SQLSELECT C.sid FROM Catalog C WHERE NOT EXISTS (SELECT P.pid Parts P FROM WHERE P.color = 'red' AND (NOT EXISTS (SELECT C1.sid FROM Catalog C1 WHERE C1.sid = C.sid AND C1.pid = P.pid)))7. ■ RA $(\pi_{sid,pid}Catalog)/(\pi_{pid}\sigma_{color='red'\vee color='green'}Parts)$ TRC  $\{T \mid \exists T1 \in Catalog(\forall X \in Parts((X.color \neq `red') \})\}$  $\land X.color \neq `green') \lor \exists T2 \in Catalog$ 

■ DRC

$$\{\langle X \rangle \mid \langle X, Y, Z \rangle \in Catalog \land \forall \langle A, B, C \rangle \in Parts \\ ((C \neq `red' \land C \neq `green') \lor \exists \langle P, Q, R \rangle \in Catalog \\ (Q = A \land P = X))\}$$

 $(T2.pid = X.pid \land T2.sid = T1.sid)) \land T.sid = T1.sid)\}$ 

■ SQL

```
\rho(R1, ((\pi_{sid,pid}Catalog)/(\pi_{pid}\sigma_{color='red'}Parts)))
\rho(R2, ((\pi_{sid,pid}Catalog)/(\pi_{pid}\sigma_{color='green'}Parts)))
R1 \cup R2
```

```
TRC
                  \{T \mid \exists T1 \in Catalog((\forall X \in Parts)\}\}
                  (X.color \neq `red' \lor \exists Y \in Catalog(Y.pid = X.pid \land Y.sid = T1.sid))
                  \forall \forall Z \in Parts(Z.color \neq `green' \lor \exists P \in Catalog
                  (P.pid = Z.pid \land P.sid = T1.sid))) \land T.sid = T1.sid)\}
         DRC
                        \{\langle X \rangle \mid \langle X, Y, Z \rangle \in Catalog \land (\forall \langle A, B, C \rangle \in Parts)\}
                        (C \neq `red' \lor \exists \langle P, Q, R \rangle \in Catalog(Q = A \land P = X))
                        \forall \forall \langle U, V, W \rangle \in Parts(W \neq `green' \lor \langle M, N, L \rangle \in Catalog
                        (N = U \land M = X)))\}
         SQL
         SELECT C.sid
         FROM
                    Catalog C
         WHERE
                    (NOT EXISTS (SELECT P.pid
                                       FROM
                                                 Parts P
                                       WHERE P.color = 'red' AND
                                       (NOT EXISTS (SELECT C1.sid
                                                         FROM
                                                                    Catalog C1
                                                         WHERE C1.sid = C.sid AND
                                                                    C1.pid = P.pid))))
                    OR ( NOT EXISTS (SELECT P1.pid
                                            FROM
                                                       Parts P1
                                            WHERE P1.color = 'green' AND
                                            (NOT EXISTS (SELECT C2.sid
                                                                          Catalog C2
                                                               FROM
                                                               WHERE
                                                                         C2.sid = C.sid AND
                                                                          C2.pid = P1.pid))))
9.
         RA
                  \rho(R1, Catalog)
                  \rho(R2, Catalog)
                  \pi_{R1.sid,R2.sid}(\sigma_{R1.pid=R2.pid \land R1.sid \neq R2.sid \land R1.cost > R2.cost}(R1 \times R2))
         TRC
                           \{T \mid \exists T1 \in Catalog(\exists T2 \in Catalog)\}
                                     (T2.pid = T1.pid \land T2.sid \neq T1.sid
                                      \land T2.cost < T1.cost \land T.sid2 = T2.sid)
                                      \land T.sid1 = T1.sid)
```

DRC

$$\{ \langle X, P \rangle \mid \langle X, Y, Z \rangle \in Catalog \land \exists P, Q, R$$
 
$$(\langle P, Q, R \rangle \in Catalog \land Q = Y \land P \neq X \land R < Z) \}$$

