

(An Almost) No Math Introduction to Deep Learning

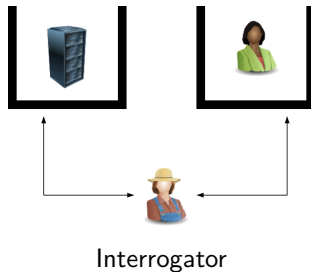
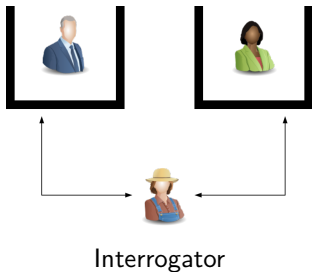
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November 19, 2020

Summary

- 1 Introduction
- 2 A little bit of math
- 3 Image processing
- 4 Machine learning
- 5 Fitting functions
- 6 References

Imitation game



Artificial intelligence

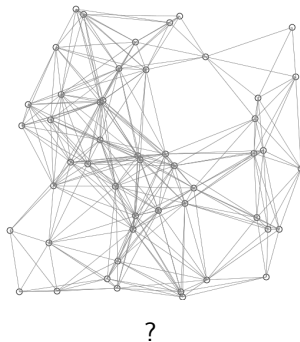
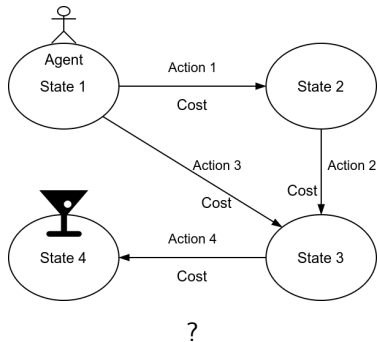
- Logic machines (50s)
- Knowledge based expert systems (80s)
- Language translation (60s) , 2000s, 2014 and later.
- Machine learning
 - Neural networks including deep learning (started in 1943)
 - Support vector machines
 - Bayesian learning
- Graphs
- Genetic algorithms and genetic programs.

Expert systems

- Database of formally described "facts" or "knowledge".
- A reasoning engine for answering questions or solving problems.

Not to be confused with a true natural language processing and question-answering system.

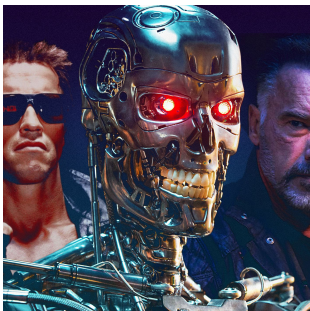
Search



Neural Networks

- 1943: Warren McCulloch and Walter Pits connected neurons, computation, logic and learning.
- 1950: Minsky and Dean Edmonds build first neural network computer. 3000 vacuum tubes, surplus auto-pilot parts from B-24 bomber. 40 Neurons.
- 1969: Minsky and Papert publishobama-funny perceptron - simple linear networks could not learn basic functions.
- 1980s: David Rumelhart, Jeff Hinton and Ronald Williams applied back propagation (again) for training multi-layer neural networks. Rumelhart's work also created the foundations for Recurrent Neural Networks.
- 1990s: LSTM networks by Hochreiter and Schmidhuber 1997. CNN for handwritten digit recognition - Yann LeCun.
- 2000s: LSTMs show promise in speech recognition
- 2012: Deep learning

