

20

$$Z = \frac{X - \mu}{\sigma}$$

$$n = 2000$$

$$\mu = 38000$$

$$\sigma = 10000$$

$$Z = \frac{50000 - 38000}{10000}$$

$$= \frac{12000}{10000}$$

$$Z = 1.2$$

area under the curve for $Z = 1.2$ is

0.8849 → left side

$$> 50,000 = 1 - 0.8849$$

$$P(X > 50000) = 0.1151 \approx 11.51\%$$

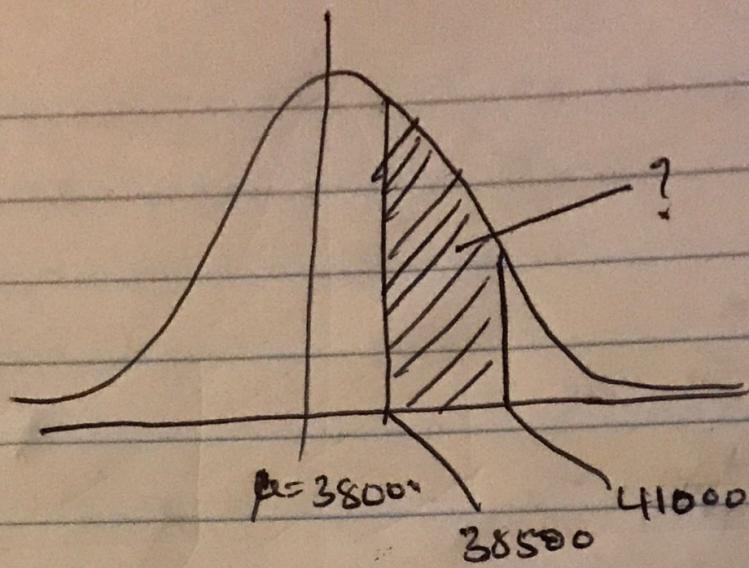
$$n = 11.51\% \text{ of } 2000$$

$$= 0.1151 \times 2000$$

$$= 230.2$$

n = 230 firms have sales over 50000

b)



$$Z_1 = \frac{x - \mu}{\sigma} = \frac{38500 - 38000}{10000}$$

$$Z_1 = \frac{500}{10000} = 0.05$$

$$Z_2 = \frac{41000 - 38000}{10000}$$

$$= 0.3$$

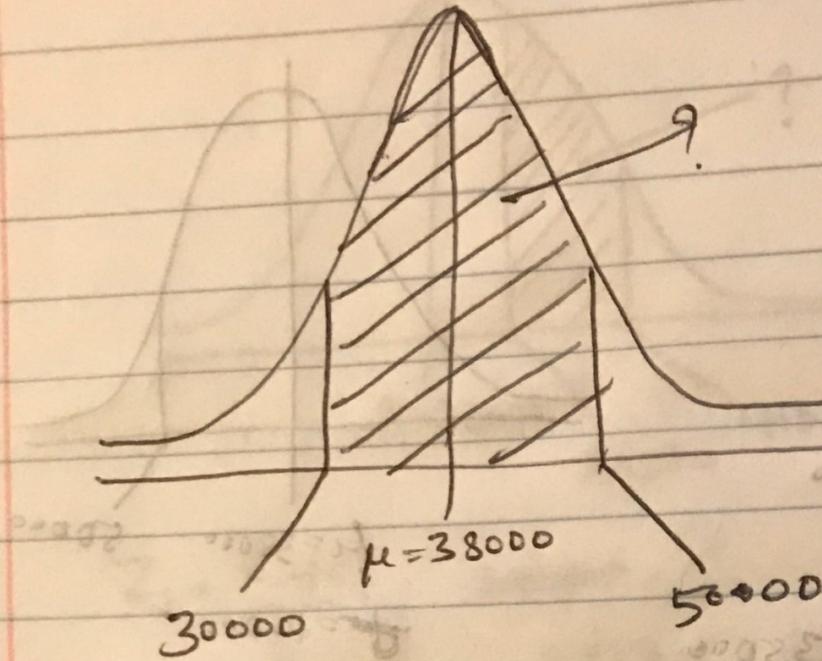
area of $Z_1 = 0.05 = 0.5199$

area of $Z_2 = 0.3 = 0.6179$

required area = $0.6179 - 0.5199$
 $= 0.098$

9.8% of firms have sales
 between 38500 & 41000.

c)



$$\frac{M-X}{\sigma} = 5$$

$$0005 = N$$

$$00028 = \Sigma$$

$$00001 = \pi$$

$$00025 - 00002 = 5$$

$$Z_1 = \frac{30000 - 38000}{10000}$$

$$= -0.8$$

$$Z_2 = \frac{50000 - 38000}{10000} = 5$$

$$-0.8 + 1.2 \leftarrow = P(1.2) = 0.8849$$

$$P(2.8 - 1) = 0.028$$

$$Z_1 \text{ area for } 1.2 - 0.8 = 0.2119$$

$$Z_2 \text{ area for } 1.2 = 0.8849$$

$$\text{Required area} = 0.8849 - 0.2119$$

$$= 0.673$$

67.3% of firms have sales between 30000 & 50000

$$0.673 \times 2000$$

$$= 1346 \text{ firms}$$

4) poisson Distribution:-

$$\lambda = 4$$

$$x=0$$

$$P(X=x) = P(X=0) = \frac{e^{-\lambda} \lambda^x}{x!}$$

$$= \frac{e^{-4} 4^0}{0!}$$

$$= e^{-4} = 0.0183$$

prob that no photon reaches = 1.83%.

