence of machine code.

## \* Structure of compiler :

### Two modules

#### Front-end

- a) lexical analyzer
- b) semantic analyzer
- c) syntax analyzer
- d) intermediate code generator

#### Back-end

- a) code Optimizer
- b) code generator

} Synthesis

### Analysis

Linear - lexical analysis  
or  
scanning

Done by lexical analyzer or scanner

Hierarchical - Syntax analysis  
or  
Parsing

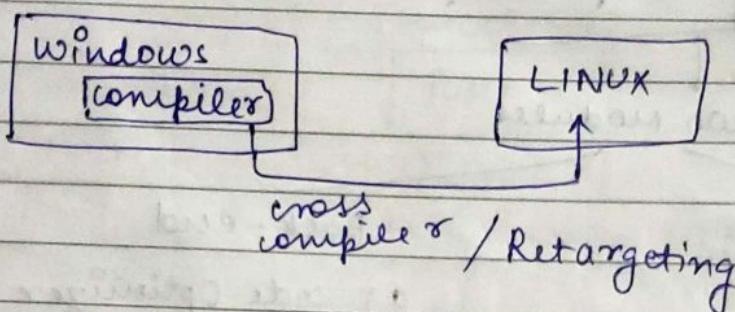
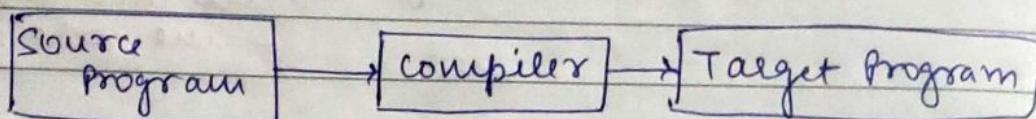
Done by Syntax analyzer or parser

» Lexemes - Sequence of characters (alphanumeric)

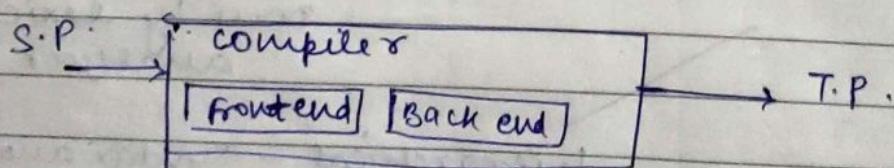
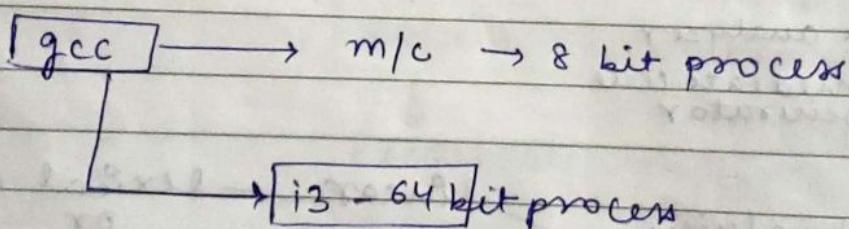
» Tokens - Group of similar lexemes defined with a pattern.

## \* Cross compiler

A cross compiler is a compiler capable of creating executable code for a platform other than one on which compiler is running.



Eg - gcc

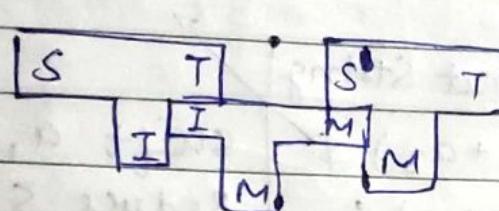
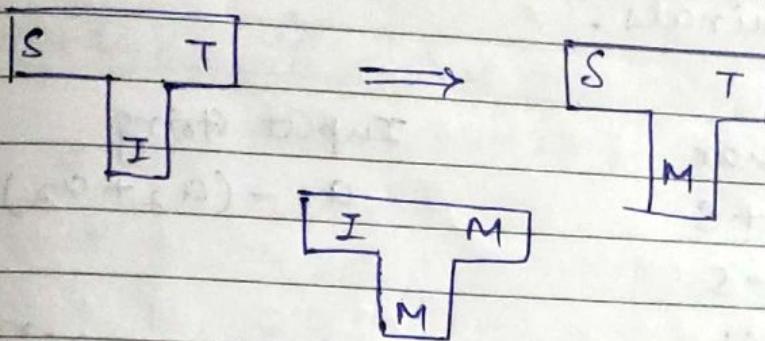


front end depends on source language ; since the language 'c' of gcc remains same but platform change , therefore , front end will remain same but backend will change.

Advantage :- We can still build code although hardware conditions of that machine are insufficient

## \* Bootstrapping :-

Bootstrapping is the process by which simple lang. is used to translate more complicated program.



$$S_M^T = S_I^T + I_M^M$$

Eg- gcc

## \* Quick and dirty compiler :-

A quick & dirty compiler are used to compile a code to check the functionality and correctness of a code. Once the written program is correct, so it is recompiled to make efficient. Its main function is to compile the codes as fast as possible.

## \* Shift - Reduce Parsing :- (\$)

It is a process of reducing a string to start symbol of a grammar.

It uses stack to hold the grammar and an ip to hold the string.

- Steps:
- ① At shift action, the current symbol in I/P string is pushed to a stack.
  - ② At each reduction, the symbol will be replaced by non-terminals.

Eg: Grammar

$$S \rightarrow S + S$$

$$S \rightarrow S - S$$

$$S \rightarrow (S)$$

$$S \rightarrow a$$

Input String

$$a_1 - (a_2 + a_3)$$

mandatory

Stack contents	Input String	Action
\$	$a_1 - (a_2 + a_3), \$$	shift $a_1$
$\$ a_1$	$- (a_2 + a_3) \$$	Reduce $S \rightarrow a$
$\$ S$	$- (a_2 + a_3) \$$	shift $-$
$\$ S -$	$(a_2 + a_3) \$$	shift $\equiv ($
$\$ S - ($	$a_2 + a_3) \$$	shift $a_2$
$\$ S - (a_2$	$+ a_3) \$$	Reduce $S \rightarrow a$
$\$ S - (S$	$+ a_3) \$$	shift $+$
$\$ S - (S +$	$a_3) \$$	shift $a_3$
$\$ S - (S + a_3$	$) \$$	Reduce $S \rightarrow a$
$\$ S - (S + S$	$) \$$	shift $)$
$\$ S - (S + S)$	$\$$	Reduce $S \rightarrow S + S$
$\$ S - (S)$	$\$$	Reduce $S \rightarrow (S)$ •
$\$ S - S$	$\$$	Reduce $S \rightarrow S - S$
$\$ S$	•	Accept

## Grammar

$$E \rightarrow 2E2$$

$$E \rightarrow 3E3$$

$$E \rightarrow 4$$

i/p string

3 2 4 2 3

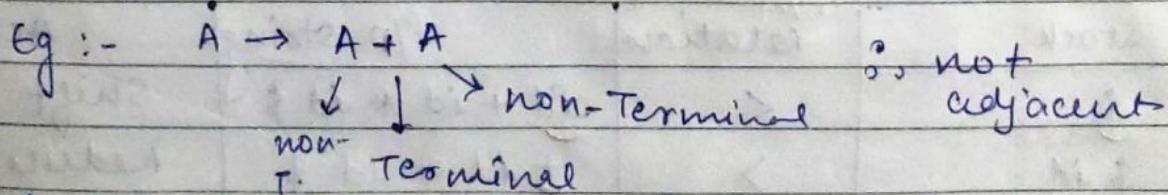
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Stack contents	i/p string	Action
\$	<del>3 4</del> 3 2 4 2 3 \$	Shift 3
\$3	2 4 2 3 \$	Shift 2
\$32	4 2 3 \$	Shift 4
\$324	2 3 \$	Reduce $E \rightarrow 4$
\$32E	2 3 \$	Shift 2
\$32E2	3 \$	Reduce $E \rightarrow 2E2$
\$3E	3 \$	Shift 3
\$3E3	\$	Reduce $E \rightarrow 3E3$
\$E	( \$ )	Accept

### \* Operator Precedence Parsing :-

A grammar  $G$  is called an operator precedence grammar if it meets following cond's:-

- There exist no production rule which contains  $\epsilon$  (Epsilon) on its right hand side.
- There exist no production rule which contains two non-terminals adjacent to each other on its RHS.