Different views



Agent



Tool

General

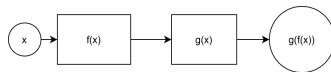
Narrow

Composition of functions

$$f(x) = ax + b \quad (1)$$

$$g(x) = \frac{1}{e^{-x} + 1} \quad (2)$$

$$g(f(x)) = \frac{1}{e^{-(ax+b)} + 1} \quad (3)$$



Composite

Derivatives

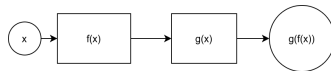
$$f(x) = ax + b \quad (4)$$

$$\frac{df(x)}{dx} = a \quad (5)$$

$$\sigma(z) = \frac{1}{e^{-z} + 1} \quad (6)$$

$$\frac{d\sigma(z)}{dz} = \sigma(z)(1 - \sigma(z)) \quad (7)$$

$$\frac{d\sigma(f(x))}{dx} = ? \quad (8)$$



Composite

Derivatives

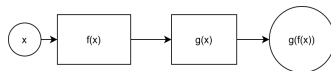
$$z = ax + b \quad (9)$$

$$\frac{dz}{dx} = a \quad (10)$$

$$\sigma(z) = \frac{1}{e^{-z} + 1} \quad (11)$$

$$\frac{d\sigma}{dz} = \sigma(z)(1 - \sigma(z)) \quad (12)$$

$$\frac{d\sigma}{dx} = \frac{d\sigma}{dz} \frac{dz}{dx} \quad (13)$$



Composite

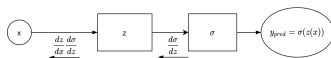
$$z = ax + b \quad (14)$$

$$\frac{dz}{dx} = a \quad (15)$$

$$\sigma(z) = \frac{1}{e^{-z} + 1} \quad (16)$$

$$\frac{d\sigma}{dz} = \sigma(z)(1 - \sigma(z)) \quad (17)$$

$$\frac{d\sigma}{dx} = \frac{d\sigma}{dz} \frac{dz}{dx} = \frac{dz}{dx} \frac{d\sigma}{dz} \quad (18)$$



Back propagation of gradients

Datasets

- Modified National Institute of Standards and Technology - MNIST (60k/10k)
- Canadian Institute For Advanced Research - CIFAR-10 (50k/10k) and CIFAR-100 (2 level, 500/100)
- Pascal Visual Object Classes (VOC) - 22k images, 20 classes
- ...
- ImageNet

ImageNet Large Scale Visual Recognition Challenge

MNIST Dataset (60k, 10k)



ImageNet (14M+, 22k)

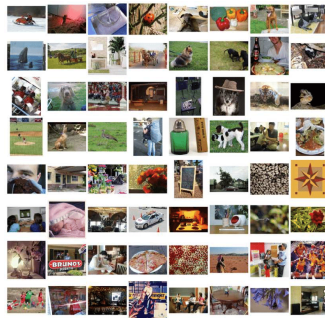
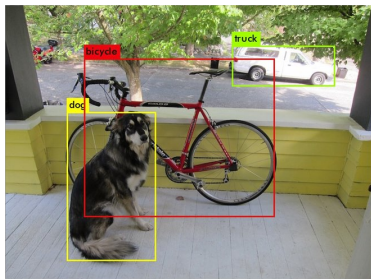
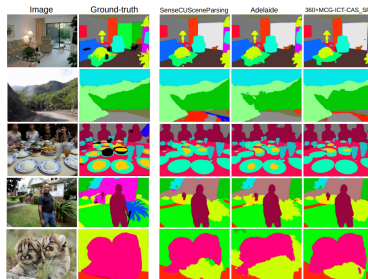


Image processing



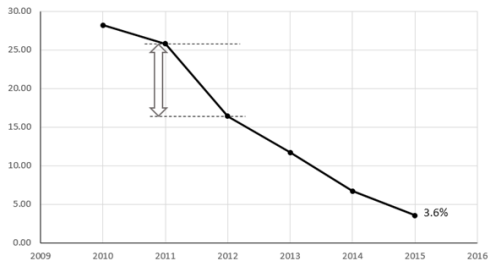
Localization



Segmentation

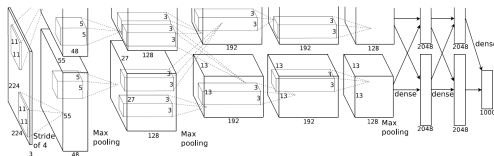
ImageNet Large Scale Visual Recognition Challenge

- Publicly available dataset - ImageNet (14M+, 22k categories)
- Annual competition
 - Image classification
 - Object detection and localization
- Increasing depth
 - 8 layer AlexNet
 - 19 layer GoogLeNet
 - 152 layer ResNet



