# Graph

## - Karun Karthik

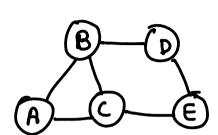
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- 1. All paths from source to target
- 2. Flood Fill
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- 4. Max Area of the Island
- 5. Find if path exist in Graph
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# lynaphi

graph G1 is a pair (V,E) where V is set of vertices E is set of edges. n = |V| E e = |E|

Eg



V = {A, B, c, D, €} N = 5 E = {AB, AC, BC, BD, CE, DE} e = 6

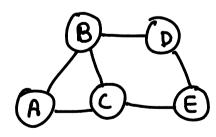
### Applications

frogle maps -> To find shortest router Social network -> user, connection Representation \_

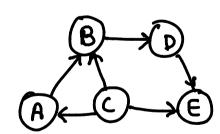
ody. matrix  $SC \rightarrow O(v^2)$ Adj List  $SC \rightarrow O(V+E)$ 

Types >

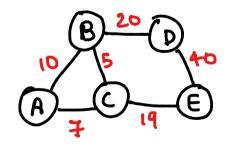
1) undirected



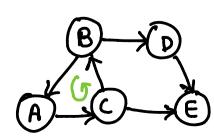
2) Directed



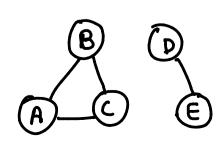
3) weighted



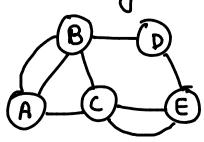
4) Cyclic



5) Disconnected



6) Multigraph



[no seftoops]

## Graph Traveral

# a) BFS , visit each and every vertex in a defined order.

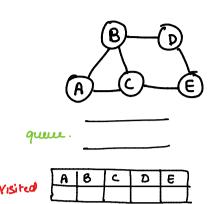
- select node

que .

ABCDE

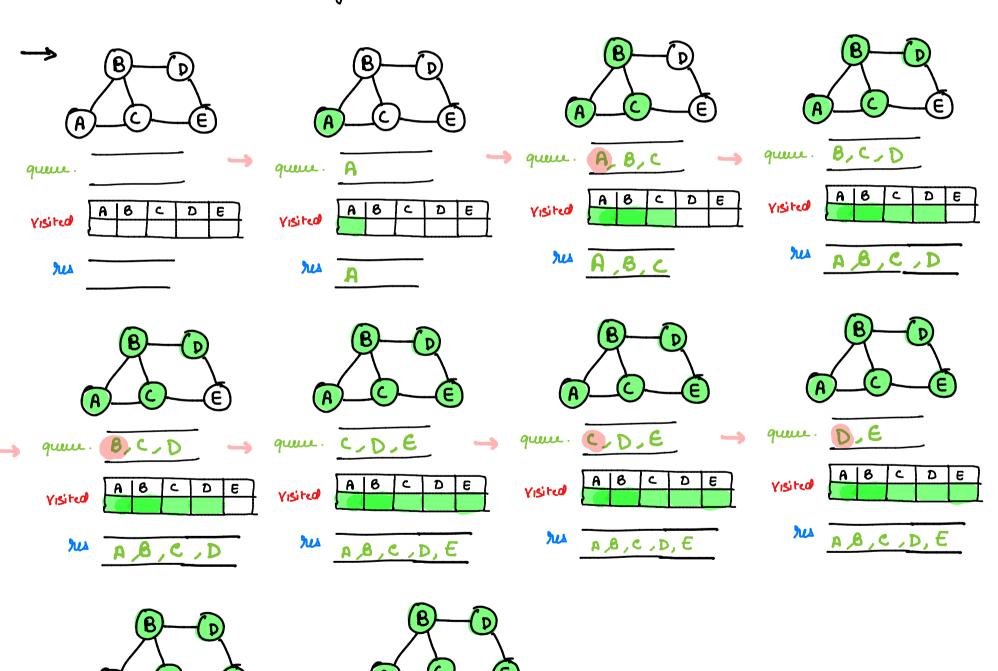
A,B,C,D,E

- visit its unvisited neighbour nodes
- malk it as visited a push into result
- put it into queue
- if no nighbours then pop.
- repeat till queue is empty



