

```
In [1]: # Importing essential libraries
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
%matplotlib inline
import seaborn as sns
from sklearn.linear_model import LinearRegression
import warnings
warnings.filterwarnings ("ignore")
```

```
In [2]: #importing dataset using pandas

concrete_df = pd.read_csv("Concrete Compressive Strength.csv")
```

```
In [3]: concrete_df
```

Out[3]:

	Cement	Blast Furnace Slag	Fly Ash	Water	Superplasticizer	Coarse Aggregate	Fine Aggregate	Age (day)	streng
0	540.0	0.0	0.0	162.0	2.5	1040.0	676.0	28	79.9861
1	540.0	0.0	0.0	162.0	2.5	1055.0	676.0	28	61.8873
2	332.5	142.5	0.0	228.0	0.0	932.0	594.0	270	40.2695
3	332.5	142.5	0.0	228.0	0.0	932.0	594.0	365	41.0527
4	198.6	132.4	0.0	192.0	0.0	978.4	825.5	360	44.2960
...
1025	276.4	116.0	90.3	179.6	8.9	870.1	768.3	28	44.2843
1026	322.2	0.0	115.6	196.0	10.4	817.9	813.4	28	31.1787
1027	148.5	139.4	108.6	192.7	6.1	892.4	780.0	28	23.6966
1028	159.1	186.7	0.0	175.6	11.3	989.6	788.9	28	32.7680
1029	260.9	100.5	78.3	200.6	8.6	864.5	761.5	28	32.4012

1030 rows × 9 columns



```
In [4]: # Separating dependent and independent variable.
X_raw = concrete_df.drop(columns=['strength'], axis=1)
Y = concrete_df['strength']
```

```
In [5]: # Preparing the data to fit Linear regression
def Prepare_data(X):
    X.columns = ['X_1', 'X_2', 'X_3', 'X_4', 'X_5', 'X_6', 'X_7', 'X_8']
    X_0 = pd.DataFrame({'X_0' : [1]*1030})
    df = pd.concat([X_0,X],axis = 1, join = 'inner')
    arr=np.array(df)
    return df,arr
```

```
In [6]: df, X = Prepare_data(X_raw)
print("_____The prepared data is_____")
df
```

_____The prepared data is_____

Out[6]:

	X_0	X_1	X_2	X_3	X_4	X_5	X_6	X_7	X_8
0	1	540.0	0.0	0.0	162.0	2.5	1040.0	676.0	28
1	1	540.0	0.0	0.0	162.0	2.5	1055.0	676.0	28
2	1	332.5	142.5	0.0	228.0	0.0	932.0	594.0	270
3	1	332.5	142.5	0.0	228.0	0.0	932.0	594.0	365
4	1	198.6	132.4	0.0	192.0	0.0	978.4	825.5	360
...
1025	1	276.4	116.0	90.3	179.6	8.9	870.1	768.3	28
1026	1	322.2	0.0	115.6	196.0	10.4	817.9	813.4	28
1027	1	148.5	139.4	108.6	192.7	6.1	892.4	780.0	28
1028	1	159.1	186.7	0.0	175.6	11.3	989.6	788.9	28
1029	1	260.9	100.5	78.3	200.6	8.6	864.5	761.5	28

1030 rows × 9 columns

```
In [7]: # function to estimate parameters
def Parameter_est( X ,y):
    Transpose = X.T
    mal = np.matmul(X.T,X)
    inv = np.linalg.inv(mal)
    b_hat = np.matmul(np.matmul(inv,X.T),y)
    return b_hat

# Assign the estimated parameters to b_hat
b_hat = Parameter_est( X ,Y)
print("_____The weight parameters are_____")
b_hat
```

_____The weight parameters are_____

Out[7]: array([-2.31637558e+01, 1.19785255e-01, 1.03847249e-01, 8.79430817e-02,
-1.50297904e-01, 2.90686943e-01, 1.80301836e-02, 2.01544557e-02,
1.14225620e-01])

```

In [8]: # Function the Linear Regression
def linearRegression(beta):
    print ( "_____The fitted equation is_____")
    print (f"y_hat={b_hat[0]:.3f}X_0+{b_hat[1]:.3f}X_1+{b_hat[2]:.3f}X_2+{b_hat[3]:.3f}X_3+{b_hat[4]:.3f}X_4+{b_hat[5]:.3f}X_5+{b_hat[6]:.3f}X_6+{b_hat[7]:.3f}X_7+{b_hat[8]:.3f}X_8")
    print ( "_____")

# Fitting the equation:
linearRegression(b_hat)

# predicting the dependent variable using the fitted equation
y_hat = X@b_hat
print("_____The Predicted Values are_____")
print(y_hat)

```

```

_____The fitted equation is_____
y_hat=-23.164X_0+0.120X_1+0.104X_2+0.088X_3+-0.150X_4+0.291X_5+0.018X_6+0.020X_7+0.114X_8}
_____
_____The Predicted Values are_____
[53.4728591  53.74331185  56.81194746 ... 26.47099254  29.11564722
 31.89398622]

```

```

In [9]: #Error calculation:
def Errors(y_true, y_pred):
    e = y_true - y_pred
    mse = ((e**2).sum())/X.shape[0]
    return mse
mse = Errors(Y,y_hat)

print("Mean squared error is: ", mse)
rmse = np.sqrt(mse)
print("Root mean squared error is: {}".format(rmse))

