

Foundations of Audio Signal Processing

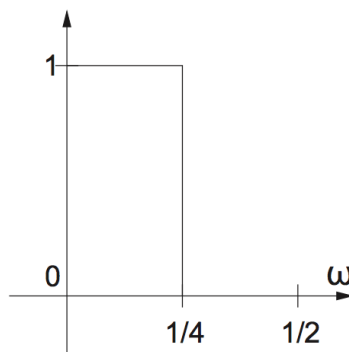
Exercise sheet 11

To be uploaded in eCampus till: 19-01-2019 22:00 (strict deadline)

Exercise 11.1

[4+2+2 = 8 points]

In this task, an ideal low pass filter along with its properties will be investigated. Consider an ideal low pass filter with cut-off frequency $\omega_0 = 1/4$, as illustrated below.



Prove that:

- (a) The filter coefficients of an ideal low pass filter with real coefficients and a cut-off frequency of $\omega_0 \in (0, \frac{1}{2})$ are given by

$$h(n) = 2\omega_0 \text{sinc}(2\omega_0 n), \quad n \in \mathbb{Z}.$$

- (b) C_h is not causal.
- (c) C_h has an infinite number of filter coefficients different from 0, i.e., C_h is IIR.

Exercise 11.2

[2 + 3 = 5 points]

Let us consider the Haar filters h and g defined as:

$$h(n) = \begin{cases} 0.5 & \text{if } n \in \{0, 1\}, \\ 0 & \text{otherwise.} \end{cases}$$

and

$$h(n) = \begin{cases} 0.5 & \text{if } n = 0, \\ -0.5 & \text{if } n = 1, \\ 0 & \text{otherwise.} \end{cases}$$

- (a) Find an explicit formula for the frequency responses of both h and g . (Hint: Calculate the Fourier transform by hand.)
- (b) The filters h and g have the properties that they divide the signals in low-frequency and high-frequency parts. Prove that by adding the two filtered signals, one gets back the original signal.

Exercise 11.3

[4 + 4 + 6 = 14 points]

- (a) Write a Matlab function which creates a lowpass filter (use the function *fircls*) that, if applied to a signal of sampling frequency 44100 Hz, lets the frequencies below 10000 Hz pass. Plot the frequency response of the above created filter.
- (b) Plot the frequency response of the filter (created in (a)) of order 10, 50 and 200. What happens if you change the order of the filter?
- (c) Write a Matlab function that performs the following:
 - Creates a sum of two sine waves of frequencies 5000 Hz and 15000 Hz. The sampling frequency has to be of 44100 Hz.
 - Applies the filter created in (a) to the sum of sine waves.
 - Plays back the original signal and the filtered version and plots their Fourier transforms.