Fast Sudoku Solver in Haskell #1: A Simple Solution

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udoku is a number placement puzzle. It consists of a 9x9 grid which is to be filled with digits from 1 to 9. Some of the cells of the grid come pre-filled and the player has to fill the rest.

Haskell is a purely functional programming language. It is a good choice to solve Sudoku given the problem's combinatorial nature. The aim of this series of posts is to write a **fast** Sudoku solver in Haskell. We'll focus on both implementing the solution and making it efficient, step-by-step, starting with a slow but simple solution in this post¹.

This is the first post in a series of posts:

- 1. Fast Sudoku Solver in Haskell #1: A Simple Solution
- 2. Fast Sudoku Solver in Haskell #2: A 200x Faster Solution
- 3. Fast Sudoku Solver in Haskell #3: Picking the Right Data Structures

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Constraint Satisfaction Problem

Solving Sudoku is a constraint satisfaction problem. We are given a partially filled grid which we have to fill completely such that each of the following constraints are satisfied:

- 1. Each of the nine rows must have all the digits, from 1 to 9.
- 2. Each of the nine columns must have all the digits, from 1 to 9.
- 3. Each of the nine 3x3 sub-grids must have all the digits, from 1 to 9.

+			- + - I				+ -		 1		- + I
4	2	•		•	•	•		•	1 .	•	
	•	8 1		•	5			4 3	•	7	
3	5	•		4 1 8	•	6		2	•	•	
+	A	Sã	amp	ole	e k) u z	Z	le			- +
6 4 1	9 8 2	3 7 5		7 5 9	8 1 6	4 2 3	+ -	5 9 8	1 3 7	2 6 4	+-
9 5 7	3 6 4	2 8 1		6 2 3	5 4 9	1 7 8		4 3 6	8 9 2	7 1 5	
3 8 2	1 5 7	9 6 4		4 1 8	7 2 3	5 9 6		2 7 1	6 4 5	8 3 9	
			т.			olu	т.				+

Each cell in the grid is member of one row, one column and one sub-grid (called *block* in general). Digits in the pre-filled cells impose constraints on the rows, columns, and sub-grids they are part of. For example, if a cell contains 1 then no other cell in that cell's row, column or sub-grid can contain 1. Given these constraints, we can devise a simple algorithm to solve Sudoku:

1. Each cell contains either a single digit or has a set of possible digits. For example, a grid showing the possibilities of all non-filled cells for the sample puzzle above:

Ĺ	4	[123456789]	[123456789]	[123456789]	[123456789]	[123456789] [123456789] [123456789]	[123456789]	[123456789]	
į	[123456789]	[123456789]	8	[123456789]	[123456789]	[123456789] [123456789] [123456789]	3		[123456789]
j	[123456789]	5	[123456789] [123456789] [123456789]	İ 1	[123456789]	[123456789] [123456789] 6	[123456789]	[123456789]	[123456789]

2. If a cell contains a digit, remove that digit from the list of the possible digits from all its neighboring cells. Neighboring cells are the other cells in the given cell's row, column and sub-grid. For example, the grid after removing the fixed value 4 of the row-2-column-1 cell from its neighboring cells:

ij	4		[123 56789]	[123 56789]	[123	56789]	[123 56789]	[123 56789]	[123 56789	[123 56789]	[123456789] [123 56789] [123456789]
ij	[123	56789]	[123456789]	8	[1234	56789]	[123456789] 9		3 [123456789	[123456789] [123456789]	7 [123456789] [123456789]
ĺ	[123	56789]	5	[123456789] [123456789] [123456789]	1		[123456789] [123456789]	[123456789] [123456789]	2 [123456789	[123456789]] [123456789]	[123456789] [123456789] [123456789]

3. Repeat the previous step for all the cells that are have been solved (or *fixed*), either pre-filled or filled in the previous iteration of the solution. For example, the grid after removing all fixed values from all non-fixed cells:

[4 [1	56789] [3 6789] [3 567 9] [1 3 6789] [3 567 9] 56789] 2 [3 567 9]	[23 567 9] [23 567 9] [3 567 9]] [234 678] [234] [123 678] [123] [1 34 678] [1 34	45 789] [5 789] [45 789] [56789] 1 [23456 89] 56789] [23 56789] [23 56 89] 56789] [3456789] [3456 89]
[2	6 9] [3 6 9] [23 6 9]	[23 6]] 5 [123	8] 4	[2 6 89] 7
[2	567 9] [4 67 9] 8	[2 67]] [12 4 67] [12 4	4 7] 3	[2 56 9] [12 56 9]
[2	567] [34 67] 1	[23 67]] 9 [234	4 78] [56 8] [2 56 8] [2 56 8]
3	[1 6789] [67 9]	4	7 [5 7 9] 2	[56789] [1 56 89]
[2	6789] 5	1		7 9] [6789] [34 6789] [34 6 89]