```

```

Mean squared error is:  107.21180273479736
Root mean squared error is:  10.354313243030527

```

```
In [10]: # Function to create ANOVA Table
def Anova(y_true,y_pred):
    # Total variation
    SSt = ((y_true-y_true.mean())**2).sum()
    degree_t = X.shape[0] - 1
    # Residual variation
    SSres= ((y_true - y_pred)**2).sum()
    degree_res = X.shape[0] - X.shape[1]
    MSres = SSres/degree_res
    # variation due to regression
    SSreg = SSt-SSres
    degree_reg = X.shape[1]-1
    MSreg= SSreg/degree_reg
    F = MSreg/MSres
    return degree_res,degree_reg, SSres,SSreg,MSres,MSreg, F

degree_res, degree_reg, SSres,SSreg,MSres,MSreg, F = Anova(Y,y_hat)
```

```
In [11]: A Table
DF':[degree_reg, degree_res, degree_reg+degree_res], 'SS':[SSreg, SSres, SSr
DataFrame(anova_dict,index=["Regression","Residual","Total"])
ANOVA Table
```



ANOVA Table

Out[11]:

	DF	SS	MS	F
Regression	8	176744.871659	22093.108957	204.269137
Residual	1021	110428.156817	108.156863	204.269137
Total	1029	287173.028476	22201.265820	204.269137

```
In [12]: # Testing Null hypothesis
print("_____")
print(f"H0: b0=b1=.....bk-1=0 against \nH1: bi!=0 for i=0 to k-1")
print("If F>F{alpha, k-1, n-k}, The H0 is rejected")
print("_____")
import scipy.stats
from scipy.stats import f
alpha = 0.05
q = 1 - alpha
f = f.ppf(q, degree_reg, degree_res)
print(f"The calcyated f value is: {f}" )
print(f"The observed f value is {F}")
if(abs(F)>f):
    print("The null hypothesis H0 is rejected")
else:
    print("The null hypothesis H0 is accepted")
```

H0: b0=b1=.....bk-1=0 against
H1: bi!=0 for i=0 to k-1
If F>F{alpha, k-1, n-k}, The H0 is rejected

The calcyated f value is: 1.9474558084667661
The observed f value is 204.2691365659187
The null hypothesis H0 is rejected

```
In [13]: # Predict R^2 value and adjusted R^2 value:
R_sq = (SSreg/ (SSres+SSreg) ) * 100
AdjR_sq = (1- MSres/(MSres+MSreg)) * 100
print(f"The R square value is:{R_sq}")
print(f"Adjusted R square value is: {AdjR_sq}")
```

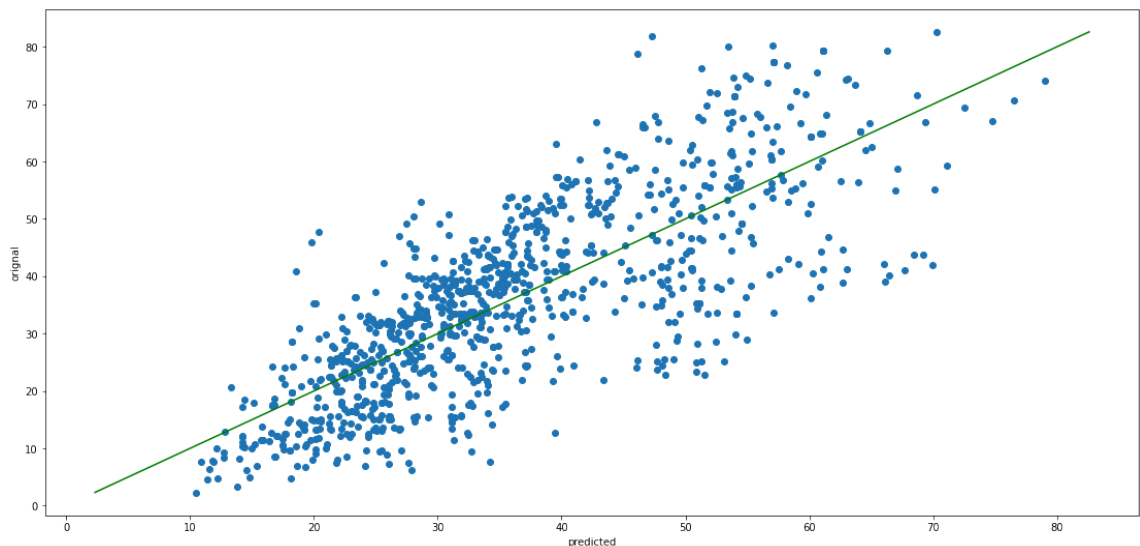
The R square value is:61.54647342657952
Adjusted R square value is: 99.51283470241574

```
In [14]: # Test on individual regression coefficient (Partial test or Marginat Test)
Corr = np.linalg.inv(X.T@X)
from scipy.stats import t
def Marginal_test(beta, C, MSres,X):
    n = X.shape[1]
    for i in range(n):
        T = beta[i]/np.sqrt(MSres*C[i][i])
        if(abs(T)>t.ppf(1-0.05, degree_res)):
            print(f"H0:b{i}=0 is rejected")
        else:
            print(f"H0:b{i}=0 is accepted")

Marginal_test(b_hat,Corr,MSres,X)
```

```
H0:b0=0 is accepted
H0:b1=0 is rejected
H0:b2=0 is rejected
H0:b3=0 is rejected
H0:b4=0 is rejected
H0:b5=0 is rejected
H0:b6=0 is rejected
H0:b7=0 is rejected
H0:b8=0 is rejected
```

```
In [15]: # Plot the regression Line fitted by the function made
plt.figure(figsize=[19 , 9])
plt.scatter( y_hat, Y)
plt.plot([Y.min(), Y.max()], [Y.min(), Y.max()], color = 'green')
plt.xlabel('predicted')
plt.ylabel('original')
plt.show()
```

