

An Informal Introduction to Formal Methods in Robotics

Presented by Abhishek Kulkarni



What this is NOT about!

- Comprehensive Coverage of Topics in Formal Methods in Robotics
- Explanation of Prerequisites



Organization of Talk

Sections

- What can Formal Methods do?
- The Formal Methods...
- How Formal Methods work?
- Where to use Formal Methods?
- Open Problems
- Meet few other friends... (if time permits!)

Section I

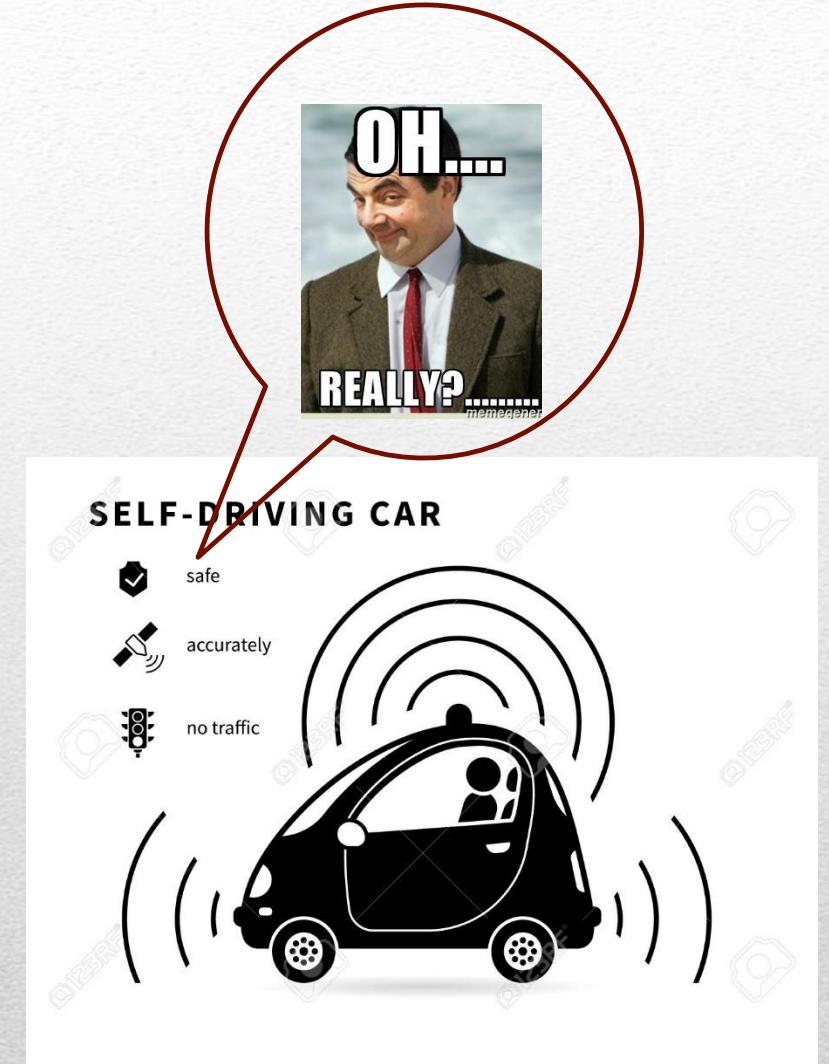
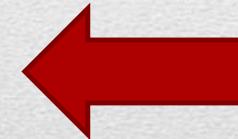
What can Formal Methods Do?

Have you wondered?

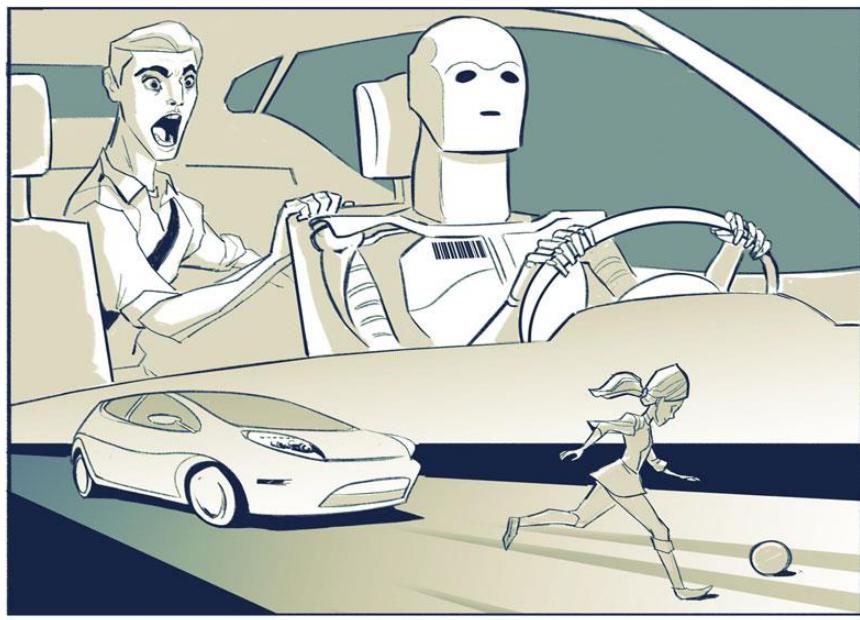
- Why your laptops work so reliably?
- Why your bank never misplaces a dime?
- If you can talk with your robot in English Language



The Big Question...



