Answers to Exercises

CHAPTER 2

- 2.1. b. Pr $\{A \cup B\} = 0.7$ c. Pr $\{A \cap B^C\} = 0.1$ d. Pr $\{A^C \cap B^C\} = 0.3$ 2.2. b. Pr $\{A\} = 9/31$, Pr $\{B\} = 15/31$, Pr $\{A,B\} = 9/31$ c. Pr $\{A \mid B\} = 9/15$ d. No: Pr $\{A\} \neq Pr\{A \mid B\}$ 2.3. a. 18/22b. 22/312.4. b. Pr $\{E_1, E_2, E_3\} = .000125$ c. Pr $\{E_1^C, E_2^C, E_3^C\} = .857$ 2.5. a. 0.82
- b. Smaller: since $Pr\{B|A\}>Pr\{B\}$, $Pr\{A\cap B\}=Pr\{B|A\}Pr\{A\}>Pr\{B\}Pr\{A\}$ 2.6. 0.20

CHAPTER 3

- 3.1. Median = 2 mm, trimean = 2.75 mm, mean = 12.95 mm
- 3.2. MAD = 0.4 mb, IQR = 0.8 mb, s = 0.88 mb
- 3.4. $\gamma_{YK} = 0.158, \gamma = 0.877$
- 3.7. $\lambda = 0$
- 3.9. z = 1.36
- 3.10. $r_0 = 1.000, r_1 = 0.652, r_2 = 0.388, r_3 = 0.281$

3.12. Pearson:
$$\begin{bmatrix} 1.000 & 0.703 & -0.830 \\ 0.703 & 1.000 & -0.678 \\ -0.830 & -0.678 & 1.000 \end{bmatrix}, \text{ Spearman} : \begin{bmatrix} 1.000 & 0.606 & -0.688 \\ 0.606 & 1.000 & -0.632 \\ -0.688 & -0.632 & 1.000 \end{bmatrix}$$

- 4.1. 0.163
- 4.2. a. 0.0364
 - b. 0.344
- 4.3. a. $\mu_{\text{drought}} = 0.056$, $\mu_{\text{wet}} = 0.565$ b. 0.054
 - c. 0.432
- 4.4. \$280 million, \$2.825 billion

4.5.
$$Np(1-p) + (Np)^2$$

b. 0.00694

4.7. a.
$$\mu = 24.8^{\circ}\text{C}$$
, $\sigma = 0.98^{\circ}\text{C}$
b. $\mu = 76.6^{\circ}\text{F}$, $\sigma = 1.76^{\circ}\text{F}$

4.10. a.
$$\alpha = 3.785$$
, $\beta = 0.934''$

b.
$$\alpha = 3.785$$
, $\beta = 23.7$ mm

4.11. a.
$$q_{30} = 2.41'' = 61.2$$
 mm; $q_{70} = 4.22'' = 107.2$ mm b. $0.30''$, or 7.7 mm

$$c. \cong 0.05$$

4.12. a.
$$q_{30} = 2.30'' = 58.3$$
 mm; $q_{70} = 4.13'' = 104.9$ mm

$$c. \cong 0.07$$

4.14. a.
$$\beta = 35.1$$
 cm, $\zeta = 59.7$ cm

b.
$$x = \zeta - \beta \ln [-\ln(F)]$$
; $\Pr\{X \le 221 \text{ cm}\} = 0.99$

4.16. a.
$$\mu_{\rm max}=31.8^{\circ}{\rm F},\,\sigma_{\rm max}=7.86^{\circ}{\rm F},\,\mu_{\rm min}=20.2^{\circ}{\rm F},\,\sigma_{\rm min}=8.81^{\circ}{\rm F},\,\rho=0.810$$
 b. 0.728

4.18. a.
$$\beta = \sum x/n$$

b.
$$-I^{-1}(\hat{\beta}) = \hat{\beta}^2/n$$

4.20.
$$x(u) = \beta \left[-\ln(1-u) \right]^{1/\alpha}$$

5.1. a.
$$z = 4.88$$
, reject H₀
b. [1.10°C, 2.56°C]