■ SQL

 $\begin{array}{ll} \mathtt{SELECT} & C1.\mathrm{sid}, \ C2.\mathrm{sid} \\ \mathtt{FROM} & Catalog \ C1, \ Catalog \ C2 \\ \mathtt{WHERE} & C1.\mathrm{pid} = C2.\mathrm{pid} \ \mathtt{AND} \ \ C1.\mathrm{sid} \neq C2.\mathrm{sid} \\ \mathtt{AND} & C1.\mathrm{cost} > C2.\mathrm{cost} \\ \end{array}$ 

10. ■ RA

$$\begin{split} & \rho(R1, Catalog) \\ & \rho(R2, Catalog) \\ & \pi_{R1.pid} \sigma_{R1.pid = R2.pid \land R1.sid \neq R2.sid} (R1 \times R2) \end{split}$$

■ TRC

$$\begin{split} \{T \mid \exists T1 \in Catalog (\exists T2 \in Catalog \\ (T2.pid = T1.pid \land T2.sid \neq T1.sid) \\ \land T.pid = T1.pid) \} \end{split}$$

■ DRC

$$\{\langle X \rangle \mid \langle X, Y, Z \rangle \in Catalog \land \exists A, B, C (\langle A, B, C \rangle \in Catalog \land B = Y \land A \neq X)\}$$

■ SQL

$$\rho(R1, \pi_{sid}\sigma_{sname='YosemiteSham'}Suppliers)$$

$$\rho(R2, R1 \bowtie Catalog)$$

$$\rho(R3, R2)$$

$$\rho(R4(1 \rightarrow sid, 2 \rightarrow pid, 3 \rightarrow cost), \sigma_{R3.cost < R2.cost}(R3 \times R2))$$

$$\pi_{pid}(R2 - \pi_{sid,pid,cost}R4)$$

■ TRC

```
 \{T \mid \exists T1 \in Catalog(\exists X \in Suppliers \\ (X.sname ='YosemiteSham' \land X.sid = T1.sid) \land \neg (\exists S \in Suppliers \\ (S.sname ='YosemiteSham' \land \exists Z \in Catalog \\ (Z.sid = S.sid \land Z.cost > T1.cost))) \land T.pid = T1.pid)
```

■ DRC

$$\{ \langle Y \rangle \mid \langle X, Y, Z \rangle \in Catalog \land \exists A, B, C \\ (\langle A, B, C \rangle \in Suppliers \land C =' YosemiteSham' \land A = X) \\ \land \neg (\exists P, Q, R(\langle P, Q, R \rangle \in Suppliers \land R =' YosemiteSham' \\ \land \exists I, J, K(\langle I, J, K \rangle \in Catalog(I = P \land K > Z)))) \}$$

■ SQL

**Exercise 4.4** Consider the Supplier-Parts-Catalog schema from the previous question. State what the following queries compute:

```
1. \ \pi_{sname}(\pi_{sid}((\sigma_{color='red'}Parts)\bowtie (\sigma_{cost<100}Catalog))\bowtie Suppliers)
```

2. 
$$\pi_{sname}(\pi_{sid}((\sigma_{color='red'}Parts) \bowtie (\sigma_{cost < 100}Catalog) \bowtie Suppliers))$$

3. 
$$(\pi_{sname}((\sigma_{color='red'}Parts) \bowtie (\sigma_{cost<100}Catalog) \bowtie Suppliers)) \cap$$

$$(\pi_{sname}((\sigma_{color='green'}Parts) \bowtie (\sigma_{cost<100}Catalog) \bowtie Suppliers))$$

4. 
$$(\pi_{sid}((\sigma_{color='red'}Parts) \bowtie (\sigma_{cost<100}Catalog) \bowtie Suppliers)) \cap$$
  
 $(\pi_{sid}((\sigma_{color='qreen'}Parts) \bowtie (\sigma_{cost<100}Catalog) \bowtie Suppliers))$ 