How to Avoid this?



COSTLY MISTAKE!!



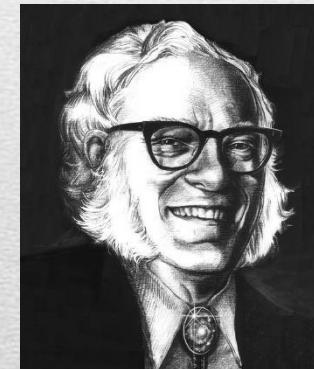
SUPER-INTELLIGENCE?

Reference: Robohub ([Link](#)) and I, Robot ([Link](#))

Formal Methods



- Guarantee Satisfaction of Specifications
 - Automatic Policy Synthesis
 - Talk to Robot in (Almost) English!
-
- Asimov is Happy!
 - Don't Kill Humans is Guaranteed 100%

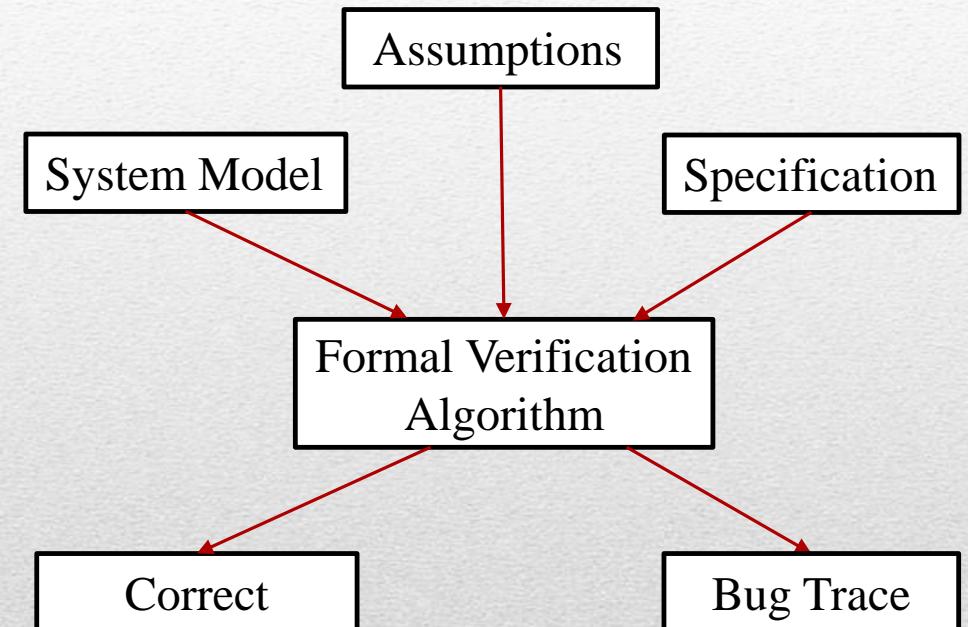


Section II

The Formal Methods . . .

Verification Problem

- We know
 - How world looks – Model
 - What robot should do – Specifications
- Question: Does any action-sequence of robot satisfy the specification?
- Remember Remember... Laptops!

