**4.2** Compute the following determinant efficiently:

$$\begin{bmatrix} 2 & 0 & 1 & 2 & 0 \\ 2 & -1 & 0 & 1 & 1 \\ 0 & 1 & 2 & 1 & 2 \\ -2 & 0 & 2 & -1 & 2 \\ 2 & 0 & 0 & 1 & 1 \end{bmatrix}$$

## Solution.

We can apply Gauss Jordan reduction to convert the matrix to an upper triangular matrix. Then, the determinant is the product of the diagonal elements.

 $\det = 2 * -1 * 1 * 1 * -3 = 6.$