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#### **Parsing**

- Process of determination whether a string can be generated by a grammar
- Parsing falls in two categories:
  - Top-down parsing:
     Construction of the parse tree starts at the root (from the start symbol) and proceeds towards leaves (token or terminals)
  - Bottom-up parsing:
     Construction of the parse tree starts from the leaf nodes (tokens or terminals of the grammar) and proceeds towards root (start symbol)

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#### Bottom up parsing

- Construct a parse tree for an input string beginning at leaves and going towards root OR
- Reduce a string w of input to start symbol of grammar Consider a grammar

 $S \rightarrow aABe$   $A \rightarrow Abc \mid b$  $B \rightarrow d$ 

And reduction of a string order.

a <u>b</u> b c d e a <u>A b c</u> d e a A <u>d</u> e <u>a A B e</u> S The sentential forms happen to be a *right most derivation in the reverse* 

S → a A <u>B</u> e

**→** a <u>A</u> d e

**→** a <u>A</u> b c d e

→ a b b c d e

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# Shift reduce parsing

- Split string being parsed into two parts
  - Two parts are separated by a special character "."
  - Left part is a string of terminals and non terminals
  - Right part is a string of terminals
- Initially the input is .w

# Shift reduce parsing ...

- Bottom up parsing has two actions
- Shift: move terminal symbol from right string to left string
   if string before shift is α.pqr
   then string after shift is αp.qr

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# Shift reduce parsing ...

 Reduce: immediately on the left of "." identify a string same as RHS of a production and replace it by LHS

if string before reduce action is  $\alpha\beta$ .pqr and  $A \rightarrow \beta$  is a production then string after reduction is  $\alpha A$ .pqr

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# Example

Assume grammar is  $E \rightarrow E+E \mid E*E \mid id$ Parse id\*id+id

Assume an oracle tells you when to shift / when to reduce

• •	c an oracic tens you w	men to simil, which to
	String	action (by oracle)
	.id*id+id	shift
	id.*id+id	reduce E→id
	E.*id+id	shift
	E*.id+id	shift
	E*id.+id	reduce E→id
	E*E.+id	reduce E→E*E
	E.+id	shift
	E+.id	shift
	E+id.	Reduce E→id
	E+E.	Reduce E→E+E
	E.	ACCEPT

# Shift reduce parsing ...

- Symbols on the left of "." are kept on a stack
  - Top of the stack is at "."
  - Shift pushes a terminal on the stack
  - Reduce pops symbols (rhs of production) and pushes a non terminal (lhs of production) onto the stack
- The most important issue: when to shift and when to reduce
- Reduce action should be taken only if the result can be reduced to the start symbol

# Issues in bottom up parsing

- How do we know which action to take
  - -whether to shift or reduce
  - –Which production to use for reduction?
- Sometimes parser can reduce but it should not:
  - X→€ can always be used for reduction!

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# Issues in bottom up parsing

- Sometimes parser can reduce in different ways!
- Given stack δ and input symbol a, should the parser
  - -Shift a onto stack (making it  $\delta a$ )
  - -Reduce by some production  $A \rightarrow \beta$  assuming that stack has form  $\alpha\beta$  (making it  $\alpha A$ )
  - -Stack can have many combinations of  $\alpha\beta$
  - How to keep track of length of  $\beta$ ?

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## **Handles**

- The basic steps of a bottom-up parser are
  - to identify a substring within a rightmost sentential form which matches the RHS of a rule.
  - when this substring is replaced by the LHS of the matching rule, it must produce the previous rightmost-sentential form.
- Such a substring is called a *handle*

#### Handle

- A *handle* of a right sentential form γ is
  - a production rule  $A \rightarrow \beta$ , and
  - an occurrence of a sub-string  $\beta$  in  $\gamma$

#### such that

• when the occurrence of  $\beta$  is replaced by A in  $\gamma$ , we get the previous right sentential form in a rightmost derivation of  $\gamma$ .

#### Handle

Formally, if

 $S \rightarrow^{rm^*} \alpha Aw \rightarrow^{rm} \alpha \beta w$ .

then

- $\beta$  in the position following  $\alpha$ ,
- and the corresponding production  $A \rightarrow \beta$  is a handle of  $\alpha\beta w$ .
- The string w consists of only terminal symbols

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#### Handle: Observation

- Only terminal symbols can appear to the right of a handle in a rightmost sentential form.
- Why?