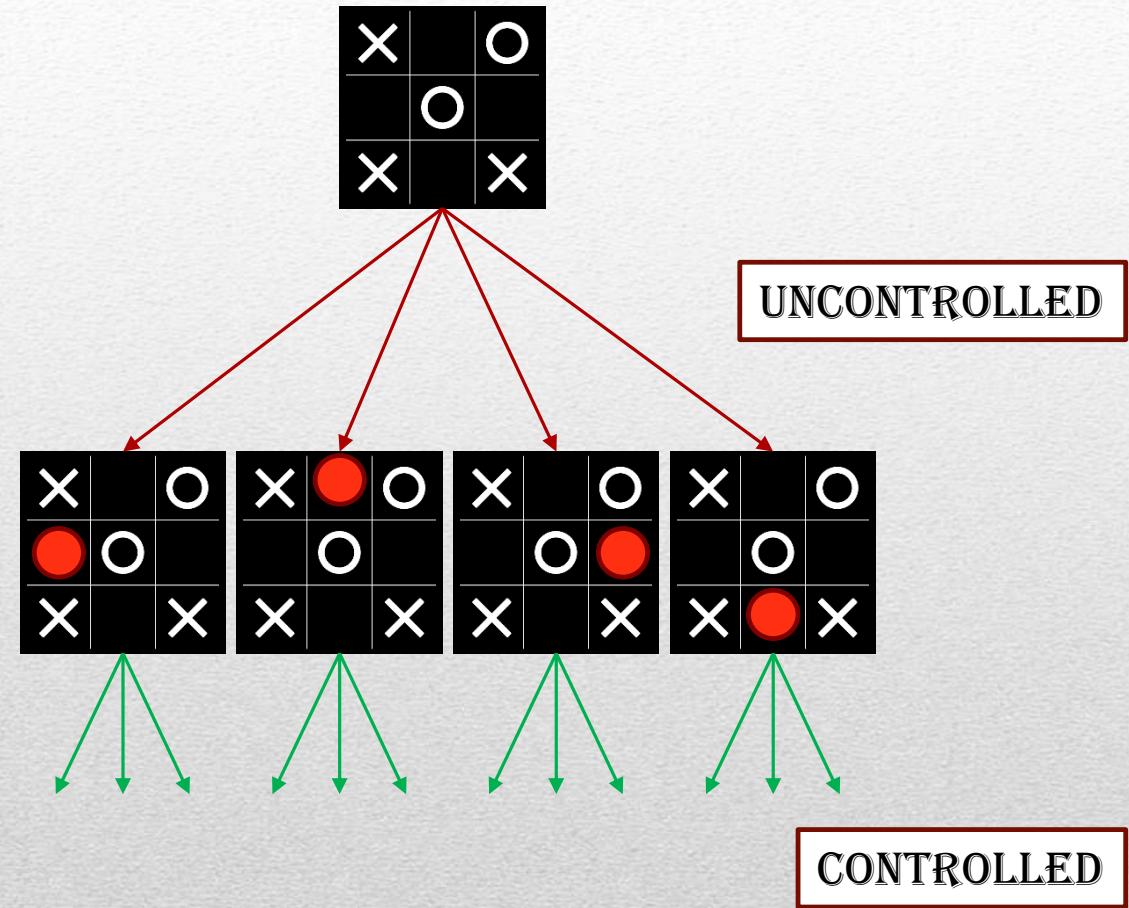


Can I Always Win?

- Classic Tic-Tac-Toe
**No matter what my opponent does,
Can I win?**

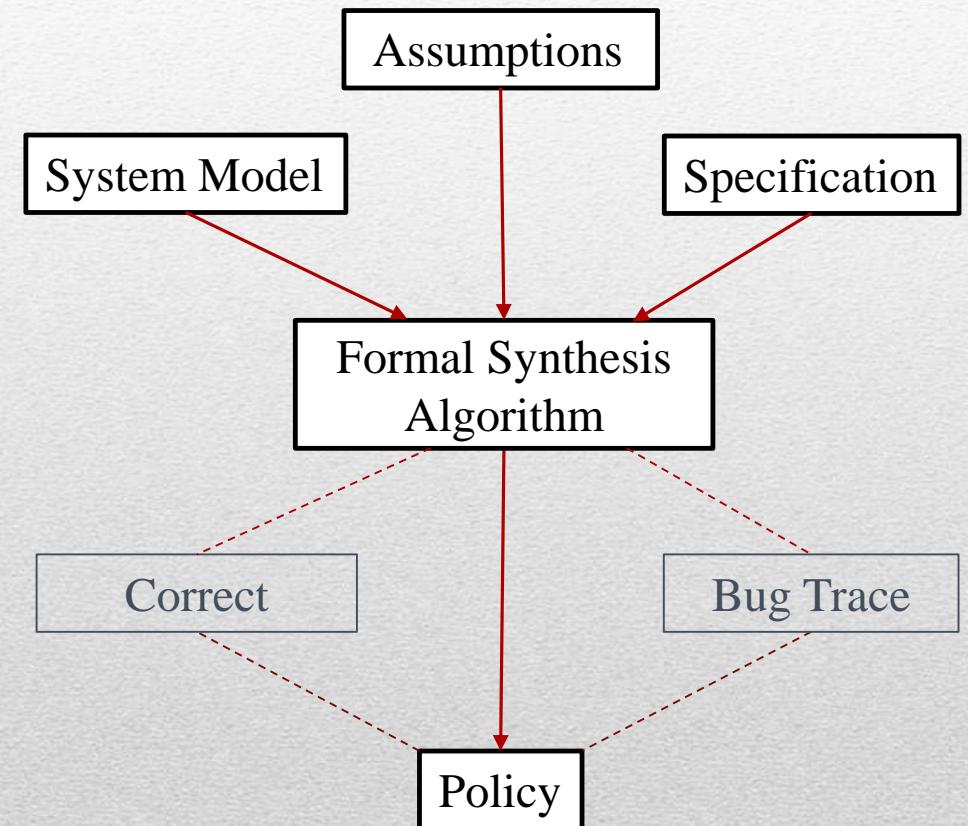
- Specification:
Reach at least 1 of winning states!

- Verification tells us: **What's guaranteed!**
- AND returns:
In what ways I can loose...



