## Maths Assignment

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## **Problem Statement**

A G.P consists of an even number of terms. If the sum of all terms is 5 times the sum of terms occupying odd places, then find its common ratio.

## Solution

Parameter	Description
n	Number of terms in the G.P (positive even integer)
x(0)	first term in the G.P
r	common ratio in the G.P
x(n)	nth term in the G.P
X(z)	Z transform of X(n)

$$x(n) = x(0)r^n (1)$$

$$X(z) = \frac{x(0)}{1 - rz^{-1}} \tag{2}$$

$$S(z) = X(z)U(z) \tag{3}$$

$$S(z) = X(z)U(z)$$

$$= \frac{x(0)}{(1 - rz^{-1})(1 - z^{-1})} |z| > |r|$$
(4)

$$=\frac{x(0)(\frac{r}{1-rz^{-1}}-\frac{1}{1-z^{-1}})}{(r-1)}\tag{5}$$

The inverse of S(z) is s(n) which is:

$$s(n) = x(0)(\frac{r^{n+1} - 1}{r - 1})u(n)$$
(6)

v(n) = x(2m), v(0) = x(0), where m is an integer. if x(n) changed to x(n/k) then X(z) changes to  $X(z^k)$  as k = 1/2 we can write

$$V(z) = X(z^{1/2}) (7)$$

The sum of terms in odd places:

$$V_o(z) = \frac{v(0)}{1 - r^2 z^{-1}} \tag{8}$$

$$S_o(z) = V_o(z)U(z) \tag{9}$$

$$= \frac{v(0)}{(1 - r^2 z^{-1})(1 - z^{-1})} \quad |z| > |r| \tag{10}$$

$$= \frac{v(0)\left(\frac{r}{1-r^2z^{-1}} - \frac{1}{1-z^{-1}}\right)}{(r^2 - 1)} \tag{11}$$

The inverse of  $S_o(z)$  is  $s_o(n)$  which is:

$$s_o(n) = v(0) \left(\frac{r^{n+1} - 1}{r^2 - 1}\right) u(n)$$
(12)

Then from (6) and (11)

$$v(0)\left(\frac{r^{n+1}-1}{r-1}\right)u(n) = 5v(0)\left(\frac{r^{n+1}-1}{r^2-1}\right)u(n)$$

$$r^2 - 5r + 4 = 0$$
(13)

$$r^2 - 5r + 4 = 0 (14)$$

$$r = 1 \quad \text{or} \quad r = 4 \tag{15}$$