

# **Quantum Key Distribution: Analyzing the BB84 Protocol with Eavesdropping** and Enhancing Security with Quantum Repeaters

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# **ABSTRACT**

Quantum Key Distribution (QKD) is a cornerstone of quantum cryptography, offering secure communication by leveraging principles like superposition and entanglement. This project simulates two scenarios: (1) the BB84 protocol with an eavesdropper (Eve) and (2) QKD with quantum repeaters to extend secure communication distances. The study aims to explore the robustness of QKD against eavesdropping and assess the role of repeaters in mitigating distance limitations. Simulations are performed using Qiskit on IBM Quantum platforms, with quantum circuits designed to analyse key rates, error detection, and quantum states. Key findings include the BB84 protocol's ability to detect eavesdropping through error rates and the performance improvement in secure key exchange with repeaters. These results demonstrate QKD's potential to enhance cryptographic security in the quantum era, addressing threats posed by advances in quantum computing.

# INTRODUCTION

#### **BACKGROUND**

Quantum computing introduces a paradigm shift in computation, leveraging principles like superposition and entanglement to solve complex problems that are intractable for classical systems. In this context, quantum cryptography emerges as a cornerstone for secure communication, utilizing these quantum principles to ensure data integrity and privacy.

Quantum Key Distribution (QKD) is a prominent application of quantum cryptography, enabling two parties to establish a secure key while detecting potential eavesdropping attempts. Among various QKD protocols, the BB84 protocol, developed in 1984 by Bennett and Brassard, is widely recognized for its simplicity and effectiveness. It encodes information in quantum states such as photons, with eavesdropping introducing detectable errors in the key.

However, the practical implementation of QKD faces significant challenges. Chief among these is the loss of quantum signals over long distances, primarily due to decoherence and attenuation. Quantum repeaters offer a promising solution to this limitation by enabling entanglement distribution and error correction across extended communication links.

#### PROBLEM STATEMENT

This project seeks to address two critical questions:

- 1. How does the BB84 protocol detect and mitigate eavesdropping?
- 2. How can quantum repeaters enhance the effectiveness of QKD over long distances?

### **SCOPE**

The scope of this project includes the simulation of QKD protocols using Qiskit, focusing on the BB84 protocol's security in the presence of an eavesdropper (Eve) and the performance improvement enabled by quantum repeaters.

#### **GOALS**

The primary objectives of the project are:

- 1. To implement and simulate the BB84 protocol, examining its ability to detect eavesdropping through quantum measurements.
- 2. To simulate QKD with quantum repeaters and evaluate their impact on secure key distribution over long distances.
- 3. To analyse the outcomes of these simulations and draw insights into the security and practicality of QKD systems.

# LITERATURE REVIEW

Quantum Key Distribution (QKD) is a well-researched area in quantum cryptography, with numerous studies highlighting its theoretical foundations, practical challenges, and advancements. Below is a summary of key findings from the literature, focusing on the BB84 protocol and the role of quantum repeaters in extending QKD capabilities.

### **BB84 Protocol**

The BB84 protocol, proposed by Bennett and Brassard (1984), remains the foundation of QKD research. The protocol leverages quantum states, encoded in orthogonal and diagonal bases, to transmit a secure key. Eavesdropping introduces measurable disturbances in the quantum states, enabling detection. Studies by Lo et al. (2005) and Scarani et al. (2009) further analyze its theoretical security, showing that errors above a certain threshold indicate an eavesdropper's presence. While the protocol is robust in detecting eavesdropping, practical implementation faces challenges like photon loss and device imperfections.

## **Challenges in Practical QKD**

Practical implementations of QKD are limited by the physical properties of quantum systems. Photon loss during transmission and detector inefficiencies are major bottlenecks. Experimental studies, such as those by Gisin et al. (2002), demonstrate the difficulty of achieving high key rates over long distances. These challenges necessitate solutions like error correction codes and decoy-state techniques to enhance protocol robustness.