 $TC \rightarrow O(V+E)$ 

 $5c \longrightarrow O(v)$ 



A,B,C,D,E () Retur Jus

que .

```
class Solution {
  public:
    vector<int> bfsOfGraph(int V, vector<int> adj[]) {
        vector<int>ans;
        vector<int>vis(V,0);
        queue<int>q;
        q.push(0);
        while(!q.empty()){
            int curr = q.front();
            q.pop();
            vis[curr]=1;
            ans.push back(curr);
            for(auto it:adj[curr]){
                if(vis[it]==0){
                    vis[it]=1;
                    q.push(it);
        return ans;
```

## applications [BFS]

- 1. Shortest path
- a Min. spanning tree for unweighted graph
- 3. Cycle detection
- 4. GPS
- 5. Social network.

## (b) DFS →

Stack select node visit its unvisited neighbour nodes mark it as visited a push into result push it into stack - if no neighbours then pop. rus - repeat till stack is empty Stack Stack Stack A rus A, rus A,B rus A,B,C Stack Stack Stack D B rus A,B,C, rus A, B, C, D rus A,B,C Stack Stack Stack D rus A,B,C,D,E rus A, B, C, D, E rus A, B, C, D, E Stack Stack TC → O(V+E) Sc -> O(V)

```
class Solution {
  public:
    void dfs(vector<int>&ans, vector<int>&vis, int node, vector<int>adj[]){
        vis[node] = 1;
        ans.push_back(node);
        for(auto it:adj[node]){
            if(!vis[it]){
                vis[it] = 1;
                dfs(ans, vis, it, adj);
    vector<int> dfsOfGraph(int V, vector<int> adj[]) {
        vector<int> ans;
        vector<int>vis(V,0);
        for(int i=0; i<V; i++){
            if(vis[i]==0)
            dfs(ans, vis, i, adj);
       return ans;
```

# Applications [DFS]

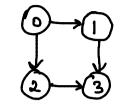
- Path finding
- 2. Cycle déteition
  3. Topological sort
- 4. Finding strongly connected components.

1) All paths from bre to target

giver a directed ocyclic graph, return au paths from node O

to node n-1.