Rules :

Highest precedence - Terminals like a, b etc. and  $\oplus$

lowest precedence -  $\$$

$\oplus \neq \oplus$

$$\$ \leftrightarrow \$ = A$$

Q Consider the foll. grammar & construct an operator precedence parser

$$E \rightarrow EAE \mid id$$

$$A \rightarrow + \mid *$$

then parse the following string :  $id + id * id$

Sol:

Step 1: check the grammar, if not operator precedence  
 make it operator precedence grammar.

$$\therefore E \rightarrow E+E \mid E * E \mid id$$

Step 2: construct operator precedence table :

Terminal symbols are = { id , + , \* , \$ }

Table :	id	+	*	\$	Acc. to rules
id	-	>	>	>	{ id ≠ id }
+	<	>	<	>	
*	<	>	>	>	
\$	<	<	<	A	

Step 3: Parsing the given string :  $id + id * id$

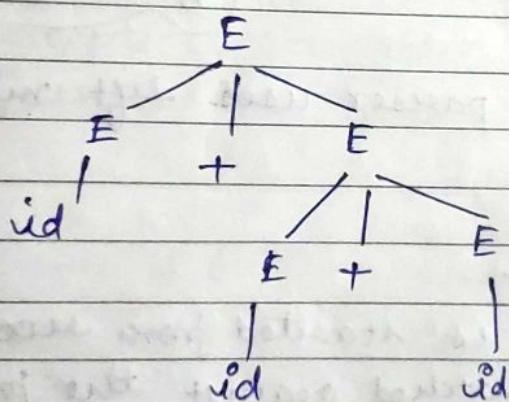
compare only terminals

stack	Relation	i/p string	Action
\$	<	<u>id + id * id \$</u>	Shift id
\$ id	>	<u>+ id * id \$</u>	Reduce $E \rightarrow id$
\$ E	<	<u>+ id * id \$</u>	Shift +
\$ E +	<	<u>id * id \$</u>	Shift id
\$ E + id	>	<u>* id \$</u>	Reduce $E \rightarrow id$
<del>\$ E + id</del>	*	<del><u>* id \$</u></del>	<del>Reduce <math>E \rightarrow id</math></del>

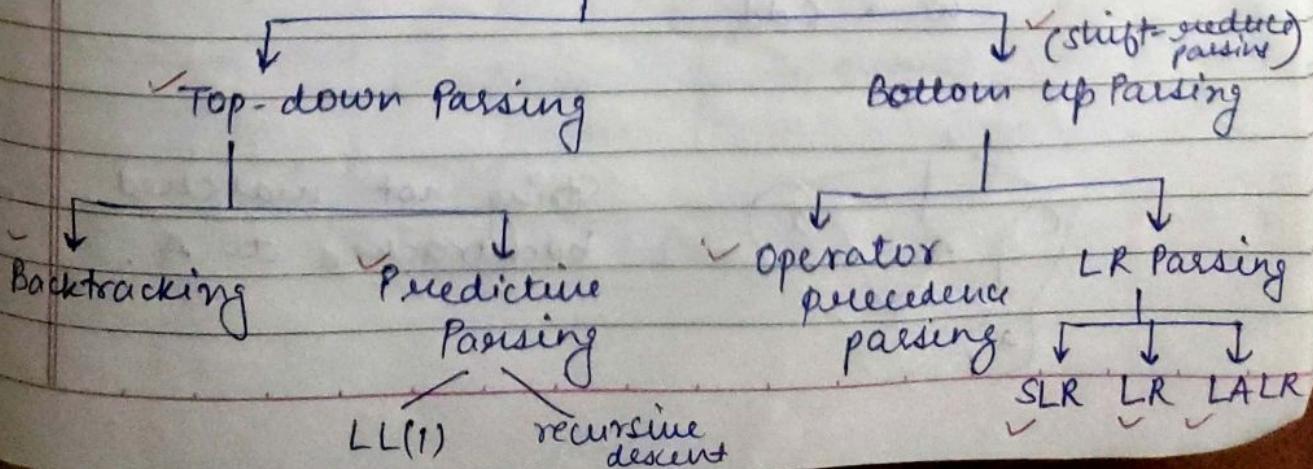
<del>\$ E + E</del>	<	* id \$	Shift *
<del>\$ E + E *</del>	<	id \$	Shift id
<del>\$ E + E * id</del>	>	f	Reduce E → id
<del>\$ E + E * E</del>	>	\$	Reduce E → E * E
<del>\$ E + E</del>	• >	\$	<del>Accept</del> Reduce E → E + E
\$ E	A	\$	Accept

**Note:** Reduce only when stack side is greater (>) than input string.

Step 4: Generating Parse Tree (Follow bottom up approach in table)



### Types of Parser



### \* Top-down Parsing :-

The process of construction of parse tree starting from root and proceed to children is called Top-down parsing i.e. starting from start symbol of grammar and reaching the I/p string.

Eg:

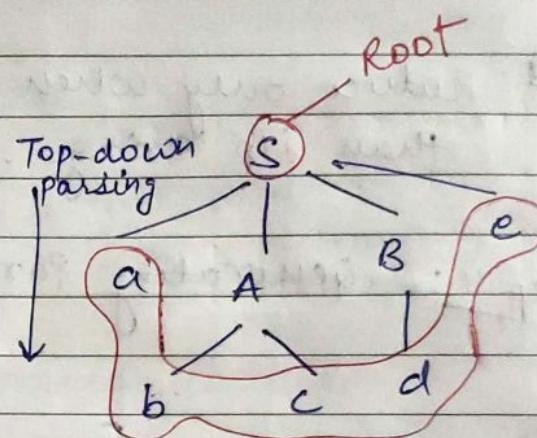
$$S \rightarrow aABe$$

$$A \rightarrow bc$$

$$B \rightarrow d$$

$$w \rightarrow abcde$$

i/p string



NOTE: Top down parser uses left most derivation.

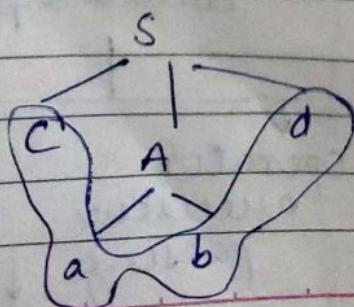
### \* Back-tracking :-

The parse tree is started from root node & its string is matched against the production rule for replacing them.

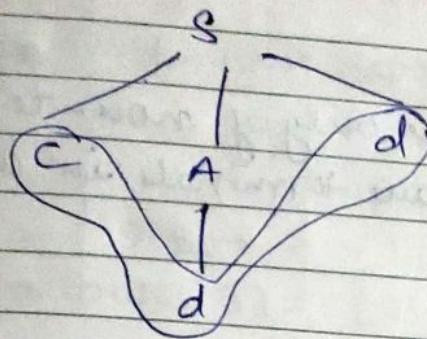
$$S \rightarrow CAD$$

$$A \rightarrow ab/d$$

$$w \rightarrow Cdd$$



String not matched, ; .  
 backtracked to A.



String matched.

- Limitation of Backtracking: If the grammar has a large no. of alternatives (production rules) then cost of backtracking is high.

### \* Predictive Parsing :- or LL Parser

It accepts LL grammar.

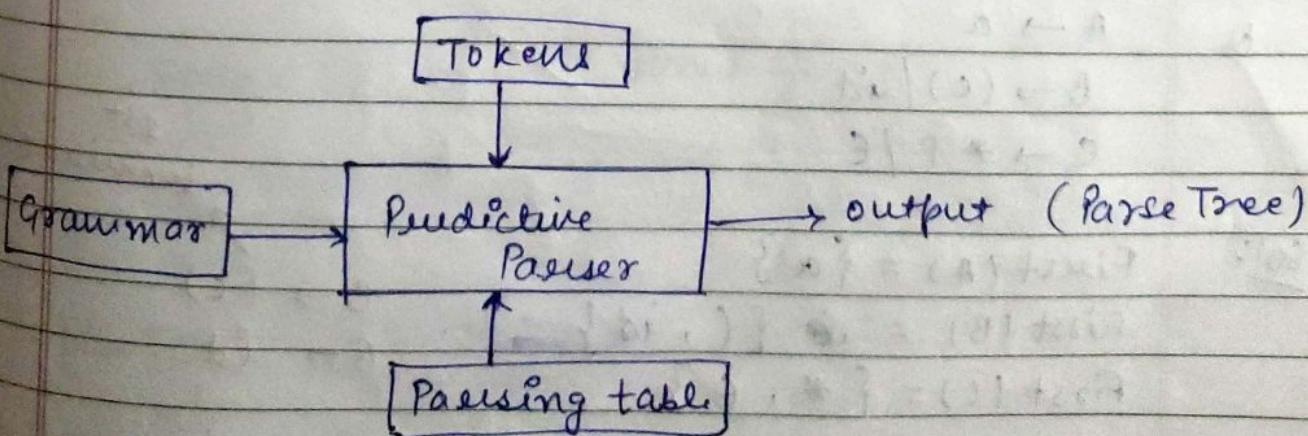
It is denoted as  $LL(k)$ .

(tracking)  
no. of look aheads  
(generally  $k=1$ )

$\downarrow$        $\downarrow$

i/p from      Left most  
left to right      derivation

A grammar  $G$  is  $LL(1)$  if there are two distinct productions.

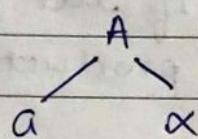


\* First and Follow :

first and follow are only of non-terminals.  
 and can only have terminals in answer.