## **Quantum Repeaters for Long-Distance QKD**

To address distance limitations, quantum repeaters have emerged as a key innovation. Quantum repeaters, as described by Briegel et al. (1998), use entanglement swapping and purification to extend the range of QKD. Subsequent studies, including Dur et al. (1999) and Simon et al. (2007), provide a framework for implementing repeaters in quantum networks, demonstrating their ability to mitigate decoherence and loss. Recent experimental implementations by Liao et al. (2018) validate their feasibility, highlighting improvements in secure communication over several hundred kilometres.

## Gaps in Existing Research

Despite significant advancements, challenges remain in scaling QKD systems. Current studies often rely on idealized conditions, overlooking real-world complexities such as environmental noise and hardware limitations. Moreover, while quantum repeaters show promise, their integration with existing QKD protocols requires further exploration. Research by Ewert and van Loock (2014) underscores the need for optimized error correction mechanisms in repeater-based QKD systems.

### **Relevance to the Project**

This project builds on the foundational work of BB84 while addressing practical challenges through simulation. By implementing QKD with repeaters, the study extends the literature by evaluating performance enhancements in a simulated environment, bridging the gap between theoretical models and practical feasibility.

# **METHODOLOGY**

#### **Tools and Frameworks**

All the standard python libraries are being used. The only libraries specific to this project are:

- qiskit
- qiskit aer

#### **Theoretical Foundations**

**1. Quantum Superposition:** Quantum superposition is a fundamental concept in quantum mechanics, where a quantum system can exist in multiple states simultaneously until it is measured. This contrasts with classical systems, which can only exist in one state at a time. For example, a qubit (quantum bit) can represent both 0 and 1 at the same time in a superposition state. Mathematically, a qubit can be described as:

$$|\psi
angle = lpha |0
angle + eta |1
angle$$

where  $\alpha$  and  $\beta$  are complex numbers representing the probability amplitudes of the system being in state  $|0\rangle$  or  $|1\rangle$ , respectively. When a measurement is performed, the superposition collapses into one of the basis states with probabilities proportional to the squared magnitudes of the amplitudes  $|\alpha|^2$  and  $|\beta|^2$ .

In the context of quantum key distribution (QKD), superposition allows the transmission of quantum information in states that are difficult for an eavesdropper to measure without introducing detectable errors. For example, in the BB84 protocol, qubits are encoded in superposition states of photon polarizations, which makes it challenging for an eavesdropper to intercept and measure without being detected.

- **2. BB84 Protocol:** The BB84 protocol, developed by Bennett and Brassard in 1984, is one of the first and most widely known quantum key distribution protocols. The protocol uses the principles of quantum mechanics, particularly the concept of quantum superposition and the no-cloning theorem, to ensure secure communication. The BB84 protocol involves four possible states of qubits, encoded using two bases:
  - Rectilinear basis (0, 1): This includes the states  $|0\rangle$  (horizontal polarization) and  $|1\rangle$  (vertical polarization).
  - Diagonal basis (+, -): This includes the states  $|+\rangle=\frac{1}{\sqrt{2}}(|0\rangle+|1\rangle)$  and  $|-\rangle=\frac{1}{\sqrt{2}}(|0\rangle-|1\rangle)$ , corresponding to +45° and -45° polarizations.

During key generation, the sender (Alice) randomly chooses one of these bases to encode each bit of the key, and the receiver (Bob) randomly chooses one of the two bases to measure each received qubit. After a series of transmissions, Alice and Bob compare their chosen bases over a public channel and keep the bits where their bases match, discarding the others. If an eavesdropper (Eve) intercepts and measures the qubits, the measurement disturbs the qubits due to the uncertainty principle, leading to detectable errors. This property makes BB84 a secure protocol, as the presence of an eavesdropper can be detected by comparing a subset of the bits and checking for discrepancies.

**3. Quantum Teleportation:** Quantum teleportation is a process by which quantum information is transferred from one location to another, without physically sending the particle itself. This phenomenon is based on the principle of **quantum entanglement**. Entanglement is a state where two particles become correlated such that the state of one particle instantly determines the state of the other, regardless of the distance between them.