Top 5 classification error rate

AlexNet 2012



Alex Krizhevsky, Sutskever, Ilya and Hinton, Geoffrey E., "ImageNet Classification with Deep Convolutional Neural Networks", 2012

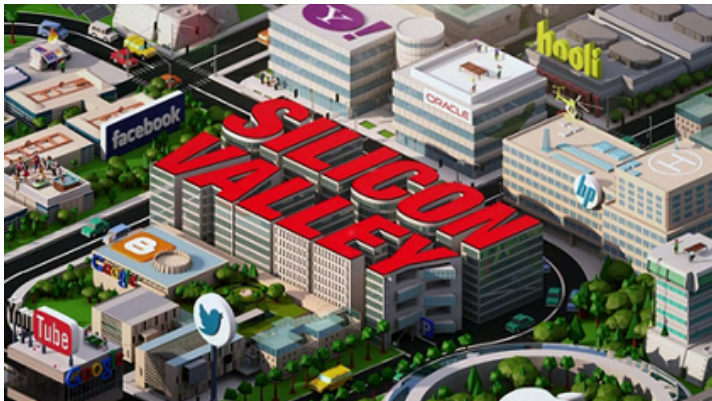
AlexNet:] 61m parameters, 8 layers

GoogLeNet: 6.7m parameter, 22 layers

ResNet: ResNet-50, ResNet-101, ResNet-152

Question: Are deeper networks always better?

Not hotdog

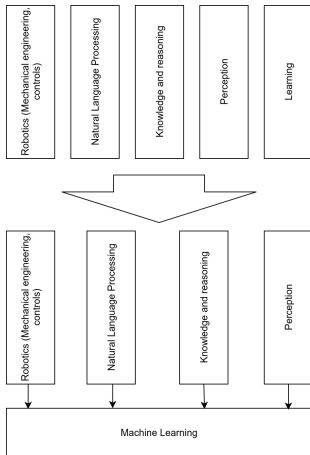


<https://www.youtube.com/watch?v=vlci3C4JkL0>

A photograph showing President Barack Obama and Vice President Joe Biden at a health fair. President Obama is standing on a small white platform, looking at a clipboard held by Vice President Biden. Biden is adjusting a device on the wall. Other men in suits are visible in the background, some smiling and talking. The setting is a hallway with a green and white checkered floor and wooden lockers in the distance.

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Late 2000s - machine learning dominates



- Image classification, localization and segmentation
- Neural machine translation, question answering, summary.
- Game playing, helicopter flying (stunts)
- Planning, self driving cars
- Text, audio and video processing, generation
- ...

Machine learning I

Models

- Build a model of the world
- Infer/predict using the model.

Machine learning

- Supervised learning
- Unsupervised learning
- Reinforcement learning

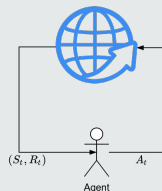
Machine learning II

Unsupervised learning

- Training a model to find patterns in a dataset, typically an unlabeled dataset.
- Learning how to extract *interesting* features.
- Learning data distribution for generating data.

Reinforcement learning

A family of algorithms that learn an optimal policy, whose goal is to maximize return when interacting with an environment.



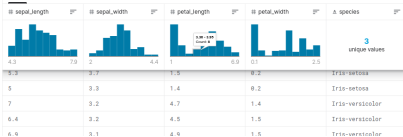
Supervised learning I

Detail Compact Column

# sepal_length	# sepal_width	# petal_length	# petal_width	Δ species
5.7	2.9	4.2	1.3	Iris-versicolor
6.2	2.9	4.3	1.3	Iris-versicolor
5.1	2.5	3	1.1	Iris-versicolor
5.7	2.8	4.1	1.3	Iris-versicolor
6.3	3.3	6	2.5	Iris-virginica
5.8	2.7	5.1	1.9	Iris-virginica
7.1	3	5.9	2.1	Iris-virginica
6.3	2.9	5.6	1.8	Iris-virginica
6.5	3	6.8	2.2	Iris-virginica