\* First (left most)

case I:  $A \rightarrow a\alpha$



$$\text{First}(A) = \{a\}$$

phle hi terminal  
 mil gya 'a' to aage  
 kuch b ho wo ni  
 dekha.

case II:  $A \rightarrow \epsilon$

$$\text{First}(A) = \{\epsilon\}$$

case III:  $A \rightarrow B$

$B \rightarrow C$

$C \rightarrow \text{id}$

$$\text{First}(A) = \{\text{id}\} \quad (\because \text{Bcoz non-terminals cannot be first on any grammar.})$$

Q  $A \rightarrow a$

$B \rightarrow (c) / \text{id}$

$C \rightarrow *T / \epsilon$

Sol:

$$\text{First}(A) = \{a\}$$

$$\text{First}(B) = \{ (, \text{id}) \}$$

$$\text{First}(C) = \{ *, \epsilon \}$$

1st terminal

$\xrightarrow{B \rightarrow (c)}$

$\xrightarrow{B \rightarrow \text{id}}$



↑

$B \rightarrow (c)$

$B \rightarrow \text{id}$

↑

$B \rightarrow \text{id}$

> Follow (right most)

[ Right most ka first  
= follow ]

case I:  $A \rightarrow \alpha B \beta$

$B \rightarrow a$

Follow (B) = { a }

Eg:  $A \rightarrow TE'$

$E' \rightarrow + F / id$

Follow (T) = { +, id }

case II:  $A \rightarrow \alpha B \beta$

$B \rightarrow \epsilon$

i.e.  $A \rightarrow \alpha B$

Follow does not include  $\epsilon$   
(epsilon)

Follow (B) = {<sup>All</sup> Follow of A}

Eg:  $E \rightarrow TE'$

given = Follow (E) = { \$, ) }

Follow (T) = { all follow of E }

= { \$, ) }

case III:  $A \rightarrow \alpha B \beta$

$B \rightarrow a | \epsilon$

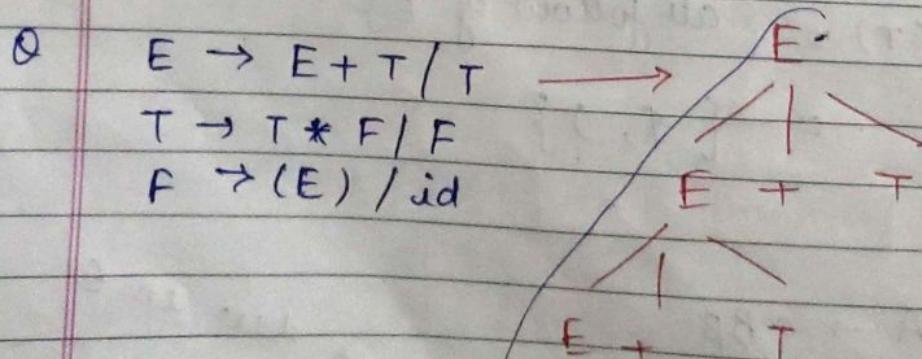
i. Follow (B) = { a, all follow of A } → due to  $\epsilon$

$E \rightarrow TE'$	$E' \rightarrow +TE'/\epsilon$	$T \rightarrow FT'$	$T' \rightarrow *FT'/\epsilon$	$F \rightarrow (E)/id$	first	follow
					$(, id$	$), \$$
					$+, \epsilon$	$), \$$
					$(, id$	$+, ), \$$
					$*, \epsilon$	$+, ), \$$
					$(, id$	$*, +, ), \$$

$S \rightarrow {}^0 E t ss'/a$	$S' \rightarrow eS/\epsilon$	$E \rightarrow b$	first	follow
			${}^0, a$	$e, \$$
			$e, \epsilon$	$e, \$$
			$b$	$t$

$E \rightarrow TQ$	$T \rightarrow FR$	$Q \rightarrow +TQ/-TQ/E$	$R \rightarrow *FR//FR/E$	$F \rightarrow (E)/id$	first	follow
					$(, id$	$), \$, +, -, (, id$
					$(, id$	$+, -, (, id$
					$+,-,(, id$	$), \$$
					$*, /, (, id$	$+, -, (, id$
					$(, id$	$*, /, (, id$

### LL(1) Parser



left  
Recursion

» Eliminating left recursion & left factoring :

left recursion

Eg :  $A \rightarrow A\alpha | B$  general form

After eliminating left recursion  
 $A \rightarrow \beta A'$

$A' \rightarrow \alpha A' | \epsilon$

Compiler can handle right recursion.

but left recursion needs to be removed.

Q

$$E \rightarrow E + T | T$$

$\alpha$        $\beta$

$$\therefore E \rightarrow TE'$$

$$E' \rightarrow +TE' | \epsilon$$

follow(Q),  
follow(R)

Q     $T \rightarrow T * F | F$

eliminating . . .

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' | \epsilon$$

left factoring

Eg :  $S \rightarrow E + T | E * T | E / T$

If compiler wants division, for that it had to open every production as it starts with same E,  $\therefore$  we remove left factoring.

$$S \rightarrow E + T | E * T | E / T$$

$$S \rightarrow ES'$$

$$S' \rightarrow +T | *T | /T$$

General form:  $A \rightarrow \alpha\beta_1 / \alpha\beta_2 / \alpha\beta_3$

then after eliminating left factoring

$$A \rightarrow \alpha A'$$

$$A' \rightarrow \beta_1 / \beta_2 / \beta_3$$

\* LL(1) Parser :

$$w = id + id * id$$

Q  $E \rightarrow E + T / T$

$$T \rightarrow T * F / F$$

$$F \rightarrow (E) / id$$

Step 1: check for left recursion & left factoring.

Eliminating ~~recursion~~ left recursion:

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' / \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' / \epsilon$$

$$F \rightarrow (E) / id$$

Step 2: find first and follow of new grammar.

	first	follow
E	(, id	), \$
E'	+, ε	), \$
T	(, id	+ , ) , \$
T'	* , ε	+ , ) , \$
F	(, id	* , ( + , ) , \$

### Step 3: Parsing Table generation

Non-Terminals	+	*	id	(	)	\$
E			$E \rightarrow TE'$	$E \rightarrow TE'$		
E'	$E' \rightarrow +TE'$					$E' \rightarrow E$
T			$T \rightarrow FT'$	$T \rightarrow FT'$		$E \rightarrow E$
T'	$T' \rightarrow E$	$T' \rightarrow *FT'$				$E \rightarrow E$
F			$F \rightarrow id$	$F \rightarrow (E)$	$T' \rightarrow E$	$T' \rightarrow \epsilon$

### Step 4: Stack Implementation

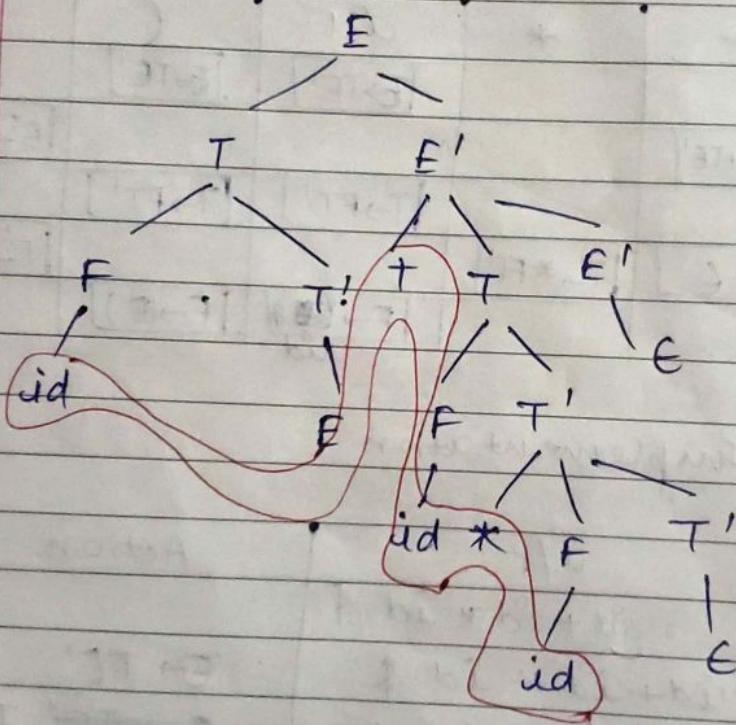
root in case of Top-down

Stack	u/p	Action
$E \$$	$id + id * id \$$	
$TE' \$$	$id + id * id \$$	$E \rightarrow TE'$
$FT'E' \$$	$id + id * id \$$	<del><math>E \rightarrow TE'</math></del> $T \rightarrow FT'$
$id T'E' \$$	$id + id * id \$$	$F \rightarrow id$
$T'E' \$$	$+ id * id \$$	<del><math>F \rightarrow id</math></del>
$E' \$$	$+ id * id \$$	$T' \rightarrow E$
$*TE' \$$	$* id * id \$$	$E' \rightarrow +TE'$
$TE' \$$	$id * id \$$	
$FT'E' \$$	$id * id \$$	$T \rightarrow FT'$
$id T'E' \$$	$* id \$$	$F \rightarrow id$
$T'E' \$$	$* id \$$	$T' \rightarrow *FT'$
$*FT'E' \$$	$* id \$$	

FT' E' \$  
 id T' E' \$  
 T' E' \$  
 E' \$  
 \$

id \$  
 id \$  
 \$  
 \$  
 \$

$F \rightarrow id$   
~~please~~  
~~E' \rightarrow T' E~~  
 $E' \rightarrow \epsilon$



Action Top - down

Q Solve the grammar using LL(1) parser.