Synthesis Problem

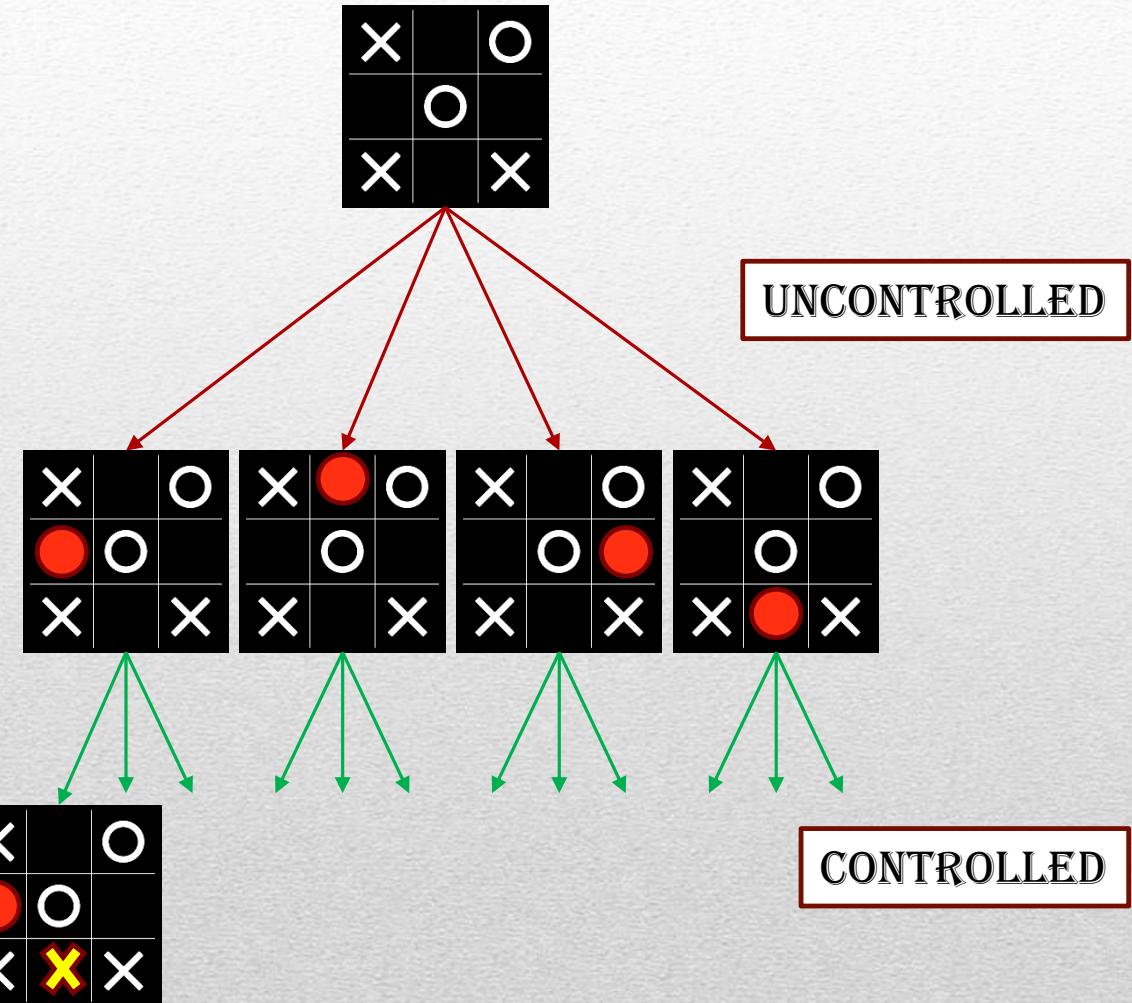
- We know
 - How world looks – Model
 - What robot should do – Specifications
- Question: What should robot do?



Tell me... How to Win!

- Classic Tic-Tac-Toe
**No matter what my opponent does,
Can I win?**
- Specification:
Reach at least 1 of winning states!
- Synthesis tells us:

PLAY LIKE THIS!



Section III

How Formal Methods Work?

Communication

- Language is fundamental to communication!
- Don't know some language – Interpreter
- Compilers!

