Graph Theory-Class 4

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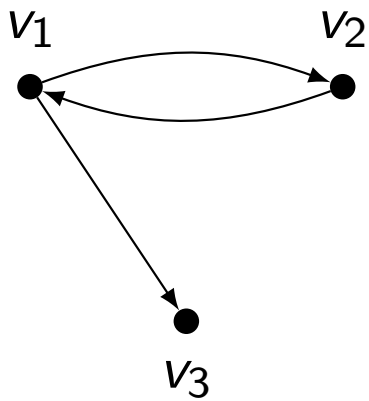

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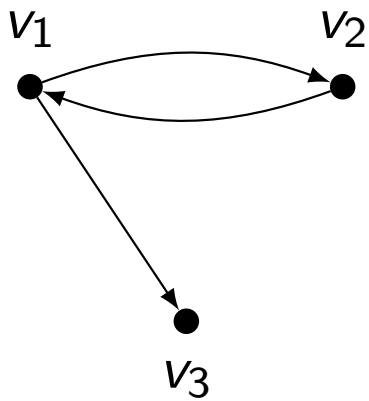

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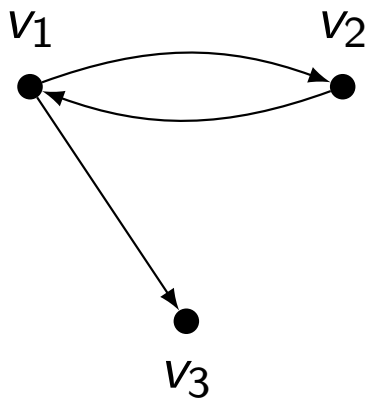

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In above graph $E = \{(v_1, v_2), (v_2, v_1), (v_1, v_3)\}$.

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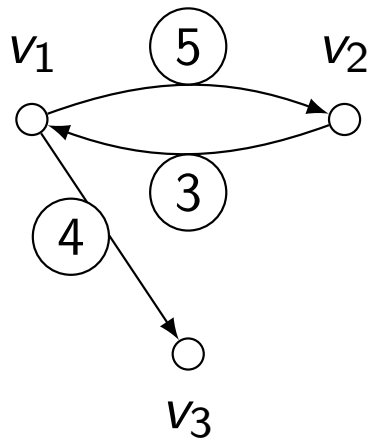

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- $d_{ij} =$ weight/distance of the edge from v_i to v_j, if such an edge exists.

PLEASE REFER TO GRAPH THEORY NOTES FOR THE Dijkstra's algorithm.