MODULE *syncCon*1

EXTENDS *Integers*, *Sequences*, *FiniteSets*, *TLC*

CONSTANT N, *FAILNUM*

ASSUME $N \leq 5 \ \land 0 \leq FAILNUM \land FAILNUM \leq 2$

$Nodes \triangleq 1 \,..\, N$

```
--algorithm syncCon1
{
    variable FailNum = FAILNUM,
             up = [n ∈ Nodes ↦ TRUE],
             pt = [n ∈ Nodes ↦ 0],
             t = [n ∈ Nodes ↦ FALSE],
             d = [n ∈ Nodes ↦ -1],
             mb = [n ∈ Nodes ↦ {}];

    define {
    SetMin(S) ≜ CHOOSE i ∈ S : ∀ j ∈ S : i ≤ j
    AllUpNodes ≜ {n ∈ Nodes : up[n] = TRUE}        A set of nodes that have not failed
    }

    macro MaybeFail( ) {
        if ( FailNum > 0 ∧ up[self] )
            { either
                { up[self] := FALSE ; FailNum := FailNum - 1 ; }
              or skip ; } ;
    }

    fair process ( n ∈ Nodes )
    variable v = 0, pv = 0, Q = {} ;
    {
P:  if ( up[self] ) {
      v := self ;
      Q := Nodes ;
PS: while ( up[self] ∧ Q ≠ {} ) {
        with ( p ∈ Q ) {
             mb[p] := mb[p] ∪ {v} ;
             Q := Q \ {p} ;
             MaybeFail() ;
         } ;
    } ;   end_while

    if ( up[self] ) pt[self] := pt[self] + 1 ;

PR: await (up[self] = TRUE ∧ ∀ k ∈ AllUpNodes : pt[self] = pt[k]) ;
        d[self] := SetMin(mb[self]) ;
        t[self] := TRUE ;

    }   end_if
```

```
    }   end_process
    }
}
```

BEGIN TRANSLATION

VARIABLES $FailNum$, up, pt, t, d, mb, pc

define statement

$SetMin(S) \triangleq$ CHOOSE $i \in S : \forall\, j \in S : i \leq j$

$AllUpNodes \triangleq \{n \in Nodes : up[n] = \text{TRUE}\}$

VARIABLES v, pv, Q

$vars \triangleq \langle FailNum,\ up,\ pt,\ t,\ d,\ mb,\ pc,\ v,\ pv,\ Q \rangle$

$ProcSet \triangleq (Nodes)$

$Init \triangleq$ Global variables

$\land\ FailNum = FAILNUM$
$\land\ up = [n \in Nodes \mapsto \text{TRUE}]$
$\land\ pt = [n \in Nodes \mapsto 0]$
$\land\ t = [n \in Nodes \mapsto \text{FALSE}]$
$\land\ d = [n \in Nodes \mapsto -1]$
$\land\ mb = [n \in Nodes \mapsto \{\}]$

Process n

$\land\ v = [self \in Nodes \mapsto 0]$
$\land\ pv = [self \in Nodes \mapsto 0]$
$\land\ Q = [self \in Nodes \mapsto \{\}]$
$\land\ pc = [self \in ProcSet \mapsto \text{“P”}]$

$P(self) \triangleq$
$\land\ pc[self] = \text{“P”}$
$\land$ IF $up[self]$
THEN $\land\ v' = [v$ EXCEPT $![self] = self]$
$\land\ Q' = [Q$ EXCEPT $![self] = Nodes]$
$\land\ pc' = [pc$ EXCEPT $![self] = \text{“PS”}]$
ELSE $\land\ pc' = [pc$ EXCEPT $![self] = \text{“Done”}]$
$\land$ UNCHANGED $\langle v,\ Q \rangle$
$\land$ UNCHANGED $\langle FailNum,\ up,\ pt,\ t,\ d,\ mb,\ pv \rangle$

$PS(self) \triangleq$
$\land\ pc[self] = \text{“PS”}$
$\land$ IF $up[self] \land Q[self] \neq \{\}$
THEN $\land \exists\, p \in Q[self] :$
$\land\ mb' = [mb$ EXCEPT $![p] = mb[p] \cup \{v[self]\}]$
$\land\ Q' = [Q$ EXCEPT $![self] = Q[self] \setminus \{p\}]$
$\land$ IF $FailNum > 0 \land up[self]$
THEN $\land\ \lor\ \land\ up' = [up$ EXCEPT $![self] = \text{FALSE}]$
$\land\ FailNum' = FailNum - 1$