5. 
$$\pi_{sname}((\pi_{sid,sname}((\sigma_{color='red'}Parts) \bowtie (\sigma_{cost<100}Catalog) \bowtie Suppliers)) \cap (\pi_{sid,sname}((\sigma_{color='green'}Parts) \bowtie (\sigma_{cost<100}Catalog) \bowtie Suppliers)))$$

Answer 4.4 The statements can be interpreted as:

- 1. Find the Supplier names of the suppliers who supply a red part that costs less than 100 dollars.
- 2. This Relational Algebra statement does not return anything because of the sequence of projection operators. Once the sid is projected, it is the only field in the set. Therefore, projecting on sname will not return anything.
- 3. Find the Supplier names of the suppliers who supply a red part that costs less than 100 dollars and a green part that costs less than 100 dollars.
- 4. Find the Supplier ids of the suppliers who supply a red part that costs less than 100 dollars and a green part that costs less than 100 dollars.
- 5. Find the Supplier names of the suppliers who supply a red part that costs less than 100 dollars and a green part that costs less than 100 dollars.

#### Exercise 4.5 Consider the following relations containing airline flight information:

```
Flights(<u>flno: integer</u>, from: string, to: string,

<u>distance: integer</u>, departs: time, arrives: time)

Aircraft(<u>aid: integer</u>, aname: string, cruisingrange: integer)

Certified(<u>eid: integer</u>, aid: integer)

Employees(eid: integer, ename: string, salary: integer)
```

Note that the Employees relation describes pilots and other kinds of employees as well; every pilot is certified for some aircraft (otherwise, he or she would not qualify as a pilot), and only pilots are certified to fly.

Write the following queries in relational algebra, tuple relational calculus, and domain relational calculus. Note that some of these queries may not be expressible in relational algebra (and, therefore, also not expressible in tuple and domain relational calculus)! For such queries, informally explain why they cannot be expressed. (See the exercises at the end of Chapter 5 for additional queries over the airline schema.)

- 1. Find the *eids* of pilots certified for some Boeing aircraft.
- 2. Find the *names* of pilots certified for some Boeing aircraft.
- 3. Find the *aids* of all aircraft that can be used on non-stop flights from Bonn to Madras.
- 4. Identify the flights that can be piloted by every pilot whose salary is more than \$100,000.
- 5. Find the names of pilots who can operate planes with a range greater than 3,000 miles but are not certified on any Boeing aircraft.

- 6. Find the *eids* of employees who make the highest salary.
- 7. Find the eids of employees who make the second highest salary.
- 8. Find the eids of employees who are certified for the largest number of aircraft.
- 9. Find the eids of employees who are certified for exactly three aircraft.
- 10. Find the total amount paid to employees as salaries.
- 11. Is there a sequence of flights from Madison to Timbuktu? Each flight in the sequence is required to depart from the city that is the destination of the previous flight; the first flight must leave Madison, the last flight must reach Timbuktu, and there is no restriction on the number of intermediate flights. Your query must determine whether a sequence of flights from Madison to Timbuktu exists for any input Flights relation instance.

**Answer 4.5** In the answers below RA refers to Relational Algebra, TRC refers to Tuple Relational Calculus and DRC refers to Domain Relational Calculus.

1. ■ RA

```
\pi_{eid}(\sigma_{aname=`Boeing'}(Aircraft\bowtie Certified))
```

■ TRC

```
\{C.eid \mid C \in Certified \land \\ \exists A \in Aircraft(A.aid = C.aid \land A.aname = `Boeing')\}
```

DRC

■ SQL

```
SELECT C.eid

FROM Aircraft A, Certified C

WHERE A.aid = C.aid AND A.aname = 'Boeing'
```

```
\pi_{ename}(\sigma_{aname='Boeing'}(Aircraft \bowtie Certified \bowtie Employees))
```

#### ■ TRC

```
\{E.ename \mid E \in Employees \land \exists C \in Certified \\ (\exists A \in Aircraft(A.aid = C.aid \land A.aname = `Boeing' \land E.eid = C.eid))\}
```