In quantum teleportation, three particles are involved:

- A pair of entangled particles (usually photons or electrons) shared between the sender (Alice) and the receiver (Bob).
- The third particle is the one whose state is being "teleported."

## The process involves:

- 1. Alice performs a **Bell-state measurement** on the particle she wishes to teleport and one of her entangled particles. This step entangles her particle with the state of the particle she wants to teleport.
- 2. Alice sends the result of her measurement (two classical bits of information) to Bob over a classical communication channel.
- 3. Bob uses the classical information to apply a unitary operation (either a bit-flip or phase-flip) to his entangled particle, thus transforming it into the state of the particle that Alice wanted to teleport.

Quantum teleportation does not involve the physical transfer of particles but relies on quantum entanglement and classical communication to replicate the state of the particle at a distant location. This concept is vital for quantum networks and could be used for secure communication and quantum computing.

**4. Quantum Repeaters:** Quantum repeaters are devices that enable long-distance quantum communication by overcoming the problem of signal loss and decoherence in quantum channels. As quantum signals, such as photons, travel through optical fibres or free space, they lose coherence due to interactions with the environment, resulting in errors or data loss. Quantum repeaters provide a solution by extending the range of quantum key distribution protocols like BB84.

The basic function of a quantum repeater involves:

- 1. **Entanglement Distribution**: Quantum repeaters generate and distribute entangled pairs of qubits over intermediate stations along the communication path. Each repeater station creates entanglement between a pair of qubits, which are then transmitted to neighbouring stations.
- 2. **Entanglement Swapping**: When the entanglement between two distant repeater stations is lost due to decoherence, entanglement swapping can be used to restore it. In this process, two previously unentangled particles become entangled by measuring them in a certain basis and using the classical communication to update the state.
- 3. **Quantum Error Correction**: Repeaters use quantum error correction codes to detect and correct errors that arise due to noise or decoherence. This allows for the creation of reliable entanglement over long distances.

Quantum repeaters are critical in the development of large-scale quantum networks. They enable secure transmission of quantum information across vast distances, which is essential for the realization of quantum internet and global quantum communication systems.

## **Implementation Steps**

## **Step 1:** Define the message.

Enter a message that you would like to transmit to Bob. The default message is 'Hello world'. The cell below takes the input message and defines the 'length of message' (slightly longer than the actual message). This will be useful to generate our key. The longer this len\_message, the better. (Keep it 3x to be on the safe side)

```
#you are ALICE
#this block deals with the breaking of message into small chucnks, need small chunks if you have small number of qubits

#message = '' #used for debugging
message = input('Enter a short message (default message is "Hello World") : ')
if len(message)<1:
    message = 'Hello World'
print('The message to be sent is "', message,'"')

#initial size of encrypttion key, arbitary number to multiply so that len of string/key is longer than the actual message!
len_message = len(message)*3

Enter a short message (default message is "Hello World") :
The message to be sent is " Hello World "</pre>
```

Define the number of qubits of the system that will be used to process. Sice we need to generate a random string of binary numbers, we need to restrict it with the maximum available qubits. We then divide the message into chunks of maximum available qubits (default 5 qubits)

As you can see from the above step, the message of lenth of message will be equal to length of the key, however this is subdivided into small bits (of size <5 bits) so that we can generate a 5 bit random binary string.

# Breakdown of the BB84 protocol (a simpler version)

Alice wants to send the above message to Bob.

- 1) Alice will generate a random string of binary numbers whose length will be equal to the length of the message (or greater).
- 2) Alice will convert this string into corresponding quibits. But, she will put them into a superposition before sending it to Bob
- 3) Alice will send this superposition to Bob
- 4) Bob recievs this superposition and randomly rotates it in the opposite direction
- 5) Now, Alice and Bob will publicly share the keys with which the qubits were rotated, when the did the same thing, both can calculate a similar key. (In theory it should be the same)
- 6) Alice and Bob create their keys which will be used to encode message by Alice and decode the message at Bobs site.

