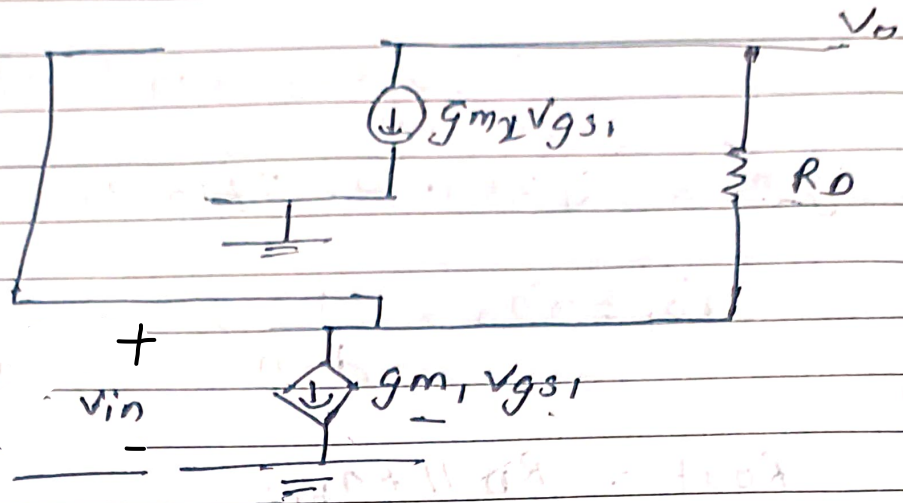
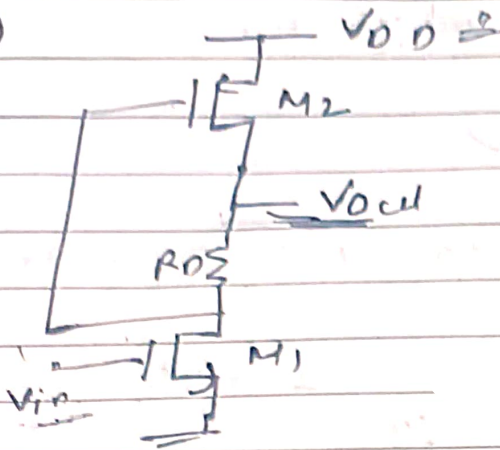


Q1)



$$V_{gs1} = V_{in}$$

$$g_{m2} V_{gs2} = -g_{m1} V_{gs1}$$

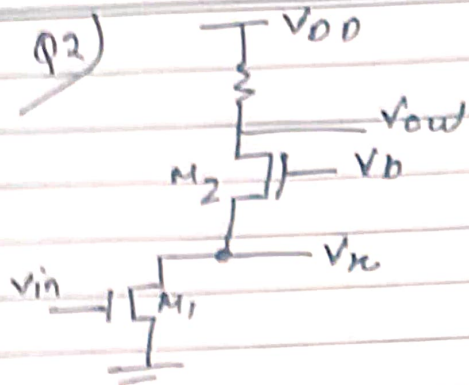
$$g_{m2} V_{gs2} = -g_{m1} V_{in}$$

$$V_{gs2} = -\frac{g_{m1}}{g_{m2}} V_{in}$$

$$V_o = (g_{m1} V_{gs1}) R_D + V_{D1}$$

$$V_o = g_{m1} V_{in} R_D + \left(-\frac{g_{m1}}{g_{m2}} \right) V_{in}$$

$$\boxed{\frac{V_o}{V_{in}} = \left(g_{m1} R_D - \frac{g_{m1}}{g_{m2}} \right)}$$



$$\left(\frac{W}{L}\right)_1 = \frac{50}{0.5}$$

$$\left(\frac{W}{L}\right)_2 = \frac{10}{0.5}$$

$$I_{D1} = I_{D2} = 0.5 \text{ mA}$$

$$R_D = 1 \text{ k}\Omega$$

$$V_{th} = 0.77 \text{ V}$$

$$V_{DSat1} = V_{GS1} - V_{th1} = \left(\frac{2I_{D1}}{\mu_n C_{ox} \left(\frac{W}{L}\right)_1} \right)^{1/2} = \left(\frac{2 \times 0.5 \times 10^{-3}}{1.34225 \times 10^{-4} \times 1000} \right)^{1/2}$$

$$V_{DSat1} = 0.2729 \text{ V}$$

$$V_{n \text{ Bias}} = 0.2729 + 50 \times 10^{-3} = 0.3229 \text{ V}$$

$$V_{th2} = 0.77 \text{ V}$$

$$V_{GS2} - V_{th2} = \left(\frac{2I_{D2}}{\mu_n C_{ox} \left(\frac{W}{L}\right)_2} \right)^{1/2}$$

