

**Report for Assignment - 1 (Computer Vision CSCI-GA.2271-001)**  
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1. Image Filtering

(a) 1. Valid

$$\begin{bmatrix} az+by+dx+ew & bz+cy+ex+fw \\ dz+ey+gx+hw & ez+fy+hx+iw \end{bmatrix}$$

2. Same

$$\begin{bmatrix} aw & ax+bw & bx+cw \\ ay+dw & az+by+dx+ew & bz+cy+ex+fw \\ dy+gw & dz+ey+gx+hw & ez+fy+hx+iw \end{bmatrix}$$

(b) Output dimension of image (h,w) convolved with filter (i,j) valid boundary conditions is (X,Y):

$$X = \max([h-\max(0,i-1)],0)$$

$$Y = \max([w-\max(0,j-1)],0)$$



Original Image

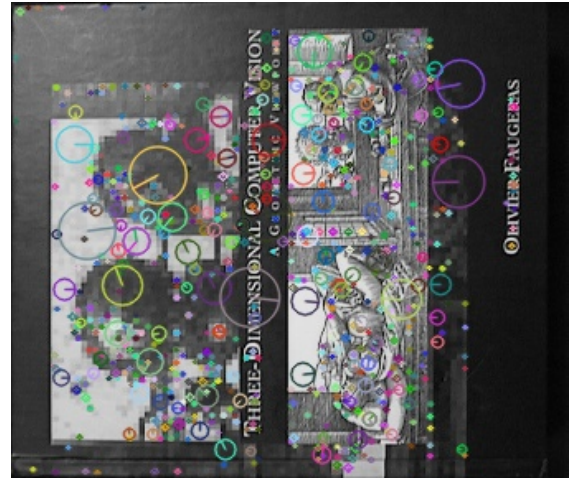
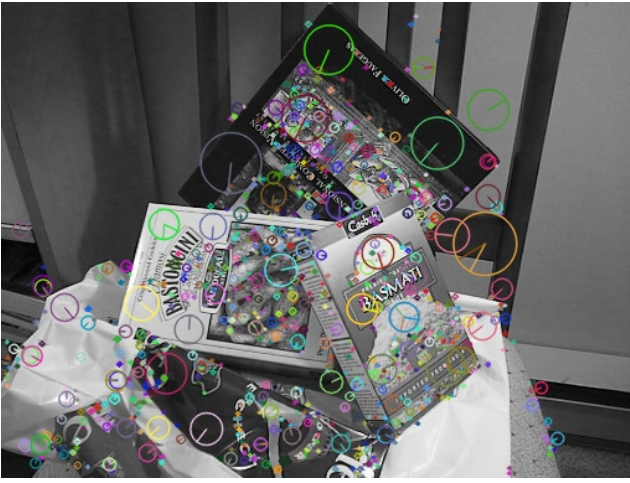
Blurred Image (width = 3)



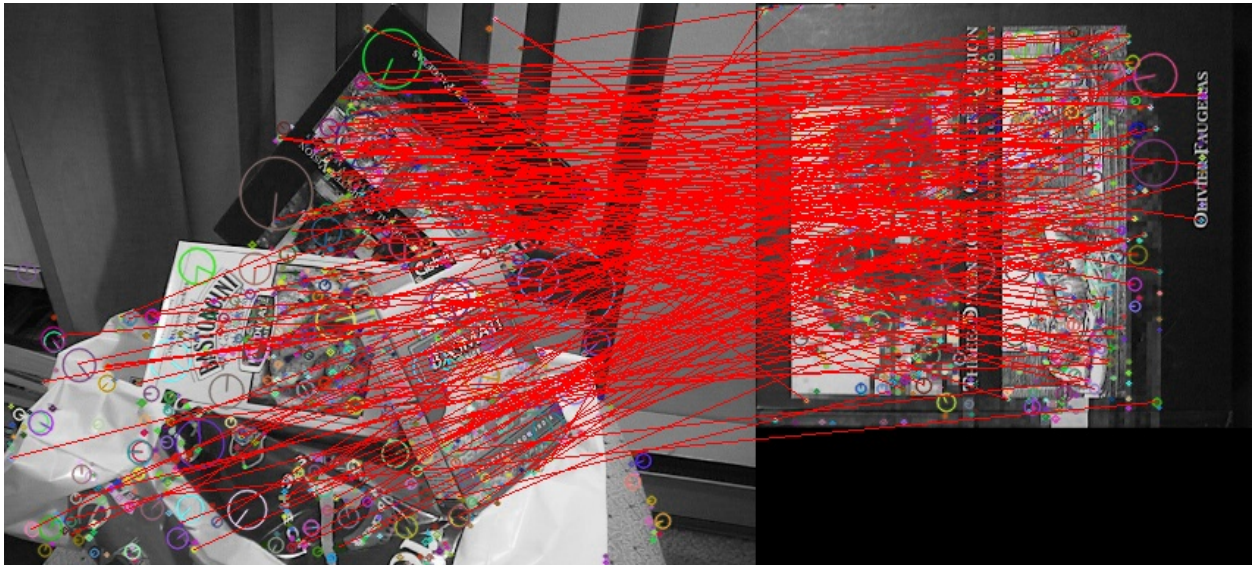
Blurred Image (width = 5)