4. Continue till the grid *settles*, that is, there are no more changes in the possibilities of any cells. For example, the settled grid for the current iteration:

[56789] [3 6789] [3 567 9]	[23 567 9] [234 6 8	3] [2345 789] [56789] 1
4	[1 3 6789] [3 567 9]	[23 567 9] [123 6 8	3] [123 5 789] [
[1	56789] 2 [3 567 9]	[3 567 9] [1 34 6 8	4] [1 345 789] [
[2	6 9] [3 6 9] [23 6 9]	[23 6] 5	[123 8] 4	[2 6 89] 7
[2	567 9] [4 67 9] 8	[2 67] [12 4 6] [12 4 7] 3	[2 56 9] [12 56 9]
[2	567] [34 67] 1	[23 67] 9	[234 78] [56 8] [2 56 8] [2 56 8]
3 [2	[1 6 89] [6 9]	4	[5 9] 2] [23 9] [[56 89] [1 56 89] 6789] [34 6789] [34 6 89] 5 7 9] [345 7 9] [1 345 9]

- 5. Once the grid settles, choose one of the non-fixed cells following some strategy. Select one of the digits from all the possibilities of the cell, and fix (assume) the cell to have that digit. Go back to step 1 and repeat.
- 6. The elimination of possibilities may result in inconsistencies. For example, you may end up with a cell with no possibilities. In such a case, discard that branch of solution, and backtrack to last point where you fixed a cell. Choose a different possibility to fix and repeat.
- 7. If at any point the grid is completely filled, you've found the solution!
- 8. If you exhaust all branches of the solution then the puzzle is unsolvable. This can happen if it starts with cells pre-filled wrongly.

This algorithm is actually a Depth-First Search on the state space of the grid configurations. It guarantees to either find a solution or prove a puzzle to be unsolvable.

Setting up

We start with writing types to represent the cells and the grid:

```
data Cell = Fixed Int | Possible [Int] deriving (Show, Eq)
type Row = [Cell]
type Grid = [Row]
```

A cell is either fixed with a particular digit or has a set of digits as possibilities. So it is natural to represent it as a sum type with Fixed and Possible constructors. A row is a list of cells and a grid is a list of rows.

We'll take the input puzzle as a string of 81 characters representing the cells, left-to-right and top-to-bottom. An example is:

```
.....1.4.......2...........5.4.7..8...3....1.9....3..4..2...5.1........8.6...
```

Here, . represents an non-filled cell. Let's write a function to read this input and parse it to our Grid data structure:

readGrid return a Just grid if the input is correct, else it returns a Nothing. It parses a . to a Possible cell with all digits as possibilities, and a digit char to a Fixed cell with that digit. Let's try it out in the *REPL*:

The output is a bit unreadable but correct. We can write a few functions to clean it up:

```
showGrid :: Grid -> String
showGrid = unlines . map (unwords . map showCell)
  where
    showCell (Fixed x) = show x
    showCell _ = "."

showGridWithPossibilities :: Grid -> String
showGridWithPossibilities = unlines . map (unwords . map showCell)
  where
    showCell (Fixed x) = show x ++ " "
    showCell (Possible xs) =
        (++ "]")
    . Data.List.foldl' (\acc x -> acc ++ if x `elem` xs then show x else " ") "["
    $ [1..9]
```