5.3.
$$p = 0.40$$

5.4.
$$z = -4.00$$

$$p = 0.000063$$

$$p = 0.000032$$

5.5.
$$n \ge 86$$

5.7.
$$|r| \ge 0.377$$

5.8. a.
$$D_n = 0.152$$
 (reject at 10%, not at 5% level)

b. For classes: [
$$<2$$
, 2 -3 , 3 -4 , 4 -5 , ≥ 5], $\chi^2 = 0.33$ (do not reject)

$$r = 0.971$$
 (do not reject)

5.9.
$$\Lambda = 21.86$$
, reject $(p < .001)$

- 5.10. a. $U_1 = 1$, reject (p < .005)b. z = -3.18, reject (p = .0007)
- $5.11. \approx [1.02, 3.59]$
- 5.12. a. Observed $(s_{E-N}^2/s_{non-E-N}^2) = 329.5$; permutation distribution critical value (1%, 2-tailed) ≈ 141 , reject H_0 (p < 0.01)
 - b. 15/10000 members of bootstrap sampling distribution for $s_{\rm E-N}^2/s_{\rm non-E-N}^2 \le 1$; 2-tailed p = 0.003
- 5.13. a. Counting method, no (need \geq 3 locally significant); FDR, yes b. p=.007 and p=.009 significant according to FDR
- 5.14. a SS df MS F 43 6777.73 Total Treatment 3 2302.82 767.61 6.86 Error 40 4447.91 111.87 SS b. df MS F Total 43 6777.73 **Blocks** 10 3721.73 372.17 15.9 Treatment 3 2302.82 767.61 32.8 30 701.18 23.37 Error

CHAPTER 6

- 6.1. a. $\alpha = 14.8$, $\beta = 7.41$
 - b. Beta distribution, with $\alpha' = 29.8$, $\beta' = 17.4$
 - c. $Pr\{X^+ = 0\} = .0094$, $Pr\{X^+ = 1\} = .0656$, $Pr\{X^+ = 2\} = .1982$, $Pr\{X^+ = 3\} = .3248$, $Pr\{X^+ = 4\} = .2895$, $Pr\{X^+ = 5\} = .1125$
- 6.2. a. $\beta = 190.8$, $\zeta = 162.3$
 - b. $\beta = 155.9$, $\zeta = 180.0$
 - c. 1040.0, 897.2
- 6.3. a. $\alpha = 1.5$, $\beta = 0.1$ b. .157
- 6.4. a. $\mu'_h = 455.6$, $\sigma'_h = 33.3$
- b. $\mu_+ = 455.6$, $\sigma_+ = 60.1$ 6.5. a. $\mu'_h = 427.4$, $\sigma'_h = 28.6$
 - b. $\mu_{\rm h} = 427.4$, $\sigma_{\rm h} = 28.6$ b. $\mu_{\rm h} = 427.4$, $\sigma_{\rm h} = 57.6$
- 6.6. a. 462.3
 - b. 400
 - c. 450

- 7.1. a. a = 959.8°C, b = -0.925°C/mb
 - c. z = -6.33
 - d. 0.690
 - e. 0.876
 - f. 0.925

7.2. a. Total

26

318.2874

```
Regression
                        1
                             316.6065
                                         316.6065
         Residual
                       25
                                1.6809
                                            0.06724
      b. 1
      c. 12.73
      d. 0.9947
      e. 0.56
      f. t = 68.6
 7.3. \ln \left[ \overline{y} / (1 - \overline{y}) \right]
 7.4. a. 1.74 mm
      b. [0 mm, 13.1 mm]
 7.5. MSE = 0.369
      slopes: -.926,-.926,-.928,-.924,-.940,-.921,-.909,-.928,-.917,-.897,-.928,-.919,-.921,
      -.921,-.854,-1.095,-.927,-.952,.850,-.922
 7.6. a. -59 n.m.
      b. -66 n.m.
 7.7. a. 65.8°F
      b. 52.5°F
      c. 21.7°F
      d. 44.5°F
 7.8. a. 0.65
      b. 0.49
      c. 0.72
      d. 0.56
 7.9. f_{MOS} = 30.8^{\circ}F + (0) (Th)
7.10. 0.20
7.11. a. 12 mm
      b. [5 mm, 32 mm], [1 mm, 55 mm]
      c. 0.625
CHAPTER 8
8.1. a. [4.9°C, 8.8°C]
     b. [5.1°C, 8.5°C]
8.2. 0.873
8.3. a. 0.059
     b. 0.345
     c. 0.143
8.4. (25.5°C, 1.3 m/s), (27.5°C, 1.8 m/s), (27.0°C, 3.1 m/s), (26.4°C, 0.7 m/s),
     (28.4°C, 2.4 m/s)
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CHAPTER 9

9.1. a. .0025 .0013 .0108 .0148 .0171 .0138 .0155 .0161 .0177 .0176 .0159 .0189 .4087 .0658 .1725 .0838 .0445 .0228 .0148 .0114 .0068 .0044 .0011 .0014 b. 0.162

b. 0.224

