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Part (a).

The atomic propositions are defined as

G : Ross wears green hat
S : Ross wears socks
Y : Ross wears yellow sweater
T : Ross wears tie
B : Ross wears blue hat.

Story in propositional logic is:

(1) $G \vee S$

(2) $(G \wedge Y) \Rightarrow \neg T \equiv \neg(G \wedge Y) \vee \neg T \quad (\because a \Rightarrow b \equiv \neg a \vee b)$
$\equiv \neg G \vee \neg Y \vee \neg T$

(3) $\neg(Y \vee S) \Rightarrow \neg G \equiv \neg(\neg(Y \vee S)) \vee \neg G \quad (\because a \Rightarrow b \equiv \neg a \vee b)$
$\equiv Y \vee S \vee \neg G \quad (\because \neg\neg a \equiv a)$

(4) $S \Rightarrow Y \equiv \neg S \vee Y \quad (\because a \Rightarrow b \equiv \neg a \vee b)$

(5) T

Thus (1), (2), (3), (4), (5) can be inferred from story.

Part(B)

Rewriting statements from Part (A)

(1) $G \vee S$

(2) $\neg G \vee \neg Y \vee \neg T$

(3) $Y \vee S \vee \neg G$

(4) $\neg S \vee Y$

(5) T

Will use resolution to deduce what else he wore yesterday.

From (1) & (3)

$G \vee S$ (1) $\quad$ $Y \vee S \vee \neg G$ (3)

$Y \vee S$ (6) $\quad$ $\neg S \vee Y$ (4)

$Y \rightarrow$ (7) $\Rightarrow$ (Thus he wore yellow sweater)

From (7) & (2)

Y (7) $\quad$ $\neg G \vee \neg Y \vee \neg T$ (2)

$\neg G \vee \neg T$ (8) $\quad$ T (5)

$\neg G \rightarrow$ (9) $\Rightarrow$ (Thus he didn't wear green hat)

From (9) & (1)

$\neg G$ (9) $\quad$ $G \vee S$ (1)

$S \rightarrow$ (10) $\Rightarrow$ (Thus he wore socks)

Thus (5), (7), (9), (10) defines.

$T \wedge Y \wedge \neg G \wedge S$

Thus yesterday along with tie (T) he wore yellow sweater (Y) and socks (S). But he didn't wear green hat (G).