Back to the REPL again:

```
*Main> Just grid = readGrid
"......1.4.......2...........5.4.7..8...3....1.9....3..4..2...5.1........8.6..."
*Main> putStrLn $ showGrid grid
. . . . . . . 1 .
4 . . . . . . . .
. 2 . . . . . . .
. . . . 5 . 4 . 7
. . 8 . . . 3 . .
. . 1 . 9 . . . .
3 . . 4 . . 2 . .
. 5 . 1 . . . . .
. . . 8 . 6 . . .
*Main> putStrLn $
                    [123456789]4
                                      [123456789][123456789][123456789][123456789]3
                                                                                     [123456789][123456789]
showGridWithPossibilities[123456789][123456789] 2
                                               [123456789][123456789][123456789][123456789] 5
                                                                                              [123456789]
                    [123456789][123456789][123456789][123456789] 8
grid
                                                                 1
                                                                           [123456789][123456789][123456789]
                    [123456789][123456789][123456789][123456789][123456789] 4
                    [123456789][123456789][123456789] 5
                                                       [123456789] 9
                                                                           [123456789][123456789][123456789]
                    [123456789][123456789][123456789][123456789][123456789][123456789][123456789] 6
                    [123456789][123456789][123456789] 4
                                                                  [123456789] 2
                                                                                     [123456789][123456789]
                             [123456789][123456789][123456789][123456789][123456789][123456789][123456789]
                    [123456789][123456789][123456789] 7
                                                        [123456789][123456789][123456789][123456789]
```

The output is more readable now. We see that, at the start, all the non-filled cells have all the digits as possible values. We'll use these functions for debugging as we go forward. We can now start solving the puzzle.

Pruning the Cells

We can remove the digits of fixed cells from their neighboring cells, one cell as a time. But, it is faster to find all the fixed digits in a row of cells and remove them from the possibilities of all the non-fixed cells of the row, at once. Then we can repeat this *pruning* step for all the rows of the grid (and columns and sub-grids too! We'll see how).

```
pruneCells :: [Cell] -> Maybe [Cell]
pruneCells cells = traverse pruneCell cells
  where
    fixeds = [x | Fixed x <- cells]

    pruneCell (Possible xs) = case xs Data.List.\\ fixeds of
      [] -> Nothing
      [y] -> Just $ Fixed y
      ys -> Just $ Possible ys
    pruneCell x = Just x
```

pruneCells prunes a list of cells as described before. We start with finding the fixed digits in the list of cells. Then we go over each non-fixed cells, removing the fixed digits we found, from their possible values. Two special cases arise:

- If pruning results in a cell with no possible digits, it is a sign that this branch of search has no solution and hence, we return a Nothing in that case.
- If only one possible digit remains after pruning, then we turn that cell into a fixed cell with that digit.

We use the traverse function for pruning the cells so that a Nothing resulting from pruning one cell propagates to the entire list.

Let's take it for a spin in the *REPL*:

It works! 6 and 1 are removed from the possibilities of the other cells. Now we are ready for ...

Pruning the Grid

Pruning a grid requires us to prune each row, each column and each sub-grid. Let's try to solve it in the *REPL* first:

```
*Main> Just grid = readGrid
                                                                                         *Main> putStr $
                                                                                *Main>
"6.....1.4......2..........5.4.7..8..3...1.9....3..4..2...5.1.......8.6..."Just grid'showGridWithPossibilities[ [123
                                                                                                                  23455678
                                                                                pruneCells
                                                                                                                  789][123
                                                                                                                  [ 5678
                                                                                grid
                                                                                                                  2345[123
                                                                                                                  789]5678
                                                                                                                  [ [123
                                                                                                                  23455678
                                                                                                                  789][123
                                                                                                                  [ 5678
                                                                                                                  2345[123
                                                                                                                  789]5678
                                                                                                                  [ [123
                                                                                                                  23455678
                                                                                                                  789][123
                                                                                                                  [ 5678
                                                                                                                  2345
                                                                                                                  789]
                                                                                                                  1
                                                                                                                  [
                                                                                                                  2345
                                                                                                                  789]
```

By traverse-ing the grid with pruneCells, we are able to prune each row, one-by-one. Since pruning a row doesn't affect another row, we don't have to pass the resulting rows between each pruning step. That is to say, traverse is enough for us, we don't need foldl here.

How do we do the same thing for columns now? Since our representation for the grid is rows-first, we first need to convert it to a columns-first representation. Luckily, that's what Data.List.transpose function does:

```
*Main> Just grid = readGrid
"693784512487512936125963874932651487568247391741398625319475268856129743274836159"
*Main> putStr $ showGrid grid
6 9 3 7 8 4 5 1 2
4 8 7 5 1 2 9 3 6
1 2 5 9 6 3 8 7 4
9 3 2 6 5 1 4 8 7
5 6 8 2 4 7 3 9 1
7 4 1 3 9 8 6 2 5
3 1 9 4 7 5 2 6 8
8 5 6 1 2 9 7 4 3
2 7 4 8 3 6 1 5 9
*Main> putStr $ showGrid $ Data.List.transpose grid
6 4 1 9 5 7 3 8 2
9 8 2 3 6 4 1 5 7
3 7 5 2 8 1 9 6 4
7 5 9 6 2 3 4 1 8
8 1 6 5 4 9 7 2 3
4 2 3 1 7 8 5 9 6
5 9 8 4 3 6 2 7 1
1 3 7 8 9 2 6 4 5
2 6 4 7 1 5 8 3 9
```

