

1.6 Covariance of two variables x and y is given by 1.41:

$$cov[x, y] = E_{x,y}[xy] - E[x]E[y]$$

The term $E_{x,y}[xy]$ is defined as:

$$E_{x,y}[xy] = \int_y \int_x xy p(x, y) dx dy$$

Since x and y are independent, $p(x, y) = p(x)p(y)$

$$\begin{aligned} \implies E_{x,y}[xy] &= \int_y \int_x xy p(x)p(y) dx dy \\ &= \int_y y p(y) \left(\int_x x p(x) dx \right) dy \\ &= \int_y y p(y) E[x] dy \\ &= E[x] \int_y y p(y) dy \\ &= E[x] E[y] \end{aligned}$$

Therefore, covariance becomes:

$$cov[x, y] = E[x]E[y] - E[x]E[y] = 0.$$