§1 SAT8 INTRO 1

(Downloaded from https://cs.stanford.edu/~knuth/programs.html and typeset on September 17, 2017)

1. Intro. This program is part of a series of "SAT-solvers" that I'm putting together for my own education as I prepare to write Section 7.2.2.2 of *The Art of Computer Programming*. My intent is to have a variety of compatible programs on which I can run experiments to learn how different approaches work in practice.

This time I'm implementing WALKSAT, a notable development of the WALK algorithm that was featured in SAT7. Instead of using completely random choices when a variable is flipped, WALKSAT makes a more informed decision. The WALKSAT method was introduced by B. Selman, H. A. Kautz, and B. Cohen in National Conference on Artificial Intelligence 12 (1994), 337–343.

2. If you have already read SAT7, or any other program of this series, you might as well skip now past the rest of this introduction, and past the code for the "I/O wrapper" that is presented in the next dozen or so sections, because you've seen it before. (Except that there are some new command-line options.)

The input appears on *stdin* as a series of lines, with one clause per line. Each clause is a sequence of literals separated by spaces. Each literal is a sequence of one to eight ASCII characters between ! and }, inclusive, not beginning with ~, optionally preceded by ~ (which makes the literal "negative"). For example, Rivest's famous clauses on four variables, found in 6.5–(13) and 7.1.1–(32) of *TAOCP*, can be represented by the following eight lines of input:

Input lines that begin with ~u are ignored (treated as comments). The output will be '~?' if the algorithm could not find a way to satisfy the input clauses. Otherwise it will be a list of noncontradictory literals that cover each clause, separated by spaces. ("Noncontradictory" means that we don't have both a literal and its negation.) The input above would, for example, yield '~?'; but if the final clause were omitted, the output would be '~x1 ~x2 x3', together with either x4 or ~x4 (but not both). No attempt is made to find all solutions; at most one solution is given.

The running time in "mems" is also reported, together with the approximate number of bytes needed for data storage. One "mem" essentially means a memory access to a 64-bit word. (These totals don't include the time or space needed to parse the input or to format the output.)

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```
So here's the structure of the program. (Skip ahead if you are impatient to see the interesting stuff.)
\#define o mems ++
                          /* count one mem */
#define oo mems += 2 /* count two mems */
#define ooo mems += 3 /* count three mems */
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include "gb_flip.h"
  typedef unsigned int uint; /* a convenient abbreviation */
  typedef unsigned long long ullng;
                                            /* ditto */
  \langle \text{Type definitions 6} \rangle;
  ⟨Global variables 4⟩;
  \langle \text{Subroutines 26} \rangle;
  main(\mathbf{int} \ argc, \mathbf{char} * argv[])
    register uint c, g, h, i, j, k, l, p, q, r, ii, kk, ll, fcount;
    \langle \text{Process the command line 5} \rangle;
    \langle \text{Initialize everything 9} \rangle;
    \langle \text{Input the clauses } 10 \rangle;
    if (verbose & show_basics) \langle Report the successful completion of the input phase 22 \rangle;
    (Set up the main data structures 29);
    imems = mems, mems = 0;
    \langle Solve the problem 37 \rangle;
    if (verbose & show_basics)
      fprintf(stderr, "Altogether_\%llu_\%llu_\mems, \_\%llu_\bytes, \_\%d_\trial\%s, \_\%llu_\steps.\n",
           imems, mems, bytes, trial + 1, trial ? "s" : "", step);
  }
4. #define show_basics 1 /* verbose code for basic stats */
#define show_choices 2
                             /* verbose code for backtrack logging */
                               /* verbose code for further commentary */
#define show_details 4
#define show_qory_details 8
                                 /* verbose code turned on when debugging */
\langle \text{Global variables 4} \rangle \equiv
  int random\_seed = 0;
                            /* seed for the random words of gb\_rand */
  int verbose = show_basics; /* level of verbosity */
  int hbits = 8; /* logarithm of the number of the hash lists */
  int buf\_size = 1024;
                           /* must exceed the length of the longest input line */
                       /* maximum steps per walk (maxthresh * n by default) */
  ullng maxsteps;
  unsigned int maxthresh = 50;
  int maxtrials = 1000000;
                               /* maximum walks to try */
  double nongreedprob = 0.4; /* the probability bias for nongreedy choices */
  unsigned long nongreedthresh; /* coerced since gb_next_rand is long */
  ullng imems, mems; /* mem counts */
                      /* report when mems exceeds this, if delta \neq 0 */
  ullng thresh = 0;
                      /* report every delta or so mems */
  ullng delta = 0;
  ullng timeout = #1ffffffffffffffffff /* give up after this many mems */
                   /* memory used by main data structures */
  ullng bytes;
See also sections 8 and 25.
This code is used in section 3.
```

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- 5. On the command line one can specify any or all of the following options:
- 'v (integer)' to enable various levels of verbose output on *stderr*.
- 'h' positive integer' 'to adjust the hash table size.
- 'b \(\rangle\) positive integer \(\rangle\)' to adjust the size of the input buffer.
- 's (integer)' to define the seed for any random numbers that are used.
- 'd\langle integer \rangle' to set delta for periodic state reports.
- 't (integer)' to define the maximum number of steps per random walk.
- 'c(integer)' to define the maximum number of steps per variable, per random walk, if the t parameter hasn't been given. (The default is 50.)
- 'w (integer)' to define the maximum number of walks attempted.
- 'p(float)' to define the probability nongreedprob of nongreedy choices.
- 'T(integer)' to set timeout: This program will abruptly terminate, when it discovers that mems > timeout.