#### ■ DRC

```
 \begin{split} & \{ \langle EN \rangle \mid \langle Eid, EN, ES \rangle \in Employees \land \\ & \exists Ceid, Caid ( \langle Ceid, Caid \rangle \in Certified \land \\ & \exists Aid, AN, AR ( \langle Aid, AN, AR \rangle \in Aircraft \land \\ & Aid = Caid \land AN = `Boeing' \land Eid = Ceid) \} \end{split}
```

# ■ SQL

SELECT E.ename

 $\begin{array}{ll} {\tt FROM} & {\tt Aircraft\ A,\ Certified\ C,\ Employees\ E} \\ {\tt WHERE} & {\tt A.aid\ =\ C.aid\ AND\ A.aname\ =\ 'Boeing'\ AND\ E.eid\ =\ C.eid} \\ \end{array}$ 

#### 3. ■ RA

```
\rho(BonnToMadrid, \sigma_{from=`Bonn' \land to=`Madrid'}(Flights)) \\ \pi_{aid}(\sigma_{cruisingrange} >_{distance}(Aircraft \times BonnToMadrid))
```

#### ■ TRC

```
 \{A.aid \mid A \in Aircraft \land \exists F \in Flights \\ (F.from = `Bonn' \land F.to = `Madrid' \land A.cruisingrange > F.distance) \}
```

# DRC

```
 \begin{aligned} & \{Aid \mid \langle Aid, AN, AR \rangle \in Aircraft \land \\ & (\exists FN, FF, FT, FDi, FDe, FA(\langle FN, FF, FT, FDi, FDe, FA \rangle \in Flights \land \\ & FF = `Bonn' \land FT = `Madrid' \land FDi < AR)) \} \end{aligned}
```

# ■ SQL

SELECT A.aid

FROM Aircraft A, Flights F

WHERE F.from = 'Bonn' AND F.to = 'Madrid' AND A.cruisingrange > F.distance

```
\pi_{flno}(\sigma_{distance < cruising range \land salary > 100,000}(Flights \bowtie Aircraft \bowtie Certified \bowtie Employees)))
```

■ TRC  $\{F.flno \mid F \in Flights \land \exists A \in Aircraft \exists C \in Certified \exists E \in Employees(A.cruisingrange > F.distance \land E.salary > 100,000 \land A.aid = C.aid \land E.eid = C.eid)\}$ 

## DRC

```
 \begin{cases} FN \mid \langle FN, FF, FT, FDi, FDe, FA \rangle \in Flights \land \\ \exists Ceid, Caid (\langle Ceid, Caid \rangle \in Certified \land \\ \exists Aid, AN, AR(\langle Aid, AN, AR \rangle \in Aircraft \land \\ \exists Eid, EN, ES(\langle Eid, EN, ES \rangle \in Employees \\ (AR > FDi \land ES > 100,000 \land Aid = Caid \land Eid = Ceid) \end{cases}
```

■ SQL

SELECT E.ename

 $\begin{array}{ll} \text{FROM} & \text{Aircraft A, Certified C, Employees E, Flights F} \\ \text{WHERE} & \text{A.aid} = \text{C.aid AND E.eid} = \text{C.eid AND} \\ & \text{distance} < \text{cruisingrange AND salary} > 100,000 \\ \end{array}$ 

- 5.  $RA \quad \rho(R1, \pi_{eid}(\sigma_{cruisingrange})) (Aircraft \bowtie Certified)))$   $\pi_{ename}(Employees \bowtie (R1 \pi_{eid}(\sigma_{aname='Boeing'}(Aircraft \bowtie Certified))))$ 
  - TRC

```
 \{E.ename \mid E \in Employees \land \exists C \in Certified(\exists A \in Aircraft \ (A.aid = C.aid \land E.eid = C.eid \land A.cruisingrange > 3000)) \land \\ \neg (\exists C2 \in Certified(\exists A2 \in Aircraft(A2.aname = 'Boeing' \land C2.aid = A2.aid \land C2.eid = E.eid))) \}
```