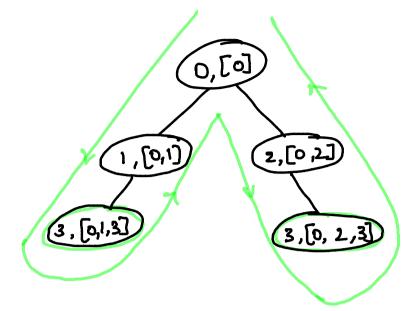




Path +1



Path-2



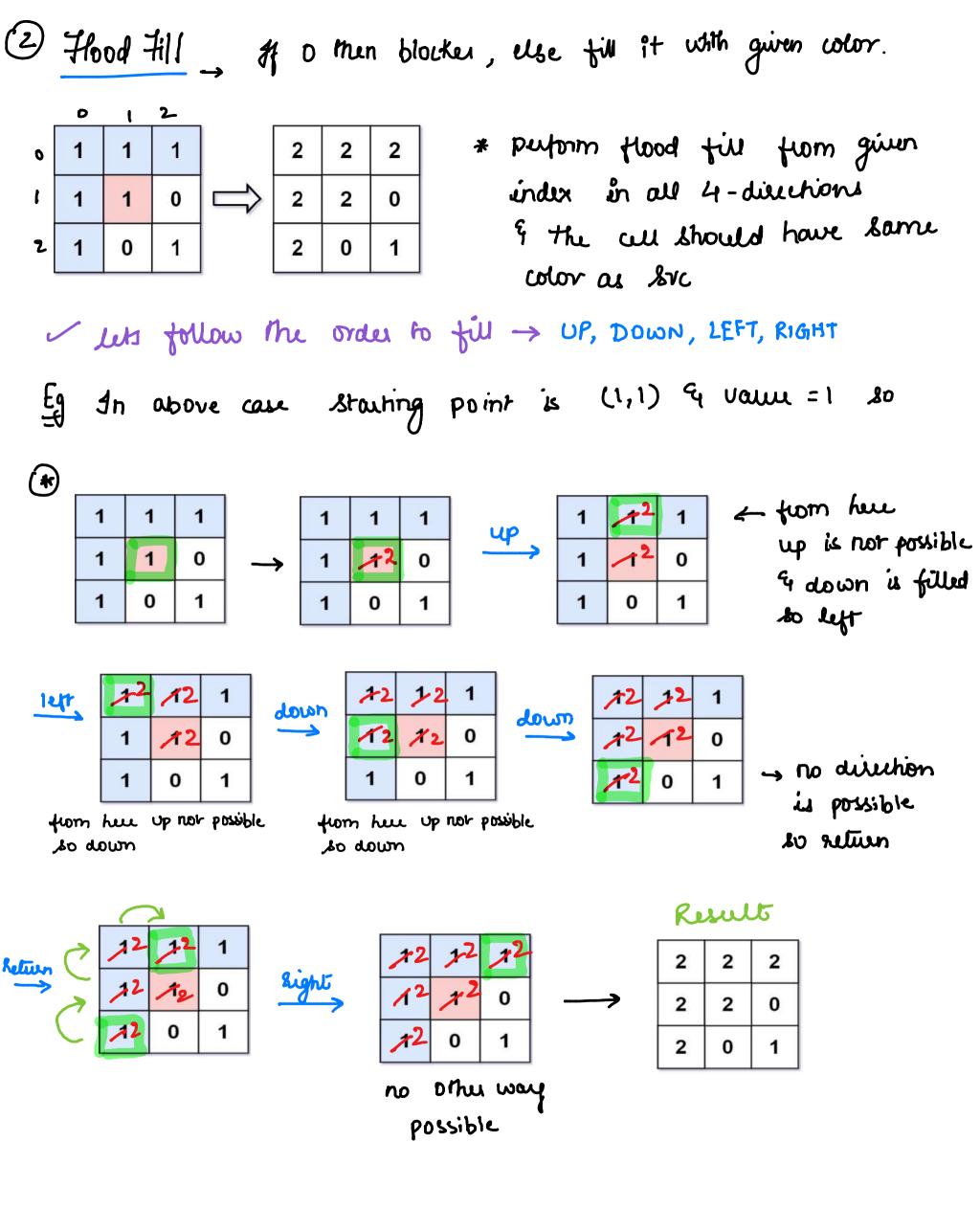
cogr -

TC → D(V+E)

V → Vertices E → edges

SC→ Recursive Stack + Result

```
class Solution {
    public:
        void findAllPaths(vector<vector<int>>&graph, int currNode, vector<bool>&visited,
                          int n, vector<int> &currPath, vector<vector<int>>&res){
            if(currNode==n-1){
                res.push_back(currPath);
                return;
            if(visited[currNode]==true) return;
11
            // backtrack for every node
            visited[currNode] = true;
            for(auto neighbour: graph[currNode]){
17
                currPath.push_back(neighbour);
                findAllPaths(graph, neighbour, visited, n, currPath, res);
                currPath.pop_back();
            visited[currNode] = false;
        vector<vector<int>> allPathsSourceTarget(vector<vector<int>>& graph) {
            vector<vector<int>> res;
            vector<int> currPath;
            int n = graph.size();
            vector<bool> visited(n);
            // traversing from 0 node
            currPath.push_back(0);
            findAllPaths(graph, 0, visited, n, currPath, res);
            return res;
    };
```



```
class Solution {
    public:
        void floodFiller(vector<vector<int>>& image, int i, int j,
        int m, int n, int currColor, int newColor)
            if(i<0 || i>=m || j<0 || j>= n || image[i][j] == newColor
                || image[i][j] != currColor)
                return;
10
            image[i][j] = newColor;
11
            floodFiller( image, i-1, j, m, n, currColor, newColor);
12
            floodFiller( image, i+1, j, m, n, currColor, newColor);
            floodFiller( image, i, j-1, m, n, currColor, newColor);
13
14
            floodFiller( image, i, j+1, m, n, currColor, newColor);
15
        }
16
17
        vector<vector<int>> floodFill(vector<vector<int>>& image, int sr,
18
        int sc, int newColor)
19
20
            int m = image.size();
21
            int n = image[0].size();
22
            int currColor = image[sr][sc];
23
            floodFiller(image, sr, sc, m, n, currColor, newColor);
24
            return image;
25
        }
26 };
```

```
Tc→ O(mn)

Sc→ O(h)

Ly Reculsive Stack
```