```
\langle \text{ Process the command line 5} \rangle \equiv
  for (j = argc - 1, k = 0; j; j - -)
     switch (argv[j][0]) {
     \mathbf{case} \ \texttt{`v':} \ k \mid = (sscanf(argv[j] + 1, \texttt{"%d"}, \&verbose) - 1); \ \mathbf{break};
     case 'h': k = (sscanf(argv[j] + 1, "\%d", \&hbits) - 1); break;
     \mathbf{case} \ \texttt{'b':} \ k \mid = (sscanf(argv[j] + 1, \texttt{"%d"}, \&\mathit{buf\_size}) - 1); \ \mathbf{break};
     case 's': k = (sscanf(argv[j] + 1, "%d", \&random\_seed) - 1); break;
     case 'd': k = (sscanf(argv[j] + 1, "\%11d", \&delta) - 1); thresh = delta; break;
     case 't': k = (sscanf(argv[j] + 1, \text{"%llu"}, \& maxsteps) - 1); break;
     case 'c': k = (sscanf(argv[j] + 1, "%u", & maxthresh) - 1); break;
     case 'w': k = (sscanf(argv[j] + 1, "%d", \& maxtrials) - 1); break;
     case 'p': k = (sscanf(argv[j] + 1, "\%lf", \&nongreedprob) - 1); break;
     case 'T': k = (sscanf(argv[j] + 1, "\%11d", \&timeout) - 1); break;
     default: k = 1;
                           /* unrecognized command-line option */
  if (k \lor hbits < 0 \lor hbits > 30 \lor buf\_size \le 0) {
     fprintf(stderr, " \sqsubseteq [t < n >] \sqsubseteq [c < n >] \sqsubseteq [p < f >] \sqsubseteq [T < n >] \sqcup ( \sqsubseteq f oo.sat \ n");
     exit(-1);
  if (nongreedprob < 0.0 \lor nongreedprob > 1.0) {
     fprintf(stderr, "Parameter_p_should_be_between_0.0_and_1.0!\n");
     exit(-666);
```

This code is used in section 3.

4 The I/O Wrapper Sats  $\S6$ 

6. The I/O wrapper. The following routines read the input and absorb it into temporary data areas from which all of the "real" data structures can readily be initialized. My intent is to incorporate these routines in all of the SAT-solvers in this series. Therefore I've tried to make the code short and simple, yet versatile enough so that almost no restrictions are placed on the sizes of problems that can be handled. These routines are supposed to work properly unless there are more than  $2^{32} - 1 = 4,294,967,295$  occurrences of literals in clauses, or more than  $2^{31} - 1 = 2,147,483,647$  variables or clauses.

In these temporary tables, each variable is represented by four things: its unique name; its serial number; the clause number (if any) in which it has most recently appeared; and a pointer to the previous variable (if any) with the same hash address. Several variables at a time are represented sequentially in small chunks of memory called "vchunks," which are allocated as needed (and freed later).

```
/* preferably (2^k - 1)/3 for some k */
#define vars_per_vchunk 341
\langle \text{ Type definitions } 6 \rangle \equiv
  typedef union {
    char ch8[8];
    uint u2[2];
    long long lng;
  } octa;
  typedef struct tmp_var_struct {
    octa name:
                     /* the name (one to eight ASCII characters) */
                     /* 0 for the first variable, 1 for the second, etc. */
    uint serial;
                    /* m if positively in clause m; -m if negatively there */
    int stamp;
                                         /* pointer for hash list */
    struct tmp_var_struct *next;
  } tmp_var;
  typedef struct vchunk_struct {
                                        /* previous chunk allocated (if any) */
    struct vchunk_struct *prev;
    tmp_var var[vars_per_vchunk];
  } vchunk:
See also sections 7 and 24.
This code is used in section 3.
```

7. Each clause in the temporary tables is represented by a sequence of one or more pointers to the **tmp\_var** nodes of the literals involved. A negated literal is indicated by adding 1 to such a pointer. The first literal of a clause is indicated by adding 2. Several of these pointers are represented sequentially in chunks of memory, which are allocated as needed and freed later.

```
#define cells_per_chunk 511 /* preferably 2<sup>k</sup> − 1 for some k */

⟨Type definitions 6⟩ +≡

typedef struct chunk_struct {

struct chunk_struct *prev; /* previous chunk allocated (if any) */

tmp_var *cell[cells_per_chunk];

} chunk;
```

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```
8. \langle \text{Global variables 4} \rangle + \equiv
                   /* buffer for reading the lines (clauses) of stdin */
  char *buf;
                          /* heads of the hash lists */
  tmp_var **hash;
  uint hash\_bits[93][8];
                              /* random bits for universal hash function */
                              /* the vchunk currently being filled */
  vchunk *cur\_vchunk;
  tmp\_var * cur\_tmp\_var;
                                 /* current place to create new tmp_var entries */
  tmp\_var *bad\_tmp\_var;
                                 /* the cur_tmp_var when we need a new vchunk */
  chunk *cur\_chunk;
                            /* the chunk currently being filled */
  tmp\_var **cur\_cell;
                             /* current place to create new elements of a clause */
  tmp_var **bad_cell;
                             /* the cur_cell when we need a new chunk */
                   /* how many distinct variables have we seen? */
  ullng vars;
  ullng clauses;
                      /* how many clauses have we seen? */
  ullng nullclauses; /* how many of them were null? */
  ullng cells;
                    /* how many occurrences of literals in clauses? */
9. \langle Initialize everything \rangle \equiv
  gb\_init\_rand(random\_seed);
  buf = (\mathbf{char} *) \ malloc(buf\_size * \mathbf{sizeof}(\mathbf{char}));
  if (\neg buf) {
     fprintf(stderr, "Couldn't_allocate_the_input_buffer_(buf_size=%d)!\n", buf_size);
     exit(-2);
  hash = (\mathbf{tmp\_var} **) \ malloc(\mathbf{sizeof}(\mathbf{tmp\_var}) \ll hbits);
  if (\neg hash) {
    fprintf(stderr, "Couldn't_uallocate_u'd_uhash_ulist_uheads_u(hbits=%d)! \\ n", 1 \ll hbits, hbits);
     exit(-3);
  for (h = 0; h < 1 \ll hbits; h \leftrightarrow) hash[h] = \Lambda;
See also section 15.
This code is used in section 3.
```

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10. The hash address of each variable name has h bits, where h is the value of the adjustable parameter hbits. Thus the average number of variables per hash list is  $n/2^h$  when there are n different variables. A warning is printed if this average number exceeds 10. (For example, if h has its default value, 8, the program will suggest that you might want to increase h if your input has 2560 different variables or more.)