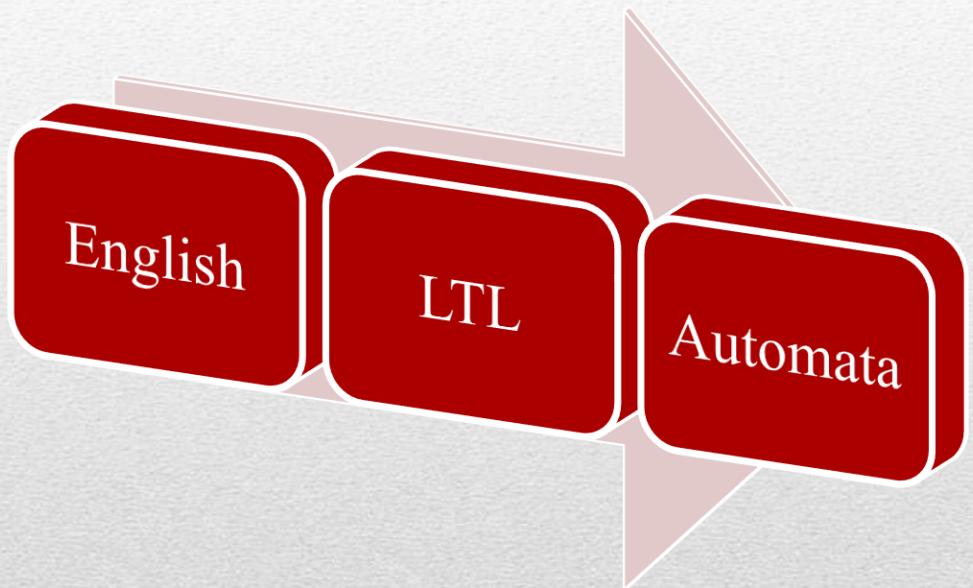


Image Reference: clip-art library ([Link](#))

Linear Temporal Logic (LTL)

LTL makes Humans and Robot's Happy!

- Human Language = Too many to write!
- Robot's Language = Automata!
- LTL is almost as expressive as English!
- Beauty: LTL → Automata is easy!



Linear Temporal Logic (LTL)

LTL makes Humans and Robot's Happy!

Example 1:

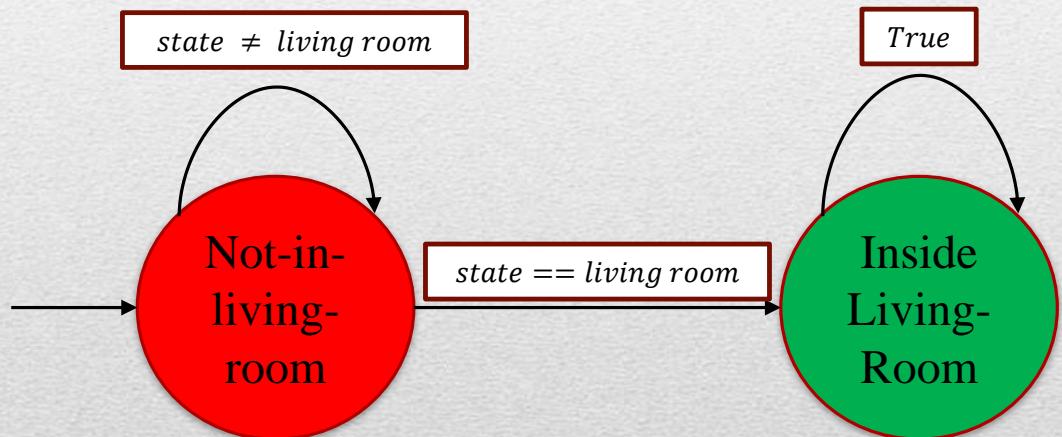
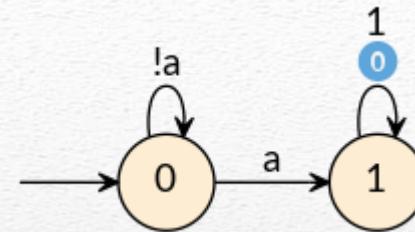
- English: Go to Living Room
- \sim LTL: Eventually (Robot in Living Room)
- LTL: $\diamond (state == \text{living room})$

Example 2:

- English: Go to Living Room AND Never Collide with Obstacle
- \sim LTL: Eventually (Robot in Living Room) AND Always (no-collision)
- LTL: $\diamond (state == \text{living room}) \wedge \square \neg \text{is_colliding}(\text{env}, \text{robot})$

Final Step: Automaton

- Recall: Automata is robot's language!
- Robot wants to reach to a ***final state!***
- Communication is complete!



◊ ($state == living\ room$)

How Robot Makes a Decision?

- **Model:** Understanding of world
 - Game Graph
 - Markov Decision Process
- **Objective:** Reach the Goal!
- **Easy Part:** Robot can choose what it want's to do!
- **Difficult Part:** It can't control what environment might do!