Detail Compact Column

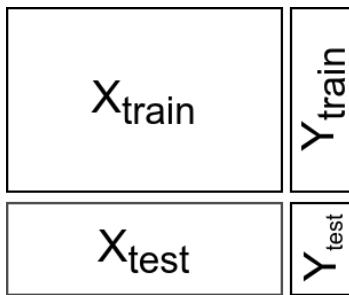
5 of 5 columns



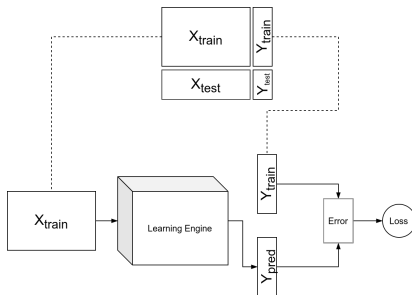
Supervised learning II

Source: <https://www.kaggle.com/arshid/iris-flower-dataset?select=IRIS.csv>

150 rows, 5 attributes (columns), 4 numerical and 1 categorical.

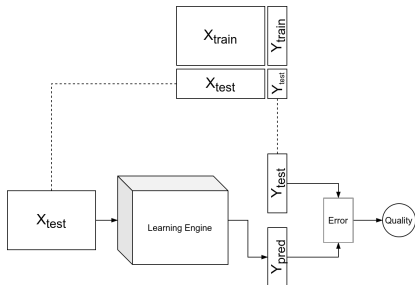


Data

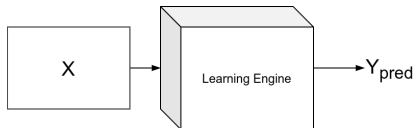


Training

Supervised learning III



Testing



Predicting

Fitting a function to data

Description (supervised learning)

Given a set of data $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$, can we find a function $y = f(x)$ that "fits" this data?

Questions

- What is this function $f(x)$?
- What does "fit" mean?
- How do we know this works?
- What kinds of problems can we solve?

More about $f(x)$

Class of functions

Starting with a function $f(x; \theta_1, \theta_2, \dots, \theta_n)$ where x is the input to the function and θ s are its parameters, we need to find the set of θ s that best "fits" the give data $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$

Class of linear functions

Consider $f(x) = ax + b$. If we can say, with some confidence, that our data is linearly related, we need to find $\theta_1 = a$, $\theta_2 = b$ that *fits* the given data. We can also write it as $f(x; a, b) = ax + b$.

Preferred,

$$f(x; \theta_1, \theta_2) = \theta_1 x + \theta_2 \quad (19)$$

Fit

Mean squared Euclidean distance as one possible measure of fit

Let L_i be the squared Euclidean distance between the predicted value, $\hat{y}_i = f(x_i)$ and the actual, y_i . Then,

$$L_i = z_i^2 \quad (20)$$

$$z_i = y_i - f(x_i) \quad (21)$$

$$= y_i - \theta_1 x_i - \theta_2 \quad (22)$$

Minimizing L_i with respect to the parameters θ_1 and θ_2 ,

$$\frac{\partial L_i}{\partial \theta_1} = \frac{\partial z_i^2}{\partial z_i} \frac{\partial z_i}{\partial \theta_1} \quad (23)$$

$$\frac{\partial L_i}{\partial \theta_2} = \frac{\partial z_i^2}{\partial z_i} \frac{\partial z_i}{\partial \theta_2} \quad (24)$$

For n data points, mean loss is

$$L = \frac{1}{n} \sum_{i=1}^{i=n} L_i = \frac{1}{n} \sum_{i=1}^{i=n} (y_i - \theta_1 x_i - \theta_2)^2$$

In practice


- Choose a small (64 or 128) random subset of training data.
- Compute predicted values, then loss.
- Compute gradients of loss W.R.T. parameters then update parameters.


An **epoch** refers to a single iteration over all training data.


Two different spaces


- Space spanned by x and y . Optimization tries to find the surface (model) in this space that best fits the data.
- Space spanned by θ s. We minimize the loss function in this space.


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 V. Dumoulin and F. Visin, “A guide to convolution arithmetic for deep learning,” 2018.


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