DRC

```
 \begin{split} & \{ \langle EN \rangle \mid \langle Eid, EN, ES \rangle \in Employees \land \\ & \exists Ceid, Caid (\langle Ceid, Caid \rangle \in Certified \land \\ & \exists Aid, AN, AR (\langle Aid, AN, AR \rangle \in Aircraft \land \\ & Aid = Caid \land Eid = Ceid \land AR > 3000)) \land \\ & \neg (\exists Aid2, AN2, AR2 (\langle Aid2, AN2, AR2 \rangle \in Aircraft \land \\ & \exists Ceid2, Caid2 (\langle Ceid2, Caid2 \rangle \in Certified \\ & \land Aid2 = Caid2 \land Eid = Ceid2 \land AN2 = `Boeing'))) \} \end{split}
```

■ SQL

SELECT E.ename

```
\label{eq:fromcontinuous} \begin{array}{ll} \text{FROM} & \text{Certified C, Employees E, Aircraft A} \\ \text{WHERE} & \text{A.aid} = \text{C.aid AND E.eid} = \text{C.eid AND A.cruisingrange} > 3000 \\ \text{AND E.eid NOT IN (SELECT C2.eid} \\ \text{FROM Certified C2, Aircraft A2} \\ \text{WHERE C2.aid} = \text{A2.aid AND A2.aname} = \text{`Boeing'}) \\ \end{array}
```

## 6. ■ RA

The approach to take is first find all the employees who do not have the highest salary. Subtract these from the original list of employees and what is left is the highest paid employees.

```
\rho(E1, Employees) \\ \rho(E2, Employees) \\ \rho(E3, \pi_{E2.eid}(E1 \bowtie_{E1.salary} > E2.salary E2) \\ (\pi_{eid}E1) - E3
```

## ■ TRC

```
\{E1.eid \mid E1 \in Employees \land \neg (\exists E2 \in Employees(E2.salary > E1.salary))\}
```

## DRC

```
 \{ \langle Eid1 \rangle \mid \langle Eid1, EN1, ES1 \rangle \in Employees \land \\ \neg (\exists Eid2, EN2, ES2 (\langle Eid2, EN2, ES2 \rangle \in Employees \land ES2 > ES1)) \}
```

# ■ SQL

## 7. ■ RA

The approach taken is similar to the solution for the previous exercise. First find all the employees who do not have the highest salary. Remove these from the original list of employees and what is left is the highest paid employees. Remove the highest paid employees from the original list. What is left is the second highest paid employees together with the rest of the employees. Then find the highest paid employees of this new list. This is the list of the second highest paid employees.

```
\rho(E1, Employees)
\rho(E2, Employees)
\rho(E3, \pi_{E2.eid}(E1 \bowtie_{E1.salary} E2.salary E2)
\rho(E4, E2 \bowtie E3)
\rho(E5, E2 \bowtie E3)
\rho(E6, \pi_{E5.eid}(E4 \bowtie_{E1.salary} E5.salary E5)
(\pi_{eid}E3) - E6
```

■ TRC

```
 \{E1.eid \mid E1 \in Employees \land \exists E2 \in Employees(E2.salary > E1.salary \land \neg (\exists E3 \in Employees(E3.salary > E2.salary)))\}
```

■ DRC

```
 \begin{split} & \{ \langle Eid1 \rangle \mid \langle Eid1, EN1, ES1 \rangle \in Employees \land \\ & \exists Eid2, EN2, ES2 (\langle Eid2, EN2, ES2 \rangle \in Employees (ES2 > ES1) \\ & \land \neg (\exists Eid3, EN3, ES3 (\langle Eid3, EN3, ES3 \rangle \in Employees (ES3 > ES2)))) \} \end{split}
```

■ SQL

8. This cannot be expressed in relational algebra (or calculus) because there is no operator to count, and this query requires the ability to count up to a number that depends on the data. The query can however be expressed in SQL as follows:

#### 9. ■ RA

The approach behind this query is to first find the employees who are certified for at least three aircraft (they appear at least three times in the Certified relation). Then find the employees who are certified for at least four aircraft. Subtract the second from the first and what is left is the employees who are certified for exactly three aircraft.

```
\begin{split} &\rho(R1,Certified) \\ &\rho(R2,Certified) \\ &\rho(R3,Certified) \\ &\rho(R4,Certified) \\ &\rho(R4,Certified) \\ &\rho(R5,\pi_{eid}(\sigma_{(R1.eid=R2.eid=R3.eid)\land(R1.aid\neq R2.aid\neq R3.aid)}(R1\times R2\times R3))) \\ &\rho(R6,\pi_{eid}(\sigma_{(R1.eid=R2.eid=R3.eid=R4.eid)\land(R1.aid\neq R2.aid\neq R3.aid\neq R4.aid)}) \end{split}
```

```
\begin{array}{l} (R1 \times R2 \times R3 \times R4))) \\ R5 - R6 \end{array}
```

TRC

```
 \begin{aligned} &\{C1.eid \mid C1 \in Certified \land \exists C2 \in Certified (\exists C3 \in Certified \\ &(C1.eid = C2.eid \land C2.eid = C3.eid \land \\ &C1.aid \neq C2.aid \land C2.aid \neq C3.aid \land C3.aid \neq C1.aid \land \\ &\neg (\exists C4 \in Certified \\ &(C3.eid = C4.eid \land C1.aid \neq C4.aid \land \\ &C2.aid \neq C4.aid \land C3.aid \neq C4.aid))))\} \end{aligned}
```

DRC

■ SQL

```
SELECT C1.eid FROM Certified C1, Certified C2, Certified C3 WHERE (C1.eid = C2.eid AND C2.eid = C3.eid AND C3.aid \neq C1.aid \neq C2.aid AND C2.aid \neq C3.aid AND C3.aid \neq C1.aid) EXCEPT SELECT C4.eid FROM Certified C4, Certified C5, Certified C6, Certified C7, WHERE (C4.eid = C5.eid AND C5.eid = C6.eid AND C6.eid = C7.eid AND C4.aid \neq C5.aid AND C4.aid \neq C7.aid AND C5.aid \neq C7.aid AND C5.aid \neq C7.aid AND C6.aid \neq C7.aid \neq
```

This could also be done in SQL using COUNT.

10. This cannot be expressed in relational algebra (or calculus) because there is no operator to sum values. The query can however be expressed in SQL as follows:

```
\begin{array}{ll} \mathtt{SELECT} & \mathtt{SUM} \; (\mathtt{E.salaries}) \\ \mathtt{FROM} & \mathtt{Employees} \; \mathtt{E} \end{array}
```

11. This cannot be expressed in relational algebra or relational calculus or SQL. The problem is that there is no restriction on the number of intermediate flights. All of the query methods could find if there was a flight directly from Madison to Timbuktu and if there was a sequence of two flights that started in Madison and ended in Timbuktu. They could even find a sequence of n flights that started in Madison and ended in Timbuktu as long as there is a static (i.e., data-independent) upper bound on the number of intermediate flights. (For large n, this would of course be long and impractical, but at least possible.) In this query, however, the upper bound is not static but dynamic (based upon the set of tuples in the Flights relation).

In summary, if we had a static upper bound (say k), we could write an algebra or SQL query that repeatedly computes (upto k) joins on the Flights relation. If the upper bound is dynamic, then we cannot write such a query because k is not known when writing the query.

**Exercise 4.6** What is *relational completeness*? If a query language is relationally complete, can you write any desired query in that language?

**Answer 4.6** Relational completeness means that a query language can express all the queries that can be expressed in relational algebra. It does not mean that the language can express any desired query.

Exercise 4.7 What is an *unsafe* query? Give an example and explain why it is important to disallow such queries.

**Answer 4.7** An *unsafe* query is a query in relational calculus that has an infinite number of results. An example of such a query is:

$$\{S \mid \neg (S \in Sailors)\}\$$

The query is for all things that are not sailors which of course is everything else. Clearly there is an infinite number of answers, and this query is unsafe. It is important to disallow unsafe queries because we want to be able to get back to users with a list of all the answers to a query after a finite amount of time.