All the hashing takes place at the very beginning, and the hash tables are actually recycled before any SAT-solving takes place; therefore the setting of this parameter is by no means crucial. But I didn't want to bother with fancy coding that would determine h automatically.

```
\langle \text{Input the clauses } 10 \rangle \equiv
      while (1) {
             if (\neg fgets(buf, buf\_size, stdin)) break;
             clauses +\!\!+;
             if (buf[strlen(buf) - 1] \neq '\n') {
                   fprintf(stderr, "The \clause \cupon \clause 
                   fprintf(stderr, "umyubuf_size_uis_uonly_u%d!\n", buf_size);
                   fprintf(stderr, "Please\_use\_the\_command-line\_option\_b<newsize>.\n");
                   exit(-4);
             \langle \text{ Input the clause in } buf \ 11 \rangle;
      if ((vars \gg hbits) \ge 10) {
             fprintf(stderr, "There_lare_l\%llu_lvariables_lbut_lonly_l\%d_lhash_ltables; \n", vars, 1 \ll hbits);
             while ((vars \gg hbits) \ge 10) hbits +++;
            fprintf(stderr, "\_maybe\_you\_should\_use\_command-line\_option\_h%d?\n", hbits);
      clauses -= nullclauses;
      if (clauses \equiv 0) {
            fprintf(stderr, "No_{\square}clauses_{\square}were_{\square}input! \n");
             exit(-77);
      if (vars \ge *80000000) {
             fprintf(stderr, "Whoa, \_the\_input\_had\_%llu\_variables! \n", vars);
             exit(-664);
      if (clauses > #80000000) {
             fprintf(stderr, "Whoa, \_the\_input\_had\_\%llu\_clauses! \n", clauses);
             exit(-665);
      if (cells > #10000000) {
             fprintf(stderr, "Whoa, \_the \_input \_had \_\%llu \_occurrences \_of \_literals! \n", cells);
             exit(-666);
This code is used in section 3.
```

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```
11. (Input the clause in buf 11) \equiv
  for (j = k = 0; ; )  {
     while (buf[j] \equiv ' \cup ') j ++;
                                         /* scan to nonblank */
     if (buf[j] \equiv '\n') break;
     if (buf[j] < , , \lor buf[j] > , , ) {
       clauses);
        exit(-5);
     if (buf[j] \equiv , \, , \, ) \ i = 1, j ++;
     else i = 0;
     \langle \text{Scan and record a variable}; \text{ negate it if } i \equiv 1 \ 12 \rangle;
  if (k \equiv 0) {
     fprintf(stderr, "(Empty line \%lld lis being ignored) \n", clauses);
                          /* strictly speaking it would be unsatisfiable */
  goto clause_done;
empty_clause: \langle Remove all variables of the current clause 19\rangle;
clause\_done: cells += k;
This code is used in section 10.
12. We need a hack to insert the bit codes 1 and/or 2 into a pointer value.
#define hack_in(q,t) (tmp_var *)(t | (ullng) q)
\langle Scan and record a variable; negate it if i \equiv 1 12\rangle \equiv
  {
     register tmp_var *p;
     if (cur\_tmp\_var \equiv bad\_tmp\_var) (Install a new vchunk 13);
     \langle \text{Put the variable name beginning at } buf[j] \text{ in } cur\_tmp\_var \neg name \text{ and compute its hash code } h \text{ 16} \rangle;
     \langle \text{Find } cur\_tmp\_var \neg name \text{ in the hash table at } p \text{ 17} \rangle;
     if (p \rightarrow stamp \equiv clauses \lor p \rightarrow stamp \equiv -clauses) (Handle a duplicate literal 18)
     else {
       p \rightarrow stamp = (i ? -clauses : clauses);
       if (cur\_cell \equiv bad\_cell) (Install a new chunk 14);
       *cur\_cell = p;
       if (i \equiv 1) *cur\_cell = hack\_in(*cur\_cell, 1);
       if (k \equiv 0) *cur\_cell = hack\_in(*cur\_cell, 2);
       cur\_cell++, k++;
  }
This code is used in section 11.
```

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```
13.
      \langle \text{Install a new vchunk } 13 \rangle \equiv
     register vchunk *new_vchunk;
     new\_vchunk = (\mathbf{vchunk} *) \ malloc(\mathbf{sizeof}(\mathbf{vchunk}));
     if (\neg new\_vchunk) {
        fprintf(stderr, "Can't_allocate_a_new_vchunk!\n");
        exit(-6);
     new\_vchunk \neg prev = cur\_vchunk, cur\_vchunk = new\_vchunk;
     cur\_tmp\_var = \&new\_vchunk \neg var[0];
     bad\_tmp\_var = \&new\_vchunk \neg var[vars\_per\_vchunk];
This code is used in section 12.
14. \langle \text{Install a new chunk } 14 \rangle \equiv
     register chunk *new_chunk;
     new\_chunk = (\mathbf{chunk} *) \ malloc(\mathbf{sizeof}(\mathbf{chunk}));
     if (\neg new\_chunk) {
        fprintf(stderr, "Can't_{\square}allocate_{\square}a_{\square}new_{\square}chunk! \n");
        exit(-7);
     new\_chunk \neg prev = cur\_chunk, cur\_chunk = new\_chunk;
     cur\_cell = \&new\_chunk \neg cell[0];
     bad\_cell = \&new\_chunk \neg cell[cells\_per\_chunk];
This code is used in section 12.
      The hash code is computed via "universal hashing," using the following precomputed tables of random
15.
bits.
\langle \text{Initialize everything } 9 \rangle + \equiv
  for (j = 92; j; j--)
     for (k = 0; k < 8; k++) hash\_bits[j][k] = gb\_next\_rand();
16. \(\rightarrow\) Put the variable name beginning at buf[j] in cur\_tmp\_var\_name and compute its hash code h 16 \(\rightarrow\)
  cur\_tmp\_var \rightarrow name.lng = 0;
  for (h = l = 0; buf[j + l] > ' " ' \land buf[j + l] \leq ' " '; l ++)  {
     if (l > 7) {
        fprintf(stderr, "Variable\_name\_%.9s...\_in\_the\_clause\_on\_line\_%lld\_is\_too\_long!\n",
             buf + j, clauses);
        exit(-8);
     h \oplus = hash\_bits[buf[j+l] - '!'][l];
     cur\_tmp\_var \rightarrow name.ch8[l] = buf[j+l];
  if (l \equiv 0) goto empty_clause; /* '~' by itself is like 'true' */
  i += l;
  h \&= (1 \ll hbits) - 1;
This code is used in section 12.
```