```
9.2. 1644 1330
       364 9064
 9.3. a. 0.863
      b. 0.493
      c. 0.578
      d. 0.691
      e. 0.407
 9.4. a. 0.074
      b. 0.097
      c. 0.761
      d. 0.406
 9.5. a. .9597
                 .0127
                         .0021
                                 .0007
         .0075
                 .0043
                         .0014
                                 .0005
         .0013
                 .0013
                         .0009
                                 .0003
         .0007
                 .0006
                         .0049
                                 .0009
      b. 0.966
      c. 0.371
      d. 0.336
 9.6. a. 5.37°F
      b. 7.54°F
      c. -0.03°F
      d. 1.95%
 9.7. a. -118%
      b. 60.0%
 9.8. a. 0.1215
      b. 0.1699
      c. 28.5%
      e. 0.392
 9.9. a. .0415
                                  .1428
                                                  .0829
                                                                                   .0553
                  .0968
                          .1567
                                          .1152
                                                          .1060
                                                                  .0829
                                                                          .0783
                                                                                           .0415
          .3627
                  .2759
                         .1635 .0856 .0498
                                                 .0230
                                                          .0204 .0102
                                                                          .0051
                                                                                   .0026
                                                                                          .0013
      c. H = .958, .862, .705, .562, .447, .364, .258, .175, .097, .042
          F = .637, .361, .198, .112, .062, .039, .019, .009, .004, .001
      d. A = 0.831, z = -14.9
9.10. 0.16
9.11. a. 0.298
      b. 16.4%
      c. 0.755
9.12. a. \pi_{MRH}(y_0)=3, \pi_{MRH}(y_1)=1, \pi_{MRH}(y_2)=2, \pi_{MRH}(y_3)2, \pi_{MRH}(y_4)=5, \pi_{MRH}(y_5)=1
      b. b = 5
9.13. a. 22
      b. 0.0192
9.14. a. 5 rank 1, 2 rank 2, 3 rank 3, 2 rank 4, 2 rank 5, 6 rank 6
      b. underdispersed
9.15. a. 0.140
```

CHAPTER 10

10.1. a.
$$p_{01} = 0.45$$
, $p_{11} = 0.79$