- · Always start dfs only if value = 1 & change its value to 0, so it cannot be visited again
  - · if initial value = 0 then skip
  - · initially ans=0

• Let start from 
$$(0,0)$$
 & try moving  $U,D,L,R$ 
 $\rightarrow$  the traversal goes in this order

 $(0,0) \rightarrow (1,0) \rightarrow (1,1) \rightarrow (0,1)$  is

& update ans.

$$[[,,0,0,0], [0,0], [0,0,0], [0,0,0], [0,0,0], [0,$$

- now, we can skip every entry from (1,0) to (2,1) as they are 01
- now stank from (2,2), as 0,0,1,R is not possible, set its value = 0 % update and.

  and = y & 2.

- · row, we can skip every enmy from (2,3) to (3,2) as they are 01
- · now start from (3,3), it goes as follows  $(3,3) \rightarrow (3,4)$
- · further travelled from (3,4) is not possible

```
class Solution {
    public:
        void countIsland(vector<vector<char>>& grid, int currRow, int currCol, int row, int col){
            if(currRow<0 || currRow>=row || currCol<0 || currCol>=col || grid[currRow][currCol]=='0')
                return;
            grid[currRow][currCol] = '0';
            countIsland(grid, currRow-1, currCol, row, col);
            countIsland(grid, currRow+1, currCol, row, col);
            countIsland(grid, currRow, currCol-1, row, col);
            countIsland(grid, currRow, currCol+1, row, col);
11
        }
12
13
        int numIslands(vector<vector<char>>& grid) {
14
15
            int ans = 0;
            int row = grid.size();
17
            int col = grid[0].size();
19
            for(int currRow = 0; currRow < row; currRow++)</pre>
20
                for(int currCol = 0; currCol < col; currCol++)</pre>
21
                     if(grid[currRow][currCol]=='1'){
22
                         ans++;
23
                         countIsland(grid, currRow, currCol, row, col);
24
                     }
25
            return ans;
        }
   };
```

$$Tc \rightarrow O(mn)$$
 Aug case  $O(m^2n^2)$  Worst case

- \* Intuition is some as plevious problem.
- \* Minor Tweak to wort number of 1s in island.
- \* Once entire island traversal is done,

compose for max sua of island.

TC -> O(mn) Augcase.

code \_

```
class Solution {
    public:
        int findArea(vector<vector<int>>& grid, int currRow, int currCol, int m, int n){
            if(currRow<0 || currCol<0 || currRow>=m || currCol>=n || grid[currRow][currCol]==0)
                 return 0;
            grid[currRow][currCol]=0;
            // this is for single cell where we started traversing
10
            int count = 1;
            count += findArea(grid, currRow-1, currCol, m, n);
11
            count += findArea(grid, currRow+1, currCol, m, n);
12
13
            count += findArea(grid, currRow, currCol-1, m, n);
            count += findArea(grid, currRow, currCol+1, m, n);
14
15
            return count;
17
        int maxAreaOfIsland(vector<vector<int>>& grid) {
18
            int m = grid.size();
19
            int n = grid[0].size();
20
            int ans = 0;
21
            for(int currRow = 0; currRow<m; currRow++)</pre>
                 for(int currCol = 0; currCol<n; currCol++){</pre>
22
23
                     if(grid[currRow][currCol]==1){
                         ans = max(ans, findArea(grid, currRow, currCol, m, n));
24
25
                     }
26
27
            return ans;
28
        }
29
    };
```

