



## Sample Lecture on System Modeling

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- **Important simplifications** in building formal models of real-life systems
  - Discussed in steps throughout the lecture.
  - Summarized in second last slide.
- Discusses a **concrete example** (of a cache coherence protocol)
  - Modeled in the input language of a model checking tool SMV.



## A Full Case Study using SMV

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CS 4271  
Abhik Roychoudhury



## So far ...

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- **Basics of modeling**
  - Includes details of SMV syntax
- **Toy examples**
  - ABP, Traffic Light Controller
- **Motivational practical applications**
  - AMBA AHB protocol
- We need to model/verify a medium sized problem completely to get the feel



## Case Studies

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- Many well-publicized successes of Model Checking in the verif. of processors / cache coherence protocols
  - Encore Gigamax Cache coherence protocol
  - IEEE FutureBus+ standard
  - T9000 virtual channel processor
- Our case study is a slightly more software centric coherence protocol, one for distributed file systems



## Note of Caution

- Following slides use CMU SMV syntax which is a bit different from Cadence SMV syntax.
  - This has been done to ensure uniformity with the reading material.
  - The syntax differences are however minimal e.g.
    - `MODULE x(...)` instead of `MODULE x(...)`
    - `VAR` instead of `{`



## Before starting ...

- SMV employs **symbolic** model checking
  - More space efficient than the explicit state MC algorithm which proceeds by graph search.
  - Uses a data structure called Binary Decision Diagrams for compact internal representation of state space.
  - This will be covered in later lectures, but you do not need to understand symbolic MC for modeling and verifying using SMV.



## Success of Model Checking

- Primarily in hardware verification
- Routinely used for processor verification (or modules of it) in Intel etc
- Employed by CAD giants and processor design companies
  - Cadence, Intel, Motorola ...



## Verification or Bug Hunting

- Model Checking verifies only the design, not the implementation
- So, MC is more of a bug detection mechanism
  - But "**Automated**" bug detection
- This line will be more acceptable to practitioners than presenting it as a formal verification technique.

## Reference

- A Case Study in Model Checking Software Systems
  - Jeanette Wing and M. Vaziri-Farhana
  - FSE 1995, CMU Tech report CMU-CS-96-124
  - Another version in "Science of Computer Programming", v20, 1997, 273-299.

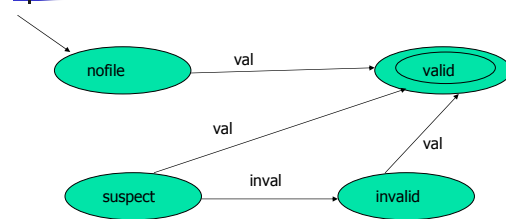
## File System Cache coherence

- Several clients and servers
- Each file is authorized by a single server
- Clients cache files on obtaining them from the server
- Clients talk directly only to the server, not to other clients.

## The Cache Coherence Problem

- A client can have a copy of a file, but
  - It may not be sure that it is the latest copy
  - It knows that it is an invalid copy
- The client will
  - Request for a validation from the server
  - Request a fresh copy

## Client's belief about its copy





## Client – State Variables

- **out** – request to the server.
  - This can be a request to
    - Fetch a file copy
    - Validate a file copy
- **belief**
  - the current belief of the client about the status of its cached copy.



## Simplification # 1

- **Do not model contents of shared files.**
  - The file contents does not affect the coherence mechanism.



## Client – State Variables

- Possible values of the “belief” variable
  - Valid
    - the client knows that the cache copy is valid
  - Invalid
    - the client knows that the cached copy is invalid
  - Suspect
    - the client is not sure of the status of the cached copy
  - Nofile
    - client does not have a cached copy



## Simplification # 2

- In reality
  - The client has a status for every shared file
- We model
  - **Only one shared file**, since the coherence issues of each file is independent
    - Hence modeling one server is enough.

## Client SMV description

- MODULE client(input)
- VAR
- out: {0, fetch, validate};
- belief: {valid, invalid, suspect, nofile};
- ASSIGN
- ...
- Receives **input** from server
- **out** and **belief** are state variables

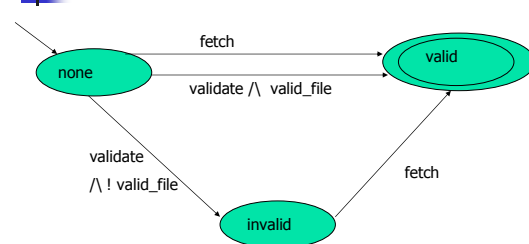
## Client- Trans. Rel. in SMV

- ASSIGN
- init(out) := 0;
- next(out) := case
- (belief = nofile) : fetch;
- (belief = invalid) : fetch;
- (belief = suspect): validate;
- 1: 0;
- esac
- ...