## Step 2: Define a function to generate a random string of binary digits.

- The input is size of the string that needs to be generated.
- The output is the random string of binary digits.

The circuit to generate random binary numbers using a 5-bit quantum computer. This gives out a 5-bit random binary number.

Alice will generate a random key called Initial Key. This will be used to generate the encryption key.

Alice and Alice only will have this key. (Initial Key)

Now, Alice will generate a random string of binary numbers again. This will be transmitted to Bob

```
#Generate a random string of binary digits which she will send to Bob
A_rot = RandomStringG (len_message)
print('Alice rotation key is :',A_rot) #print this random string

Alice rotation key is : 0000001001000000010110000000000011
```

Similarly, Bob will generate a random string. Bob will send this to Alice

Now both Alice and Bob have generated and shared their rotation keys.

Now, Alice uses this \*\*Alice's Rotation Key\*\*. She wants to a send a Superposition of Qubits to Bob. For that first she checks if the bit is 0, then she will prepare a qubit on the negative z axis. If the bit is one, she will prepare a qubit on the positive z axis. This is done by the X gate.

Furthermore, Alice checks that if it is a 1 bit, she will rotate the quibit using a H gate.

Now she sends this superposition to Bob.

He will take this and rotate it in the opposite direction with a H gate. After that Bob measures the qubit and records the result, this is stored in Bob\_result.

If a third party observes this superposition, the key/state will be broken and Bob and Alice will know!

• Note: Only Alice's Rotation Key and Bob's Rotation Key are public

The above mentioned string is Bobs observation of the Superposition. \*\*This belongs to Bob and Bob only\*\*

Now, Alice and Bob has shared their random strings with one and another and Bob has observed the Qubits that were in superposition (sent by Alice.)

Given the public information i.e. Rotation Keys, Alice and Bob will generate a secret quantum encryption/decryption key.

If a bit in Alice's rotation string is the same as the corresponding bit in Bob's they know that Bob's result is the same as what Alice sent.

(In brief, both the keys should be the same) (Alice based on her original key/Initial Key and Bob based on his measured results/Bob\_results).

```
if A_key == B_key:
    print('The key is a match!')
    else:
        print('Error, Key not matched')

The key is a match!
```

As you can see, the keys are a perfect match, if they were not, someone tried to eavesdrop on your superposition.

### Note: In practice this doesn't happen, there is a lot of noise that gets added to this and thereby the keys don't match. In order to overcome this we need to mitigate the errors by taking multiple measurements.

Now we have a secure key that no one knows, we can use \*\*THIS\*\* key to encrypt and decrypt messages

#### Presence of Eve

Eve is eavesdropping!

In order to simulate what will happen if another third person tries to listen to this communication.

Consider Eve is trying to listen what Alice sent to Bob. Eve knows Alice's and Bob's Public rotation keys.

Alice has sent a superposition of random qubits to Bob. Now Eve tries to read these qubits and listen to Alice and Bobs conversation. Consider the situation where Alice has sent Bob a superposition of the qubits and Eve tries to measure them.

```
Eve_result = ''

#break the message in length of less than 5 bits for 5 qubit operation. (chunks of 5 bits)
for loc, BM_num in enumerate(break_message): #break_message contains how the message/string is divided

if BM_num cnum_phits:
    temp_key = key[num_qbits*loc:num_qbits*loc:BM_num]
    A_r_temp = A_rot[num_qbits*loc:num_qbits*loc:BM_num]
    #ave uses Public rotation key of Alice to try to decode the string
else:
    temp_key = key[BM_num*loc:BM_num*(loc+1)]

#quantum computer tokes over from here
#generate a register (clossical and quantum) and a quantum circuit
q = Quantumkegister(BM_num)
    c = ClassicalRegister(BM_num)
    c = ClassicalRegister(BM_num)
    ev_QC = Quantumkclircuit(q,c)

#prepare qubits based on key; add Hadamard gates based on Alice's and Bob's
#rotation strings
for i,j,n in zip(temp_key,A_r_temp,range(0,len(temp_key))):
    i = int(1)
    j = int(3)
    if i > 0:
        Eve_QC.*(c[n])
    if j > 0:
        Eve_pc.*(clossical one decomposition of the preparation of the preparatio
```

Since Eve read/observed the superposition the wave function collapsed. Now if Bob doesn't receive any communication, he would know someone was trying to eavesdrop.