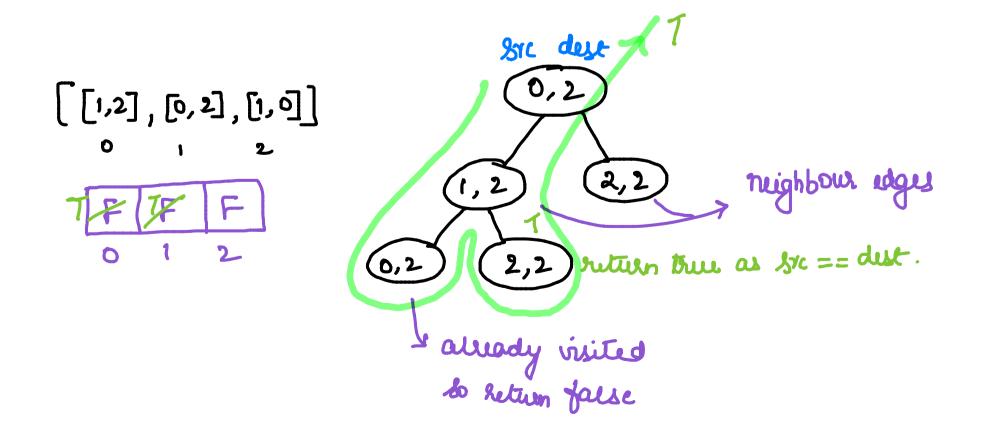
(5) Find if path exist in graph.

yourn Brc, dust, no. of nodes & set of edges, find it path exist by src & dust.

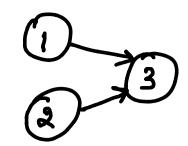
$$\frac{1}{2} \bigcirc (0,1), [1,2], [2,0] ] \text{ edges.}$$

n=3 edges = [[0,1],[1,2],[2,0]] &rc=0, dest=2.

- 1) Create a graph using adjuist sep. [[1,2], [0,2], [1,0]]
- 2) Perform dfs



```
class Solution {
    public:
        bool validPath(int n, vector<vector<int>>& edges, int src, int dest) {
           vector<vector<int>>graph(n);
            for(int i=0;i<edges.size();i++)</pre>
                 int v1 = edges[i][0];
                 int v2 = edges[i][1];
10
                graph[v1].push_back(v2);
11
                 graph[v2].push_back(v1);
12
13
            }
14
            vector<bool>vis(n,false);
15
            return pathExist(src, dest, graph, vis);
16
        }
17
        bool pathExist(int src , int dest, vector<vector<int>>&graph, vector<bool>&vis){
18
19
20
            if(src==dest)return true;
21
22
            vis[src]=true;
23
24
            for(int i=0;i<graph[src].size();i++)</pre>
25
                 if(vis[graph[src][i]]==false)
26
                     if(pathExist(graph[src][i],dest,graph,vis)==true)
27
                         return true;
28
29
            return false;
30
31
    };
```



if indegen == 0 &&

outdegen == 
$$n-1$$

then return that vertex

```
class Solution {
 2
    public:
        int findJudge(int n, vector<vector<int>>& trust) {
             vector<int>indegree(n+1,0);
             vector<int>outdegree(n+1,0);
             for(int i=0;i<trust.size();i++)</pre>
             {
                 int v1 = trust[i][0];
                 int v2 = trust[i][1];
                 outdegree[v1]+=1;
10
                 indegree[v2]+=1;
11
12
             }
             for(int i=1;i<=n;i++)</pre>
13
14
             {
                 if(outdegree[i]==0 && indegree[i]==n-1)
15
16
                     return i;
17
18
             return -1;
19
        }
20
    };
```

