

Roll Number :

CS 228 Spring 2022

18-04-2022

Total Marks: 50

- *If you need to make any assumptions, state them clearly.*
- *If needed, you may cite results/proofs covered in class without reproducing them.*

1. [10 marks]

Consider the following formula where $Gtn, f, NonEmpty, L$ are predicates and convert it into FOL CNF.

$$\neg \exists n. \forall w. [Gtn(w) \Rightarrow \exists x, y, z. (f(x, y, z) = w \wedge NonEmpty(y) \wedge \neg Gtn(f(x, y)) \wedge (\forall k. L(x, y, z, k)))]$$

2. [5+5=10 marks]

Consider a CNF formula F equivalent to $p_1 \oplus \dots \oplus p_n$. F only contains variables p_1, \dots, p_n .

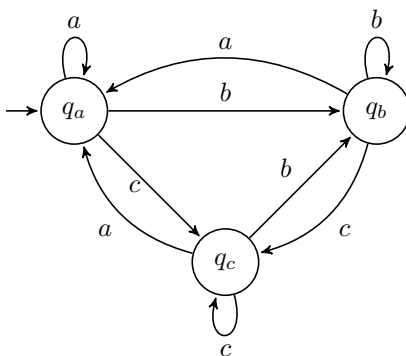
- (a) Show that the size of each clause in F is at least n .
- (b) Show that F has at least 2^{n-1} clauses.

3. [5 marks]

Write an MSO formula that captures all bipartite graphs. Remember that the signature allows only the binary relation E . Explain why your formula is correct.

4. [10 marks]

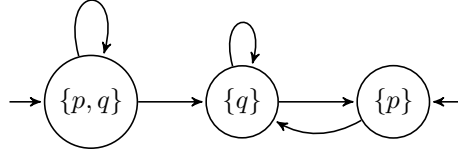
Consider the DBA given below.



- (a) What is the language accepted if q_c is the only good state?
- (b) Draw an NBA which is the complement of the DBA.

5. [3+5+2=10 marks]

Consider the transition system TS given below.



Let $\varphi = \Box(p \rightarrow \bigcirc(\Diamond\Box q))$. Does $TS \models \varphi$? To answer this, you must

- (a) draw an NBA $A_{\neg\varphi}$ for $\neg\varphi$,
 - (b) construct $TS' = TS \otimes A_{\neg\varphi}$,
 - (c) write an appropriate persistence property P_{pers} to be checked on TS' .
- Finally, your answer for TS satisfying (or not) φ must be linked to TS' satisfying (or not) P_{pers} .

6. [15 marks]

Write LTL formulae φ which capture each requirement.

Requirement	Your LTL formula φ
Finitely many a 's	
Infinitely many a 's and finitely many b 's	
Eventually a and eventually forever $\neg a$	
There is an a which is never eventually followed by two occurrences of b 's	
There is atleast one c , and b holds since the last occurrence of c	