

$$\begin{aligned} \mathbf{1.3} \quad p(\text{fruit} = \text{apple}) &= p(\text{fruit} = \text{apple} \mid \text{box} = \text{red}) * p(\text{box} = \text{red}) \\ &+ p(\text{fruit} = \text{apple} \mid \text{box} = \text{blue}) * p(\text{box} = \text{blue}) \\ &+ p(\text{fruit} = \text{apple} \mid \text{box} = \text{green}) * p(\text{box} = \text{green}) \end{aligned}$$

$$= \frac{3}{10} * 0.2 + \frac{1}{2} * 0.2 + \frac{3}{10} * 0.6$$

$$= 0.3 * 0.2 + 0.1 + 0.18$$

$$= 0.06 + 0.1 + 0.18$$

$$= 0.34$$

Next, we find the probability that the box was green, given that the fruit we selected was an orange.

Using Baye's rule,

$$p(\text{box} = \text{green} \mid \text{fruit} = \text{orange}) = \frac{p(\text{fruit} = \text{orange} \mid \text{box} = \text{green}) * p(\text{box} = \text{green})}{p(\text{fruit} = \text{orange})}$$

$$\begin{aligned} p(\text{fruit} = \text{orange}) &= p(\text{fruit} = \text{orange} \mid \text{box} = \text{red}) * p(\text{box} = \text{red}) \\ &+ p(\text{fruit} = \text{orange} \mid \text{box} = \text{blue}) * p(\text{box} = \text{blue}) \\ &+ p(\text{fruit} = \text{orange} \mid \text{box} = \text{green}) * p(\text{box} = \text{green}) \end{aligned}$$

$$= \frac{4}{10} * 0.2 + \frac{1}{2} * 0.2 + \frac{3}{10} * 0.6$$

$$= 0.4 * 0.2 + 0.1 + 0.3 * 0.6$$

$$= 0.08 + 0.1 + 0.18$$

$$= 0.36$$

$$p(\text{fruit} = \text{orange} \mid \text{box} = \text{green}) * p(\text{box} = \text{green}) = 0.18$$

$$\text{Therefore, } p(\text{box} = \text{green} \mid \text{fruit} = \text{orange}) = \frac{0.18}{0.36} = 0.5.$$