

# Indexing chemical fingerprints for efficient querying of molecular databases

Abhik Mondal (CS10B061)

IIT Madras

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Project Guide: Dr. Sayan Ranu

# Overview

- 1 Motivation
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- 3 Our Contribution
  - M-tree based index
  - Inverted Index
- 4 Experiments and Results
- 5 Conclusion

# Motivation

- Fast database search is vital in drug discovery, where the aim is identifying chemical compounds with high similarity to known drugs.

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- ZINC database contains over 35 million purchasable compounds.

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- Exact Search?
  - Billions of dollars are spent for experiments on a single drug.
  - Not looking for approximation methods like Locally Sensitive Hashing.

# Chemical Compounds

- Representation of molecules? Sub-graph Isomorphism is NP-complete. Solution?

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<sup>1</sup>Source : <http://icep.wikispaces.com>

# Chemical Compounds

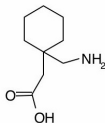
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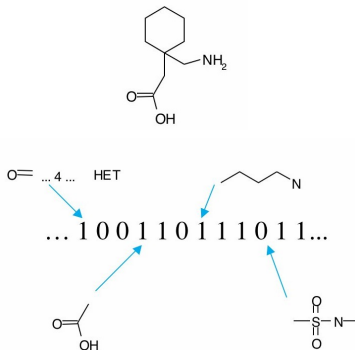


Figure : Fingerprint construction <sup>1</sup>

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# Challenges

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- But why index?

## Range Search Problem

Given a fingerprint, say ' $f$ ', a similarity measure ' $sim$ ', a threshold distance ' $\theta$ ' and a database of chemical compounds  $D$ , we find the subset  $S \subset D$  of all fingerprints, such that:

$$S = \{g \mid g \in D, sim(f, g) < \theta\} \quad (1)$$

# Some more concepts/definitions

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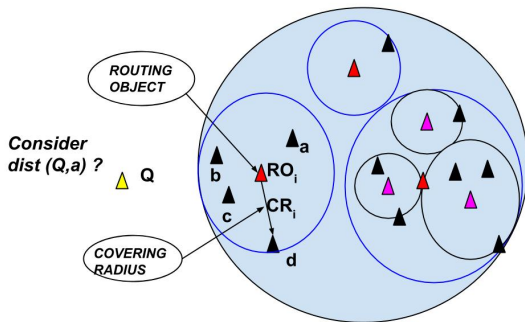
- Distance measure? Metric?

# M-tree

- Routing objects
- Covering radius

# M-tree

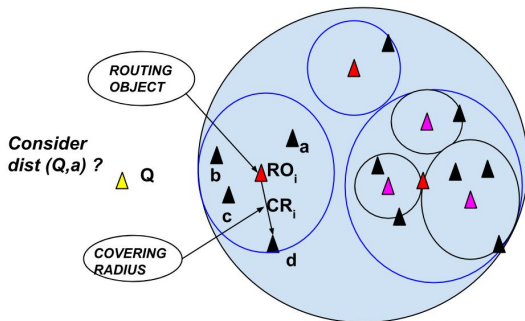
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## M-TREE STRUCTURE

# M-tree

- Routing objects
- Covering radius



## M-TREE STRUCTURE

- Max:  $|dist(Q, RO_i) + CR_i|$ , Min:  $|dist(Q, RO_i) - CR_i|$



# Indexing approach ...

- Select pivots? Number?

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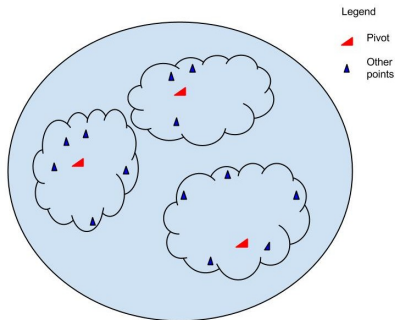
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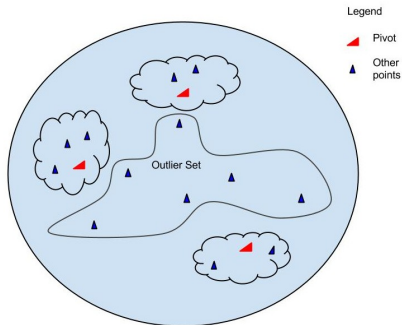
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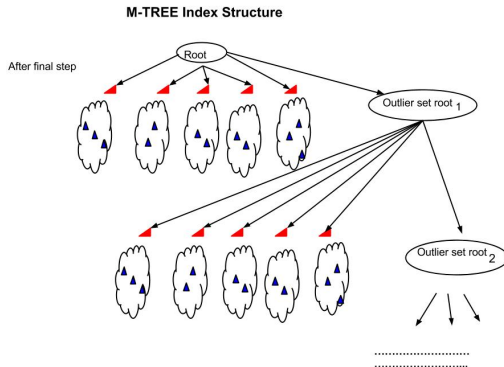
# Indexing approach

- Repeat procedure on outlier set.