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#### Handle

- We only want to reduce handle and not any RHS
- Handle pruning: If  $\beta$  is a handle and  $A \rightarrow \beta$  is a production then replace  $\beta$  by A
- A right most derivation in reverse can be obtained by handle pruning.

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#### Handle: Observation

Is this scenario possible:

- $\alpha\beta\gamma$  is the content of the stack
- $A \rightarrow \gamma$  is a handle
- The stack content reduces to  $\alpha \beta A$
- Now B  $\rightarrow \beta$  is the handle

In other words, handle is not on top, but buried *inside* stack

Not Possible! Why?

#### Handles ...

 Consider two cases of right most derivation to understand the fact that handle appears on the top of the stack

$$S \rightarrow \alpha Az \rightarrow \alpha \beta Byz \rightarrow \alpha \beta \gamma yz$$
  
 $S \rightarrow \alpha BxAz \rightarrow \alpha Bxyz \rightarrow \alpha \gamma xyz$ 

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#### **Shift Reduce Parsers**

- The general shift-reduce technique is:
  - if there is no handle on the stack then shift
  - If there is a handle then reduce
- Bottom up parsing is essentially the process of detecting handles and reducing them.
- Different bottom-up parsers differ in the way they detect handles.

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#### Handle always appears on the top

Case I:  $S \rightarrow \alpha Az \rightarrow \alpha \beta Byz \rightarrow \alpha \beta \gamma yz$ stack input action  $\alpha \beta \gamma$  yz reduce by  $B \rightarrow \gamma$   $\alpha \beta B$  yz shift y  $\alpha \beta By$  z reduce by  $A \rightarrow \beta By$ 

Case II:  $S \rightarrow \alpha B x A z \rightarrow \alpha B x y z \rightarrow \alpha \gamma x y z$ 

stackinputaction $\alpha \gamma$ xyzreduce by  $B \rightarrow \gamma$  $\alpha B$ xyzshift x $\alpha Bx$ yzshift y $\alpha Bxy$ zreduce  $A \rightarrow y$  $\alpha BxA$ z

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#### **Conflicts**

- What happens when there is a choice
  - What action to take in case both shift and reduce are valid?

shift-reduce conflict

–Which rule to use for reduction if reduction is possible by more than one rule?

reduce-reduce conflict

#### **Conflicts**

 Conflicts come either because of ambiguous grammars or parsing method is not powerful enough

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#### Shift reduce conflict

Consider the grammar  $E \rightarrow E+E \mid E^*E \mid id$ and the input id+id\*id

stack	input	action
E+E	*id	reduce by $E \rightarrow E + E$
E	*id	shift
E*	id	shift
E*id		reduce by E→id
E*E		reduce byE→E*E
E		

stack	input	action
E+E	*id	shift
E+E*	id	shift
E+E*id		reduce by E→id
E+E*E		reduce by $E \rightarrow E^*E$
E+E		reduce by E→E+E
E		

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# Reduce reduce conflict

C+C

Consider the grammar M  $\rightarrow$  R+R | R+c | R R  $\rightarrow$  c

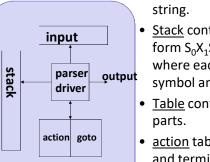
#### and the input

# Stack input action c+c shift c +c reduce by R→c R +c shift R+ c shift R+c reduce by R→c R+R reduce by M→R+R M

# Stack input action c+c shift c +c reduce by R→c R +c shift R+ c shift R+c reduce by M→R+c M

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# LR parsing



Parse table

- <u>Input</u> buffer contains the input string.
- Stack contains a string of the form S<sub>0</sub>X<sub>1</sub>S<sub>1</sub>X<sub>2</sub>.....X<sub>n</sub>S<sub>n</sub> where each X<sub>i</sub> is a grammar symbol and each S<sub>i</sub> is a state.
- <u>Table</u> contains action and goto parts.
- <u>action</u> table is indexed by state and terminal symbols.
- goto table is indexed by state and non terminal symbols.