Pruning columns is easy now:

First, we transpose the grid to convert the columns into rows. Then, we prune the rows by traverse-ing pruneCells over them. And finally, we turn the rows back into columns by transpose-ing the grid back again. The last transpose needs to be fmap-ped because traverse pruneCells returns a Maybe.

Pruning sub-grids is a bit trickier. Following the same idea as pruning columns, we need two functions to transform the sub-grids into rows and back. Let's write the first one:

```
subGridsToRows :: Grid -> Grid
subGridsToRows =
  concatMap (\rows -> let [r1, r2, r3] = map (Data.List.Split.chunksOf 3) rows
                       in zipWith3 (a b c \rightarrow a ++ b ++ c) r1 r2 r3)
  . Data.List.Split.chunksOf 3
And try it out:
*Main> Just grid = readGrid
"693784512487512936125963874932651487568247391741398625319475268856129743274836159"
*Main> putStr $ showGrid grid
6 9 3 7 8 4 5 1 2
4 8 7 5 1 2 9 3 6
1 2 5 9 6 3 8 7 4
9 3 2 6 5 1 4 8 7
5 6 8 2 4 7 3 9 1
7 4 1 3 9 8 6 2 5
3 1 9 4 7 5 2 6 8
8 5 6 1 2 9 7 4 3
2 7 4 8 3 6 1 5 9
*Main> putStr $ showGrid $ subGridsToRows grid
6 9 3 4 8 7 1 2 5
7 8 4 5 1 2 9 6 3
5 1 2 9 3 6 8 7 4
9 3 2 5 6 8 7 4 1
6 5 1 2 4 7 3 9 8
4 8 7 3 9 1 6 2 5
3 1 9 8 5 6 2 7 4
4 7 5 1 2 9 8 3 6
```

You can go over the code and the output and make yourself sure that it works. Also, it turns out that we don't need to write the back-transform function. subGridsToRows is its own back-transform:

2 6 8 7 4 3 1 5 9

```
*Main> putStr $ showGrid grid
6 9 3 7 8 4 5 1 2
4 8 7 5 1 2 9 3 6
1 2 5 9 6 3 8 7 4
9 3 2 6 5 1 4 8 7
5 6 8 2 4 7 3 9 1
7 4 1 3 9 8 6 2 5
3 1 9 4 7 5 2 6 8
8 5 6 1 2 9 7 4 3
2 7 4 8 3 6 1 5 9
*Main> putStr $ showGrid $ subGridsToRows $ subGridsToRows $ grid
6 9 3 7 8 4 5 1 2
4 8 7 5 1 2 9 3 6
1 2 5 9 6 3 8 7 4
9 3 2 6 5 1 4 8 7
5 6 8 2 4 7 3 9 1
7 4 1 3 9 8 6 2 5
3 1 9 4 7 5 2 6 8
8 5 6 1 2 9 7 4 3
2 7 4 8 3 6 1 5 9
```

Nice! Now writing the sub-grid pruning function is easy:

It works well. Now we can string together these three steps to prune the entire grid. We also have to make sure that result of pruning each step is fed into the next step. This is so that the fixed cells created into one step cause more pruning in the further steps. We use monadic bind (>>=) for that. Here's the final code:

```
pruneGrid' :: Grid -> Maybe Grid
pruneGrid' grid =
  traverse pruneCells grid
  >>= fmap Data.List.transpose . traverse pruneCells . Data.List.transpose
  >>= fmap subGridsToRows . traverse pruneCells . subGridsToRows
```

And the test:

```
*Main> Just grid = readGrid
                                                                                                                6 4
                                                                               *Main>
                                                                                        *Main> putStr $
"6.....1.4.......2......5.4.7..8...3...1.9....3..4..2...5.1......8.6..."Just grid'showGridWithPossibilities[ 3[1 3
                                                                                                                789]789]
                                                                               pruneGrid'
                                                                                                                [ 33 5
                                                                                                                5 7 9] [
                                                                               grid
                                                                                                                9] [23 5
                                                                                                                23 59]
                                                                                                                7 9][123
                                                                                                                [ 678
                                                                                                                234 [123
                                                                                                                78 ]789]
                                                                                                                [ 5678
                                                                                                                2345[ 23
                                                                                                                789]5678
                                                                                                                [ [ 23
                                                                                                                5 56 8
                                                                                                                789]
                                                                                                                 1
                                                                                                                [
                                                                                                                2345
                                                                                                                89]
```