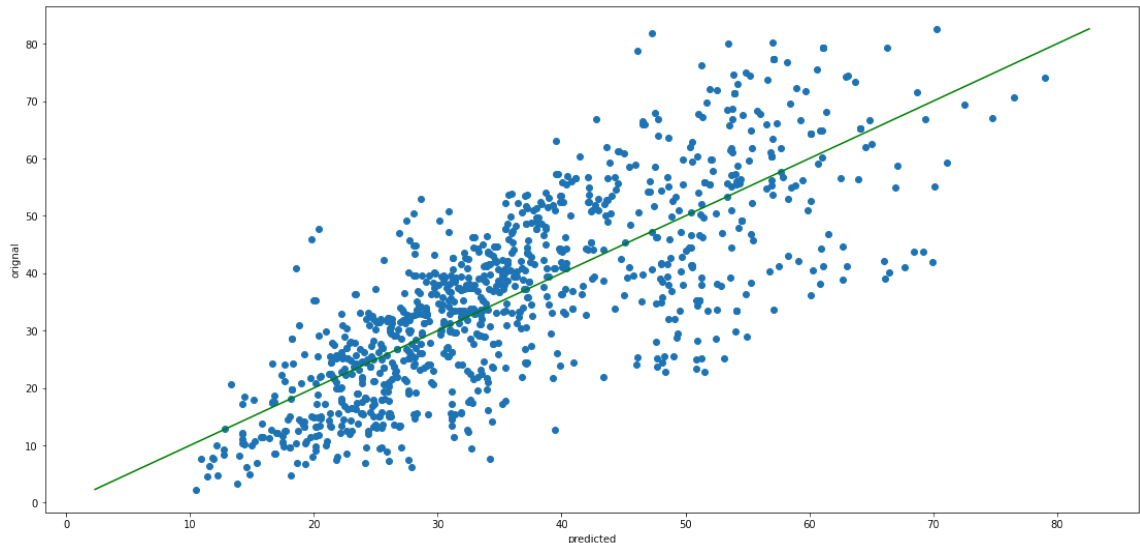


```
In [16]: # trying the inbuilt regression functionn
from sklearn.linear_model import LinearRegression
from sklearn.metrics import mean_squared_error
lr = LinearRegression()
fit = lr.fit(X,Y)
print( '.....')
y_predict = lr.predict(X)
print( 'mean_ squired_error is ==',mean_squared_error(Y, y_predict))
rms = np.sqrt(mean_squared_error(Y,y_predict))
print( 'root mean squared error is == {}'.format(rms))
print("_____The predicted values
y_predict
```

```
.....
mean_ squired_error is == 107.21180273479737
root mean squared error is == 10.354313243030528
_____The predicted values are__
_____
```

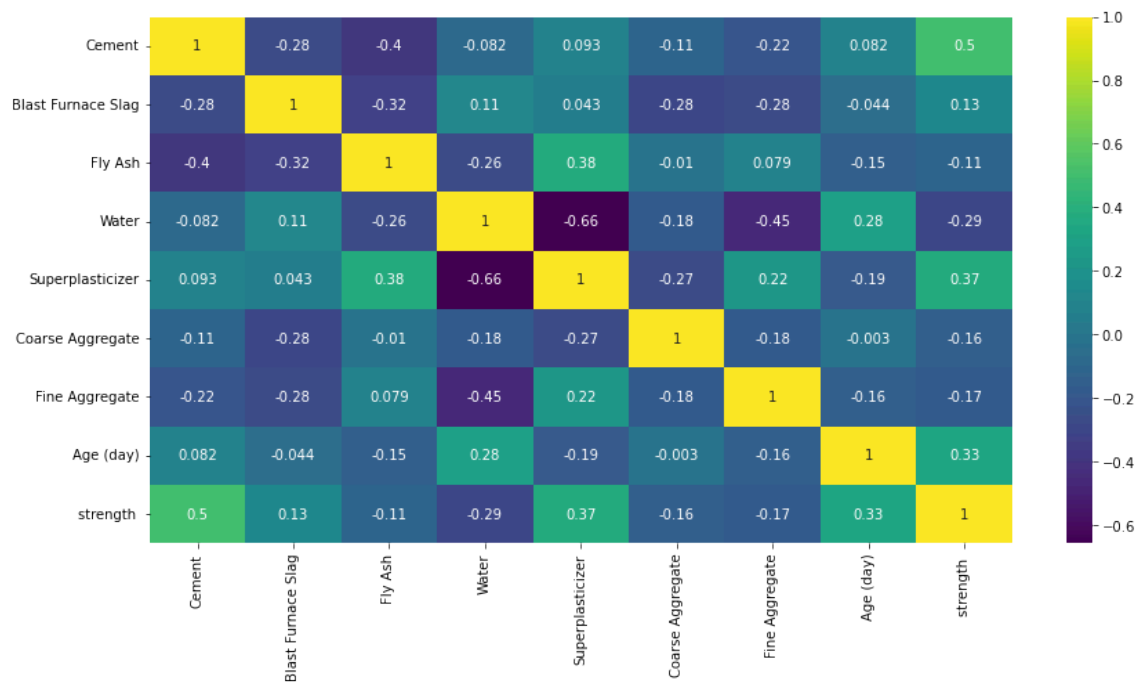
```
Out[16]: array([53.4728591 , 53.74331185, 56.81194746, ..., 26.47099254,
                29.11564722, 31.89398622])
```

```
In [17]: # Plot the regression Line fitted by the inbuilt libraries in python
plt.figure(figsize=[19 , 9])
plt.scatter( y_predict, Y)
plt.plot([Y.min(), Y.max()], [Y.min(), Y.max()], color = 'green')
plt.xlabel('predicted')
plt.ylabel('original')
plt.show()
```



```
In [18]: # Plot heatmap to check multicollinearity
plt.figure(figsize = (14,7))
sns.heatmap(concrete_df.corr( ), annot=True, cmap='viridis')
```