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```
17. \langle \text{Find } cur\_tmp\_var \neg name \text{ in the hash table at } p \mid 17 \rangle \equiv
   for (p = hash[h]; p; p = p \rightarrow next)
     if (p \rightarrow name.lng \equiv cur\_tmp\_var \rightarrow name.lng) break;
  if (\neg p) {
                    /* new variable found */
     p = cur\_tmp\_var ++;
     p \rightarrow next = hash[h], hash[h] = p;
     p \rightarrow serial = vars ++;
     p \rightarrow stamp = 0;
This code is used in section 12.
     The most interesting aspect of the input phase is probably the "unwinding" that we might need to do
when encountering a literal more than once in the same clause.
\langle Handle a duplicate literal \frac{18}{}\rangle \equiv
     if ((p \rightarrow stamp > 0) \equiv (i > 0)) goto empty\_clause;
This code is used in section 12.
19. An input line that begins with "" is silently treated as a comment. Otherwise redundant clauses are
logged, in case they were unintentional. (One can, however, intentionally use redundant clauses to force the
order of the variables.)
\langle Remove all variables of the current clause 19 \rangle \equiv
   while (k) {
     \langle \text{Move } cur\_cell \text{ backward to the previous cell } 20 \rangle;
     k--;
  if ((buf[0] \neq ```) \lor (buf[1] \neq `\Box`))
     fprintf(stderr, "(The_{\sqcup}clause_{\sqcup}on_{\sqcup}line_{\sqcup}%lld_{\sqcup}is_{\sqcup}always_{\sqcup}satisfied)\n", clauses);
   null clauses ++;
This code is used in section 11.
20. \langle \text{Move } cur\_cell \text{ backward to the previous cell } 20 \rangle \equiv
  if (cur\_cell > \& cur\_chunk \rightarrow cell[0]) cur\_cell ---;
  else {
     register chunk *old\_chunk = cur\_chunk;
```

cur\_chunk = old\_chunk¬prev; free(old\_chunk);
bad\_cell = &cur\_chunk¬cell[cells\_per\_chunk];

 $cur\_cell = bad\_cell - 1;$ 

This code is used in sections 19 and 33.

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21. Notice that the old "temporary variable" data goes away here. (A bug bit me in the first version of the code because of this.)

```
 \langle \text{Move } \textit{cur\_tmp\_var} \text{ backward to the previous temporary variable } 21 \rangle \equiv \\ \text{if } (\textit{cur\_tmp\_var} > \&\textit{cur\_vchunk} \rightarrow \textit{var}[0]) \; \textit{cur\_tmp\_var} --; \\ \text{else } \{ \\ \text{register vchunk} *\textit{old\_vchunk} = \textit{cur\_vchunk}; \\ \textit{cur\_vchunk} = \textit{old\_vchunk} \rightarrow \textit{prev}; \; \textit{free} (\textit{old\_vchunk}); \\ \textit{bad\_tmp\_var} = \&\textit{cur\_vchunk} \rightarrow \textit{var}[\textit{vars\_per\_vchunk}]; \\ \textit{cur\_tmp\_var} = \textit{bad\_tmp\_var} - 1; \\ \} \\ \text{This code is used in section } 35.
```

22.  $\langle$  Report the successful completion of the input phase  $22 \rangle \equiv fprintf(stderr, "(\%llu_variables, \_\%llu_\lambdallu_clauses, \_\%llu_\lambdallu_literals_usuccessfully_read) \n", vars, clauses, cells);$ 

This code is used in section 3.

**23. SAT solving, version 8.** The WALKSAT algorithm is only a little bit more complicated than the WALK method, but the differences mean that we cannot simulate simultaneous runs with bitwise operations. Let  $x = x_1 \dots x_n$  be a binary vector that represents all n variables, and let T be a given tolerance (representing the amount of patience that we have). We start by setting x to a completely random vector; then we repeat the following steps, at most T times:

Check to see if x satisfies all the clauses. If so, output x; we're done! If not, select a clause c that isn't true, uniformly at random from all such clauses; say c is the union of k literals,  $l_1 \vee \cdots \vee l_k$ . Sort those literals according to their "break count," which is the number of clauses that will become false when that literal is flipped. Choose a literal to flip by the following method: If no literal has a break count of zero, and if a biased coin turns up heads, choose  $l_j$  at random from among all k literals. Otherwise, choose  $l_j$  at random from among those with smallest break count. Then change the bit of x that will make  $l_j$  true.

If that random walk doesn't succeed, we can try again with another starting value of x, until we've seen enough failures to be convinced that we're probably doomed to defeat.

**24.** The data structures are somewhat interesting, but not tricky: There are four main arrays, *cmem*, *vmem*, *mem*, and *tmem*. Structured **clause** nodes appear in *cmem*, and structured **variable** nodes appear in *vmem*. Each clause points to a sequential list of literals in *mem*; each literal points to a sequential list of clauses in *tmem*, which is essentially the "transpose" of the information in *mem*. If *fcount* clauses are currently false, the first *fcount* entries of *cmem* also contain the indices of those clauses.

As in most previous programs of this series, the literals x and  $\bar{x}$  are represented internally by 2k and 2k+1 when x is the kth variable.

The symbolic names of variables are kept separately in *nmem*, not in *vmem*, for reasons of efficiency. (Otherwise a **variable** struct would take up five octabytes, and addressing would be slower.)

```
#define value(l) (vmem[(l) \gg 1].val \oplus ((l) \& 1))
\langle \text{Type definitions } 6 \rangle + \equiv
  typedef struct {
                   /* the variable's current value */
    uint val;
                          /* how many clauses are false except for this variable */
    uint breakcount:
    uint pos_start, neg_start;
                                    /* where the clause lists start in tmem */
  } variable;
  typedef struct {
                     /* where the literal list starts in mem */
    uint start;
    uint tcount;
                      /* how many of those literals are currently true? */
                      /* if tcount = 0, which fslot holds this clause? */
    uint fplace;
                    /* the number of a false clause, if needed */
    uint fslot;
  } clause;
25. \langle Global variables 4\rangle + \equiv
  clause *cmem;
                       /* the master array of clauses */
                        /* the master array of variables */
  variable *vmem:
  uint *mem;
                   /* the master array of literals in clauses */
  uint *cur\_mcell;
                        /* the current cell of interest in mem */
                    /* the master array of clauses containing literals */
  uint *tmem;
  octa *nmem;
                     /* the master array of symbolic variable names */
                /* which trial are we on? */
  int trial:
  ullng step:
                  /* which step are we on? */
  uint *best;
                  /* temporary array to hold literal names for a clause */
```

12

Here is a subroutine that prints a clause symbolically. It illustrates some of the conventions of the data structures that have been explained above. I use it only for debugging.

```
\langle \text{Subroutines 26} \rangle \equiv
  void print_clause(uint c)
        /* the first clause is called clause 1, not 0 */
     register uint l, ll;
     fprintf(stderr, "%d:", c); /* show the clause number */
     for (l = cmem[c-1].start; l < cmem[c].start; l++) {
       ll = mem[l];
       fprintf(stderr, "_{l}\%s\%.8s(%d)", ll \& 1?"": "", nmem[ll \gg 1].ch8, value(ll));
     fprintf(stderr, "\n");
See also sections 27 and 28.
This code is used in section 3.
```

27. Another version of that routine, used to display unsatisfied clauses in verbose mode, shows the current breakcounts of each literal.