$S \rightarrow A$

$A \rightarrow aB / Ad$

$B \rightarrow b$

$C \rightarrow g$

$w = abd$

Step ① : Eliminating left recursion :

$$\begin{aligned}
 S &\rightarrow A \\
 A &\rightarrow aBA' \\
 A' &\rightarrow dA' / \epsilon \\
 B &\rightarrow b \\
 C &\rightarrow g
 \end{aligned}$$

Step ②: first and follow :

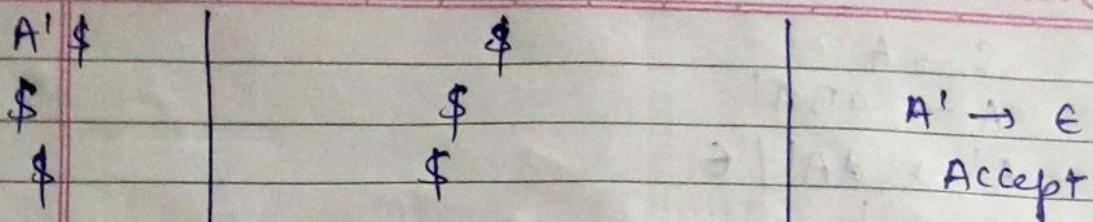
	first	follow
S	a	\$
A	a	\$
A'	d, $\epsilon$	\$
B	b	d, \$
C	g	NA

Step ③: Parse Table :

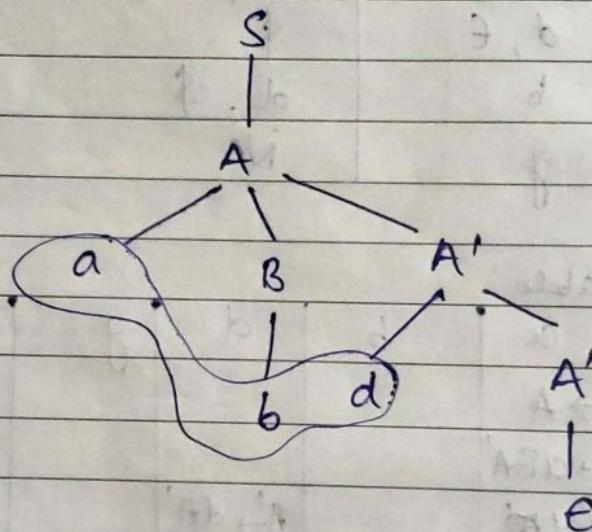
	a	b	d	g	\$
S	$S \rightarrow A$				
A	$A \rightarrow aBA'$				
A'	<del><math>A' \rightarrow dA'</math></del>		$A' \rightarrow dA'$		$A' \rightarrow \epsilon$
B		$B \rightarrow b$			
C				$C \rightarrow g$	

Step ④: Stack Implementation :

Stack	input string	Action
S \$	abd \$	
A \$	abd \$	<del>A</del> $S \rightarrow A$
aBA' \$	abd \$	<del>A</del> $A \rightarrow aBA'$
BA' \$	bd \$	
BA' f	b d \$	$B \rightarrow b$
A' f	d f	
A' f	d f	$A' \rightarrow dA'$



step 5: Parse Tree



Q Check whether the given grammar is LL(1) or not.

$$\begin{aligned} S &\rightarrow {}^0E \pm s \quad / \quad {}^1E \pm s \quad / \quad a \\ E &\rightarrow b \end{aligned}$$

step 0: Eliminating left ~~recursion~~ factoring.

$$\begin{aligned} S &\rightarrow {}^0E \pm s \quad / \quad a \\ S' &\rightarrow es \quad / \quad \epsilon \quad \because S \rightarrow {}^0E \pm s \\ E &\rightarrow b \quad \text{nothing left} \therefore \epsilon \end{aligned}$$

Step ②:

	first	follow
S	a, $\epsilon$	e, \$
S'	e, $\epsilon$	e, \$
E	b	t

Step ③: Parsing Table

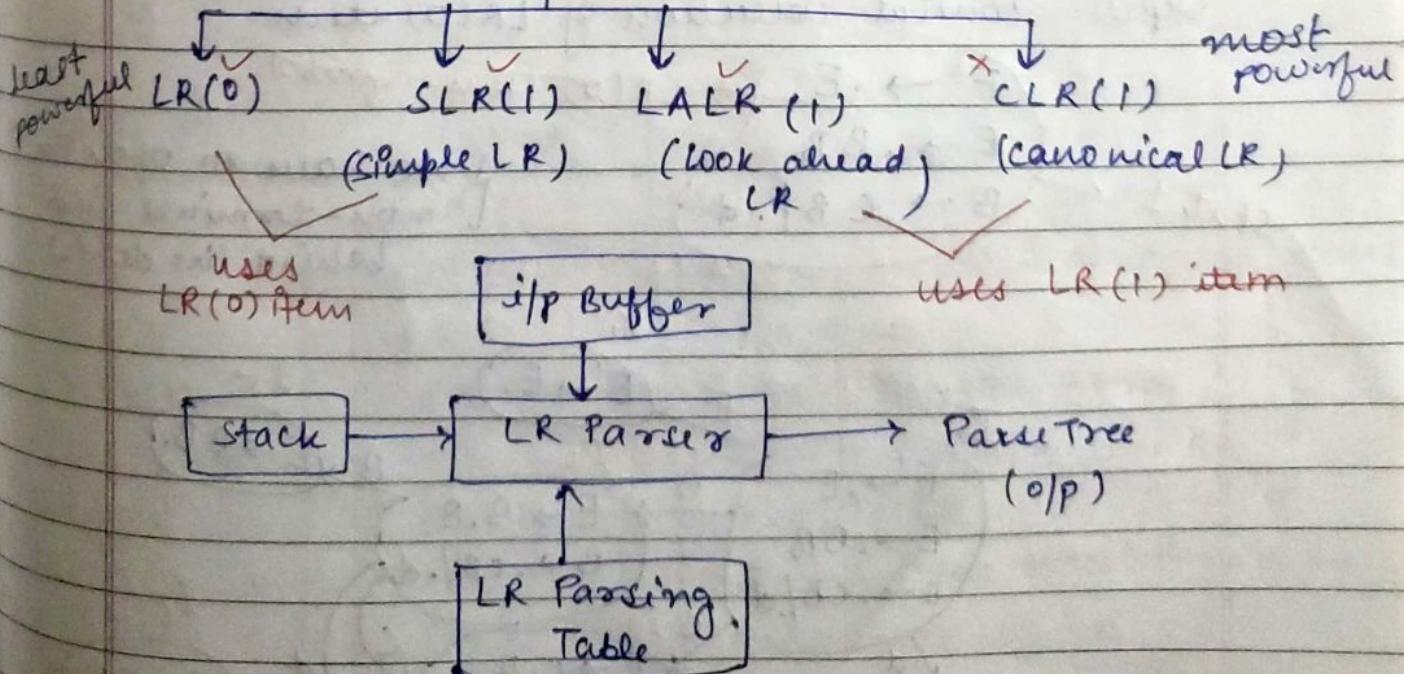
	a	b	c	$\epsilon^0$	t	\$
S	$S \rightarrow a$					
S'				$S' \xrightarrow{S \rightarrow \epsilon S}$		
E		$E \rightarrow b$	$S' \xrightarrow{S \rightarrow \epsilon}$			$S' \xrightarrow{S \rightarrow \epsilon}$

∴ The grammar is not LL(1) because there are more than one production in S'.

### \* Bottom-up Parser

#### LR Parser

LR → construction of right most derivation in reverse  
 left to right scanning of i/p stream



\* LR(0) :

» Steps to solve LR(0) sums :

1. Augment the given grammar (self-created grammar)
2. Draw conical collection of LR(0) item
3. Number the production.
4. Create the Parsing Table.
5. Stack implementation.
6. Draw Parse Tree.

