1. Intro. Find a comma-free block code of length n, having one code in each cyclic equivalence class, if one exists.

Codewords are represented as hexadecimal numbers.

```
#define maxn 25    /* must be at most 32, to keep the variable names small */
#include <stdio.h>
#include <stdlib.h>
  int n;    /* command-line parameter */
  char a[maxn + 1];
  main(int argc, char *argv[])
  {
    register int i, j, k;
    register unsigned int x, y, z;
    register unsigned long long m, acc, xy;
    ⟨Process the command line 2⟩;
    ⟨Generate the positive clauses 3⟩;
    ⟨Generate the negative clauses 5⟩;
  }
```

2. ⟨Process the command line 2⟩ ≡

```
  if (argc ≠ 2 ∨ sscanf(argv[1], "%d", &n) ≠ 1) {
    fprintf(stderr, "Usage:␣%s␣n\n", argv[0]);
    exit(−1);
  }
  if (n < 2 ∨ n > maxn) {
    fprintf(stderr, "n␣should␣be␣between␣2␣and␣%d,␣not␣%d!\n", maxn, n);
    exit(−2);
  }
  printf("~␣sat-commafree␣%d\n", n);
```

This code is used in section 1.

3. Here I use Algorithm 7.2.1.1F to find the prime binary strings.

⟨Generate the positive clauses 3⟩ ≡

```
f1: a[0] = −1, j = 1;
f2: if (j ≡ n) ⟨Visit the prime string a_1 ... a_n 4⟩;
f3: for (j = n; a[j] ≡ 1; j−−) ;
f4: if (j) {
      a[j] = 1;
  f5: for (k = j + 1; k ≤ n; k++) a[k] = a[k − j];
      goto f2;
  }
```

This code is used in section 1.

4. ⟨Visit the prime string $a_1 \ldots a_n$ 4⟩ ≡

```
  {
    for (i = 0; i < n; i++) {
      for (x = 0, k = 0; k < n; k++) x = (x ≪ 1) + a[1 + ((i + k) % n)];
      printf("␣%x", x);
    }
    printf("\n");
  }
```

This code is used in section 3.

5. ⟨Generate the negative clauses 5⟩ ≡

```
m = (1LL ≪ n) − 1;
for (x = 0; x < (1 ≪ n); x++) {
  ⟨If x is cyclic, continue 6⟩;
  for (y = 0; y < (1 ≪ n); y++) {
    ⟨If y is cyclic, continue 7⟩;
    ⟨Generate the clauses for x followed by y 9⟩;
  }
}
```

This code is used in section 1.

6. ⟨If x is cyclic, **continue** 6⟩ ≡

```
acc = (((unsigned long long) x) ≪ n) + x;
for (k = 1; k < n; k++)
  if (((acc ≫ k) & m) ≡ x) break;
if (k < n) continue;
```

This code is used in section 5.

7. ⟨If y is cyclic, **continue** 7⟩ ≡

```
acc = (((unsigned long long) y) ≪ n) + y;
for (k = 1; k < n; k++)
  if (((acc ≫ k) & m) ≡ y) break;
if (k < n) continue;
```

This code is used in section 5.

8. ⟨If z is cyclic, **continue** 8⟩ ≡

```
acc = (((unsigned long long) z) ≪ n) + z;
for (k = 1; k < n; k++)
  if (((acc ≫ k) & m) ≡ z) break;
if (k < n) continue;
```

This code is used in section 9.

9. ⟨Generate the clauses for x followed by y 9⟩ ≡

```
xy = (((unsigned long long) x) ≪ n) + y;
for (j = 1; j < n; j++) {
  z = (xy ≫ j) & m;
  ⟨If z is cyclic, continue 8⟩;
  printf("~%x␣~%x␣~%x\n", x, y, z);
}
```

This code is used in section 5.

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SAT-COMMAFREE