

2.53

$$\begin{aligned}\sum_{n=1}^N \sin(\theta_n - \theta_0) &= 0 \\ \implies \sum_{n=1}^N (\cos \theta_0 \sin \theta_n - \cos \theta_n \sin \theta_0) &= 0 \\ \implies \cos \theta_0 \sum_{n=1}^N \sin \theta_n - \sin \theta_0 \sum_{n=1}^N \cos \theta_n &= 0 \\ \implies \cos \theta_0 \sum_{n=1}^N \sin \theta_n &= \sin \theta_0 \sum_{n=1}^N \cos \theta_n \\ \implies \tan \theta_0 &= \left\{ \frac{\sum_{n=1}^N \sin \theta_n}{\sum_{n=1}^N \cos \theta_n} \right\} \\ \implies \theta_0^{ML} &= \tan^{-1} \left\{ \frac{\sum_{n=1}^N \sin \theta_n}{\sum_{n=1}^N \cos \theta_n} \right\}\end{aligned}$$

which is the result in 2.184 that we wanted.