Eg1:  $E \rightarrow BB$  if  $p = ccd\$\bar{}$   
 $B \rightarrow CB/d$

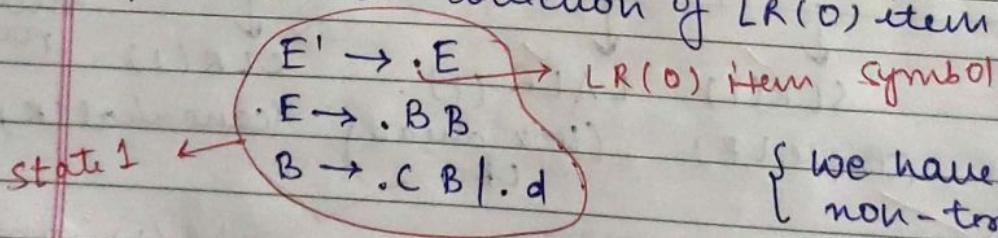
Step ① : Augment grammar.

$$E' \rightarrow E$$

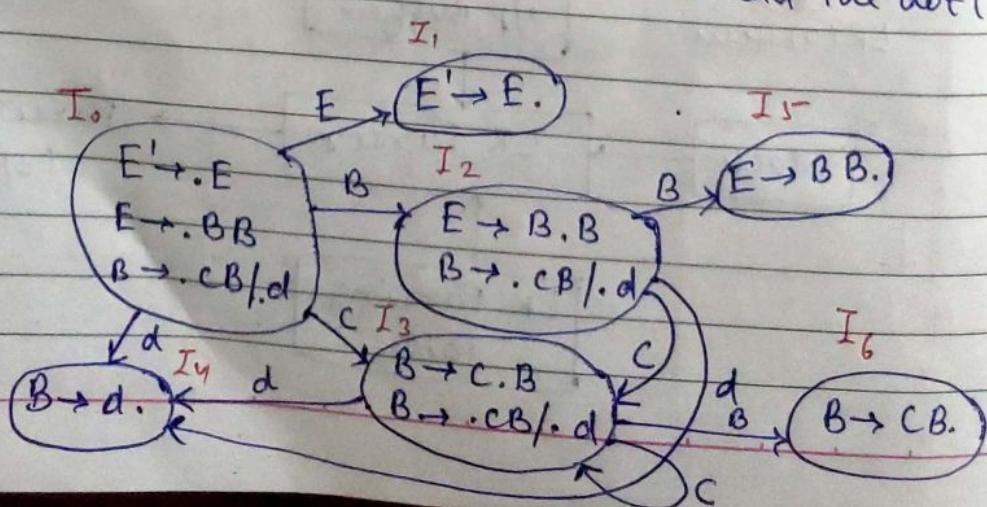
$$E \rightarrow BB$$

$$B \rightarrow CB/d$$

Step ②: conical collection of LR(0) item



{ we have to open the non-terminal just behind the dot(.) }



Step 3: Number the Production

$$E' \rightarrow E$$

$$E \rightarrow BB \quad ①$$

$$B \rightarrow cB \quad | \quad d \quad ② \quad ③$$

Step 4: Parsing Table

Terminals

Non-Terminals

State	Action			Goto	
	c	d	\$	E	B
I <sub>0</sub>	S <sub>3</sub>	S <sub>4</sub>	(self-created)	1	2
I <sub>1</sub>	<del>S<sub>3</sub></del>	<del>S<sub>4</sub></del>	Accept		
I <sub>2</sub>	S <sub>3</sub>	S <sub>4</sub>			5
I <sub>3</sub>	S <sub>3</sub>	S <sub>4</sub>			6
I <sub>4</sub>	r <sub>3</sub>	r <sub>3</sub>	r <sub>3</sub>		
I <sub>5</sub>	r <sub>1</sub>	r <sub>1</sub>	r <sub>1</sub>		
I <sub>6</sub>	r <sub>2</sub>	r <sub>2</sub>	r <sub>2</sub>		

Step 5: stack implementation

stack first state	input	Action
\$0	ccdd \$	shift c in stack and goto state 3
\$0C3	cdd \$	shift c in stack and goto state 3
\$0C3C3	dd \$	Shift d in " & " S4.
\$0C3C3d4	d \$	Reduce r <sub>3</sub> i.e. B → d
\$0C3C3B6	d \$	Reduce r <sub>2</sub> i.e. B → CB
\$0C3B6	d \$	Reduce r <sub>2</sub> i.e. B → CB
\$0B2	d \$	Shift d in stack & goto S4.
\$0B2d4	\$	Reduce r <sub>3</sub> i.e. B → d
\$0B2B5	\$	Reduce r <sub>1</sub> i.e. E → BB

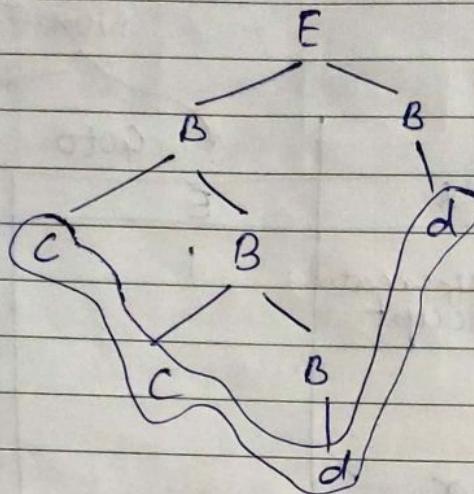
\$ O E I

\$

Accept

↑ Bottom  
up

Step ①: Parse Tree



Eg 2: grammar:

$$S \rightarrow AA$$

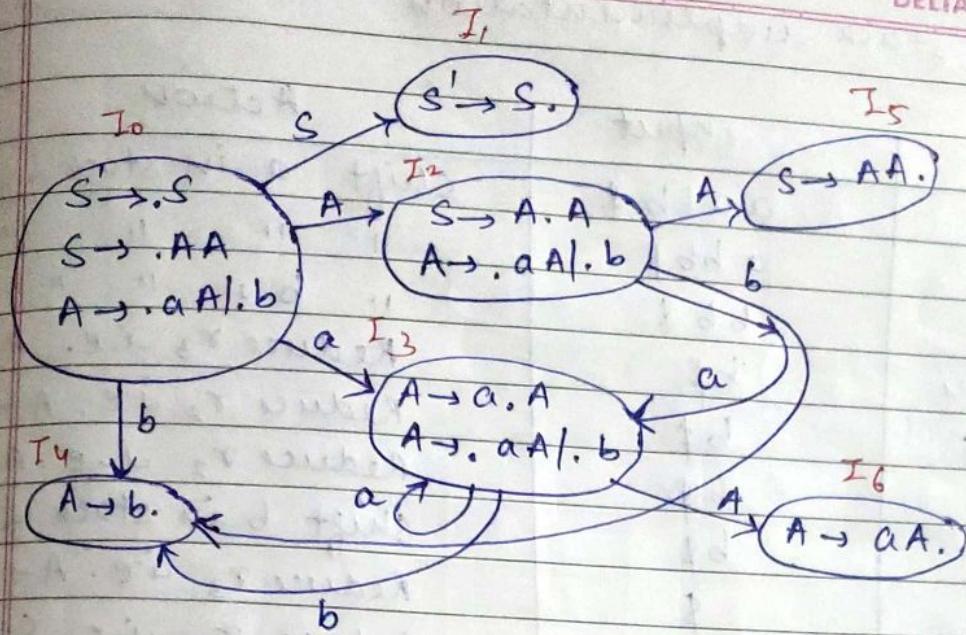
$$A \rightarrow aA \mid b$$

Step ①: Augment grammar

- $S' \rightarrow S$
- $S \rightarrow AA$
- $A \rightarrow aA \mid b$

Step ②: Canonical collection of LR(0) items:

- $S' \rightarrow .S$
- $S \rightarrow .AA$
- $A \rightarrow ,aA \mid .b$



Step ③: Number the production.

$$\begin{aligned}
 &S' \rightarrow S \\
 &S \rightarrow AA \quad ① \\
 &A \rightarrow AA \quad / \quad b \\
 &\quad ② \quad ③
 \end{aligned}$$

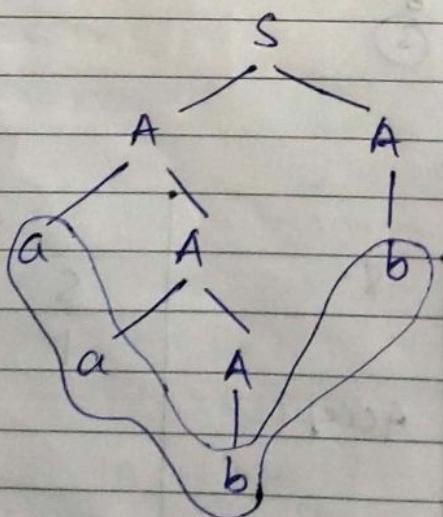
Step ④: Parsing Table

State	Action			Goto	
	a	b	\$	S	A
I <sub>0</sub>	s <sub>3</sub>	s <sub>4</sub>		1	2
I <sub>1</sub>			Accept		
I <sub>2</sub>	s <sub>3</sub>	s <sub>4</sub>			5
I <sub>3</sub>	s <sub>3</sub>	s <sub>4</sub>	.		6
I <sub>4</sub>	r <sub>3</sub>	r <sub>3</sub>	r <sub>3</sub>		
I <sub>5</sub>	r <sub>1</sub>	r <sub>1</sub>	r <sub>1</sub>		
I <sub>6</sub>	r <sub>2</sub>	r <sub>2</sub>	r <sub>2</sub>		

## Step ⑤ : stack implementation

Stack	input	Action
\$ 0	a a bb \$	shift a in stack & goto S <sub>3</sub>
\$ 0 a 3	a bb \$	" " "
\$ 0 a 3 a 3	bb \$	" b \$ "
\$ 0 a 3 a 3 b 4	b \$	Reduce r <sub>3</sub> i.e. A → b
\$ 0 a 3 a 3 A 6	b \$	Reduce r <sub>2</sub> i.e. A → AA
\$ 0 a 3 A 6	b \$	Reduce r <sub>2</sub> i.e. A → AA
\$ 0 A 2	b \$	Shift b in stack & goto S <sub>4</sub>
\$ 0 A 2 b 4	\$	Reduce r <sub>3</sub> i.e. A → b
\$ 0 A 2 A 5	\$	Reduce r <sub>1</sub> i.e. S → AA
\$ 0 S 1	\$	Accept

## Step ⑥: Parse Tree



\* SLR (1)

Same steps as LR(0)  
only difference in parsing Table.