```
\langle \text{Subroutines } 26 \rangle + \equiv
  void print_unsat_clause(uint c)
     register uint l, ll;
    fprintf(stderr, "%d:", c);
                                    /* show the clause number */
     for (l = cmem[c-1].start; l < cmem[c].start; l \leftrightarrow) {
       ll = mem[l];
       fprintf(stderr, "_{l}\%s\%.8s(\%d)", ll \& 1? "^{"}: "", nmem[ll \gg 1].ch8, vmem[ll \gg 1].breakcount);
     fprintf(stderr, "\n");
```

28. Similarly, we can list the clause numbers that contain a given literal. (Notice the limits on c in the loop here.)

```
\langle Subroutines 26\rangle + \equiv
  void print_literal_uses(uint l)
  {
    register uint ll, c;
    ll = l \gg 1;
    fprintf(stderr, \%s\%.8s(\%d)_lis_lin, l \& 1? \% : \%, nmem[ll].ch8, value(l));
    for (c = (l \& 1 ? vmem[ll].neg\_start : vmem[ll].pos\_start);
            c < (l \& 1 ? vmem[ll + 1].pos\_start : vmem[ll].neg\_start); c++) fprintf(stderr, "\d",tmem[c]);
    fprintf(stderr, "\n");
```

29. Initializing the real data structures. We're ready now to convert the temporary chunks of data into the form we want, and to recycle those chunks.

```
\langle Set up the main data structures 29\rangle \equiv
   \langle Allocate the main arrays 30\rangle;
   \langle \text{ Initialize the } pos\_start \text{ and } neg\_start \text{ fields } 31 \rangle;
   (Copy all the temporary cells to the mem and cmem arrays in proper format 32);
   (Copy all the temporary variable nodes to the nmem array in proper format 35);
   \langle \text{ Set up the } tmem \text{ array } 34 \rangle;
   \langle \text{ Check consistency 36} \rangle;
This code is used in section 3.
30. \langle Allocate the main arrays 30 \rangle \equiv
   free(buf); free(hash);
                                   /* a tiny gesture to make a little room */
   vmem = (variable *) malloc((vars + 1) * sizeof(variable));
   if (\neg vmem) {
     exit(-12);
   bytes = (vars + 1) * sizeof(variable);
   nmem = (\mathbf{octa} *) \ malloc(vars * \mathbf{sizeof}(\mathbf{octa}));
  if (\neg nmem) {
     fprintf(stderr, "Oops, \sqcup I_{\sqcup}can't_{\sqcup}allocate_{\sqcup}the_{\sqcup}nmem_{\sqcup}array! \n");
     exit(-13);
   bytes += vars * sizeof(octa);
   mem = (\mathbf{uint} *) \ malloc(cells * \mathbf{sizeof}(\mathbf{uint}));
  if (\neg mem) {
     fprintf(stderr, "Oops, \sqcup I_{\sqcup}can't_{\sqcup}allocate_{\sqcup}the_{\sqcup}big_{\sqcup}mem_{\sqcup}array! \n");
     exit(-10);
   bytes += cells * sizeof(uint);
   tmem = (\mathbf{uint} *) \ malloc(cells * \mathbf{sizeof}(\mathbf{uint}));
   if (\neg tmem) {
     fprintf(stderr, "Oops, \sqcup I \sqcup can't \sqcup allocate \sqcup the \sqcup big \sqcup tmem \sqcup array! \n");
     exit(-14);
   bytes += cells * sizeof(uint);
   cmem = (clause *) malloc((clauses + 1) * sizeof(clause));
  if (\neg cmem) {
     fprintf(stderr, "Oops, \sqcup I_{\sqcup} can't_{\sqcup} allocate_{\sqcup} the_{\sqcup} cmem_{\sqcup} array! \n");
   bytes += (clauses + 1) * sizeof(clause);
This code is used in section 29.
     \langle \text{ Initialize the } pos\_start \text{ and } neg\_start \text{ fields } 31 \rangle \equiv
   for (c = vars; c; c--) o, vmem[c-1].pos\_start = vmem[c-1].neg\_start = 0;
This code is used in section 29.
```

14

```
32.
      \langle \text{Copy all the temporary cells to the } mem \text{ and } cmem \text{ arrays in proper format } 32 \rangle \equiv
  for (c = clauses, cur\_mcell = mem + cells, kk = 0; c; c--) {
     o, cmem[c].start = cur\_mcell - mem, k = 0;
     (Insert the cells for the literals of clause c 33);
     if (k > kk) kk = k;
                                /* maximum clause size seen so far */
  if (cur\_mcell \neq mem) {
     fprintf(stderr, "Confusion_about_the_number_of_cells!\n");
     exit(-99);
  cmem[0].start = 0;
  best = (\mathbf{uint} *) \ malloc(kk * \mathbf{sizeof}(\mathbf{uint}));
  if (\neg best) {
     fprintf(stderr, "Oops, \sqcup I_{\sqcup} can't_{\sqcup} allocate_{\sqcup} the_{\sqcup} best_{\sqcup} array! \n");
     exit(-16);
  bytes += kk * sizeof(uint);
This code is used in section 29.
      The basic idea is to "unwind" the steps that we went through while building up the chunks.
#define hack\_out(q) (((ullng) q) & #3)
#define hack\_clean(q) ((tmp_var *)((ullng) q \& -4))
(Insert the cells for the literals of clause c 33) \equiv
  for (i = 0; i < 2; k++) {
     \langle \text{Move } cur\_cell \text{ backward to the previous cell } 20 \rangle;
     i = hack\_out(*cur\_cell);
     p = hack\_clean(*cur\_cell) \rightarrow serial;
     cur\_mcell --;
     o, *cur\_mcell = l = p + p + (i \& 1);
     if (l \& 1) oo, vmem[l \gg 1]. neg\_start +++;
     else oo, vmem[l \gg 1].pos\_start ++;
This code is used in section 32.
34. \langle Set up the tmem array 34 \rangle \equiv
  for (j = k = 0; k < vars; k++) {
     o, i = vmem[k].pos\_start, ii = vmem[k].neg\_start;
     o, vmem[k].pos\_start = j + i, vmem[k].neg\_start = j + i + ii;
     j = j + i + ii;
  o, vmem[k].pos\_start = j;
                                    /* j = cells at this point */
  for (c = k = 0, o, kk = cmem[1].start; k < cells; k++) {
     if (k \equiv kk) o, c++, kk = cmem[c+1].start;
     l = mem[k];
    if (l \& 1) ooo, i = vmem[l \gg 1].neg\_start - 1, tmem[i] = c, vmem[l \gg 1].neg\_start = i;
     else ooo, i = vmem[l \gg 1].pos\_start - 1, tmem[i] = c, vmem[l \gg 1].pos\_start = i;
This code is used in section 29.
```