Now, Eve tries to be sneaky and tries to generate a superposition of qubits and sends it to Bob so that he doesn't become suspicious. (but that is what Eve thinks).

```
#the code is similar to the above one

for loc, BM_num in enumerate(break_message):
    if BM_num < num_qbits:
        temp_key = key[num_qbits*loc:num_qbits*loc:num_qbits*loc+BM_num]
        temp_key = key[num_qbits*loc:num_qbits*loc+BM_num]
        B_r_temp = B_rot[num_qbits*loc:num_qbits*loc+BM_num]
    else:
        temp_key = key[BM_num*loc:BM_num*(loc+D)]
        temp_key = key[BM_num*loc:BM_num*(loc+1)]

#create a quantum circuit to generate superposition as per Eve_results

q = QuantumRegister(BM_num)
    c = classicalRegister(BM_num)
    c = classicalRegister(BM_num)
    fve_2, Qc = QuantumCircuit(q , c)

#prepare qubits and send the superpositon

for i,j,n in zip(temp_eve,B_r_temp,range(0,len(temp_key))):
    i = int(i)
    j = int(j)
    if i > 0:
        Eve_2, Qc.x(q[n])
    if j > 0:
        Eve_2, Qc.x(q[n])

#technically Eve will send the superposition of qubits from here to Bob

Eve_2, Qc.measure(q[n],c[n])

#At Bob's site this is what he will observe!

Bob_bad_result += list(execute(Eve_2, Qc, backend, shots=1).result().get_counts(Eve_2, Qc).keys())[0][::-1]

print("Bob's previous results (w/o Eve):",Bob_result) #original result

print("Bob's results from Eve:\t\t\t\t\t\",Bob_bad_result) #bad/intercepted result

Bob's previous results (w/o Eve):".Bob_dad_result) #bad/intercepted result
```

Bob should have observed the first result (w/o Eve), however since Eve tried to eavesdrop and generate a new random superposition, Bob will receive a new superposition of qubits.

The next cell will show that if Bob tries to generate a key, it will be different than what Alice will generate. Thereby, Bob won't be able to decrypt the message that Alice has sent!

```
#make keys for Alice and Bob with the bad result Eve sent
A_key_new = KeyGen(B_rot,A_rot,key)
B_key_new = KeyGen(B_rot,A_rot,Bob_bad_result)

print("Alice's key: ",A_key_new)
print("Bob's new key: ",B_key_new)

if not A_key_new == B_key_new:
    print("Keys don't match !") #this is just for our reference

Alice's key: 0011010010100
Bob's new key: 0011100010100
Keys don't match !
```

Since the keys don't match, the encrypted text that Alice will send, Bob won't be able to decrypt it. But how will both Alice and Bob check this?

In order to check the discrepancy, Alice will generate a Check key, i.e. a random key same as the length of the A\_new\_key. She will then send this random key to Bob who will check his B\_new\_key for discrepancies

```
#generate a random key by Alice and send it to Bob
check_key = RandomStringG(len(A_key_new))
print('spots to check:',check_key)

spots to check: 0100011011001
```

```
#print the faulty subsection of public keys and send it to Alice

print("subset of Bob's key: ",sub_B,key)

#now Alice and Bob sends their faulty keys (which are a part of the public knowledge,as they were shared) to one and another

#compare Alice and Bob's key subsets

secure = True

for i,j in zip(sub_A,key,sub_B,key):
    if i == j:
        secure = True
    else:
        secure = False
        break;
if not secure:
    print('Eve detected!')
else:
    print('No evesdropper detected')

subset of Alice's key: 010100
subset of Bob's key: 000100
Eve detected!
```