### Eg 1 of LR(0)

$$\begin{aligned} E' &\rightarrow E \\ E &\rightarrow BB \\ B &\rightarrow CB/d \end{aligned}$$

Date \_\_\_\_\_  
DELTA Pg No. \_\_\_\_\_

state	Action	goto
$I_0$	c	
$I_1$	d	
$I_2$	$s_3$	
$I_3$	$s_3$	
$I_4$	$s_3$	Accept
$I_5$	$r_3$	
$I_6$	$r_2$	
		$E$
		$B$
		1
		2
		5
		6

$I_4 \quad B \rightarrow d$

$\text{follow}(B) = c, d, \epsilon \text{ i.e } \$$

$I_5 \quad E \rightarrow BB$

$\text{follow}(E) = \$$

$I_6 \quad B \rightarrow CB$

$\text{follow}(B) = c, d, \$$

Q Why SLR(1) is used? → To remove or minimize these two conflicts to an extent.

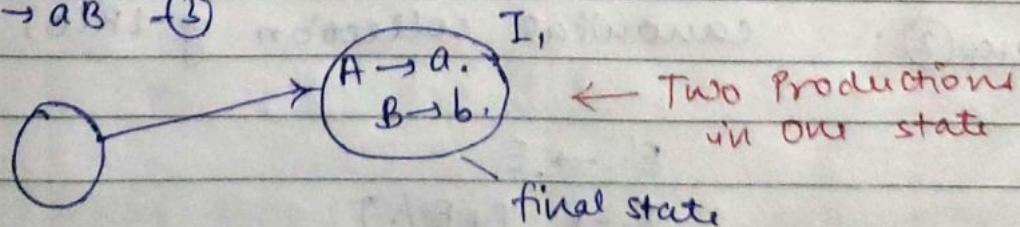
conflict :-

① RR (reduce reduce)

$$A \rightarrow a \quad \textcircled{1}$$

$$B \rightarrow b \quad \textcircled{2}$$

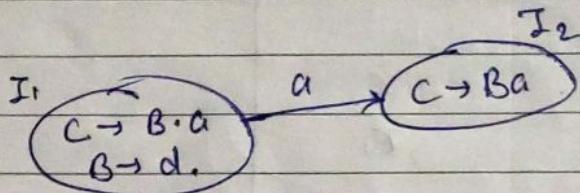
$$C \rightarrow aB \quad \textcircled{3}$$



state	Action	goto
$I_1$	a      b      \$	$r_1/r_2$ $r_1/r_2$ $r_1/r_2$

## (2) SR (shift reduce)

$$\begin{array}{l} C \rightarrow Ba - (1) \\ B \rightarrow d - (2) \end{array}$$



state	Action	Goto	
	a	d	\$
I <sub>1</sub>	s <sub>2</sub> / s <sub>2</sub>	r <sub>2</sub>	r <sub>2</sub>

↓  
 B → d      ↓  
 B → d

Eg: Check whether the (i) grammar is LR(0) or not, (ii) grammar is SLR(1) or not.

$$E \rightarrow T + E / T$$

$$T \rightarrow i$$

Sol:- Step (1): Augment grammar

$$E' \rightarrow E$$

$$E \rightarrow T + E / T$$

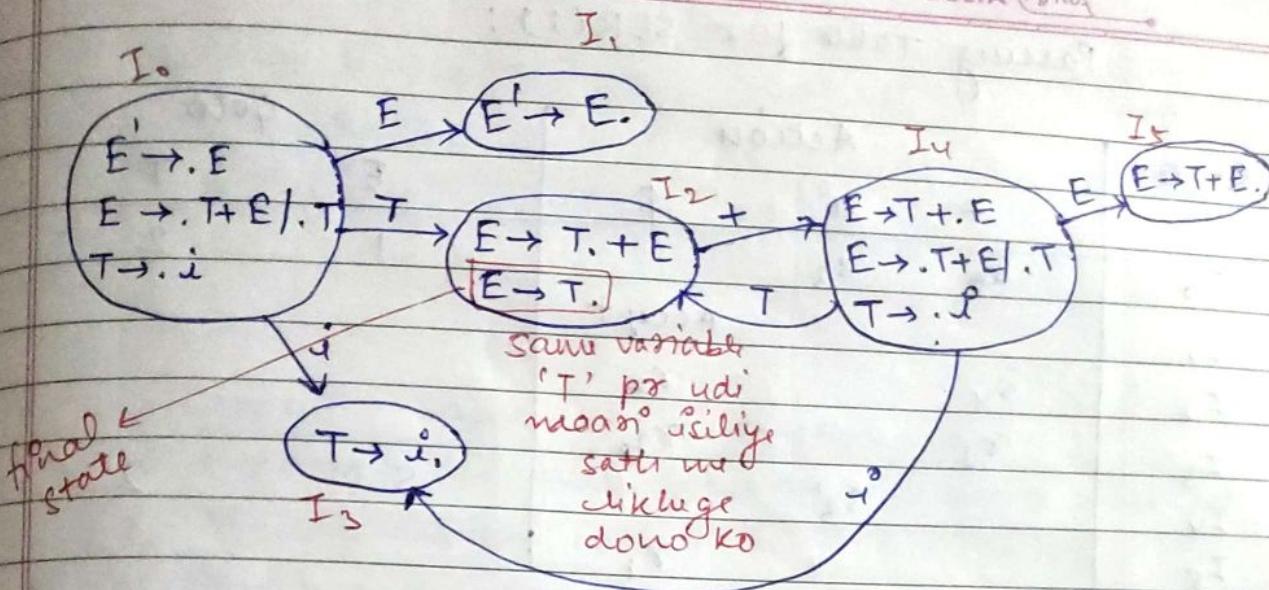
$$T \rightarrow i$$

Step (2): Canonical collection of LR(0) items:

$$E' \rightarrow .E$$

$$E \rightarrow .T + E / .T$$

$$T \rightarrow .i$$



Step ③ : Number the productions.

$$\begin{aligned} E' &\rightarrow E \quad ① \\ E &\rightarrow T+E|T \quad ② \\ T &\rightarrow i \quad ③ \end{aligned}$$

Step ④: Parsing Table

State	Action	Goto	
	$\epsilon$ + \$	E	T
I <sub>0</sub>	s <sub>3</sub>	1	2
I <sub>1</sub>	Accept		
I <sub>2</sub>	s <sub>4/r<sub>2</sub></sub>	r <sub>2</sub>	
I <sub>3</sub>	r <sub>3</sub>	r <sub>3</sub>	
I <sub>4</sub>	s <sub>3</sub>	5	2
I <sub>5</sub>	r <sub>1</sub>	r <sub>1</sub>	

state I<sub>2</sub> has two productions, i.e., grammar is not LR(0).

### Parsing Table for SLR(1) :

State	Action			Goto	
	+	$\cdot^0$	$\cdot^f$	E	T
I <sub>0</sub>	s <sub>2</sub>	s <sub>3</sub>		1	2
I <sub>1</sub>			Accept		
I <sub>2</sub>	s <sub>4</sub>		r <sub>2</sub>		
I <sub>3</sub>		r <sub>3</sub>	r <sub>3</sub>		
I <sub>4</sub>		s <sub>3</sub>		5	
I <sub>5</sub>			r <sub>1</sub>		2

Given  
 $\therefore$  Grammar is SLR(1) as it does not contain two productions for one state.



LR(0)  $\rightarrow$  Put reduce in full row

SLR(1)  $\rightarrow$  Put reduce in follow of P

CLR(1)

and LALR(1)  $\rightarrow$  Put reduce only on lookahead

LR(0)  $\overset{\text{item}}{\sim} = (\cdot)$  dot production

LR(1) item = LR(0) item + Look ahead

\* How to find Lookahead :-

Eg:  $E \rightarrow BB$

$B \rightarrow CB/d$

Step ①: Augment grammar and writing LR(1) item.

$E' \rightarrow .E, \$$  → Lookahead of start symbol (augmented grammar)

Jis prod? →  $E \rightarrow .BB, \$$   
 ko humne →  $B \rightarrow .CB/d, c/d$

open kr rhe

hai, use k

bad jo b

hai uska

first w?

Lookahead

wala.

