

## ASSIGNMENT-I

### Sub-CALCULUS B

**Choose the correct choice with proper Explanation**

**Q.1** The area of a triangle formed by the tips of vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  is

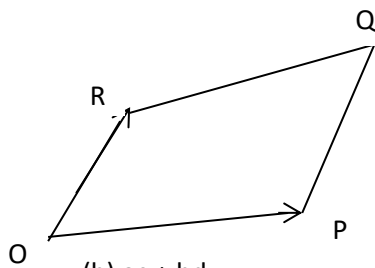
- (a)  $\frac{1}{2}(\vec{a}-\vec{b})\cdot(\vec{a}-\vec{c})$       (b)  $\frac{1}{2}|(\vec{a}-\vec{b}) \times (\vec{a}-\vec{c})|$   
 (c)  $\frac{1}{2}|\vec{a} \times \vec{b} \times \vec{c}|$       (d)  $\frac{1}{2}(\vec{a} \times \vec{b})\cdot \vec{c}$

**Q.2** If  $\vec{a}$  and  $\vec{b}$  are two arbitrary vectors with magnitudes  $a$  and  $b$ , respectively,  $|\vec{a} \times \vec{b}|^2$

Will be equal to

- (a)  $a^2b^2 - (\vec{a} \cdot \vec{b})^2$       (b)  $ab - \vec{a} \cdot \vec{b}$   
 (c)  $a^2b^2 + (\vec{a} \cdot \vec{b})^2$       (d)  $ab + \vec{a} \cdot \vec{b}$

**Q.3** For the parallelogram OPQR shown in the sketch,  $\vec{OP} = a\hat{i} + b\hat{j}$  and  $\vec{OR} = c\hat{i} + d\hat{j}$ . The area of the -----



- (a)  $ad - bc$       (b)  $ac + bd$   
 (c)  $ad + bc$       (d)  $ab - bd$

**Q.4** The area of a triangle formed by the tips of vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  is

- (a)  $\frac{1}{2}(\vec{a}-\vec{b})\cdot(\vec{a}-\vec{c})$       (b)  $\frac{1}{2}|(\vec{a}-\vec{b}) \times (\vec{a}-\vec{c})|$   
 (c)  $\frac{1}{2}|\vec{a} \times \vec{b} \times \vec{c}|$       (d)  $\frac{1}{2}(\vec{a} \times \vec{b})\cdot \vec{c}$

**Q.5** The angle (in degree) between two planes vectors

$$\vec{a} = \frac{\sqrt{3}}{2}\hat{i} + \frac{1}{2}\hat{j} \text{ and } \vec{b} = \frac{-\sqrt{3}}{2}\hat{i} + \frac{1}{2}\hat{j}$$

- (a) 30      (b) 60  
 (c) 90      (d) 120

**Q.6** The inner (dot) product of two nonzero vectors  $\vec{P}$  and  $\vec{Q}$  is zero. The angle (degrees) between The two vectors is

- (a) 0      (b) 30      (c) 90      (d) 120

**Q.7** Velocity vector of a flow field is given as  $\vec{V} = 2xy\hat{i} - x^2z\hat{j}$ . The velocity vector at (1, 1, 1) is

- (a)  $4\hat{i} - \hat{j}$       (b)  $4\hat{i} - \hat{k}$       (c)  $\hat{i} - 4\hat{j}$       (d)  $\hat{i} - 4\hat{k}$

**Q.8** If A (0, 4, 3), B (0,0,0) and C (3, 0, 4) are three points defined in x, y, z co-ordinate system, then

Which of the following vector is perpendicular to both vectors  $\vec{AB}$  and  $\vec{BC}$ .

- (a)  $16\hat{i} + 9\hat{j} - 12\hat{k}$       (b)  $16\hat{i} - 9\hat{j} + 12\hat{k}$       (c)  $16\hat{i} - 9\hat{j} - 12\hat{k}$       (d)  $16\hat{i} + 9\hat{j} + 12\hat{k}$

**Q.9** The vector that is NOT perpendicular to the vector  $(\mathbf{i} + \mathbf{j} + \mathbf{k})$  and  $(\mathbf{i} + 2\mathbf{j} + 3\mathbf{k})$  is \_\_\_\_\_.

- (a)  $(\mathbf{i} - 2\mathbf{j} + \mathbf{k})$       (b)  $(-\mathbf{i} + 2\mathbf{j} - \mathbf{k})$       (c)  $(\mathbf{0i} + \mathbf{0j} + \mathbf{0k})$       (d)  $(4\mathbf{i} + 3\mathbf{j} + 5\mathbf{k})$

**Q.10**  $\vec{a}, \vec{b}, \vec{c}$  are three orthogonal vectors, Given that  $\vec{a} = \hat{i} + 2\hat{j} + 5\hat{k}$  and  $\vec{b} = \hat{i} + 2\hat{j} - \hat{k}$ , the vector  $\vec{c}$  is parallel to

- (a)  $\hat{i} + 2\hat{j} + 3\hat{k}$       (b)  $2\hat{i} + \hat{j}$       (c)  $2\hat{i} - \hat{j}$       (d)  $4\hat{k}$

**Answer the following questions**

**Q.11** Determine whether the points A (1,3, 2), B (3, -1, 6), C (5, 2, 0) and D (3, 6, -4) lie in the same plane.

**Q.12** Find a vector equation and parametric equation for the line segment that joins P to Q.

$$P(0, -1, 1), \quad Q\left(\frac{1}{2}, \frac{1}{3}, \frac{1}{4}\right).$$

**Q.13.** Determine whether the lines  $L_1$  and  $L_2$  are parallel, skew, or intersecting. If they intersect, find the point of intersection.

$$L_1: x=3+2t, y=4-t, z=1+3t$$

$$L_2: x=1+4s, y=3-2s, z=4+5s$$

**Q.14** Find the velocity, acceleration, and speed of a particle with the given position function.

$$\mathbf{r}(t) = t^2\mathbf{i} + 2t\mathbf{j} + \ln t \mathbf{k}.$$

**Q.15** Find the position vector of the particle that has given acceleration and the specified initial velocity and position.  $\mathbf{a}(t) = t\mathbf{i} + e^t\mathbf{j} + e^{-t}\mathbf{k}$   $\mathbf{v}(0) = \mathbf{k}$ ,  $\mathbf{r}(0) = \mathbf{j} + \mathbf{k}$

**Q.16** Find the curvature of  $\mathbf{r}(t) = \langle t, t^2, t^3 \rangle$  at the point (1, 1, 1).

**Q.17** Find the length of the curve  $\mathbf{r}(t) = 12t\mathbf{i} + 8t^{3/2}\mathbf{j} + 3t^2\mathbf{k}$ ,  $0 \leq t \leq 1$

**Q.18** Find equations of the normal plane and osculating plane of the curve at the given point.

$$x = 2 \sin 3t, y = t, z = 2 \cos 3t; (0, \pi, -2).$$

**Q.19** A projectile is fired with an initial speed of 200 m/s and angle of elevation  $60^\circ$ . Find (a) the range of the projectile, (b) the maximum height reached, and (c) the speed at impact.

**Q.20** Find the tangential and normal components of the acceleration vector.

$$\mathbf{r}(t) = e^t\mathbf{i} + \sqrt{2}t\mathbf{j} + e^{-1}\mathbf{k}.$$

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