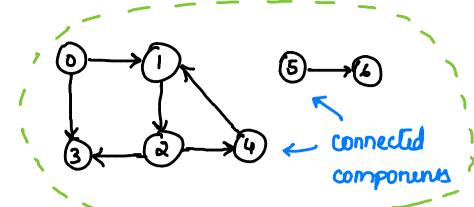
7 Detect cycle in a directed graph

Consider a geaph with 'n' verties labelled as [0.-11-1]

每 口= 7 [0,1,2,3,4,5,6]

Graph -> 1

\* To detect cycle, check for backedge



Let's star ats from 0 vectors.

\* It every vertex, check if its already visited, it already visited then check if it is present in recursive stack.

If present, then it indicates back edge -> Returns Truce



recursive stack

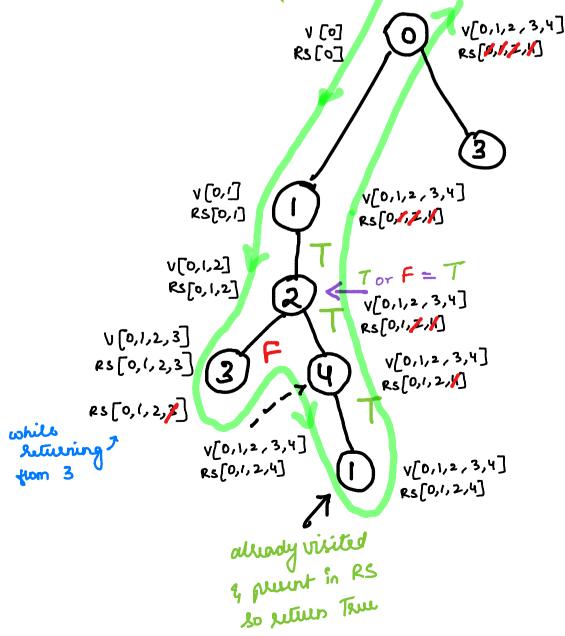
Visited → ₹ 0,1, 2,3,4

Recuesive → ₹0,1,2,3,4

\* At 3 voter, there's no neighbour & no cycle is detected so settlen F. Before setwing, undo change made in Recursive stack by popping it.

Visited  $\rightarrow \{0,1,2,3,4,1\}$  & Recuesive  $\rightarrow \{0,1,2,3,4\}$  stack  $\rightarrow \{0,1,2,3,4\}$ 

I is already present in recuring

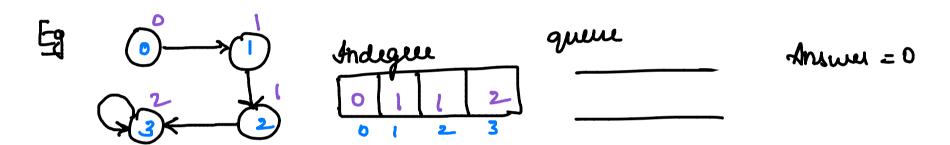


```
class Solution {
      public:
        bool dfs(int node, vector<int>&vis, vector<int>&rs, vector<int> adj[])
        {
             vis[node]=1;
             rs[node]=1;
             for(auto it:adj[node])
                 if(vis[it]==0){
10
                     if(dfs(it,vis,rs,adj))
11
                         return true;
12
13
                 else if(rs[it]==1)
14
                     return true;
15
16
             rs[node]=0;
17
             return false;
18
        }
        bool isCyclic(int V, vector<int> adj[]) {
19
20
             vector<int>vis(V,0);
21
22
             vector<int>rs(V,0);
23
24
             for(int i=0;i<V;i++)</pre>
25
                 if(vis[i]==0)
26
27
                 if(dfs(i,vis,rs,adj))
28
                     return true;
29
             }
30
             return false;
31
        }
32
    };
```