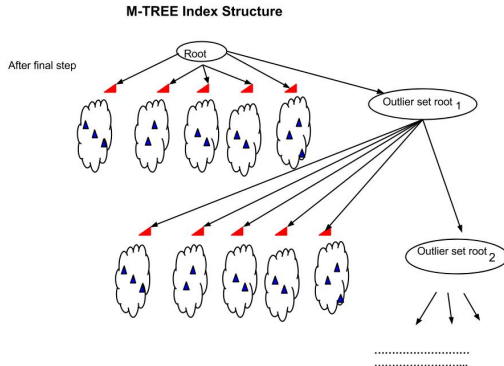
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- Termination?

# Range Search

- Start from the root as pivot  $p$
- Apply triangle inequality bounds to prune or include all points from sub-tree.
- If not, then go to the children of  $p$  and repeat the process with them as the new pivot, till we reach leaf.

# Inverted Index

- High dimensionality and sparsity of chemical data are an impediment to our indexing process.
- Use of inverted index motivated by its use in text mining.

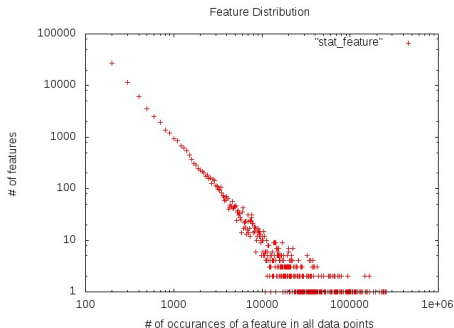
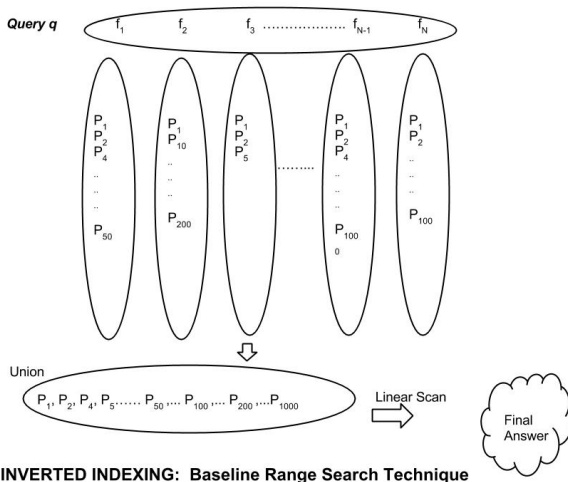
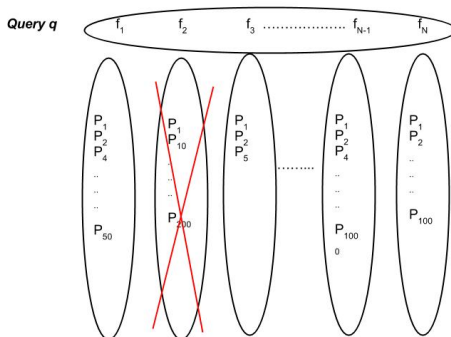


Figure : Distribution of data points against the features

# Range Search



# Pruning



Consider  $P_{200}$ , not present in any set other than of  $f_2$   
 Maximum Similarity possible for such a point with the query?

$$1 / (N_q - 1 + V_2)$$

( $N_q$  - number of features in query,  
 $V_2$  - minimum number of  
 features present in any point  
 containing  $f_2$ )

**Can we prune the set ?**

# Greedy Technique

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- Sort the features based on popularity.
- Start from the most popular feature.
- If till the  $i^{th}$  feature is considered, if  $j$  features (call it set  $R$ ) have been pruned till now, we can prune the  $i^{th}$  feature as well if the following holds.

$$\frac{j+1}{N_q - 1 + \min(V_i, \rho)} < 1 - t \quad (4)$$

where  $\rho$  is the minimum number of features present in any point containing atleast one of the features pruned until now i.e  $\rho = \min_{k \in R} V_k$

# Extension to non-binary fingerprints

Prune  $i^{th}$  feature if:

$$\frac{\min(j_i, W_i)}{S_q - W_i - k_i + l_i + \max(k_i, V_i)} < 1 - t \quad (5)$$

Here  $j_i$  is the maximum feature value taken for the feature  $f_i$ ,

$W_i$  is the  $i^{th}$  feature value of query  $q$ ,

$S_q$  is the sum magnitude of the feature values of the query  $q$ ,

$k_i$  is the minimum feature value taken for the feature  $f_i$ ,

$l_i$  is the minimum sum of feature values for any point containing the feature  $f_i$ ,

$t$  is the threshold similarity.