Out[18]: <AxesSubplot:>



```
In [19]: # check for any duplicate values in the data
duplicates = concrete_df.duplicated()
concrete_df[duplicates]
duplicates.value_counts( )
```

Out[19]: False 1005
True 25
dtype: int64


```
In [20]: # Dropping duplicate values.
concrete_df=concrete_df.drop_duplicates()
concrete_df
```

Out[20]:

	Cement	Blast Furnace Slag	Fly Ash	Water	Superplasticizer	Coarse Aggregate	Fine Aggregate	Age (day)	streng
0	540.0	0.0	0.0	162.0	2.5	1040.0	676.0	28	79.9861
1	540.0	0.0	0.0	162.0	2.5	1055.0	676.0	28	61.8873
2	332.5	142.5	0.0	228.0	0.0	932.0	594.0	270	40.2695
3	332.5	142.5	0.0	228.0	0.0	932.0	594.0	365	41.0527
4	198.6	132.4	0.0	192.0	0.0	978.4	825.5	360	44.2960
...	
1025	276.4	116.0	90.3	179.6	8.9	870.1	768.3	28	44.2843
1026	322.2	0.0	115.6	196.0	10.4	817.9	813.4	28	31.1787
1027	148.5	139.4	108.6	192.7	6.1	892.4	780.0	28	23.6966
1028	159.1	186.7	0.0	175.6	11.3	989.6	788.9	28	32.7680
1029	260.9	100.5	78.3	200.6	8.6	864.5	761.5	28	32.4012

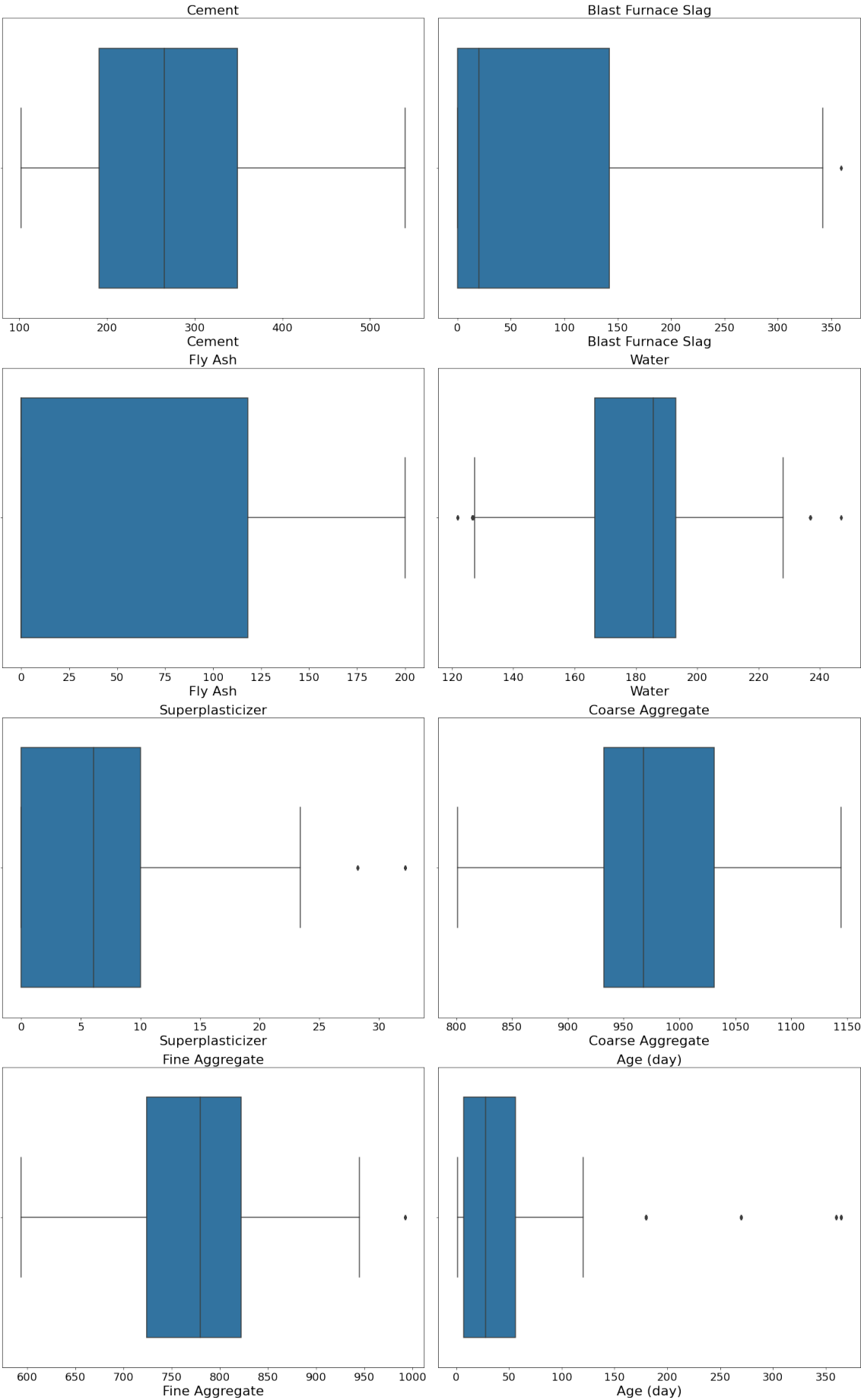
1005 rows × 9 columns



```
In [21]: fig, axes = plt.subplots(nrows=len(concrete_df.iloc[:, :-1].columns)//2, nco
axes = axes.flatten()

for i, column in enumerate(concrete_df.iloc[:, :-1].columns):
    sns.boxplot(concrete_df[column], ax=axes[i])
    axes[i].set_title(column, fontsize = 22)
    axes[i].tick_params(axis='x', labelsiz=18)
    axes[i].set_xlabel(column, fontsize=22)

plt.tight_layout()
plt.show()
```