$$V_{GS2} = 0.77 + \left(\frac{2 \times 0.5 \times 10^{-3}}{1.34225 \times 10^{-4} \times 20} \right)^{1/2}$$

$$V_{GS2} = 1.3803 \text{ V}$$

$$V_{GS2} = V_b - V_{n}$$

$$V_b = V_{GS2} + V_n$$

$$V_b = 1.3803 + 0.2729 = 1.6532 \text{ V}$$

$$b) \quad g_{m1} = \sqrt{2 \times 1.34225 \times 10^{-4} \times 100 \times 0.5 \times 10^{-3}}$$

$$\Rightarrow 3.6636 \times 10^{-3} \text{ A/V}$$

$$g_{m2} = \sqrt{2 \times 1.34225 \times 10^{-4} \times 20 \times 0.5 \times 10^{-3}} = 1.6384 \times 10^{-3} \text{ A/V}$$

$$r_{o1} = r_{o2} = \frac{1}{\lambda I_D} = \frac{1}{0.1 \times 0.5 \times 10^{-3}} = 20 \text{ K}$$

$$R_{out} = R_D \parallel R_{out1}$$

$$R_{out1} = \left[(1 + g_{m1} r_{o2}) r_{o1} + r_{o2} \right]$$

$$R_{out} = R_D \parallel \left[(1 + g_{m1} r_{o2}) r_{o1} + r_{o2} \right]$$

$$R_{out} = 10^3 \parallel \left[(1 + 1.6384 \times 10^{-3} \times 20 \times 10^3) 20 \times 10^3 + 20 \times 10^3 \right]$$

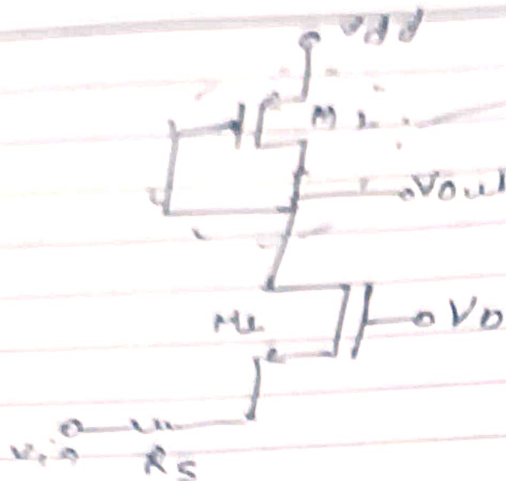
$$R_{out} = 998.564 \, \Omega$$

$$A_v = -g_{m1} R_{out}$$

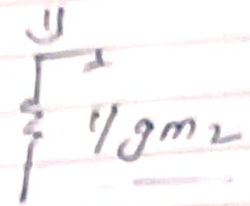
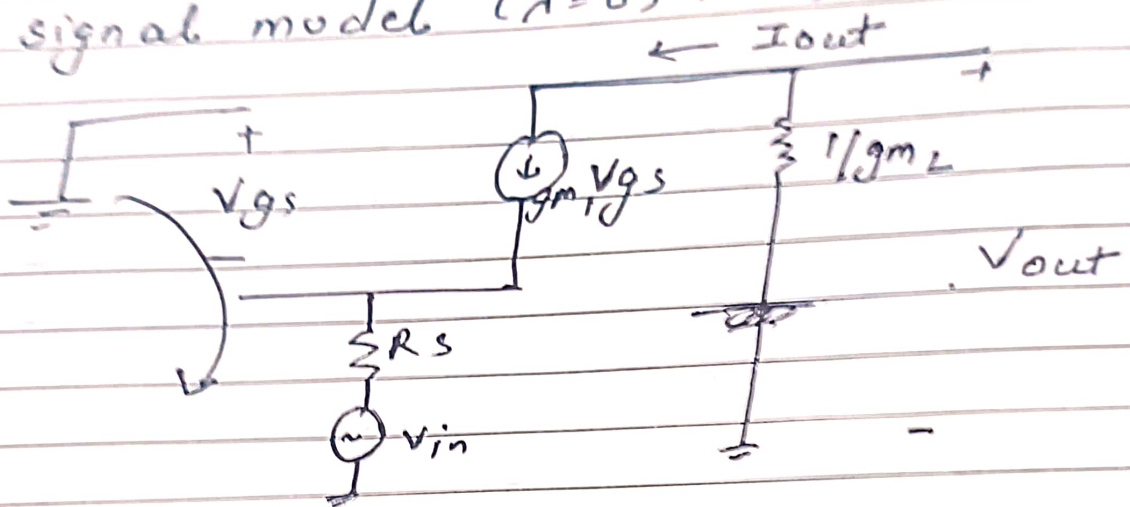
$$A_v = - (3.6636 \times 10^{-3}) \times (998.564)$$

$$\boxed{A_v \approx -3.658}$$

Q3)



diode connected

Small signal model ($\lambda=0, r=0$)