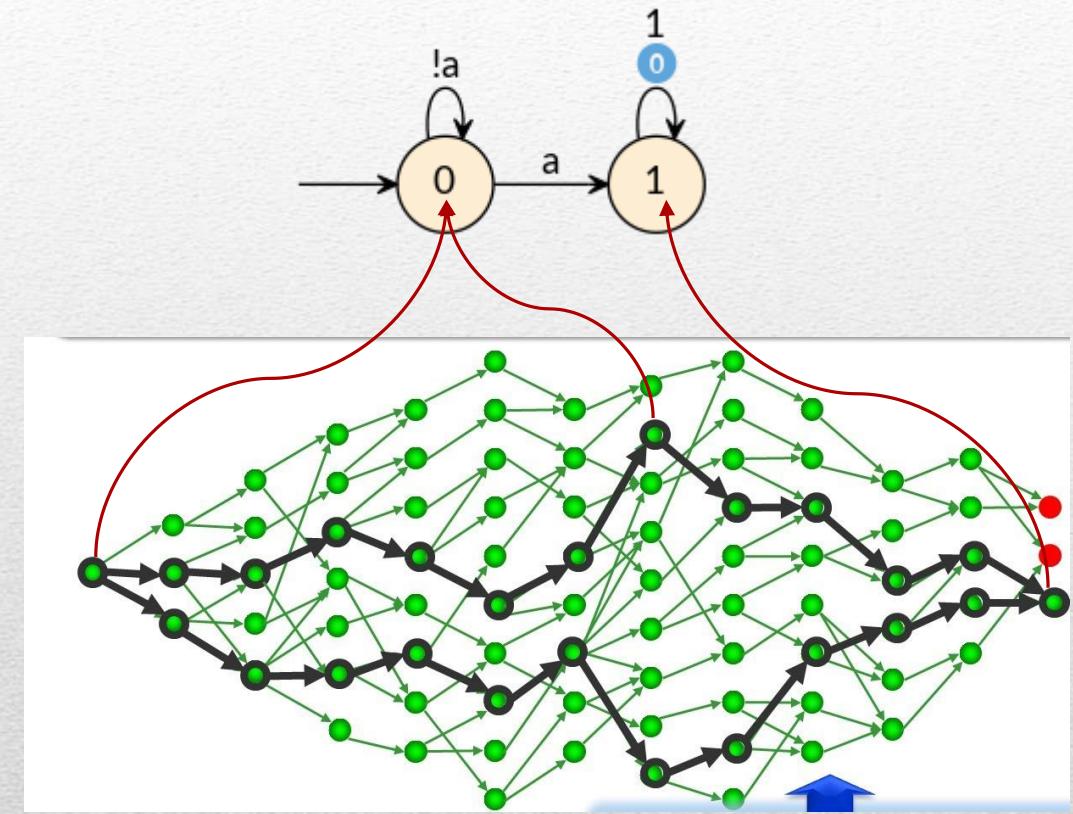


Image Reference: Mentor Graphics Questa Platform Video ([Link](#))

The beauty of FM

- It's a BAD IDEA to find and check all paths from start to end!
- GOOD IDEA: Somehow compress a complete path into a state!
- That's a Product Operation.
- And that's how life becomes easy!