In []:

```
In [22]: def remove_outlier(col):
col_sorted = sorted(col, reverse=True)
Q1, Q3 = pd.Series(col_sorted).quantile([0.25, 0.75])
IQR = Q3 - Q1
lower_range = Q1 - (1.5 * IQR)
upper_range = Q3 + (1.5 * IQR)
return lower_range, upper_range

for i in concrete_df.columns:
    l_r, u_r = remove_outlier(concrete_df[i])
    concrete_df[i].loc[~concrete_df[i].between(l_r, u_r)] = pd.NA

concrete_df
```

Out[22]:

	Cement	Blast Furnace Slag	Fly Ash	Water	Superplasticizer	Coarse Aggregate	Fine Aggregate	Age (day)	strength
0	540.0	0.0	0.0	162.0	2.5	1040.0	676.0	28	<N
1	540.0	0.0	0.0	162.0	2.5	1055.0	676.0	28	61.8873
2	332.5	142.5	0.0	228.0	0.0	932.0	594.0	<NA>	40.2695
3	332.5	142.5	0.0	228.0	0.0	932.0	594.0	<NA>	41.052
4	198.6	132.4	0.0	192.0	0.0	978.4	825.5	<NA>	44.2960
...
1025	276.4	116.0	90.3	179.6	8.9	870.1	768.3	28	44.2843
1026	322.2	0.0	115.6	196.0	10.4	817.9	813.4	28	31.1787
1027	148.5	139.4	108.6	192.7	6.1	892.4	780.0	28	23.6966
1028	159.1	186.7	0.0	175.6	11.3	989.6	788.9	28	32.7680
1029	260.9	100.5	78.3	200.6	8.6	864.5	761.5	28	32.4012

1005 rows × 9 columns



```
In [23]: rows_with_nan = concrete_df[concrete_df.isna().any(axis=1)]
```

```
rows_with_nan
```

Out[23]:

	Cement	Blast Furnace Slag	Fly Ash	Water	Superplasticizer	Coarse Aggregate	Fine Aggregate	Age (day)	strength
0	540.0	0.0	0.0	162.0	2.5	1040.0	676.0	28	<NA>
2	332.5	142.5	0.0	228.0	0.0	932.0	594.0	<NA>	40.2695
3	332.5	142.5	0.0	228.0	0.0	932.0	594.0	<NA>	41.052
4	198.6	132.4	0.0	192.0	0.0	978.4	825.5	<NA>	44.2960
6	380.0	95.0	0.0	228.0	0.0	932.0	594.0	<NA>	43.6982
...
862	140.0	164.0	128.0	<NA>	6.0	869.0	656.0	28	35.2253
873	237.0	92.0	71.0	<NA>	6.0	853.0	695.0	28	28.6270
908	313.0	145.0	0.0	<NA>	8.0	1000.0	822.0	28	44.5194
936	236.9	91.7	71.5	<NA>	6.0	852.9	695.4	28	28.6298
1019	139.7	163.9	127.7	<NA>	5.8	868.6	655.6	28	35.2253

94 rows × 9 columns



```
In [24]: concrete_df.dropna(inplace=True)
concrete_df
```