5) $\lambda = 3$

$$x=0$$

$$P(X=x) = P(X=0) = \frac{e^{-\lambda} \lambda^x}{x!} = \frac{e^{-3} 3^0}{0!}$$

$$= e^{-3} = 0.0497 =$$

$$b) P(X \geq 2) = e^{-\lambda} \sum_{i=0}^{\infty} \lambda^i / i! \quad 4.97\%$$

$$P(X \geq 2) = P(X=2) + P(X=3) + P(X=4) - - -$$

$$= 1 - [P(X=0) + P(X=1) + P(X=2)]$$

$$= 1 - e^{-3} \left[\frac{\lambda^0}{0!} + \frac{\lambda^1}{1!} + \frac{\lambda^2}{2!} \right] = 1 - 0.0497 (1+3+4.5)$$

$$= 1 - 0.0497 (8.5)$$

$$= 0.5775 = 57.75\%$$

Prob that at least 2 calls arrive in 2min

$$6) \quad r=3$$

$$n=4$$

$p = 0.8$ = Success = not defective

$q = 0.2$ = failure = defective

$$P(X=r) = {}^n C_r p^r q^{n-r}$$

$$= {}^4 C_3 (0.8)^3 (0.2)^1$$

$$= (0.8)^3 (0.2) \times 4$$

$$= 0.1024 \times 4$$

$$= 0.4096$$

8)

- T) $p = 0.3$ = probability of success
 $q = 0.7$ = probability of failure
 $n = 5$

γ = atmost 2 are accepted i.e., $(X \leq 2)$

$$P(X \leq 2) = P(X=0) + P(X=1) + P(X=2)$$

$$= \left[{}^5 C_0 (0.3)^0 (0.7)^5 \right] + \left[{}^5 C_1 (0.3)^1 (0.7)^4 \right] + \left[{}^5 C_2 (0.3)^2 (0.7)^3 \right]$$

$$= \left(\frac{5!}{0!} 0.7^5 \right) + (5 \times 0.3 \times 0.7^4) + (10 \times 0.3^2 \times 0.7^3)$$

$$= 0.1681 + 0.3602 + 0.3087$$

$$= 0.837$$

= 83.7% = probability of atmost 2 are accepted.

which is greater than 800kg ∴ it's not safe.

$$8) \mu = 70 \text{ kg}$$
$$\sigma = 200$$

$$X = 800 \text{ kg} - \text{given}$$

probability of safety for 10 adults

$$\mu = 10 \times 70 = 700 \text{ kgs}$$

$$Z = \frac{X - \mu}{\sigma} = \frac{800 - 700}{200} = \frac{1}{2} = 0.5$$
$$= 0.6915$$

probability of Safety for 10 adults is
69.15%.

$$\text{for 12 adults} = \mu = 12 \times 70 = 840 \text{ kg}$$

$$Z = \frac{800 - 840}{200} = \frac{-40}{200} = \frac{-1}{5}$$
$$= -0.2$$
$$= 0.4207$$

probability of Safety for 12 adults

$$= 42.07\%$$

$$nCr p^r q^{n-r} - \text{Binomial Dist.}$$

$$9) n = 50$$

$x = \text{atleast } 20$ to be answered correctly

$$p(x \geq 20)$$

$p = \frac{1}{2}$ = probability of success (2 choices)

$q = \frac{1}{2}$ = probability of failure

$$p(x \geq 20) = 1 - p(x < 20)$$

$$= 1 - [p(x=0) + p(x=1) + p(x=2) + p(x=3) + \dots + p(x=19)]$$

$$= 1 - [p(x=0) + p(x=1) + p(x=2) + \dots + p(x=19)]$$

$$= 1 - [({}^{50}C_0 0.5^0 0.5^{50}) + ({}^{50}C_1 0.5^1 0.5^{49}) + \dots + {}^{50}C_{19} 0.5^{19} 0.5^{31}]$$

4 choices

$$p = \frac{1}{4} = \text{probability of success} = 0.25$$

$$q = \frac{3}{4} = \text{probability of failure} = 0.75$$

$$p(x \geq 20) = 1 - p(x < 20)$$

$$= 1 - [{}^{50}C_0 0.25^0 0.75^{50} + {}^{50}C_1 0.25^1 0.75^{49} + {}^{50}C_2 0.25^2 0.75^{48} + \dots + {}^{50}C_{19} 0.25^{19} 0.75^{31}]$$