$$
\begin{array}{l}
\qquad\qquad\qquad\qquad\qquad\qquad\qquad\qquad \lor \land \text{TRUE} \\
\qquad\qquad\qquad\qquad\qquad\qquad\qquad\qquad\quad \land \text{UNCHANGED } \langle \mathit{FailNum},\ \mathit{up} \rangle \\
\qquad\qquad\qquad\qquad\qquad\qquad\quad \text{ELSE} \quad \land \text{TRUE} \\
\qquad\qquad\qquad\qquad\qquad\qquad\qquad\qquad\quad \land \text{UNCHANGED } \langle \mathit{FailNum},\ \mathit{up} \rangle \\
\qquad\qquad\qquad\qquad\qquad\quad \land pc' = [pc \text{ EXCEPT } ![\mathit{self}] = \text{“PS”}] \\
\qquad\qquad\qquad\qquad\qquad\quad \land pt' = pt \\
\qquad\qquad\qquad\qquad\quad \text{ELSE} \quad \land \text{IF } \mathit{up}[\mathit{self}] \\
\qquad\qquad\qquad\qquad\qquad\qquad\quad \text{THEN} \quad \land pt' = [pt \text{ EXCEPT } ![\mathit{self}] = pt[\mathit{self}] + 1] \\
\qquad\qquad\qquad\qquad\qquad\qquad\quad \text{ELSE} \quad \land \text{TRUE} \\
\qquad\qquad\qquad\qquad\qquad\qquad\qquad\qquad\quad \land pt' = pt \\
\qquad\qquad\qquad\qquad\qquad\quad \land pc' = [pc \text{ EXCEPT } ![\mathit{self}] = \text{“PR”}] \\
\qquad\qquad\qquad\qquad\qquad\quad \land \text{UNCHANGED } \langle \mathit{FailNum},\ \mathit{up},\ \mathit{mb},\ Q \rangle \\
\qquad\qquad\qquad\qquad \land \text{UNCHANGED } \langle t,\ d,\ v,\ pv \rangle
\end{array}
$$

$$
\begin{array}{lll}
PR(\mathit{self}) & \triangleq & \land pc[\mathit{self}] = \text{“PR”} \\
& & \land (\mathit{up}[\mathit{self}] = \text{TRUE} \land \forall\, k \in \mathit{AllUpNodes} : pt[\mathit{self}] = pt[k]) \\
& & \land d' = [d \text{ EXCEPT } ![\mathit{self}] = \mathit{SetMin}(\mathit{mb}[\mathit{self}])] \\
& & \land t' = [t \text{ EXCEPT } ![\mathit{self}] = \text{TRUE}] \\
& & \land pc' = [pc \text{ EXCEPT } ![\mathit{self}] = \text{“Done”}] \\
& & \land \text{UNCHANGED } \langle \mathit{FailNum},\ \mathit{up},\ pt,\ \mathit{mb},\ v,\ pv,\ Q \rangle
\end{array}
$$

$$
n(\mathit{self}) \triangleq P(\mathit{self}) \lor PS(\mathit{self}) \lor PR(\mathit{self})
$$

$$
\begin{array}{lll}
\mathit{Next} & \triangleq & (\exists\, \mathit{self} \in \mathit{Nodes} : n(\mathit{self})) \\
& & \quad \lor \text{ Disjunct to prevent deadlock on termination} \\
& & \quad ((\forall\, \mathit{self} \in \mathit{ProcSet} : pc[\mathit{self}] = \text{“Done”}) \land \text{UNCHANGED } \mathit{vars})
\end{array}
$$

$$
\begin{array}{lll}
\mathit{Spec} & \triangleq & \land \mathit{Init} \land \Box[\mathit{Next}]_{\mathit{vars}} \\
& & \land \forall\, \mathit{self} \in \mathit{Nodes} : \mathrm{WF}_{\mathit{vars}}(n(\mathit{self}))
\end{array}
$$

$$
\mathit{Termination} \triangleq \Diamond(\forall\, \mathit{self} \in \mathit{ProcSet} : pc[\mathit{self}] = \text{“Done”})
$$

END TRANSLATION

$$
\mathit{Inv} \triangleq \forall\, i, j \in \mathit{Nodes} : (t[i] \land t[j]) \Rightarrow (d[i] = d[j])
$$

Violation of Agreement property: The decision value, $d\Box$, is set to the minimum of $mb[self]$ value. Now, when there is no crash node, all nodes send their value to $mb\Box$ and minimum is selected. But, when one or more nodes fail, they are not able to send their value (which could be minimum of all values) to the mailbox of other nodes. Hence, when the other nodes terminate, they may not able to correctly determine the minimum value. *i.e* $min(node\ i)$ may not be equal to $min(node\ j)$

This is submission for following students:

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