b. $\chi^2 = 3.51$, $p \approx 0.064$

c.
$$\pi_1 = 0.682$$
, $n_{\bullet 1}/n = 0.667$

d.
$$r_0 = 1.00$$
, $r_1 = 0.34$, $r_2 = 0.12$, $r_3 = 0.04$

10.2. a.
$$r_0 = 1.00$$
, $r_1 = 0.40$, $r_2 = 0.16$, $r_3 = 0.06$, $r_4 = 0.03$, $r_5 = 0.01$

a.
$$r_0 = 1.00$$
, $r_1 = 0.41$, $r_2 = -0.41$, $r_3 = -0.58$, $r_4 = -0.12$, $r_5 = 0.32$

10.3. a. AR(1):
$$\phi = 0.80$$
; $s_{\varepsilon}^2 = 36.0$

AR(2):
$$\phi_1 = 0.89$$
, $\phi_2 = -0.11$; $s_{\varepsilon}^2 = 35.5$

AR(3):
$$\phi_1 = 0.91$$
, $\phi_2 = -0.25$, $\phi_3 = 0.16$; $s_{\varepsilon}^2 = 34.7$

b.
$$AR(1)$$
: BIC = 369.6

c.
$$AR(1)$$
: $AIC = 364.4$

10.4.
$$x_1 = 71.5, x_2 = 66.3, x_3 = 62.1$$

10.7. a.
$$C_1 = 16.92$$
°F, $\phi_1 = 199$ °; $C_2 = 4.16$ °F, $\phi_2 = 256$ °

c.
$$C_1^2$$
, $p = .00593$

d.
$$C_1^2$$
, $p = .00593 < 0.05/6$

e.
$$C_1^2$$

10.11. a. e.g.,
$$f_A = 1 - .0508 \text{ mo}^{-1} = .9492 \text{ mo}^{-1}$$

b.
$$\approx$$
 twice monthly

11.1.
$$\begin{bmatrix} 216.0 & -4.32 \\ 135.1 & 7.04 \end{bmatrix}$$

11.2.
$$([X]^T y)^T = [627, 11475], [X^T X]^{-1} = \begin{bmatrix} .06263 & -.002336 \\ -.00236 & .0001797 \end{bmatrix}, \quad \boldsymbol{b}^T = [12.46, 0.60]$$
11.3. 90°

11.6.
$$\frac{1}{n}(\overline{x} - \mu)^T [S]^{-1}(\overline{x} - \mu)$$

11.7. [E]**u**

11.8. a.
$$\begin{bmatrix} 59.5 & 58.1 \\ 58.1 & 61.8 \end{bmatrix}$$

b.
$$\begin{bmatrix} .205 & -.193 \\ -.193 & .197 \end{bmatrix}$$

c.
$$\begin{bmatrix} .205 & -.193 \\ -.193 & .197 \end{bmatrix}$$

d.
$$\begin{bmatrix} 6.16 & 4.64 \\ 4.64 & 6.35 \end{bmatrix}$$

11.9. a.
$$\begin{bmatrix} 59.52 & 75.43 & 58.07 & 51.70 \\ 75.43 & 185.47 & 81.63 & 110.80 \\ 58.07 & 81.63 & 61.85 & 56.12 \\ 51.70 & 110.80 & 56.12 & 77.58 \end{bmatrix}$$

b.
$$\boldsymbol{\mu}_{y}^{T} = [21.4, 26.0]$$

$$[S_{y}] = \begin{bmatrix} 98.96 & 75.77 \\ 75.55 & 62.92 \end{bmatrix}$$

CHAPTER 12

12.2. a.
$$\boldsymbol{\mu} = [29.87, 13.00]^{\mathrm{T}}, \quad [S] = \begin{bmatrix} 4.96 & 0.15 \\ 0.15 & 27.12 \end{bmatrix}$$

b.
$$N_2(\boldsymbol{\mu} [\Sigma]); \boldsymbol{\mu} = [-1.90, 5.33]^T \quad [\Sigma] = \begin{bmatrix} 5.23 & 7.01 \\ 7.01 & 50.24 \end{bmatrix}$$

12.4. a. $N_1(31.4, 21.4)$

b. 0.306

12.5.
$$r = 0.974 > r_{\text{crit}} (10\%) = 0.970$$
; do not reject 12.6. a. $T^2 = 68.5 >> 18.421 = \chi_2^2 (.9999)$; reject b. $\boldsymbol{a} \propto [-.6217, .1929]^{\text{T}}$

12.7. a.
$$T^2 = 7.80$$
, reject @ 5%
b. $\boldsymbol{a} \propto [-.0120, .0429]^T$

CHAPTER 13

- 13.1. a. 3.78, 4.51
 - b. 118.8