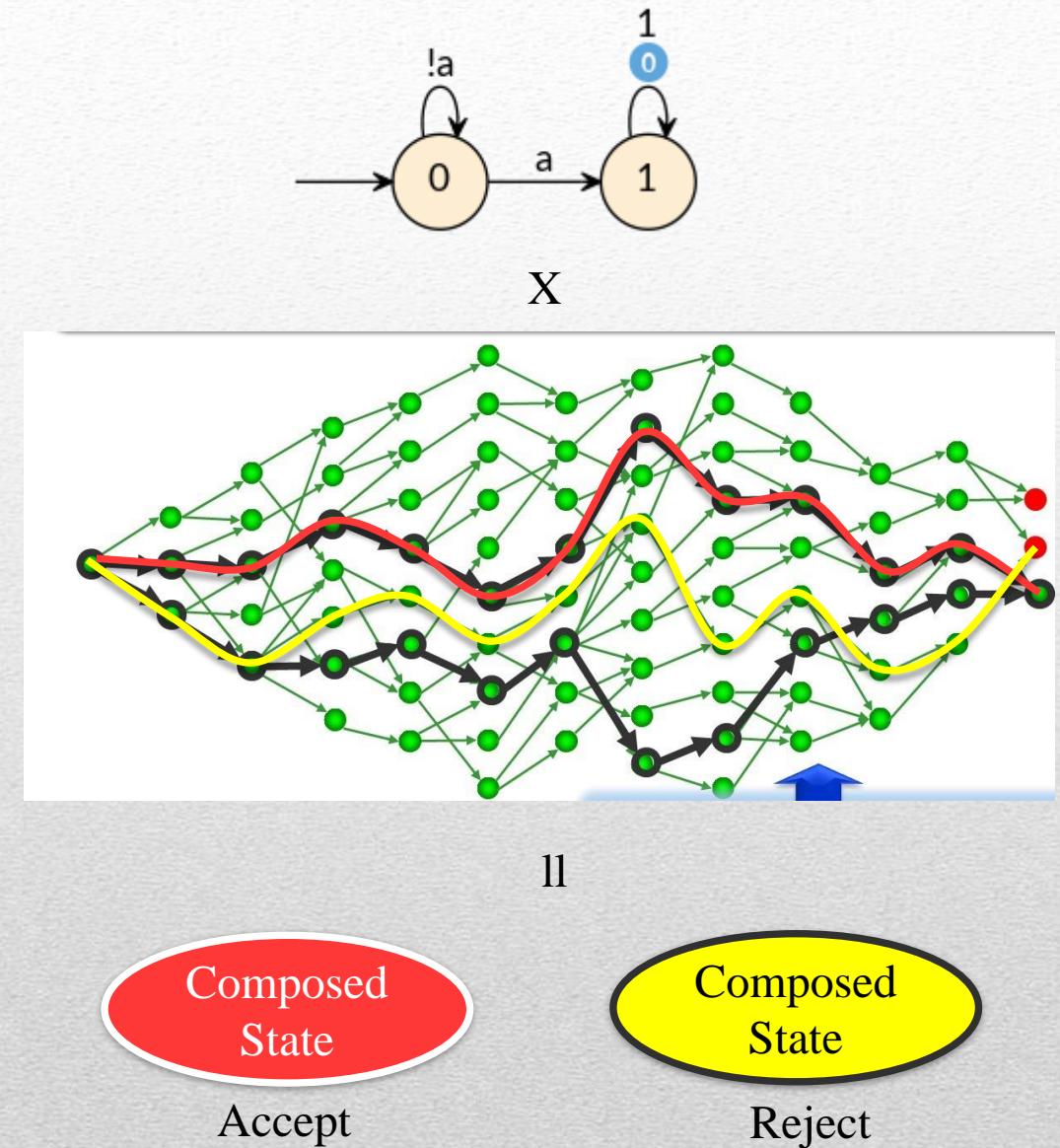


Image Reference: Mentor Graphics Questa Platform Video ([Link](#))

Section IV

Where to use Formal Methods?

Application 1: Autopilots

- TAM Flight 402
 - Autopilot Engaged Reverse Thrusters Incorrectly
 - Airplane has 100's of sensors
 - Autopilot is modularly designed.
 - How do we detect – accidental dependencies?
- Idea: Specify using (English-like) LTL what **shouldn't** happen with aircraft at any time



Video Reference: Air Crash Investigation Series

Application 2: Surgical Robots

- **Objective 1:** Safety – MUST ALWAYS HOLD!
 - Don't let needle move outside a particular volume
 - Or patient is history!
- **Objective 2:** Liveness – Satisfy if possible
 - Insert needle within a given area
 - And inject the medicine
- FMR allows full controller synthesis!

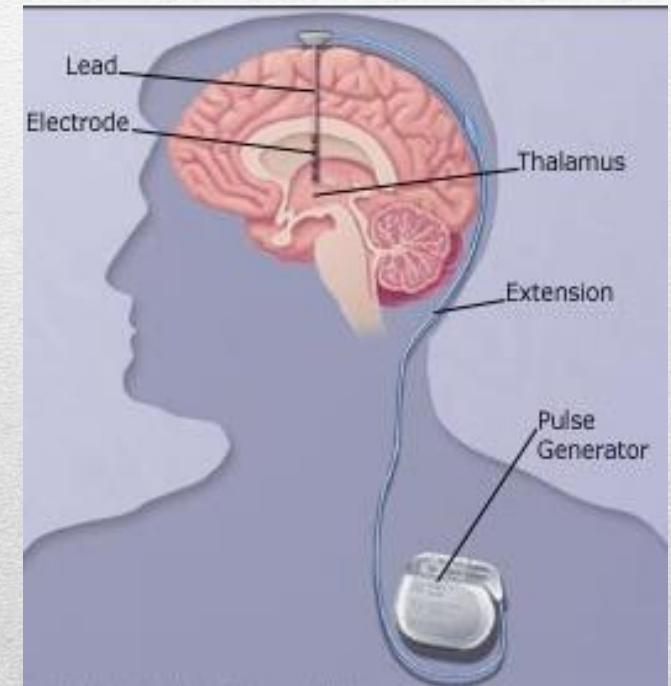


Image Reference: WebMD, Inc. ([Link](#))

Section V

Open Problems

Theoretical

- Thanks to Mathematicians and Computer Scientists in 50-100 years!
- **Problem 1:** State Explosion
 - Recall Product Operation ([Link](#))
- **Problem 2:** Parallelism
 - Mathematicians had different aims for FM development.
 - Roboticists want speed and accuracy!
 - We need to develop parallel algorithms that are provably-correct

Extending FMR

- Majority FMR studies are with
 - Linear Temporal Logic **or** Dynamic Differential Logic
 - Zero-Sum Games
- Problem 1: Different Logics
 - Explore use of different logics like Probabilistic Logics.
 - If you love physics – Try Quantum Logic!
- Problem 2:
 - Generally, cars on highway are not your enemies. But they have objective and can be aggressive! This is different game
 - Use FMR with a non-zero sum game models.

Apply FMR

- Majority FMR researchers are theoretical! Thrust something into reality!
- **Problem 1:** Toolkits
 - Develop Generalized and Efficient Toolkits
 - Modular, Abstract!
- **Problem 2:** Cyber-Physical Systems
 - Control – Automatic Controller Synthesis for Autonomous Car, Quadrotors etc.
 - Coordination – Multi-Agent Behaviors, Platoons etc.

Section V

Meet some friends... .

Concept 1: Abstraction

- Robot may reason at higher level – like Behaviors
- How can robot understand what behavior to use?
- Abstraction is mathematical tool to do this!