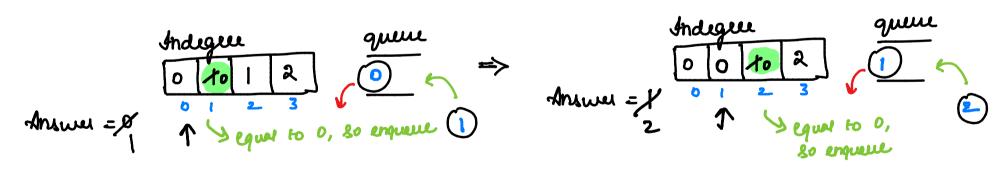
Kahn's Algorithm \_, To find topological Ordering Can be used to find yell using BFS.

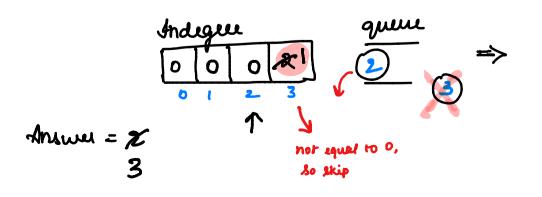
- 1) Find indeque of every vertex in graph & answer = 0
- 2) If windegree of vertex is 0, then put into queue & do bots till queue is not empty & while doing bots decrease the indegree of neighbour by 1.

  if indegree of neighbour = 0, then enqueue & increment answer by 1
- 3 of answer != no. of vertices then you is present.



As indeque of 10 is 0, we push into queue & do bots till queue is not empty.





Answer = 3
No of vertices = 4
... yelle resent.

```
class Solution{
       public:
           bool isCyclic(int V, vector<int> adj[]) {
             vector<int>indegree(V,0);
             for (int i = 0; i < V; i++)
               for(int it : adj[i])
                 indegree[it]++;
 9
10
             queue<int>q;
11
             int ans = 0;
12
             unordered_set<int>vis;
13
14
             for (int i=0;i<V;i++)
15
16
                 if(indegree[i]==0){
17
                     q.push(i);
18
                     ans+=1;
19
                 }
20
             }
21
             while(!q.empty())
22
23
24
                 int currvertex = q.front();
25
                 q.pop();
                 if(vis.find(currvertex)!=vis.end())
26
27
                     continue;
28
                 vis.insert(currvertex);
29
                 for(int neighbour:adj[currvertex])
30
31
                     indegree[neighbour]-=1;
32
                     if(indegree[neighbour]==0)
33
                      {
34
                           q.push(neighbour);
35
                           ans+=1;
36
                      }
                 }
37
38
             }
39
             if(ans==V) return false;
40
             return true;
        }
41
42
    };
```

→ use Kahn's algorithm. & odd node to result while performing dfs.

```
Code_
```

```
TC \rightarrow O(V + E)
SC \rightarrow O(V)
```

```
class Solution
    {
        public:
        vector<int> topoSort(int V, vector<int> adj[])
             vector<int> indegree(V,0) ,res;
             for(int i=0; i<V; i++)
                 for(auto it:adj[i])
                     indegree[it]++;
11
12
            queue<int> q;
13
            int ans = 0;
            unordered_set<int>vis;
14
15
            for(int i=0; i<V; i++)
17
                if(indegree[i]==0){
18
19
                    q.push(i);
20
                    ans+=1;
                }
21
22
23
            while(!q.empty())
25
                int curr = q.front();
26
27
                q.pop();
28
29
                // add to res
30
                res.push_back(curr);
31
                if(vis.find(curr)!=vis.end())
33
                     continue;
                vis.insert(curr);
36
                for(int neighbour: adj[curr])
37
                    indegree[neighbour]-=1;
                    if(indegree[neighbour]==0)
41
                         q.push(neighbour);
42
43
                         ans+=1;
                    }
45
47
            return res;
        }
50
    };
```

