

Q1. diff b/w registers and L1 cache as cache

- CPU can only directly access registers (as it is part of CPU memory)
- register memory is much smaller than faster access
- Data loaded in registers is dictated by program unlike L1 cache. This is the main/important/conceptual difference

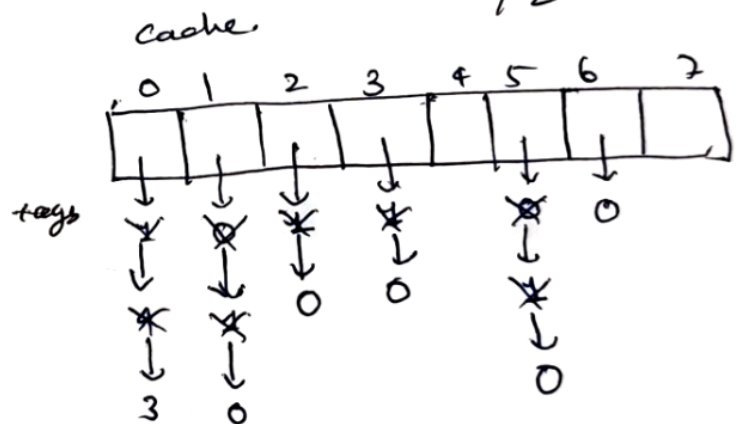
Q2. Cache is SRAM, smaller, closer to CPU hence making it faster than main memory (DRAM)

Q3. main memory =  $2^8$  words.  
block size = 2 words  
cache memory =  $2^3$  blocks.

last three bits of main mem block #

word #  $n \rightarrow$  main mem block #  $\lfloor n/2 \rfloor \xrightarrow{DM}$  cache block #  $\lfloor n/2 \rfloor / 2$   
tag  $\rightarrow$  tag =  $(n/2) / 2^3 = n/2^4$

word #	cache block #	tag	hit/miss
2	1	0	miss
3	1	0	hit
11	5	0	miss
16	0	1	miss
21	2	1	miss
13	6	0	miss
64	0	4	miss
48	0	3	miss
19	1	1	miss
11	5	0	hit
3	1	0	miss
22	3	1	miss
4	2	0	miss
27	5	1	miss
6	3	0	miss
11	5	0	miss



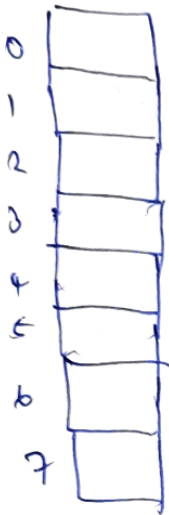
Q4 main memory size = 1024 words. =  $2^{10}$  words

# blocks in main memory =  $2^9$

# blocks in cache =  $2^3$

would be same as Q3

since the seq. #s same  
just tag size would be larger by 2 bits.



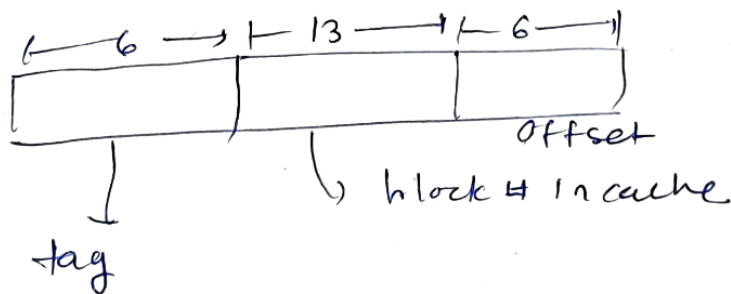
Q5. main memory = 32 MB =  $2^{10} \cdot 2^{10} \cdot 2^5 = 2^{25}$  bytes  
 cache size = 512 KB =  $2^{10} \cdot 2^9 = 2^{19}$  bytes  
 block size = 16-word =  $2^4 \cdot 2^2 = 2^6$  bytes

# blocks in cache =  $2^{19} / 2^6 = 2^{13}$

Assuming we need <sup>both</sup> valid, dirty bits. per block

$$25 - (13 + 6) = 6$$

DM:



0 bits comparator

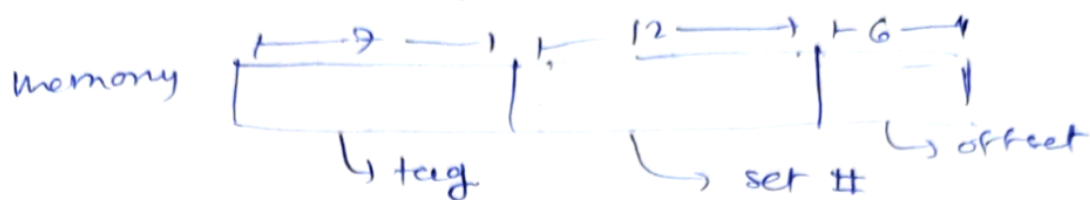
metadata = (tag ~~for~~ 2) bits each block  
 =  $2^{13} \cdot (2^2)$  bits.  
 =  $2^{15}$  bytes = 8 KB.