## Client – Trans. Rel. in SMV

- init(belief) := nofile, suspect;
- next(belief) :=
- case
- (belief=nofile)&(input=val): valid;
- (belief=suspect)&(input=val): valid;
- (belief=suspect)&(input=invalid): invalid;
- (belief=invalid)&(input=val): valid;
- 1 : belief
- esac
- belief is updated based on current value, and input from server.

## Server – State Diagram



Server receives fetch, validate from Client.

## Server – State Variables

- belief : the belief of the server about the status of a cached copy in a particular client
  - Valid
  - Invalid
  - None : Server has no knowledge (the client might or might not have a cached copy)
- For each client  $i$ , the server should model a belief[ $i$ ]
  - But we will simplify further and model only one client !!

## Server – State Variables

- out : the output of the server to the client
  - val: indicates to the client that its cached copy is valid
  - inval : indicates to the client that its cached copy is invalid
  - 0 : default output. Ignored by client.

## Simplification # 3

- Server has another state variable **valid\_file**
  - Boolean variable
- Models updates to the server by other clients
  - Which need not be modeled explicitly
- Suppose  $C.belief = suspect$ 
  - Then  $C$  sends a validate message to Server
- If Server has received a file update message by another client  $C'$  by now
  - Then server deems cached copy of  $C$  as invalid
  - Else ...

## Modeling other clients

- Whether Server receives a new update from another client is modeled by the variable **valid\_file**
  - Set non-deterministically since we do not model the other clients explicitly
- Modeled one client, and exploited the star topology to implicitly model the effects of other clients on the server
  - Drastically cuts down the state space.

## Simplification #4 (uncommon)

- Our modeling considers only finite traces
  - "Final" states in Client and Server
  - Restricted modeling of a single session
  - But can be used for verifying invariant properties
    - $AG(\text{boolean formula of atomic propositions})$
  - If we still find a violation of such properties they would have occurred in the generic modeling with infinite execution traces as well
    - The finite execution traces modeled are possible prefixes of the actual traces if the system was modeled in details

## System description in SMV

```
MODULE main
VAR
    Client : client(Server.out);
    Server: server(Client.out);
```

- Client module already presented
- Let us look at the Server.

## Server : SMV description

```
MODULE server(input)
VAR
    out      : {0, val, inval};
    belief    : {none, valid, invalid };
    valid_file : boolean;
ASSIGN
    valid_file := {0,1};
    ...
```

## Server's Transition Relation

```
init(belief) := none;
next(belief) :=
case
    (belief=none)&(input=fetch): valid;
    (belief=none)&(input=validate)&valid_file:valid;
    (belief=none)&(input=validate)& !valid_file:
        invalid;
    (belief=invalid)&(input=fetch): valid;
    1 : belief
esac
```

## Server's Transition Relation

```
■ init(out) := 0;
■ next(out) :=
■ case
■   (belief=none) & (input=fetch) : val;
■   (belief=none) & (input=validate) & valid_file:
■                                     val;
■   (belief=none) & (input=validate) & !valid_file:
■                                     inval;
■   (belief=invalid) & (input=fetch) : val;
■   1 : 0
■ esac
```

## Properties to Verify # 1

- If client C believes cached copy of file f is valid, it does not go to server
  - In this case, server also should believe that C's cached copy of f is valid
  - AG (C.belief=valid  $\Rightarrow$  S.belief = valid)
    - Always if C.belief=valid then S.belief = valid
      - We will learn about Temporal Logics in the next lecture at a formal level.
  - Verified to be true by CMU SMV

## Property # 2

- We can also check
  - AG(S.belief = valid  $\Rightarrow$  C.belief = valid)
  - Otherwise, client might sometimes unnecessarily go to the server for validation
    - Inefficiency : additional traffic from client to server !!
  - SMV produces a counter-example.

## SMV Counter-example

- **state 1.1**
  - C.out = 0, C.belief = nofile
  - S.out = 0, S.belief = none, S.valid\_file = 0
- **State 1.2**
  - C.out = fetch
- **State 1.3**
  - S.out = val, S. belief = valid



## SMV counterexample

- If client C does not have a copy of a shared file (cache miss), it requests from the server via **fetch**
- Server S sends a fresh copy and updates its belief about the status of cached copy at C
- Due to the transit delay between S and C, the client still has not updated its belief, but it will do in a few steps
  - This leads to the counter-example
  - Not a cause of concern in terms of additional traffic from the client to the server.

## Some useful simplifications ...

- ... employed in today's case study
  - Do not model data of the data items
    - Files in this case !
  - Model only a single data item
    - Hence model a single server
  - Model only one client
    - Other clients modeled implicitly by considering their effect on the server.

## Property specification

- We have not learnt about the Property Specification Language
  - Temporal Logics
  - In two flavors
    - Linear Time (LTL)
    - Branching Time (CTL)
- In next class ...