\* Steps to solve LR(1) items sum:

1. Augment the given grammar & write with lookahead
2. Draw canonical collection of LR(1) item
3. Number the prod<sup>2</sup>.
4. Draw Parsing Table.
5. Stack Implementation.
6. Parse Tree

Eg:

$$E \rightarrow BB$$

$$B \rightarrow CB/d$$

### CLR(1)

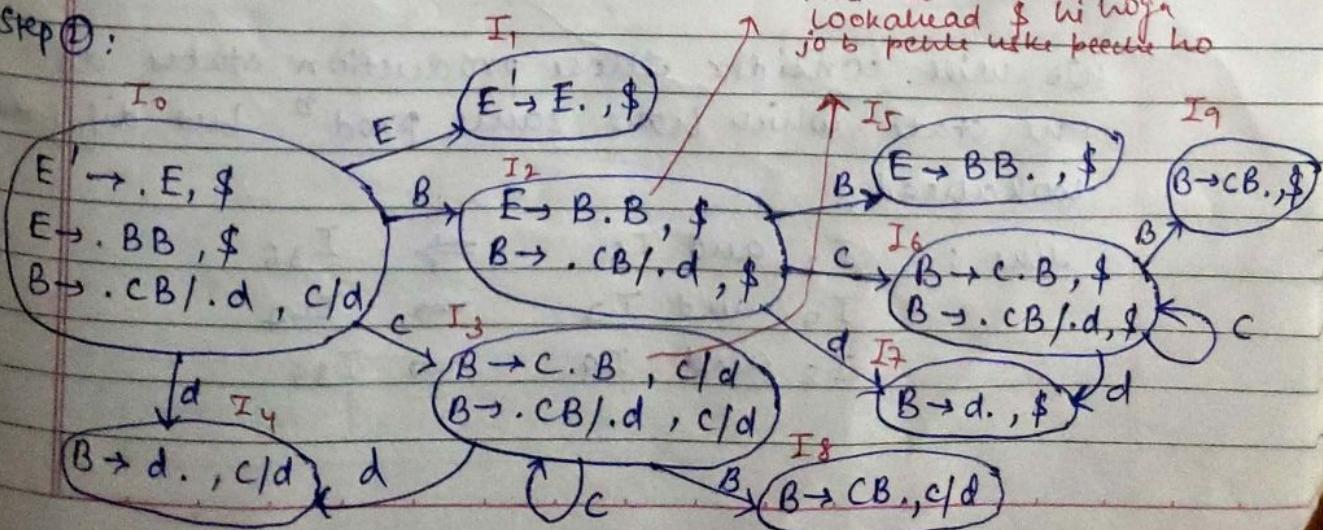
Step ①

$$E' \rightarrow .E, \$$$

$$E \rightarrow .BB, \$$$

$$B \rightarrow .CB/.d, c/d$$

Step ②:



Step ③ :

$$E' \rightarrow E$$

$$E \rightarrow BB \quad ①$$

$$B \rightarrow CB / d \quad ② \quad ③$$

Step ④ :

State	Action			Goto	
	c	d	\$	E	B
I <sub>0</sub>	s <sub>3</sub>	s <sub>4</sub>			1
I <sub>1</sub>			Accept		2
I <sub>2</sub>	s <sub>6</sub>	s <sub>7</sub>			5
I <sub>3</sub>	s <sub>3</sub>	s <sub>4</sub>			8
I <sub>4</sub>	r <sub>3</sub>	r <sub>3</sub>			
I <sub>5</sub>			r <sub>1</sub>		
I <sub>6</sub>	s <sub>6</sub>	s <sub>7</sub>			9
I <sub>7</sub>			r <sub>3</sub>		
I <sub>8</sub>	r <sub>2</sub>	r <sub>2</sub>			
I <sub>9</sub>			r <sub>2</sub>		

reduce comes only in look ahead in CLR(1).

### \* LALR(1)

We will consider those production states as one state which have same prod<sup>n</sup> but different lookahead.

$$\text{like : } I_3 \text{ and } I_6 \Rightarrow I_{36}$$

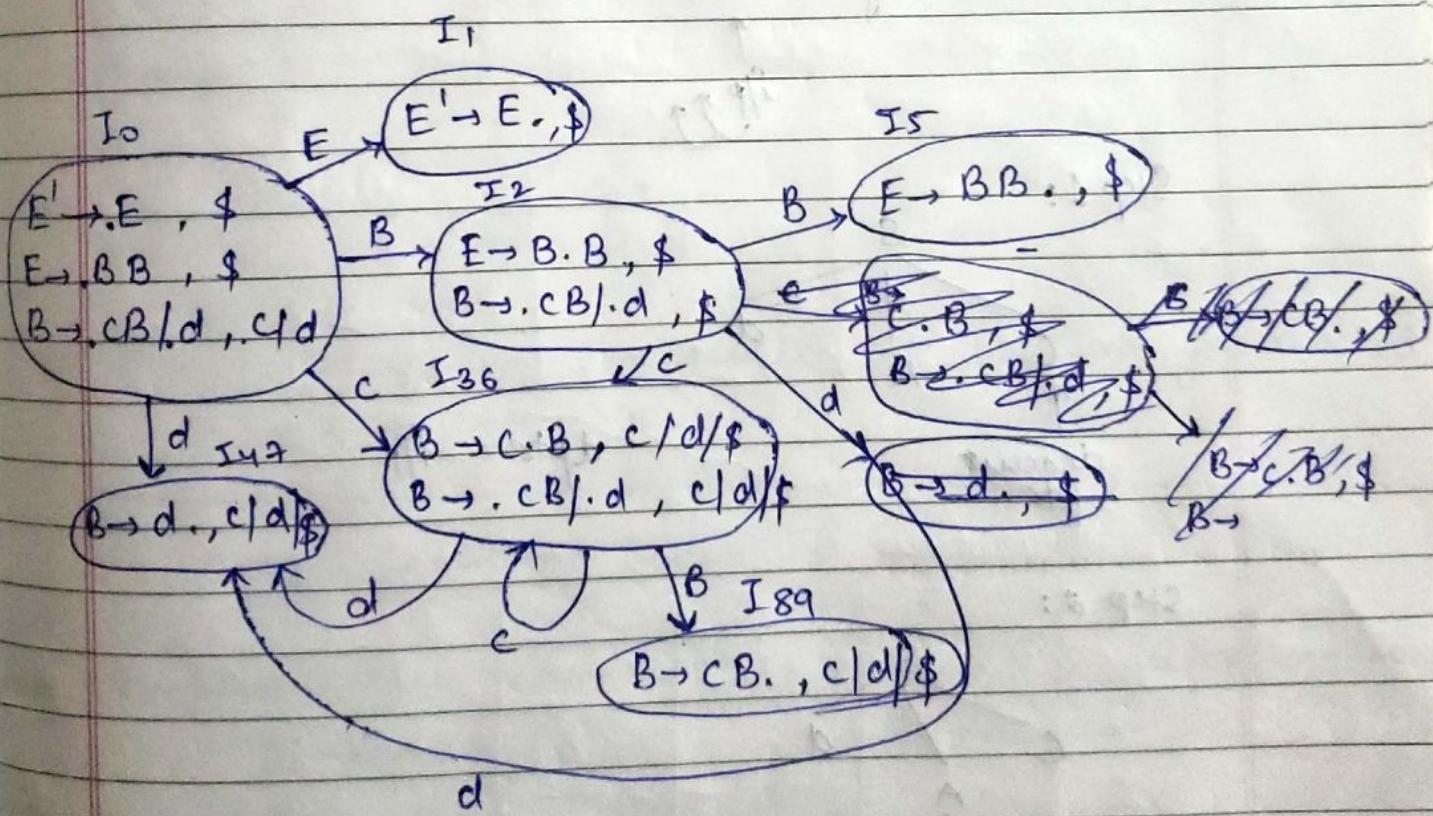
$$I_4 \text{ and } I_7 \Rightarrow I_{47}$$

$$I_8 \text{ and } I_9 \Rightarrow I_{89}$$

## Parsing Table for LALR(1) :

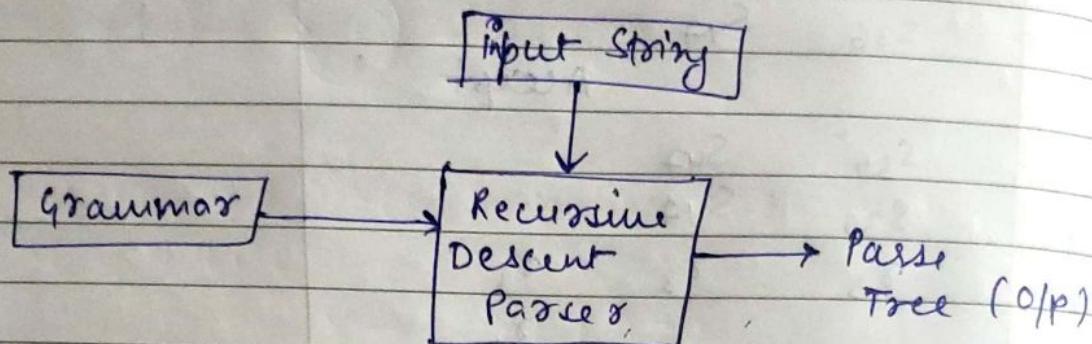
State	Action			Goto
	c	d	\$	
I <sub>0</sub>	S <sub>36</sub>	S <sub>47</sub>	Accept	E I 1
I <sub>1</sub>	S <sub>36</sub>	S <sub>47</sub>		B 2 5
I <sub>2</sub>	S <sub>36</sub>	S <sub>47</sub>		89
I <sub>36</sub>	r <sub>3</sub>	r <sub>3</sub>	r <sub>3</sub>	
I <sub>43</sub>		r <sub>3</sub>	r <sub>1</sub>	
I <sub>5</sub>		r <sub>2</sub>	r <sub>2</sub>	
I <sub>89</sub>		r <sub>2</sub>	r <sub>2</sub>	

Reductions merge



\* Recursive Descent Parsing ;

Recursive Descent Parsing is one of top-down parsing techniques that uses a set of recursive procedures to scan its input. May involve backtracking.

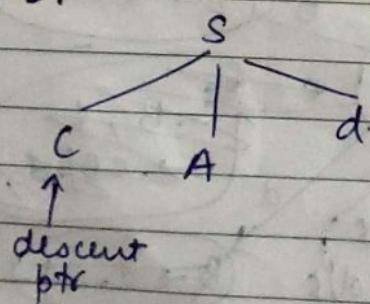


Eg :  $S \rightarrow cAd$

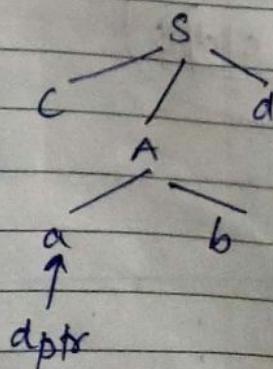
$A \rightarrow ab/a$

i/p string = cad  
 ↑  
 i/p →

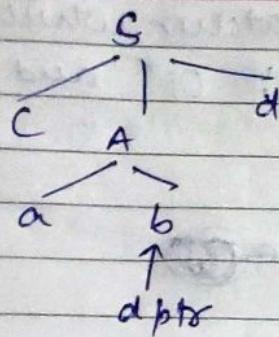
Step 1:



Step 2:



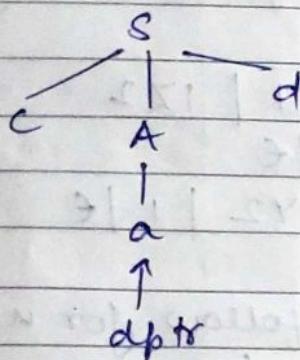
Step 3:



$dptr \neq i/p$

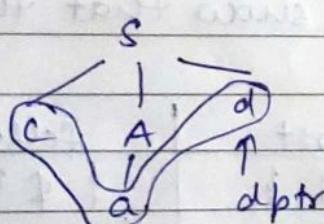
∴ Backtracks

Step 4:



$dptr = i/p$

Step 5:



∴ string matches , Parse Tree generated.

### 2018 Sessional Paper

Q Improve the grammar by removing left recursion.

$$S \rightarrow AAB \mid b$$

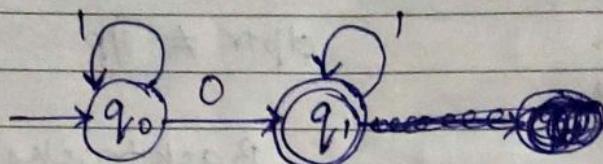
$$A \rightarrow Aab \mid Aba \mid a$$

$$B \rightarrow a$$

$$\left\{ \begin{array}{l} S \rightarrow AabB \mid b \\ A \rightarrow aA' \\ A' \rightarrow abA' \mid \epsilon \mid baA' \\ B \rightarrow a \end{array} \right.$$

$A \rightarrow A\alpha \mid B$ $A \rightarrow Aba/a$ $A \rightarrow aA'$ $A' \rightarrow baA'/\epsilon$	$A \rightarrow BA'$ $A' \rightarrow \alpha A'/\epsilon$
--	--

- a) Generate a pattern matcher which can recognise following two patterns :  $01^*$  and  $1^*0$ .



- b) Consider the follow. grammar given below  
 $\epsilon = \text{NULL}$ .

$$\begin{aligned} X &\rightarrow 0Y1 \mid 1Z2 \\ Y &\rightarrow 2 \mid \epsilon \\ Z &\rightarrow 1Y2 \mid 1 \mid \epsilon \end{aligned}$$

- a) calculate first & follow for non-terminals.  
 b) create a predictive parsing table for above grammar. Also show that this grammar is not LL(1).

	first	follow
X	{0, 1}	{\\$}
Y	{2, \epsilon}	{1, 2}
Z	{1, \epsilon}	{2}

b) Predictive

	0	1	2	\$
X	$X \rightarrow 0Y1$	$X \rightarrow 1Z2$		
Y			$Y \rightarrow 2$	$Y \rightarrow \epsilon$
Z		$Z \rightarrow 1Y2$	$Z \rightarrow \epsilon$	

∴ it is not LL(1) grammar.

Q consider the grammar

$$S \rightarrow L = R \mid R$$

$$L \rightarrow *R \mid id$$

$$R \rightarrow L$$

design LALR Parser for this grammar

Sol: step 1: Augment grammar

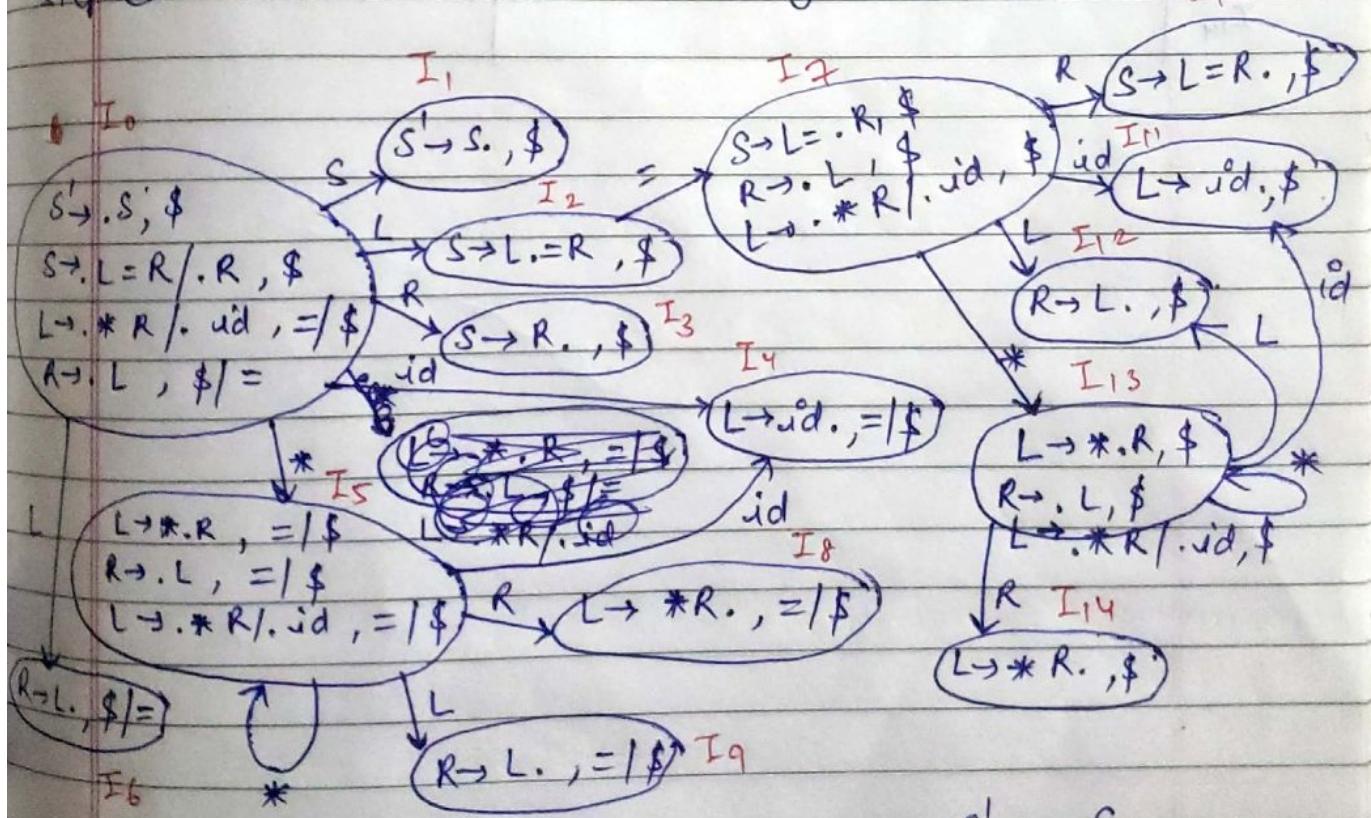
$$S' \rightarrow .S, \$$$

$$S \rightarrow .L = R \mid .R, \$$$

$$L \rightarrow .*R \mid .id, = \mid \$$$

$$R \rightarrow .L, \$ \mid =$$

Step ②: canonical collection of LR(0) item :  $I_{1,0}$



Step ③:

$$\begin{aligned} S' &\rightarrow .S \\ S &\rightarrow .L = R \mid .R \\ S &\rightarrow .*R \mid .id \\ R &\rightarrow .L \end{aligned}$$