$$Tc \rightarrow O(V+E)$$
  
Sc  $\rightarrow O(V+E)$ 

code ->

```
class Solution {
    public:
        vector<vector<int>> createGraph(int n, vector<vector<int>>& pre){
             vector<vector<int>> graph(n);
              for(auto it:pre){
                  int v = it[1];
                  int u = it[0];
                  graph[v].push back(u);
              }
10
              return graph;
        }
11
12
13
        bool canFinish(int n, vector<vector<int>>& pre) {
14
             vector<vector<int>> graph = createGraph(n, pre);
15
             vector<int>indegree(n,0);
             for(int i=0; i<n; i++)
17
                 for(int it: graph[i])
                     indegree[it]++;
19
20
             queue<int> q;
21
             int ans = 0;
             unordered_set<int> vis;
22
23
24
             for(int i=0; i<n; i++)
25
                 if(indegree[i]==0){
                     q.push(i);
27
                     ans++;
28
                 }
29
30
             while(!q.empty()){
31
                 int currvertex = q.front();
32
                 q.pop();
                 if(vis.find(currvertex)!=vis.end())
                     continue;
35
                 vis.insert(currvertex);
                 for(int neighbour: graph[currvertex]){
36
37
                     indegree[neighbour]--;
                     if(indegree[neighbour]==0){
                         q.push(neighbour);
40
                         ans++;
41
                     }
                 }
42
43
44
             if(ans==n) return true;
45
            return false;
46
        }
47
    };
```

10 Course Schedule - II

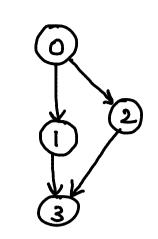
n -> no. of courses [vertices]

Topological sort only for DAG

"u should be completed before V"

 $\frac{E_{9}}{\mu k} \quad n \to 4 \quad (0,1,2,3)$   $\mu k \to [[1,0],[2,0],[3,1],[3,2]]$ 

Initially V = [] Rs = [], travelled = []



topological order in V = [0, 1, 3, 2]V = [0] RS = [#] RS = [D] T=[3,1,2,0] > revere! T=[] T = [0,1,2,3]V = [0,1,3,2] V = [0,1] RS=[0,2] Rs = [0,1] T = [3,1,2] T=[] V = [0, 1, 3, 2] V=[0,1,<mark>3</mark>] RS = [0,2] RS = [0,1,8] T = [3,1] V=[0,1,3] R5 = [0,1,3] T=[] V=[0,1,3] (2-3 is not backedge R5 = [0,1,8] ou it is not in RS) T=[3]

pop 3 & push into traversal away.

Peters F, as no cycle is found

```
class Solution {
    public:
        bool dfs(vector<vector<int>>&graph, int i, vector<int> &vis,
        vector<int> &rs, vector<int> &traversal){
            vis[i] = 1;
            rs[i] = 1;
            for(int neighbour: graph[i]){
                if(vis[neighbour]==0){
                     if(dfs(graph, neighbour, vis, rs, traversal))
10
                         return true;
11
12
                else if(rs[neighbour]==1)
13
                                            return true;
14
15
            traversal.push_back(i);
16
            rs[i]=0;
17
            return false;
18
        }
19
20
        vector<vector<int>> createGraph(int n, vector<vector<int>>& pre){
21
            vector<vector<int>> graph(n);
22
             for(auto it:pre){
23
                 int v = it[1];
                 int u = it[0];
24
25
                 graph[v].push_back(u);
26
27
             return graph;
        }
28
29
30
        vector<int> findOrder(int n, vector<vector<int>>& pre) {
31
            vector<vector<int>> graph = createGraph(n, pre);
            vector<int> vis(n,0), rs(n,0), traversal;
32
33
            for(int i=0; i<n; i++){
                if(vis[i]==0)
35
                if(dfs(graph, i, vis, rs, traversal)) return {};
36
            reverse(traversal.begin(), traversal.end());
37
38
            return traversal;
39
        }
   };
```

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