Exa	ımp	ole	Cons and	ider a its par	gram rse tak	ımar ole	Т	→ E · → T · → ( E	* F	F
State	id	+	*	(	)	\$	Е	Т	F	
0	s5			s4			1	2	3	
1		s6				асс				
2		r2	s7		r2	r2				
3		r4	r4		r4	r4				
4	s5			s4			8	2	3	
5		r6	r6		r6	r6				
6	s5			s4				9	3	
7	s5			s4					10	action
8		s6			s11			(		
9		r1	s7		r1	r1				
10		r3	r3		r3	r3 <b>←</b>				goto
11		r5	r5		r5	r5			~	25

## Actions in an LR (shift reduce) parser

- Assume S<sub>i</sub> is top of stack and a<sub>i</sub> is current input symbol
- Action [S<sub>i</sub>,a<sub>i</sub>] can have four values
  - 1. sj: shift a<sub>i</sub> to the stack, goto state S<sub>i</sub>
  - 2. rk: reduce by rule number k
  - 3. acc: Accept
  - 4. err: Error (empty cells in the table)

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# Driving the LR parser

Stack:  $S_0X_1S_1X_2...X_mS_m$  Input:  $a_ia_{i+1}...a_n$ \$

- If action[S<sub>m</sub>,a<sub>i</sub>] = shift S
   Then the configuration becomes
   Stack: S<sub>0</sub>X<sub>1</sub>S<sub>1</sub>.....X<sub>m</sub>S<sub>m</sub>a<sub>i</sub>S Input: a<sub>i+1</sub>...a<sub>n</sub>\$
- If  $action[S_m,a_i] = reduce A \rightarrow \beta$ Then the configuration becomes  $Stack: S_0X_1S_1...X_{m-r}S_{m-r} AS$  Input:  $a_ia_{i+1}...a_n$ \$ Where  $r = |\beta|$  and  $S = goto[S_{m-r},A]$

Driving the LR parser

Stack:  $S_0X_1S_1X_2...X_mS_m$  Input:  $a_ia_{i+1}...a_n$ \$

- If action[S<sub>m</sub>,a<sub>i</sub>] = accept
   Then parsing is completed. HALT
- If action[S<sub>m</sub>,a<sub>i</sub>] = error (or empty cell)
   Then invoke error recovery routine.

Pa	arse	e: id	+ b	id <sup>;</sup>	* id						$E \rightarrow E + T$ $E \rightarrow T$ $T \rightarrow T * F$
State	id	+	*	(	)	\$	Е	Т	F	4.	T→ F
0	s5			s4			1	2	3		F→ (E)
1		s6				acc				6.	F→ id
1 2 3 4 5		r2	s7		r2	r2					
3		r4	r4		r4	r4					
4	s5			s4			8	2	3		
5		r6	r6		r6	r6					
6	s5			s4				9	3		
7	s5			s4					10		
8		s6			s11						
9		r1	s7		r1	r1					
10		r3	r3		r3	r3					
11		r5	r5		r5	r5					29
					•					-	

	Parse id +	id * id	
Stack	Input	Action	
0	id+id*id\$	shift 5	
0 id 5	+id*id\$	reduce by F→id	
0 F 3	+id*id\$	reduce by $T \rightarrow F$	
0 T 2	+id*id\$	reduce by $E \rightarrow T$	
0 E 1	+id*id\$	shift 6	
0 E 1 + 6	id*id\$	shift 5	
0 E 1 + 6 id 5	*id\$	reduce by F→id	
0 E 1 + 6 F 3	*id\$	reduce by $T \rightarrow F$	
0 E 1 + 6 T 9	*id\$	shift 7	
0E1+6T9*7	id\$	shift 5	
0 E 1 + 6 T 9 * 7 id 5	\$	reduce by F→id	
0E1+6T9*7F10	\$	reduce by T→T*F	
0 E 1 + 6 T 9	\$	reduce by E→E+T	
0 E 1	\$	ACCEPT	30

# Configuration of a LR parser

- The tuple
   <Stack Contents, Remaining Input> defines a configuration of a LR parser
- Initially the configuration is

$$,  $a_0a_1...a_n$ $ >$$

 Typical final configuration on a successful parse is

$$< S_0 X_1 S_i, $>$$

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# LR parsing Algorithm

```
Initial state: Stack: S<sub>0</sub> Input: w$

while (1) {
  if (action[S,a] = shift S') {
    push(a); push(S'); ip++
  } else if (action[S,a] = reduce A→β) {
    pop (2*|β|) symbols;
    push(A); push (goto[S",A])
    (S" is the state at stack top after popping symbols)
  } else if (action[S,a] = accept) {
    exit
  } else { error }
```