```
35. ⟨Copy all the temporary variable nodes to the nmem array in proper format 35⟩ ≡ for (c = vars; c; c--) {
   ⟨Move cur_tmp_var backward to the previous temporary variable 21⟩;
   o, nmem[c-1].lng = cur_tmp_var name.lng;
}
36. We should now have unwound all the temporary data chunks back to their beginnings.
⟨Check consistency 36⟩ ≡
   if (cur_cell ≠ &cur_chunk -cell[0] ∨ cur_chunk -prev ≠ Λ ∨ cur_tmp_var ≠
        &cur_vchunk -var[0] ∨ cur_vchunk -prev ≠ Λ) {
        fprintf(stderr, "This_can't_happen_(consistency_check_failure)!\n");
        exit(-14);
    }
    free(cur_chunk); free(cur_vchunk);
This code is used in section 29.
```

16 Doing it sate  $\S37$ 

**37.** Doing it. So we take random walks.

```
\langle Solve the problem 37 \rangle \equiv
  if (maxsteps \equiv 0) maxsteps = maxthresh * vars;
  nongreed thresh = nongreed prob * (unsigned long) #80000000;
  for (trial = 0; trial < maxtrials; trial ++) {
     if (delta \land (mems \ge thresh)) {
        thresh += delta;
       fprintf(stderr, "\_after\_\%11d\_mems, \_beginning\_trial\_\%d\n", mems, trial + 1);
     } else if (verbose & show_choices) fprintf(stderr, "beginning_trial_\%d\n", trial + 1);
     \langle \text{Initialize all values 38} \rangle;
     if (verbose & show_details) \langle Print the initial guess 47 \rangle;
     ⟨Initialize the clause data structures 39⟩;
     for (step = 0; ; step ++) {
       if (fcount \equiv 0) (Print a solution and goto done 48);
       if (mems > timeout) {
          fprintf(stderr, "TIMEOUT!\n");
          goto done;
       if (step \equiv maxsteps) break;
        \langle Choose a random unsatisfied clause, c 40\rangle;
        \langle \text{ Choose a literal } l \text{ in } c \text{ 41} \rangle;
        \langle Flip the value of l 42\rangle;
     }
  printf("~?\n");
                         /* we weren't able to satisfy all the clauses */
  if (verbose & show_basics) fprintf(stderr, "DUNNO\n");
  trial --:
                /* restore the actual number of trials made */
  done:
This code is used in section 3.
```

**38.** The macro  $gb\_next\_rand()$  delivers a 31-bit random integer, and my convention is to charge four mems whenever it is called.

```
 \langle \text{Initialize all values } 38 \rangle \equiv \\ \text{for } (k=0,r=1;\ k < vars;\ k++) \ \{ \\ \text{if } (r\equiv 1)\ mems \ += 4, r = gb\_next\_rand() + (1_{\text{U}} \ll 31); \\ o, vmem[k].val = r \& 1, r \gg = 1; \\ vmem[k].breakcount = 0; \\ \}  This code is used in section 37.
```

 $\S39$  SAT8 DOING IT 17

```
39.
     \langle Initialize the clause data structures 39\rangle \equiv
  fcount = 0;
  for (c = k = 0; c < clauses; c++) {
    o, kk = cmem[c+1].start;
    p = 0;
              /* p true literals seen so far in clause c */
    for ( ; k < kk; k ++)  {
      o, l = mem[k];
      if (o, value(l)) p++, ll = l;
    o, cmem[c].tcount = p;
    if (p \le 1) {
      if (p) oo, vmem[ll \gg 1]. breakcount +++;
      else oo, cmem[c].fplace = fcount, cmem[fcount++].fslot = c;
This code is used in section 37.
40. (Choose a random unsatisfied clause, c 40) \equiv
  if (verbose & show_gory_details) {
    fprintf(stderr, "currently_false:\n");
    for (k = 0; k < fcount; k++) print_unsat_clause(cmem[k].fslot + 1);
  mems += 5, c = cmem[qb\_unif\_rand(fcount)].fslot;
  if (verbose & show_choices) fprintf(stderr, "in_{\square}\%u(\%d)", c+1, fcount);
This code is used in section 37.
41. \langle Choose a literal l in c 41\rangle \equiv
  oo, k = cmem[c].start, kk = cmem[c+1].start, h = kk - k;
  ooo, p = mem[k], r = vmem[p \gg 1].breakcount, best[0] = p, j = 1;
  for (k +++; k < kk; k +++) {
    oo, p = mem[k], q = vmem[p \gg 1].breakcount;
    if (q \le r) {
      if (q < r) o, r = q, best[0] = p, j = 1;
      else o, best[j++] = p;
  if (r \equiv 0) goto greedy;
  if (mems += 4, (gb\_next\_rand() < nongreedthresh)) {
    mems += 5, l = mem[kk - 1 - gb\_unif\_rand(h)], g = 0;
    goto got_{-}l;
greedy: g = 1;
  if (j \equiv 1) l = best[0];
  else mems += 5, l = best[gb\_unif\_rand(j)];
qot_l: p = l \gg 1;
  if (verbose & show_choices) {
    fprintf(stderr, "\_flip_\%s\%.8s_\(cost_\%d)\n", vmem[p].val?"": "~", nmem[p].ch8,
         vmem[p].breakcount);
This code is used in section 37.
```

18 Doing it sate  $\S42$ 