Out[24]:

	Cement	Blast Furnace Slag	Fly Ash	Water	Superplasticizer	Coarse Aggregate	Fine Aggregate	Age (day)	strength
1	540.0	0.0	0.0	162.0	2.5	1055.0	676.0	28	61.8873
5	266.0	114.0	0.0	228.0	0.0	932.0	670.0	90	47.0298
7	380.0	95.0	0.0	228.0	0.0	932.0	594.0	28	36.447
8	266.0	114.0	0.0	228.0	0.0	932.0	670.0	28	45.8542
9	475.0	0.0	0.0	228.0	0.0	932.0	594.0	28	39.289
...
1025	276.4	116.0	90.3	179.6	8.9	870.1	768.3	28	44.2843
1026	322.2	0.0	115.6	196.0	10.4	817.9	813.4	28	31.1787
1027	148.5	139.4	108.6	192.7	6.1	892.4	780.0	28	23.6966
1028	159.1	186.7	0.0	175.6	11.3	989.6	788.9	28	32.7680
1029	260.9	100.5	78.3	200.6	8.6	864.5	761.5	28	32.4012

911 rows × 9 columns



```
In [25]: # Separating dependent and independent variable.
X_raw = concrete_df.drop(columns=['strength'], axis=1)
Y = concrete_df['strength']
```

```
In [26]: X_raw
```

Out[26]:

	Cement	Blast Furnace Slag	Fly Ash	Water	Superplasticizer	Coarse Aggregate	Fine Aggregate	Age (day)
1	540.0	0.0	0.0	162.0	2.5	1055.0	676.0	28
5	266.0	114.0	0.0	228.0	0.0	932.0	670.0	90
7	380.0	95.0	0.0	228.0	0.0	932.0	594.0	28
8	266.0	114.0	0.0	228.0	0.0	932.0	670.0	28
9	475.0	0.0	0.0	228.0	0.0	932.0	594.0	28
...
1025	276.4	116.0	90.3	179.6	8.9	870.1	768.3	28
1026	322.2	0.0	115.6	196.0	10.4	817.9	813.4	28
1027	148.5	139.4	108.6	192.7	6.1	892.4	780.0	28
1028	159.1	186.7	0.0	175.6	11.3	989.6	788.9	28
1029	260.9	100.5	78.3	200.6	8.6	864.5	761.5	28

911 rows × 8 columns

```
In [27]: arr = np.array(X_raw)
```

```
In [28]: print("_____The prepared data is_____")
X_raw
```

_____The prepared data is_____

Out[28]:

	Cement	Blast Furnace Slag	Fly Ash	Water	Superplasticizer	Coarse Aggregate	Fine Aggregate	Age (day)
1	540.0	0.0	0.0	162.0	2.5	1055.0	676.0	28
5	266.0	114.0	0.0	228.0	0.0	932.0	670.0	90
7	380.0	95.0	0.0	228.0	0.0	932.0	594.0	28
8	266.0	114.0	0.0	228.0	0.0	932.0	670.0	28
9	475.0	0.0	0.0	228.0	0.0	932.0	594.0	28
...
1025	276.4	116.0	90.3	179.6	8.9	870.1	768.3	28
1026	322.2	0.0	115.6	196.0	10.4	817.9	813.4	28
1027	148.5	139.4	108.6	192.7	6.1	892.4	780.0	28
1028	159.1	186.7	0.0	175.6	11.3	989.6	788.9	28
1029	260.9	100.5	78.3	200.6	8.6	864.5	761.5	28

911 rows × 8 columns

```
In [29]: X_raw = X_raw.astype(float)
X = X_raw
X.info()
```

```
<class 'pandas.core.frame.DataFrame'>
Int64Index: 911 entries, 1 to 1029
Data columns (total 8 columns):
#   Column                Non-Null Count  Dtype
---  -
0   Cement                911 non-null    float64
1   Blast Furnace Slag    911 non-null    float64
2   Fly Ash               911 non-null    float64
3   Water                 911 non-null    float64
4   Superplasticizer      911 non-null    float64
5   Coarse Aggregate      911 non-null    float64
6   Fine Aggregate        911 non-null    float64
7   Age (day)             911 non-null    float64
dtypes: float64(8)
memory usage: 64.1 KB
```

```
In [30]: # function to estimate parameters
def Parameter_est( X ,y):
    Transpose = X.T
    mal = np.matmul(X.T,X)
    inv = np.linalg.inv(mal)
    b_hat = np.matmul(np.matmul(inv,X.T),y)
    return b_hat

# Assign the estimated parameters to b_hat
b_hat = Parameter_est( X ,Y)
print("_____The weight parameters are_____")
b_hat
```