(b) 2 way Set associative.

i) Each set has 2 blocks

$$\# \text{ of sets} = \frac{2^{13}}{2} = 2^{12}$$

$$25 - (12 + 6)$$



ii) ~~1~~ bits Each comparator

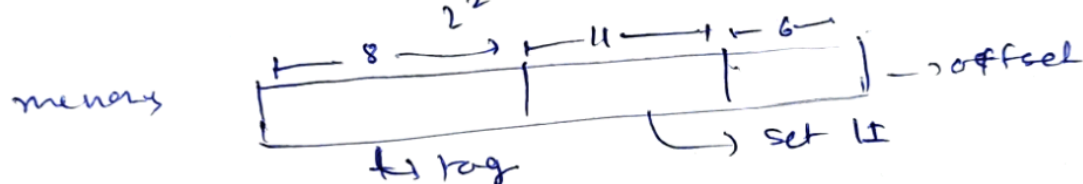
$$\# \text{ of comparator} = \# \text{ of blocks in set} = 2$$

iii)  $\# \text{ of bits compared/comparator} = \text{tag size} = 7$

iv) metadata =  $9 \times 2^{13} \text{ bits} = \frac{9 \times 2^{10} \text{ bytes}}{1} = 9 \text{ KB}$

(c) 4 way set associative  
each set has 4 blocks.

i)  $\# \text{ of sets} = \frac{2^{13}}{2^2} = 2^{11}$

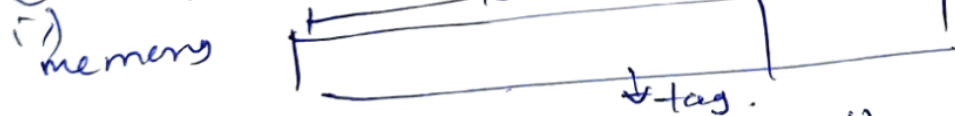


ii)  $\# \text{ of comparator} = 4$

iii)  $\# \text{ of bits compared/comparator} = 8$

iv) metadata size =  $(8 + 2) \times 2^{13} \text{ bits} = 10 \times 2^{10} \text{ bytes} = 10 \text{ KB}$

(d) fully associative  $\# \text{ of sets} = 1$  offset



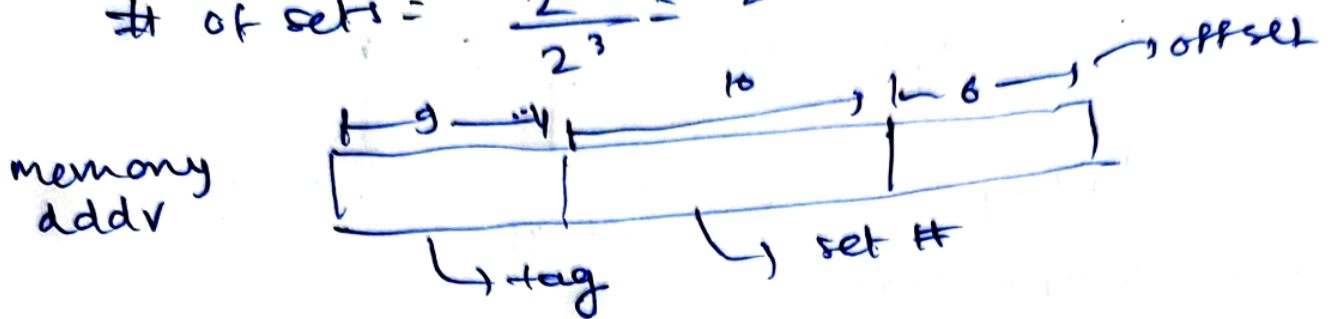
ii)  $\# \text{ of comparators} = 2^{13} = \# \text{ of blocks in cache}$

iii)  $\# \text{ of bits compared/comparator} = 19$

iv) metadata size =  $(19 + 2) \times 2^{13} \text{ bits} = 21 \text{ KB}$

(d) 8-way set associative.

i) each set has 8 blocks  
 $\# \text{ of sets} = \frac{2^{13}}{2^3} = 2^{10}$



ii)  $\# \text{ of comparators} = 8$

iii)  $\# \text{ of bits comp / comparator} = 9$

iv) metadata size =  $(9 + 2) \times 2^{13} \text{ bits}$   
 $= 11 \text{ KB}$