```
42.
      At this point p = l \gg 1.
\langle Flip the value of l 42\rangle \equiv
  if (l & 1) {
     oo, k = vmem[p].neg\_start, kk = vmem[p+1].pos\_start;
     \langle \text{ Make clauses } tmem[k], tmem[k+1], \dots \text{ happier } 43 \rangle;
     o, vmem[p].breakcount = h, vmem[p].val = 0;
     k = vmem[p].pos\_start, kk = vmem[p].neg\_start;
     \langle \text{ Make clauses } tmem[k], tmem[k+1], \dots \text{ sadder } 44 \rangle;
  } else {
     o, k = vmem[p].pos\_start, kk = vmem[p].neg\_start;
     \langle \text{ Make clauses } tmem[k], tmem[k+1], \dots \text{ happier } 43 \rangle;
     o, vmem[p].breakcount = h, vmem[p].val = 1;
     o, k = kk, kk = vmem[p+1].pos\_start;
     \langle \text{ Make clauses } tmem[k], tmem[k+1], \dots \text{ sadder } 44 \rangle;
This code is used in section 37.
43. \langle \text{ Make clauses } tmem[k], tmem[k+1], \dots \text{ happier } 43 \rangle \equiv
  for (h = 0; k < kk; k++) {
     ooo, c = tmem[k], j = cmem[c].tcount, cmem[c].tcount = j + 1;
     if (j \le 1) {
       if (j) \langle Decrease the breakcount of c's critical variable 45\rangle
                     /* delete c from false list */
           oo, i = cmem[c].fplace, q = cmem[--fcount].fslot;
           oo, cmem[i].fslot = q, cmem[q].fplace = i;
                     /* the flipped literal is now critical */
  }
This code is used in section 42.
44. \langle \text{ Make clauses } tmem[k], tmem[k+1], \dots \text{ sadder } 44 \rangle \equiv
  for ( ; k < kk; k++)  {
     ooo, c = tmem[k], j = cmem[c].tcount - 1, cmem[c].tcount = j;
     if (j \le 1) {
       if (j) (Increase the breakcount of c's critical variable 46)
                    /* insert c into false list */
           oo, cmem[fcount].fslot = c, cmem[c].fplace = fcount +++;
     }
This code is used in section 42.
```

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```
We know that c has exactly one true literal at this moment.
\langle Decrease the breakcount of c's critical variable 45\rangle \equiv
     for (o, i = cmem[c].start; ; i++) {
       o, q = mem[i];
       if (o, value(q)) break;
     o, vmem[q \gg 1].breakcount ---;
  }
This code is used in section 43.
46. As an experiment, I'm swapping the first true literal into the first position of its clause, hoping that
subsequent "decrease" loops will thereby be shortened.
(Increase the breakcount of c's critical variable 46) \equiv
  {
     for (o, ii = i = cmem[c].start; ; i++) {
       o, q = mem[i];
       if (o, value(q)) break;
    o, vmem[q \gg 1].breakcount ++;
    if (i \neq ii) oo, mem[i] = mem[ii], mem[ii] = q;
This code is used in section 44.
47. \langle Print the initial guess 47 \rangle \equiv
     fprintf(stderr, "\_initial\_guess");
    for (k = 0; k < vars; k++) fprintf (stderr, "_\%s\%.8s", vmem[k].val?"": "~", nmem[k].ch8);
    fprintf(stderr, "\n");
This code is used in section 37.
    \langle \text{ Print a solution and goto } done | 48 \rangle \equiv
     for (k = 0; k < vars; k++) printf("u')s''.8s", vmem[k].val?"": "~", nmem[k].ch8);
     printf("\n");
    if (verbose & show_basics) fprintf(stderr, "!SAT!\n");
    goto done;
This code is used in section 37.
```

20 INDEX SAT8  $\S49$ 

## 49. Index.

 $argc: \underline{3}, 5.$  $i: \underline{3}$ . ii: 3, 34, 46.argv: 3, 5. $bad\_cell: 8, 12, 14, 20.$ imems:  $3, \underline{4}$ .  $bad\_tmp\_var: 8, 12, 13, 21.$ j:  $\underline{3}$ . best: 25, 32, 41.  $k: \underline{3}.$ breakcount: 24, 27, 38, 39, 41, 42, 45, 46. *kk*: 3, 32, 34, 39, 41, 42, 43, 44. buf: 8, 9, 10, 11, 16, 19, 30.  $l: \ \underline{3}, \ \underline{26}, \ \underline{27}, \ \underline{28}.$  $\textit{buf\_size}\colon \quad \underline{4}, \ 5, \ 9, \ 10.$  $ll: \ \underline{3}, \ \underline{26}, \ \underline{27}, \ \underline{28}, \ 39.$ bytes:  $3, \underline{4}, 30, 32.$  $lng: \underline{6}, 16, 17, 35.$  $c: \ \underline{3}, \ \underline{26}, \ \underline{27}, \ \underline{28}.$  $main: \underline{3}.$ cell: 7, 14, 20, 36. malloc: 9, 13, 14, 30, 32. cells: 8, 10, 11, 22, 30, 32, 34.  $maxsteps: \underline{4}, 5, 37.$  $cells\_per\_chunk$ : 7, 14, 20. maxthresh: 4, 5, 37. **chunk**: 7, 8, 14, 20.  $maxtrials: \underline{4}, 5, 37.$  $chunk\_struct\colon \ \ \underline{7}.$ mem: 24, 25, 26, 27, 30, 32, 34, 39, 41, 45, 46. *ch8*: <u>6, 16, 26, 27, 28, 41, 47, 48.</u> mems:  $3, \underline{4}, 5, 37, 38, 40, 41.$ clause: 24, 25, 30. $name: \underline{6}, 16, 17, 35.$  $clause\_done: 11.$ neg\_start: 24, 28, 31, 33, 34, 42. clauses: 8, 10, 11, 12, 16, 19, 22, 30, 32, 39.  $new\_chunk: \underline{14}.$ *cmem*: 24, <u>25,</u> 26, 27, 30, 32, 34, 39, 40, 41,  $new\_vchunk: \underline{13}.$ 43, 44, 45, 46.  $next: \underline{6}, 17.$ nmem: 24, 25, 26, 27, 28, 30, 35, 41, 47, 48.  $cur\_cell: 8, 12, 14, 20, 33, 36.$  $cur\_chunk: \underline{8}, 14, 20, 36.$  $nongreedprob: \underline{4}, 5, 37.$  $cur\_mcell$ : 25, 32, 33. nongreed thresh: 4, 37, 41.cur\_tmp\_var: 8, 12, 13, 16, 17, 21, 35, 36. null clauses: 8, 10, 11, 19. $cur\_vchunk: \underline{8}, 13, 21, 36.$  $o: \underline{3}.$ delta:  $\underline{4}$ ,  $\underline{5}$ ,  $\underline{37}$ . octa:  $\underline{6}$ , 25, 30. done: 37, 48.  $old\_chunk: \underline{20}.$  $old\_vchunk: \underline{21}.$  $empty\_clause: 11, 16, 18.$ exit: 5, 9, 10, 11, 13, 14, 16, 30, 32, 36. oo: <u>3,</u> 33, 39, 41, 42, 43, 44, 46. fcount: 3, 24, 37, 39, 40, 43, 44. ooo:  $\underline{3}$ , 34, 41, 43, 44. fgets: 10. $p: \ \ \underline{3}, \ \underline{12}.$ fplace: 24, 39, 43, 44. pos\_start: 24, 28, 31, 33, 34, 42. fprintf: 3, 5, 9, 10, 11, 13, 14, 16, 19, 22, 26, 27, prev: 6, 7, 13, 14, 20, 21, 36. 28, 30, 32, 36, 37, 40, 41, 47, 48.  $print\_clause$ : 26. free: 20, 21, 30, 36.  $print\_literal\_uses$ : fslot: 24, 39, 40, 43, 44.  $print\_unsat\_clause$ : 27, 40. printf: 37, 48.  $g: \underline{3}.$  $gb\_init\_rand$ : 9.  $q: \underline{3}$ .  $gb\_next\_rand$ : 4, 15, 38, 41. r: 3.  $qb\_rand$ : 4.  $random\_seed: \underline{4}, 5, 9.$  $gb\_unif\_rand$ : 40, 41. serial: 6, 17, 33. $got_l$ :  $\underline{41}$ .  $show\_basics: 3, \underline{4}, 37, 48.$ greedy:  $\underline{41}$ .  $show\_choices: \underline{4}, 37, 40, 41.$  $show\_details: \underline{4}, 37, 41.$  $h: \quad \underline{3}.$  $hack\_clean: \underline{33}.$  $show\_qory\_details$ : 4, 40. sscanf: 5.  $hack_in: \underline{12}.$ stamp: 6, 12, 17, 18.  $hack\_out$ : 33. hash: 8, 9, 17, 30. start: 24, 26, 27, 32, 34, 39, 41, 45, 46.  $hash\_bits: 8, 15, 16.$ stderr: 3, 5, 9, 10, 11, 13, 14, 16, 19, 22, 26, 27, hbits:  $\underline{4}$ , 5, 9, 10, 16. 28, 30, 32, 36, 37, 40, 41, 47, 48.