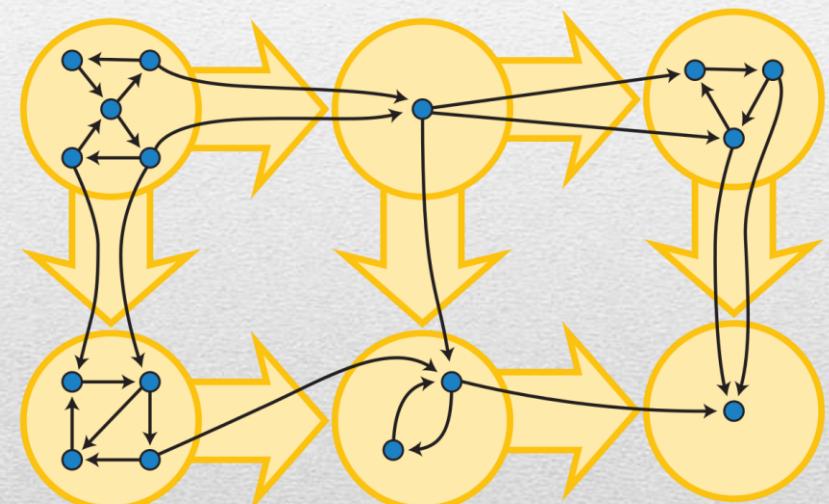
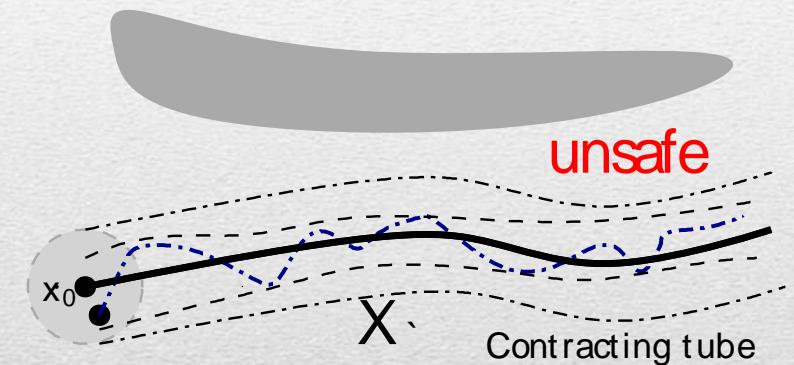


Image Reference: Wikipedia ([Link](#))

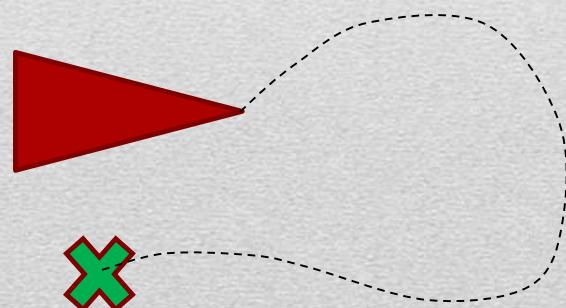
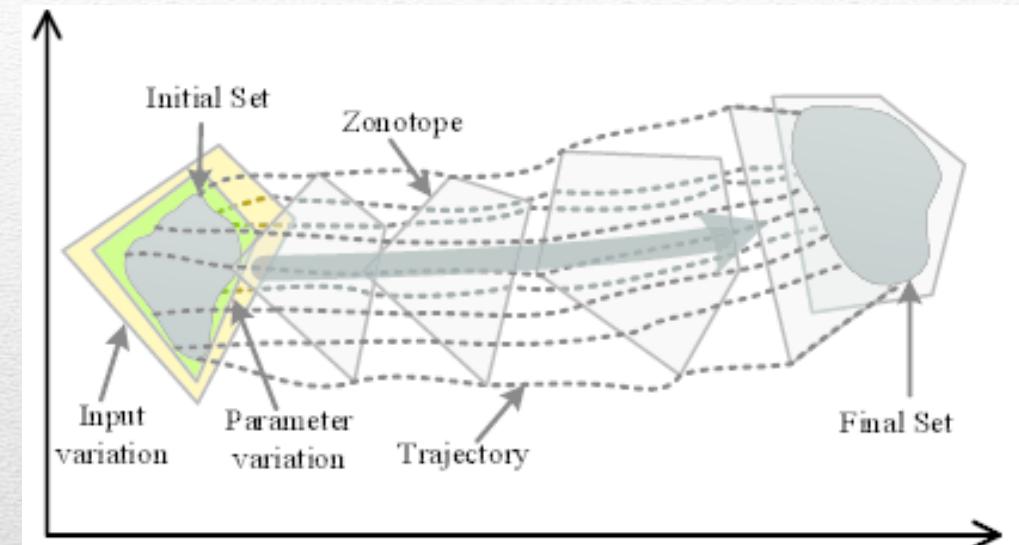
Concept 2: Contraction Theory

- Allows checking stability of trajectories!
- Intuition: Binary Search
 - Sandwich from above and below
 - And say Hurray!



Concept 3: Reachability

- Intuition:
 - As time progresses...
 - Which all points can I reach?
- Example:
 - Green point is not reachable in 1-step for the robot



Disclaimer

Ask Questions!

Thank You!