

The keys in a binary search tree are always stored in such a way as to satisfy the *binary-search-tree property*:

For all nodes x and y , if y belongs to the left subtree of x , then the key at y is less than the key at x , and if y belongs to the right subtree of x , then the key at y is greater than the key at x .

Each node has the following attributes:

- *p , left, and right, which are pointers to the parent, the left child, and the right child, respectively, and*
- *key, which is key stored at the node*

How a tree is ordered depends on how it is going to be accessed. The process of accessing each node in a tree is called a *tree traversal*. There are three types of traversal

- *Inorder. The ordering is: the left subtree, the current node, the right subtree.*
- *Preorder. The ordering is: the current node, the left subtree, the right subtree.*
- *Postorder. The ordering is: the left subtree, the right subtree, the current node.*

Inorder(node)

1. if node == null then return
2. else
- 3 Inorder(node.left)
- 4 print node.key
- 5 Inorder(node.right)

preorder(node)

- 1 if node == null then return

```
2  else
3    print node.key
4    preorder(node.left)
5    preorder(node.right)
```

postorder(node)

```
1  if node == null then return
2  else
3    postorder(node.left)
4    postorder(node.right)
5    print node.key
```

Maxdepth(node)

```
1  if node == null return 0
2  else
3    Maxdepth(node.left)
4    Maxdepth(node.right)
5    check the largest branch left or right
6    return (left+1 or right+1)
```

Insertion

Suppose that we need to insert a node z such that $k = \text{key}[z]$. Using binary search we find a node y and a nil such that replacing it by z does not break the BST-property.

BtreeInsert(x, z, k)

if x = NIL then return "Error"

y ← x

while true do {

if key[y] < k

then z ← left[y]

else z ← right[y]

if z = NIL break

}

if key[y] > k then left[y] ← z

else right[p[y]] ← z

Problem: Complete the Inorder, preorder, postorder and insert function of the code given in btree.c file.