 - c. 0.979
- 13.2. a. 0.430, -0.738

- 13.3. a. Correlation matrix: $\Sigma \lambda_k = 3$
 - b. 1, 1, 1
 - c. 2.3 mm
- 13.4. a. [1.51, 6.80], [0.22, 0.98], [0.10, 0.46]
 - b. λ_2 and λ_3 may be entangled

13.5. a.
$$\begin{bmatrix} .593 & .332 & .734 \\ .552 & -.831 & -.069 \\ -.587 & -.446 & .676 \end{bmatrix}$$

b.
$$\begin{bmatrix} .377 & .556 & 1.785 \\ .351 & -1.39 & -.168 \\ -.373 & -.747 & 1.644 \end{bmatrix}$$

- 13.6. 9.18, 14.34, 10.67
- 13.7. 37.5 + .838 IPpt + 1.831 IMax + 5.017 IMin + .341 CPpt + 2.42 CMax + 4.876 CMin

CHAPTER 14

- 14.1. 6 Jan: $v_1 = .038$, $w_1 = .433$; 7 Jan: $v_1 = .868$, $w_1 = 1.35$
- 14.2. 39.0°F, 23.6°F

$$14.3. \ \ a. \ \ \begin{bmatrix} 1.883 & 0 & 1.838 & -.212 \\ 0 & .927 & .197 & .791 \\ 1.838 & .197 & 1.904 & 0 \\ -.212 & .791 & 0 & .925 \end{bmatrix}$$

b.
$$\boldsymbol{a}_1 = [.728, .032]^{\mathrm{T}}, \boldsymbol{b}_1 = [.718, -.142]^{\mathrm{T}}, r_{\mathrm{C}_1} = 0.984$$

 $\boldsymbol{a}_2 = [-.023, 1.038]^{\mathrm{T}}, \boldsymbol{b}_2 = [.099, 1.030]^{\mathrm{T}}, r_{\mathrm{C}_2} = 0.867$

CHAPTER 15

15.1. b.
$$R_1$$
: $-1 \le x \le 0.25$
 R_2 : $0.25 < x \le 1.5$

$$R_2$$
: 0.23 $< x \le 1.3$
c. R_1 : $-1 \le x \le -0.33$

$$R_2$$
: $-0.33 < x \le 1.5$

15.2. a.
$$\boldsymbol{a}_{1}^{T} = [0.83, -0.56]$$

- b. 1953
- c. 1953
- 15.3. a. [.734 .367]^T

b.
$$w = 0.66 > 0 =$$
 "yes" group

c. 0.66

15.4. a.
$$\delta_1 = 38.65$$
, $\delta_2 = -14.99$; Group 3 b. 5.2 x 10^{-12} , 2.8 x 10^{-9} , 0.99999997

15.5. a. 0.006 b. 0.059 c. 0.934

16.1.
$$\begin{bmatrix} 0 \\ 3.59 & 0 \\ 2.29 & 1.59 & 0 \\ 3.12 & 0.82 & 0.89 & 0 \\ 0.71 & 4.27 & 2.89 & 3.75 & 0 \\ 1.64 & 2.24 & 0.71 & 1.59 & 2.20 & 0 \end{bmatrix}$$

- 16.2. a. 1967+1970, d = 0.71; 1965+1969, d = 0.71; 1966+1968, d = 0.82; (1967+1970) + (1966+1968), d = 1.59; all, d = 1.64.
 - b. 1967+1970, d=0.71; 1965+1969, d=0.71; 1966+1968, d=0.82; (1967+1970)+(1966+1968), d=2.24; all, d=4.27.
 - c. 1967+1970, d=0.71; 1965+1969, d=0.71; 1966+1968, d=0.82; (1967+1970)+(1966+1968), d=1.58; all, d=2.97.
- 16.3. a. 1967 + 1970, d = 0.50; 1965 + 1969, d = 0.60; 1966 + 1968, d = 0.70; (1967 + 1970) + (1965 + 1969), d = 1.25; all, d = 1.925.
 - b. 1967+1970, d=0.125; 1965+1969, d=0.180; 1966+1968, d=.245; (1967+1970)+(1965+1969), d=1.868; all, d=7.053.
- 16.4. {1966, 1967}, {1965, 1968, 1969, 1970}; {1966, 1967, 1968}, {1965, 1969, 1970}; {1966, 1967, 1968, 1970}, {1965, 1969}.
- 16.5. a. f_1 b. $Pr\{f_1\}=0.71$, $Pr\{f_2\}=0.29$