We can clearly see the massive pruning of possibilities all around the grid. We also see a 7 pop up in the row-7-column-5 cell. This means that we can prune the grid further, until it settles. If you are familiar with Haskell, you may recognize this as trying to find a fixed point for the pruneGrid' function, except in a monadic context. It is simple to implement:

```
pruneGrid :: Grid -> Maybe Grid
pruneGrid = fixM pruneGrid'
  where
    fixM f x = f x >>= \x' -> if x' == x then return x else fixM f x'
```

The crux of this code is the fixM function. It takes a monadic function f and an initial value, and recursively calls itself till the return value settles. Let's do another round in the *REPL*:

```
*Main> Just grid = readGrid
                                                                               *Main>
                                                                                       *Main> putStr $
                                                                                                               6 4
"6.....1.4......2..........5.4.7..8...3....1.9....3...4..2...5.1.......8.6..."Just
                                                                                        showGridWithPossibilities[ 3[1 3
                                                                                                                789]789]
                                                                               pruneGrid
                                                                                                               [ 33 5 7
                                                                                                               5 7 9] [
                                                                               grid
                                                                                                               9] [23 56
                                                                                                               23 59]
                                                                                                               7 9][123
                                                                                                                [ 68]
                                                                                                               234 [123
                                                                                                                8 ] 789]
                                                                                                                [ 56789
                                                                                                               2345[ 23
                                                                                                                789]56789
                                                                                                               [ [ 23
                                                                                                                5 56 89
                                                                                                                789]
                                                                                                                1
                                                                                                               2345
                                                                                                                89]
```

We see that 7 in the row-7-column-5 cell is eliminated from all its neighboring cells. We can't prune the grid anymore. Now it is time to make the choice.

Making the Choice

One the grid is settled, we need to choose a non-fixed cell and make it fixed by assuming one of its possible values. This gives us two grids, next in the state-space of the solution search:

- one which has this chosen cell fixed to this chosen digit, and,
- the other in which the chosen cell has all the other possibilities except the one we chose to fix.

We call this function, nextGrids:

```
nextGrids :: Grid -> (Grid, Grid)
nextGrids grid =
  let (i, first@(Fixed _), rest) =
       fixCell
        . Data.List.minimumBy (compare `Data.Function.on` (possibilityCount . snd))
        . filter (isPossible . snd)
        . zip [0..]
        . concat
        $ grid
  in (replace2D i first grid, replace2D i rest grid)
    isPossible (Possible _) = True
   isPossible _
                           = False
    possibilityCount (Possible xs) = length xs
   possibilityCount (Fixed _) = 1
    fixCell (i, Possible [x, y]) = (i, Fixed x, Fixed y)
    fixCell (i, Possible (x:xs)) = (i, Fixed x, Possible xs)
                                 = error "Impossible case"
    fixCell
    replace2D :: Int -> a -> [[a]] -> [[a]]
    replace2D i v =
      let (x, y) = (i `quot` 9, i `mod` 9) in replace x (replace y (const v))
    replace p f xs = [if i == p then f x else x | (x, i) \leftarrow zip xs [0..]]
```

We choose the non-fixed cell with least count of possibilities as the pivot. This strategy make sense intuitively, as with a cell with fewest possibilities, we have the most chance of being right when assuming one. Fixing a non-fixed cell leads to one of the two cases:

a. the cell has only two possible values, resulting in two fixed cells, or,b. the cell has more than two possible values, resulting in one fixed and one non-fixed cell.