_____The weight parameters are_____

```
Out[30]: 0    0.114994
         1    0.090383
         2    0.067183
         3   -0.176913
         4    0.266261
         5    0.005134
         6    0.010068
         7    0.307632
dtype: object
```



```
In [31]: # Function the Linear Regression
def linearRegression(beta):
    print ( "_____The fitted equation is_____")
    print (f"y_hat={b_hat[0]:.3f}X_1+{b_hat[1]:.3f}X_2+{b_hat[2]:.3f}X_3+{b_hat[3]:.3f}X_4+{b_hat[4]:.3f}X_5+{b_hat[5]:.3f}X_6+{b_hat[6]:.3f}X_7+{b_hat[7]:.3f}X_8")
    print ( "_____")

    # Fitting the equation:
    linearRegression(b_hat)

    # predicting the dependent variable using the fitted equation
    b_hat = b_hat.values
    y_hat = X_raw@b_hat
    print("_____The Predicted Values are_____")
    print(y_hat)
```

```
_____The fitted equation is_____
_____
y_hat=0.115X_1+0.090X_2+0.067X_3+-0.177X_4+0.266X_5+0.005X_6+0.010X_7+0.308X_8}
_____
_____The Predicted Values are_____
_____
1      54.938918
5      39.7736
7      31.327257
8      20.700388
9      33.665311
...
1025   39.747941
1026   33.914072
1027   25.553784
1028   28.750184
1029   31.866135
Length: 911, dtype: object
```

```
In [32]: #Error calculation:
def Errors(y_true, y_pred):
    e = y_true - y_pred
    mse = ((e**2).sum())/X.shape[0]
    return mse
mse = Errors(Y,y_hat)

print("Mean squared error is: ", mse)
rmse = np.sqrt(mse)
print("Root mean squared error is: {}".format(rmse))
```

```
Mean squared error is: 60.91449792340837
Root mean squared error is: 7.804774046915668
```

```
In [33]: from sklearn.preprocessing import PolynomialFeatures
from sklearn import linear_model
poly = PolynomialFeatures ( degree=3, interaction_only=False , include_bias
x = poly.fit_transform(X)
poly_clf = linear_model.LinearRegression()
poly_clf.fit (x, Y)
print(poly_clf.score(x,Y))
```

0.9127489832026829

```
In [34]: print( '.....' )
y_predict = poly_clf.predict(x)
print( 'mean_squared_error is ==' , mean_squared_error(Y,y_predict) )
rms = np.sqrt(mean_squared_error(Y,y_predict))
print( 'root mean squared error is == {} '.format(rms))
```

.....
mean_squared_error is == 21.901554707092167
root mean squared error is == 4.679909690057295

```
In [35]: # Function to create ANOVA Table
def Anova(y_true,y_pred):
    # Total variation
    SSt = ((y_true-y_true.mean())**2).sum()
    degree_t = X.shape[0] - 1
    # Residual variation
    SSres= ((y_true - y_pred)**2).sum()
    degree_res = X.shape[0] - X.shape[1]
    MSres = SSres/degree_res
    # variation due to regression
    SSreg = SSt-SSres
    degree_reg = X.shape[1]-1
    MSreg= SSreg/degree_reg
    F = MSreg/MSres
    return degree_res,degree_reg, SSres,SSreg,MSres,MSreg, F

degree_res, degree_reg, SSres,SSreg,MSres,MSreg, F = Anova(Y,y_hat)
```

```
In [36]: # Creating ANOVA Table
anova_dict = {'DF':[degree_reg, degree_res, degree_reg+degree_res], 'SS':[S
Anova_df = pd.DataFrame(anova_dict,index=["Regression","Residual","Total"])
print("_____ANOVA Table_____")
Anova_df
```

_____ANOVA Table_____

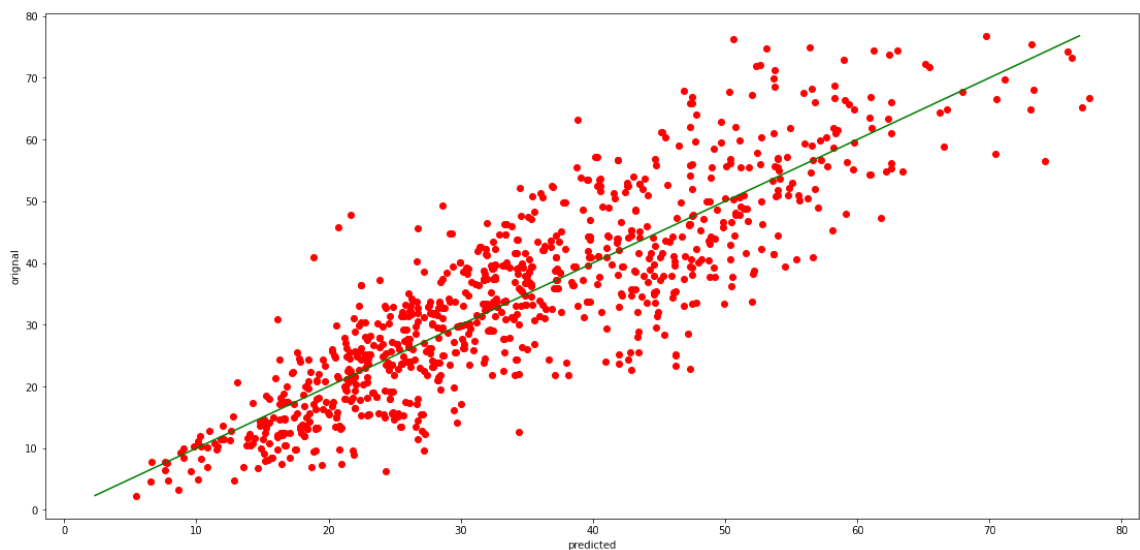
Out[36]:

	DF	SS	MS	F
Regression	7	173184.070842	24740.581549	402.585944
Residual	903	55493.107608	61.454161	402.585944
Total	910	228677.178451	24802.035710	402.585944

```
In [37]: # Predict R^2 value and adjusted R^2 value:  
R_sq = (SSreg / (SSreg + SSres)) * 100  
AdjR_sq = (1 - MSres / (MSres + MSreg)) * 100  
print(f"The R square value is: {R_sq}")  
print(f"Adjusted R square value is: {AdjR_sq}")
```

The R square value is: 75.73299269117916
Adjusted R square value is: 99.75222130164006

```
In [38]: # Plot the regression Line fitted by the function made  
plt.figure(figsize=[19, 9])  
plt.scatter(y_hat, Y, color='red')  
plt.plot([Y.min(), Y.max()], [Y.min(), Y.max()], color='green')  
plt.xlabel('predicted')  
plt.ylabel('original')  
plt.show()
```



In [39]: `poly_clf.coef_`

Out[39]: array([1.17601191e+06, -1.21797726e+02, -9.77272550e+01, -3.53238116e+02,
 -3.76676754e+02, 7.75298927e+02, -1.18724136e+02, -1.19179473e+02,
 6.76041295e+01, 4.58569642e-02, 9.58166294e-02, 2.45367886e-01,
 2.12243912e-01, -5.60072240e-01, 8.08168778e-02, 1.11840962e-01,
 -2.67501692e-02, 3.75291857e-02, 2.29013507e-01, 1.98304855e-01,
 -3.92699353e-01, 3.46025865e-02, 1.13145075e-01, -1.88148393e-02,
 2.29256936e-01, 6.41643557e-01, -4.57355352e-02, 2.31437236e-01,
 3.36810371e-01, -9.65166159e-02, 3.98257271e-01, -1.86652966e+00,
 3.21019876e-01, 2.71458231e-01, -1.92018555e-01, -4.76295366e-01,
 -2.95132699e-01, -9.73777597e-01, 5.63309522e-01, 4.51403155e-02,
 7.60088304e-02, -6.04224989e-02, 4.35843106e-02, -3.54123111e-02,
 8.47042616e-03, -6.06689386e-06, -2.20257117e-05, -4.76340947e-05,
 -2.63211185e-05, 1.38001638e-04, -1.53867352e-05, -2.34148406e-05,
 2.89179034e-06, -2.38577527e-05, -9.52081729e-05, -6.92818608e-05,
 2.02832790e-04, -2.33398617e-05, -5.41903497e-05, 7.61137495e-06,
 -7.55985889e-05, -1.91994847e-04, 1.47059216e-04, -7.83991712e-05,
 -1.23243121e-04, 3.86206262e-05, -7.56230220e-05, 6.23000777e-04,
 -7.63596192e-05, -1.11817041e-04, 3.69673001e-05, 1.42895591e-04,
 1.13123415e-04, 3.26173368e-04, -3.76855626e-04, -1.38787925e-05,
 -3.44717012e-05, 9.40944118e-06, -2.42730306e-05, 1.26708725e-05,
 -1.86758801e-05, -4.97891804e-06, -4.65633877e-05, -1.95809431e-05,
 1.57178620e-04, -4.83027976e-06, -2.69114663e-05, -3.52802014e-06,
 -7.93912150e-05, -1.84597292e-04, 6.19061213e-05, -5.91607219e-05,
 -1.27288785e-04, 2.64160414e-05, -1.14313346e-04, 2.62857960e-04,
 -3.53890651e-05, -1.23902927e-04, 3.98766328e-05, -2.99250314e-04,
 1.05528209e-04, 2.23774686e-04, -2.23500602e-04, -1.78748905e-07,
 -2.47184991e-05, 6.14728402e-06, -2.84803363e-05, 8.87615050e-06,
 -2.67067742e-05, -4.75929813e-05, -2.07327890e-04, -1.49501786e-04,
 -6.97120622e-05, -1.14466730e-04, 3.70891174e-05, -2.51396756e-04,
 4.58600950e-04, -2.05987207e-04, -3.45136754e-04, 9.02871623e-05,
 2.56148746e-04, -1.17655684e-04, 9.06445894e-05, -2.76395054e-04,
 -3.75746659e-05, -1.13619411e-04, 3.06424205e-05, -7.19747602e-05,
 4.61584203e-05, -2.17620055e-05, -9.22905995e-05, 1.12007898e-03,
 -2.14705143e-04, -1.38523167e-04, 1.02402436e-04, -2.17934930e-03,
 1.68745775e-04, 1.40963824e-03, -2.74291537e-04, -7.58363680e-05,
 -8.54061515e-05, 9.10081018e-05, -5.93612645e-05, 5.62805167e-05,
 5.38827762e-06, 2.62793533e-05, -5.74879886e-05, 8.53082669e-04,
 -1.89034298e-08, 3.27361420e-06, 3.03961629e-04, -2.07486199e-04,
 2.02739725e-04, -2.17014698e-04, -2.99956218e-05, -5.14819789e-06,
 -1.41634667e-05, 1.48009276e-05, -1.19784175e-05, 1.43270799e-05,
 -9.54203623e-06, -4.54050266e-06, 3.98634058e-06, -1.09147175e-05,
 7.88327226e-05])

In []: