

Let us suppose s_A, s_B, s_{AB}, s_0 denote the supply & $d_A, d_B, d_{AB}, d_0 \rightarrow$ demand.

We can construct our graph $G = (V, E)$ as follows

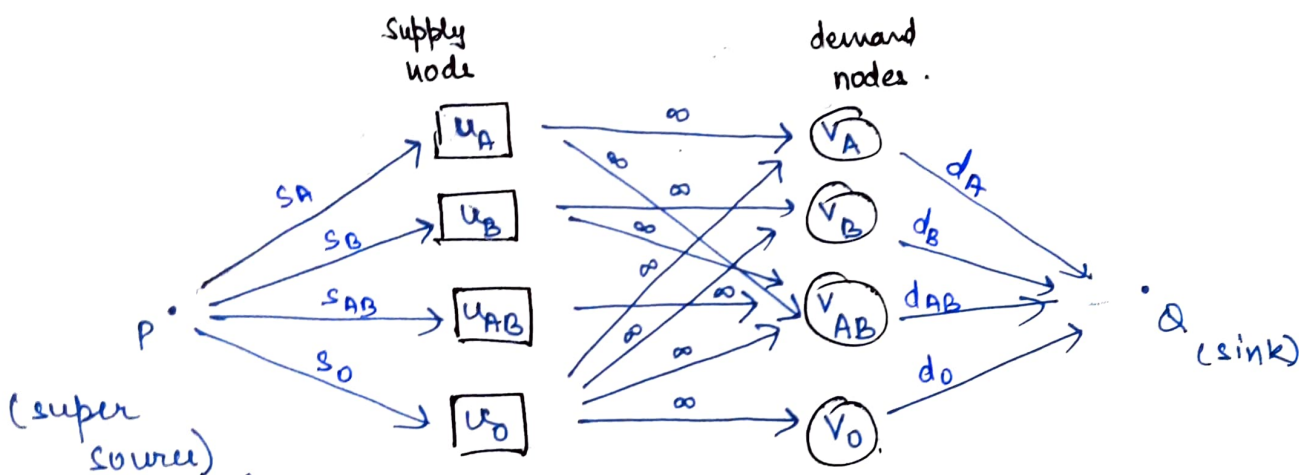
Vertices

1. One super source and one super sink (P and Q resp.)
2. 4 supply nodes (u_A, u_B, u_{AB}, u_0) & 4 demand nodes (v_A, v_B, v_{AB}, v_0)

Edges

1. $(P, u_i) \in E$ $\text{cap}(P, u_i) = s_i$ where $i \in \{A, B, AB, 0\}$
2. $(v_i, Q) \in E$ $\text{cap}(v_i, Q) = d_i$ where $i \in \{A, B, AB, 0\}$
3. $(u_i, v_j) \in E$ where type j can receive from type i $\text{cap}(u_i, v_j) = \infty$

The graph can be visualised as: :-



GRAPH G .

Our problem is to evaluate if current supply would suffice for projected demand. Thus

Theorem ~~There~~ The current supply is sufficient for projected demand if and only if edges from demand node to sink are all saturated (ie. $f(e) = c(e)$, for $e \in (k, Q)$ in the resulting max-flow of graph G .)

$f(e)$ = flow of edge e
 $c(e)$ = cap of edge e
 $Q \rightarrow$ sink node.