Note: It is important to have longer keys so that it becomes easier to detect the presence of Eve

# **RESULTS & DISCUSSION**

#### **Simulation Results**

The project simulates the Quantum Key Distribution (QKD) protocol, specifically the BB84 protocol, using quantum computing platforms like Qiskit. Two key simulations are conducted:

- 1. **BB84 Protocol with Eavesdropping**: This simulation models the transmission of quantum bits (qubits) from Alice to Bob, with the presence of an eavesdropper (Eve) trying to intercept the qubits. As part of the simulation, we observed how the presence of Eve affects the transmission fidelity and how discrepancies in the received key can be used to detect eavesdropping. The results show that when Eve intercepts the qubits and performs a measurement, the qubits' polarization states are disturbed, causing errors in the final key that Alice and Bob can detect through basis comparison.
  - Error Rate: We observed that, with the presence of Eve, the error rate in the transmitted key increases significantly, demonstrating the protocol's effectiveness in detecting eavesdropping.
  - Key Distribution Efficiency: The simulation also revealed that the efficiency of the key distribution process decreases when Eve is active. The higher the number of intercepted qubits, the higher the error rate, suggesting that the protocol can secure the key by detecting any tampering attempts.
- 2. **BB84 Protocol with Quantum Repeaters**: The second simulation focuses on the enhancement of QKD over long distances using quantum repeaters. The repeaters are designed to extend the range of quantum communication by distributing entanglement and using error correction techniques. In the simulation, quantum repeaters are introduced to bridge gaps in the transmission path, thereby allowing for longer, more secure key exchanges.
  - Distance Enhancement: The simulation demonstrates that quantum repeaters significantly extend the communication distance by overcoming photon loss and decoherence in the channel. The use of repeaters enables successful key distribution over distances that would be otherwise impossible using direct transmission.
  - Error Correction and Entanglement Swapping: The simulation also confirms that error correction and entanglement swapping techniques used by repeaters can restore and maintain the integrity of the quantum states over long distances. As a result, the error rate remains lower compared to conventional direct transmission, even over extended distances.

## **Analysis**

The results show that the BB84 protocol is highly effective in detecting eavesdropping due to the fundamental properties of quantum mechanics, particularly the disturbance caused by measurements on quantum states. The presence of Eve leads to detectable errors in the final key, which is a key advantage of quantum cryptography over classical methods. Additionally, the simulation highlights that with the introduction of quantum repeaters, the transmission distance of secure quantum communication is greatly enhanced, making long-range QKD feasible. This is crucial for building large-scale quantum networks.

Moreover, the use of quantum repeaters enables the maintenance of low error rates over extended distances, which is essential for ensuring the reliability of the key exchange. The

combination of entanglement swapping and error correction ensures that the quantum states remain coherent and secure, even when transmitted over long distances. The results emphasize the importance of quantum repeaters in overcoming the physical limitations of quantum communication, such as photon loss and decoherence.

## **Comparison with Classical Counterparts**

The results from the quantum simulations were compared with classical counterparts, such as traditional key distribution systems. Classical methods typically rely on mathematical algorithms to secure communication, but they do not offer the same level of security as quantum protocols like BB84. In classical systems, eavesdropping does not result in detectable disturbances, making it harder to detect unauthorized access.

Quantum systems, on the other hand, offer provable security based on the laws of quantum mechanics. The disturbance caused by measurement in quantum systems can be directly observed, which is not possible in classical systems. Therefore, the BB84 protocol's ability to detect eavesdropping, even when the attacker is powerful enough to intercept all communication, sets it apart from classical key distribution methods.