- Datasets
  - PubChem Dataset (264016 compounds, 785985 features)
  - DUD Dataset (128374 compounds, 32198 features)
- Evaluations
  - Compared range search result with that of full database scan.
  - Compared average run-times of range search with the state of the art Bit-bound technique <sup>2</sup>

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<sup>2</sup>**Source:** Swamidass, S Joshua and Baldi, Pierre. *Bounds and algorithms for fast exact searches of chemical fingerprints in linear and sublinear time.*

# M-tree based index analysis

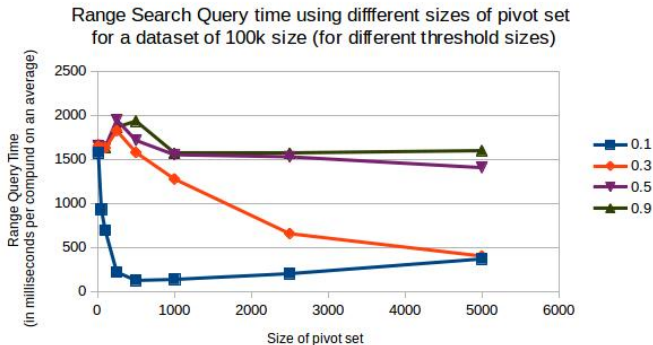
- Indexing time per compound on average increases linearly with data-set size as well as with size of pivot-set
- Outlier base limit size has no significant effect.

# M-tree based index analysis...

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- Indexing time per compound on average is constant. Does not change with data-set size.
- Pruning upto 50-100 features on average for low threshold distances.



# Comparison

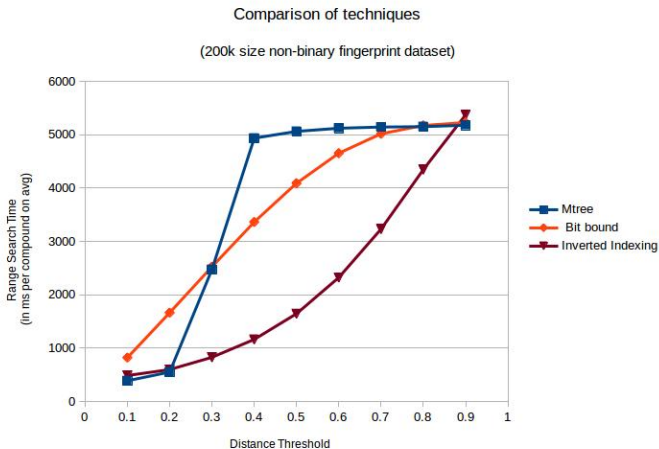


Figure : PubChem-n dataset

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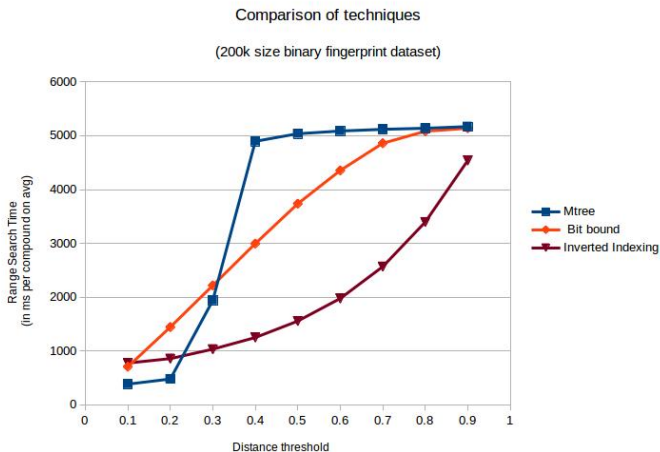


Figure : PubChem-b dataset

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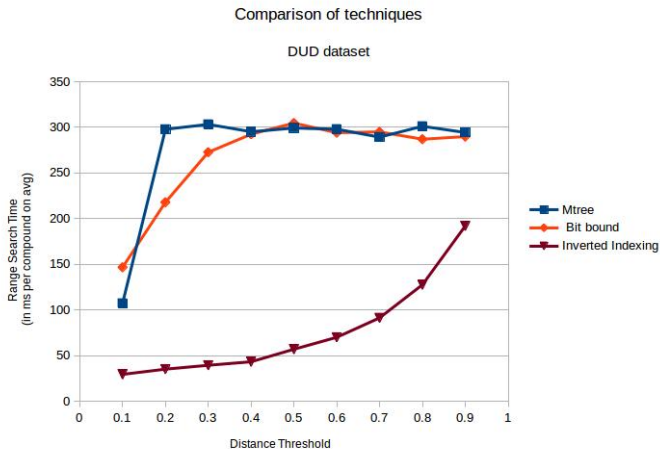


Figure : DUD dataset

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- Proposed a novel Inverted Indexing technique which achieved 5-6 times speed-up over the Bit-Bound Technique.
- Showed the effectiveness of our techniques through comprehensive analysis on 2 real world datasets (both binary and non-binary).

Thank You!