

The two persons will be in the same place if and only if they take the same number of times in their N chances, to move right. The probability that they each move to the right exactly k times is given by:

$$\binom{N}{k} 2^{-N}$$

Now we sum this from $k=0$ to N .

$$\begin{aligned}
 P &= \sum_{k=0}^N \left(\binom{N}{k} 2^{-N} \right)^2 \\
 &= \frac{\sum_{k=0}^N \binom{N}{k}^2}{2^{2N}} = \frac{2^N C_N}{2^{2N}}
 \end{aligned}$$