## Challenges

Several challenges were encountered during the implementation of the QKD protocol, especially in simulating long-distance communication:

- 1. **Photon Loss**: In simulations involving long-distance transmission, simulating photon loss and decoherence accurately was challenging. While quantum repeaters helped mitigate this problem, creating realistic models of loss over distance remains a complex task.
- 2. **Hardware Limitations**: Simulating quantum systems is computationally intensive, particularly when attempting to model the complex interactions and large numbers of qubits involved in real-world scenarios. The available hardware, while powerful, still faces constraints when simulating larger-scale quantum networks.
- 3. **Implementation of Repeaters**: While the concept of quantum repeaters is well-established in theory, their practical implementation in simulations required careful modeling of entanglement swapping and error correction. Additionally, optimizing the repeater network for maximum efficiency is still an area of ongoing research.

#### **Future Considerations**

The results from this study open the door for further research into improving the efficiency and scalability of QKD systems. Future work could focus on optimizing the quantum repeater architecture to minimize error rates further, exploring new error correction protocols, and implementing more complex simulations of real-world quantum networks.

## CONCLUSION & FUTURE WORK

## **Summary**

This project aimed to investigate and simulate the implementation of the Quantum Key Distribution (QKD) protocol, specifically the BB84 protocol, in the presence of eavesdropping and extended communication distances using quantum repeaters. The main objectives were to demonstrate how quantum communication can be secured against eavesdropping, and to explore the enhancement of QKD over long distances using quantum repeaters. The methods involved simulating the BB84 protocol and quantum repeaters using quantum computing platforms such as Qiskit. The simulations also included analyzing the impact of an eavesdropper's interference on the transmission and comparing key generation efficiency with and without repeaters.

The key findings of the project were:

- The BB84 protocol effectively detects eavesdropping by causing measurable disturbances in quantum states, leading to a higher error rate in the final key when an eavesdropper intercepts the communication.
- The introduction of quantum repeaters significantly extends the range of quantum key distribution, allowing for secure communication over longer distances by mitigating photon loss and decoherence.
- Error correction and entanglement swapping used in quantum repeaters helped maintain key transmission integrity, even over long distances.

### **Conclusion**

This project contributes to the growing body of knowledge in quantum computing and quantum cryptography by providing valuable insights into the practical implementation of secure quantum communication. By simulating the BB84 protocol with and without quantum repeaters, the project demonstrated the effectiveness of QKD in protecting against eavesdropping and highlighted the potential of quantum repeaters in overcoming distance limitations in quantum networks. The ability to secure communication in the presence of eavesdropping is a major step forward in the field of quantum cryptography, and the use of quantum repeaters opens up new possibilities for global-scale quantum communication networks.

The findings of this project are relevant not only to the academic community but also to real-world applications such as secure communication systems, quantum internet, and global data protection. As quantum computing and quantum communication technologies continue to evolve, the insights from this project will be instrumental in advancing secure, long-distance quantum communication.

#### **Future Work**

While the current work successfully simulates the BB84 protocol and quantum repeaters, there are several areas where further research and improvement can be made:

- 1. **Improvement of Quantum Repeater Models**: The current simulation of quantum repeaters could be expanded to include more complex error correction protocols and optimized entanglement swapping techniques. This would help improve the efficiency and reliability of repeaters in real-world quantum communication networks.
- 2. **Real-World Implementation**: Future work could focus on translating the simulated models into real-world quantum communication systems. This would involve tackling challenges such as hardware imperfections, photon loss, and environmental noise in a physical quantum network.
- 3. **Scalability of QKD Systems**: As the scope of quantum networks expands, research could focus on optimizing the scalability of QKD systems, including improving the integration of quantum repeaters with existing communication infrastructure. Additionally, exploring the use of different quantum protocols, such as entanglement-based QKD or continuous-variable QKD, may yield new insights into enhancing the security and efficiency of quantum key distribution.
- 4. **Quantum Internet and Global Security**: Long-term research could look into building a global-scale quantum internet, where secure quantum communication and key distribution are integrated across countries. This would require advanced quantum networking techniques, improved quantum repeaters, and seamless integration with classical networks.

By addressing these areas, the future of quantum key distribution and secure quantum communication systems can become more practical, scalable, and efficient, ultimately contributing to the development of a quantum-safe world.

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