

$$\frac{\partial E}{\partial \text{out} H_1} = \frac{\partial E}{\partial \text{out} y} \times \frac{\partial \text{out} y}{\partial y} \times \frac{\partial y}{\partial \text{out} H_1}$$

$$= [-2(T - \text{out} y) \times \sigma(y)(1 - \sigma(y)) \times \omega_{11}^2]$$

$$\frac{\partial E}{\partial \text{out} H_2} = \frac{\partial E}{\partial \text{out} y} \times \frac{\partial \text{out} y}{\partial y} \times \frac{\partial y}{\partial \text{out} H_2}$$

$$= [-2(T - \text{out} y) \times \sigma(y)(1 - \sigma(y)) \times \omega_{12}^2]$$

$$\frac{\partial E}{\partial w_{11}} = \frac{\partial E}{\partial \text{out} H_1} \times \frac{\partial \text{out} H_1}{\partial H_1} \times \frac{\partial H_1}{\partial w_{11}}$$

$$= \left[\frac{\partial E}{\partial \text{out} H_1} * \sinh H_1 \cosh H_1 * x_1 \right]$$

$$\frac{\partial E}{\partial w_{21}} = \frac{\partial E}{\partial \text{out} H_1} \times \frac{\partial \text{out} H_1}{\partial H_1} \times \frac{\partial H_1}{\partial w_{21}}$$

$$= \left[\frac{\partial E}{\partial \text{out} H_1} * \sinh H_1 \cosh H_1 * x_2 \right]$$

$$\frac{\partial E}{\partial w_{12}} = \frac{\partial E}{\partial \text{out} H_2} \times \frac{\partial \text{out} H_2}{\partial H_2} \times \frac{\partial H_2}{\partial w_{12}}$$

$$= \left[\frac{\partial E}{\partial \text{out} H_2} * \sinh H_2 \cosh H_2 * x_1 \right]$$

$$\frac{\partial E}{\partial w_{22}} = \frac{\partial E}{\partial \text{out} H_2} \times \frac{\partial \text{out} H_2}{\partial H_2} \times \frac{\partial H_2}{\partial w_{22}}$$

$$= \left[\frac{\partial E}{\partial \text{out} H_2} * \sinh H_2 \cosh H_2 * x_2 \right]$$

So

$$w_{ij}^k \leftarrow w_{ij}^k + \eta \frac{\partial E}{\partial w_{ij}^k}$$

~~for all~~
 $\forall i, j \in \{1, 2\}$
 $k \in \{1, 2\}$