10) $p = 0.3$ = probability of success = faulty

$q = 0.7$ = probability of failure = good

$n = 6$

$\gamma = 2$ faulty

$$P(X=2) = {}^n C_r p^r q^{n-r}$$

$$= {}^6 C_2 (0.3)^2 (0.7)^4$$

$$= 15 \times 0.3^2 \times 0.7^4$$

$$= 0.3241$$

probability that exactly 2 are faulty

$$= 32.41 \%$$

11) 6 errors per hour

6 errors per 60 minutes

$$\text{for 1 minute} = \frac{6}{60} = 0.1 \text{ error} = \lambda$$

for 2 errors in 322 word report

given 77 words per minute

then 322 words in = 4.18 minutes

$$\text{for } 4.18 \text{ min} \quad \lambda = (0.1)(4.18)$$

$$\hookrightarrow \text{so } \lambda = (0.1)(4.18)$$

$$= 0.418$$

$$\gamma = 2$$

$$P(X=2) = \frac{e^{-\lambda} \lambda^2}{2!} = \frac{e^{-0.418} (0.418)^2}{2!}$$

$$= \frac{(0.6584) * 0.1747}{2}$$

$$= 0.0575$$

probability of 2 errors = 5.75%
in 322 word report

- (2) $P = 0.05\%$ = probability of success =
 contain soil residues of
 dioxin
- $n = 20$
- $r = \text{less than } 1$
- $P(X < 1)$
- $q = 0.95\%$ = probability of failure
 = doesn't contain soil residues
 of dioxin

$$P(r) = P(X < 1) = P(X=0) = {}^n C_r p^r q^{n-r}$$

$$= {}^{20} C_0 (0.05)^0 (0.95)^{20}$$

$$= (0.95)^{20} = 0.3585$$

probability that less than 1 site exceeds recommended level of dioxin. = 35.85%.

$$\text{b) } P(X \leq 1) = P(X=0) + P(X=1)$$

$$P(X=0) = 0.3585$$

$$P(X=1) = {}^{20} C_1 (0.05)^1 (0.95)^{19}$$

$$= 20 \times 0.05 \times 0.3774 = 0.3774$$

$$P(X \leq 1) = 0.3585 + 0.3774 = 0.7359 = 73.59\%$$

c) atmost 2 sites

$$P(X \leq 2) = P(X=0) + P(X=1) + P(X=2)$$

$$P(X=0) = 0.3585$$

$$P(X=1) = 0.3774$$

$$P(X=2) = 20 \times 0.0025 \times 0.95^{18}$$

$$= 190 \times 0.0025 \times 0.3972$$

$$= 0.1887$$

$$P(X \leq 2) = 0.3585 + 0.3774 + 0.1887$$

$$= 0.9247$$

$$= 92.47\%$$

13) $p = 0.05\%$. = probability of success = Revenue Audits
 $q = 0.95\%$. = probability of failure = Non revenue audit companies

$$n = 5$$

$$x = 2$$

$$P(X=2) = P(X=2) = {}^5C_2 (0.05)^2 (0.95)^3 \\ = 10 \times 0.0025 \times 0.8574 \\ = 0.0214$$

prob that 'RWD' will be selected exactly twice in next 5 yrs

by exactly twice in next 2 years

$$n = 2$$

$$x = 2$$

$$P(X=2) = {}^2C_2 (0.05)^2 (0.95)^0 \\ = 0.05 \times 0.05 \\ = 0.0025 \\ = 0.25\%$$

c) atleast once in next 4 years $P(X \geq 1)$; $n = 4$

$$P(X=1) + P(X=2) + P(X=3) + P(X=4) = 1 - P(X=0)$$

$$[1 - P(X=0)] = 1 - {}^4C_0 (0.05)^0 (0.95)^4 \\ = 1 - 0.8145 = 0.1855 = 18.55\%$$

14) $p = 0.2 = p(\text{success})$ = must stop at any one of traffic signals

$q = 0.8 = p(\text{failure})$ = not failed - not stopping
 $n=15$

a) must stop at exactly 2 signals

$$\delta = 2$$

$$p(X=\delta) = p(X=2) = {}_{15}C_2 p^2 q^{15-2}$$

$$= {}_{15}C_2 (0.2)^2 (0.8)^{13}$$

$$= 105 \times 0.04 \times 0.05498$$

$$= 0.2309$$

= 23.09% is the probability that a student must stop exactly at 2 signals.

b) $p(X \geq 1)$

$$= p(X=1) + p(2) +$$

$$= p(X=1) + p(X=2) + p(X=3) + \dots + p(X=15)$$

$$= 1 - p(X=0)$$

$$= 1 - {}_{15}C_0 (0.2)^0 (0.8)^{15}$$

$$= 1 - (0.8)^{15}$$

$$= 1 - 0.0352$$

$$= 0.9648$$