Using KVL in the g/p loop :-

$$-V_{gs} - R_S g_{m1} V_{gs1} - V_{in} = 0$$

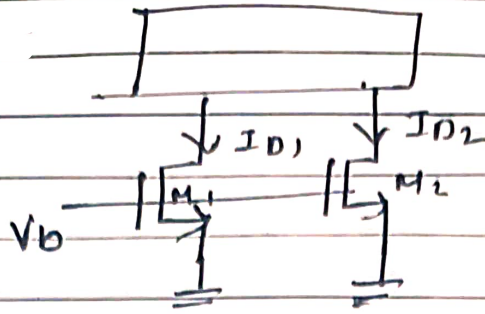
or

$$V_{in} = -V_{gs1} (R_S g_{m1} + 1)$$

$$V_{out} = -g_{m1} V_{gs1} \times \left(\frac{1}{g_{m2}} \right)$$

$$A_v = \frac{V_{out}}{V_{in}} = \frac{(g_{m1} / g_{m2})}{(1 + g_{m1} R_S)}$$

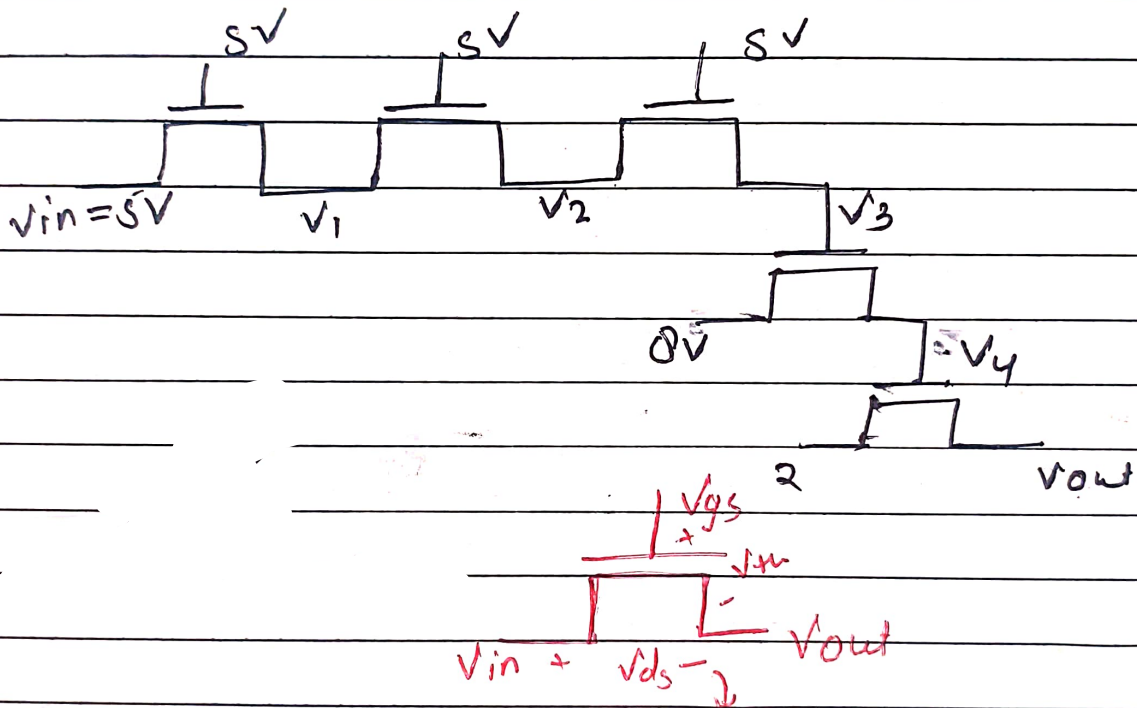
Q4)



$$I_{D1} - I_{D2} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_b - V_{th})^2 (\lambda V_{DS1} - \lambda V_{DS2})$$

$$= \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_b - V_{th})^2 (\lambda \Delta V)$$

Q5)



$$V_{out} = \min(V_{gs} - V_{th}, V_{ds})$$

$$V_1 = 4V$$

$$V_2 = 4V$$

$$V_3 = 4V$$

$$V_4 = 3V$$

$$V_{out} = 2V$$