Then all we are left with is replacing the non-fixed cell with its fixed and fixed/non-fixed choices, which we do with some math and some list traversal. A quick check on the *REPL*:

```
*Main> Just grid = readGrid
                                                                             *Main> *Main> putStr $
                                                                                     showGridWithPossibilities[ 3[1 3
"6.....1.4......2.......5.4.7..8...3...1.9....3...4..2...5.1.....8.6..."Just
                                                                                                             789]789]
                                                                             pruneGrid
                                                                                                            [ 33 5 7
                                                                                                             5 7 9] [
                                                                             grid
                                                                                                             9] [23 56
                                                                                                             23 59]
                                                                                                             7 9][123
                                                                                                             [ 68]
                                                                                                             234 [123
                                                                                                             8 ] 789]
                                                                                                             [ 56789
                                                                                                             2345[ 23
                                                                                                             789]56789
                                                                                                             [ [ 23
                                                                                                             5 56 89
                                                                                                             789]
                                                                                                              1
                                                                                                             2345
                                                                                                             89]
```

Solving the Puzzle

We have implemented parts of our algorithm till now. Now we'll put everything together to solve the puzzle. First, we need to know if we are done or have messed up:

```
isGridFilled :: Grid -> Bool
isGridFilled grid = null [ () | Possible _ <- concat grid ]</pre>
isGridInvalid :: Grid -> Bool
isGridInvalid grid =
  any isInvalidRow grid
  || any isInvalidRow (Data.List.transpose grid)
  || any isInvalidRow (subGridsToRows grid)
 where
    isInvalidRow row =
      let fixeds
                        = [x \mid Fixed x < - row]
          emptyPossibles = [x | Possible x <- row, null x]</pre>
      in hasDups fixeds || not (null emptyPossibles)
    hasDups l = hasDups' l []
    hasDups' [] _ = False
    hasDups' (y:ys) xs
      | y `elem` xs = True
      | otherwise = hasDups' ys (y:xs)
```

isGridFilled returns whether a grid is filled completely by checking it for any Possible cells. isGridInvalid checks if a grid is invalid because it either has duplicate fixed cells in any block or has any non-fixed cell with no possibilities.

Writing the solve function is almost trivial now:

We prune the grid as before and pipe it to the helper function solve'. solve' bails with a Nothing if the grid is invalid, or returns the solved grid if it is filled completely. Otherwise, it finds the next two grids in the search tree and solves them recursively with backtracking by calling the solve function. Backtracking here is implemented by the using the Alternative (<|>) implementation of the Maybe type². It takes the second branch in the computation if the first branch returns a Nothing.

Whew! That took us long. Let's put it to the final test now:

```
*Main> Just grid =
  readGrid
"6.....1.4.......2..........5.4.7..8...3....1.9....3..4..2...5.1........8.6..."
*Main> putStr $ showGrid grid
6 . . . . . 1 .
4 . . . . . . . . .
. 2 . . . . . .
. . . . 5 . 4 . 7
. . 8 . . . 3 . .
. . 1 . 9 . . . .
3 . . 4 . . 2 . .
. 5 . 1 . . . . .
. . . 8 . 6 . . .
*Main> Just grid' = solve grid
*Main> putStr $ showGrid grid'
6 9 3 7 8 4 5 1 2
4 8 7 5 1 2 9 3 6
1 2 5 9 6 3 8 7 4
9 3 2 6 5 1 4 8 7
5 6 8 2 4 7 3 9 1
7 4 1 3 9 8 6 2 5
3 1 9 4 7 5 2 6 8
8 5 6 1 2 9 7 4 3
2 7 4 8 3 6 1 5 9
```

It works! Let's put a quick main wrapper around solve to call it from the command line:

```
main :: IO ()
main = do
  inputs <- lines <$> getContents
  Control.Monad.forM_ inputs $ \input ->
    case readGrid input of
    Nothing -> putStrLn "Invalid input"
    Just grid -> case solve grid of
    Nothing -> putStrLn "No solution found"
    Just grid' -> putStrLn $ showGrid grid'
```

And now, we can invoke it from the command line:

And, we are done.

If you want to play with different puzzles, the file here lists some of the toughest ones. Let's run³ some of them through our program to see how fast it is:

It took about 117 seconds to solve a hundred puzzles, so, about 1.2 seconds per puzzle. This is pretty slow but we'll get around to making it faster in the subsequent posts.

Conclusion

In this rather verbose article, we learned how to write a simple Sudoku solver in Haskell step-by-step. In the later parts of this series, we'll delve into profiling the solution and figuring out better algorithms and data structures to solve Sudoku more efficiently. The code till now is available here. Discuss this post on r/haskell or leave a comment.

Footnotes

2. Alternative implementation of Maybe:

3. All the runs were done on my MacBook Pro from 2014 with 2.2 GHz Intel Core i7 CPU and 16 GB memory. $\!\mathbb{I}$

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