 $\S49$  SAT8 INDEX 21

```
stdin: 2, 8, 10.
step\colon \ \ 3,\ \underline{25},\ 37.
strlen: 10.
tcount: 24, 39, 43, 44.
thresh: \underline{4}, 5, 37.
timeout: \underline{4}, 5, 37.
tmem: 24, \underline{25}, 28, 30, 34, 43, 44.
tmp\_var: \underline{6}, 7, 8, 9, 12, 33.
tmp\_var\_struct: \underline{6}.
trial: 3, \underline{25}, 37.
uint: 3, 6, 8, 24, 25, 26, 27, 28, 30, 32.
ullng: <u>3</u>, 4, 8, 12, 25, 33.
u2: \underline{6}.
val: <u>24</u>, 38, 41, 42, 47, 48.
value \colon \ \ \underline{24}, \ 26, \ 28, \ 39, \ 45, \ 46.
var\colon \quad \underline{6},\ 13,\ 21,\ 36.
variable: \underline{24}, \underline{25}, \underline{30}.
vars: 8, 10, 17, 22, 30, 31, 34, 35, 37, 38, 47, 48.
vars\_per\_vchunk: \underline{6}, 13, 21.
vchunk: \underline{6}, 8, 13, 21.
vchunk_struct: \underline{6}.
verbose: 3, \underline{4}, 5, 37, 40, 41, 48.
vmem: 24, 25, 27, 28, 30, 31, 33, 34, 38, 39,
      41, 42, 45, 46, 47, 48.
```

22 NAMES OF THE SECTIONS SAT8

```
(Allocate the main arrays 30) Used in section 29.
 Check consistency 36 \ Used in section 29.
 Choose a literal l in c 41 \quad Used in section 37.
 Choose a random unsatisfied clause, c 40 \ Used in section 37.
 Copy all the temporary cells to the mem and cmem arrays in proper format 32 \ Used in section 29.
 Copy all the temporary variable nodes to the nmem array in proper format 35 \ Used in section 29.
 Decrease the breakcount of c's critical variable 45 \rangle Used in section 43.
 Find cur\_tmp\_var \rightarrow name in the hash table at p \mid 17 Used in section 12.
 Flip the value of l 42 \rightarrow Used in section 37.
 Global variables 4, 8, 25 Used in section 3.
(Handle a duplicate literal 18) Used in section 12.
(Increase the breakcount of c's critical variable 46) Used in section 44.
(Initialize all values 38) Used in section 37.
(Initialize everything 9, 15) Used in section 3.
(Initialize the clause data structures 39) Used in section 37.
\langle \text{ Initialize the } pos\_start \text{ and } neg\_start \text{ fields } 31 \rangle Used in section 29.
\langle \text{ Input the clause in } buf 11 \rangle Used in section 10.
\langle \text{Input the clauses } 10 \rangle Used in section 3.
(Insert the cells for the literals of clause c 33)
                                                         Used in section 32.
(Install a new chunk 14) Used in section 12.
(Install a new vchunk 13) Used in section 12.
\langle \text{ Make clauses } tmem[k], tmem[k+1], \dots \text{ happier } 43 \rangle Used in section 42.
 Make clauses tmem[k], tmem[k+1], ... sadder 44 Used in section 42.
(Move cur_cell backward to the previous cell 20) Used in sections 19 and 33.
\langle \text{Move } cur\_tmp\_var \text{ backward to the previous temporary variable 21} \rangle Used in section 35.
\langle \text{ Print a solution and } \mathbf{goto} \text{ } done \text{ } 48 \rangle Used in section 37.
(Print the initial guess 47) Used in section 37.
\langle \text{ Process the command line 5} \rangle Used in section 3.
Put the variable name beginning at buf[j] in cur\_tmp\_var \rightarrow name and compute its hash code h 16 \quad Used
     in section 12.
(Remove all variables of the current clause 19) Used in section 11.
(Report the successful completion of the input phase 22) Used in section 3.
\langle Scan and record a variable; negate it if i \equiv 1 \mid 12 \rangle Used in section 11.
(Set up the main data structures 29) Used in section 3.
 Set up the tmem array 34 \rangle Used in section 29.
\langle Solve the problem 37 \rangle Used in section 3.
(Subroutines 26, 27, 28) Used in section 3.
\langle \text{ Type definitions } 6, 7, 24 \rangle Used in section 3.
```

## SAT8

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