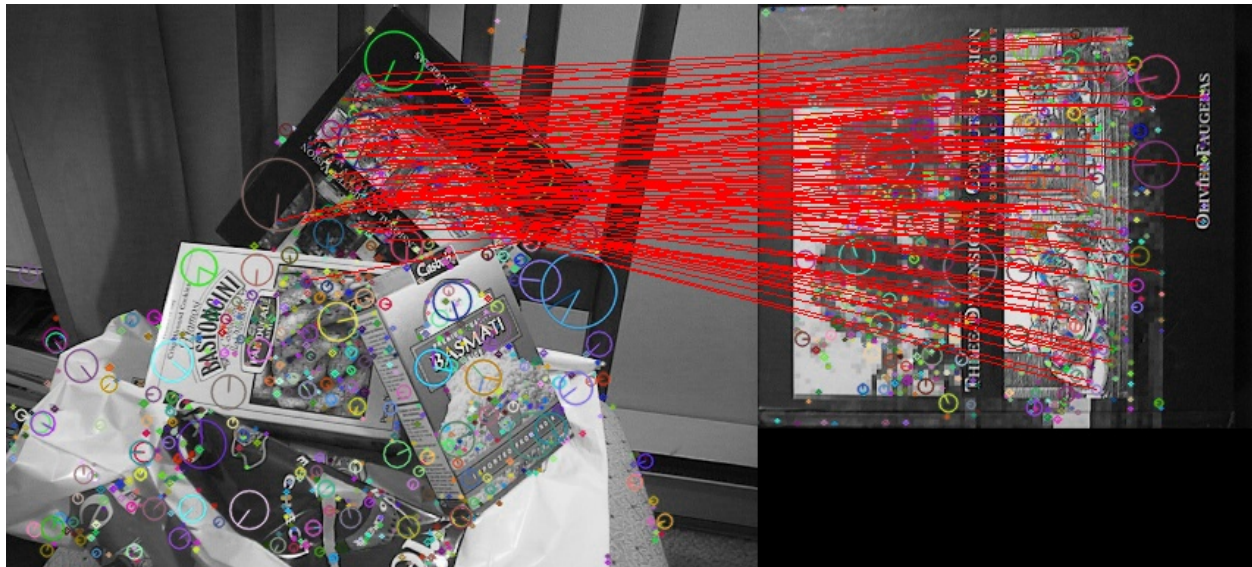
## 2. Image Alignment



SIFT keypoints of both images. Each keypoint is represented with its size and orientation(circle).



There were 248 good matches with a threshold of 0.9. The above image is before RANSAC.

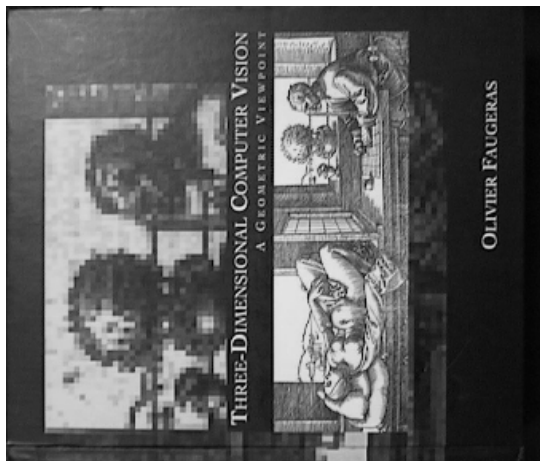


Feature matching between the 119 inliers (48% of good matches). The above image is after RANSAC.

Final transformation (H) Matrix

$$\begin{bmatrix} 1.1109896 & -1.20025397 & 38.0034649 \\ 1.21704437 & 1.07267689 & -330.64476206 \end{bmatrix}$$

As we can see below, the pose of the book is almost the same in both the images.



Real image



Warped image after affine transformation

### 3. Estimating the camera parameters

Camera matrix P

```
[[ -1.27000127e-01 -2.54000254e-01 -3.81000381e-01 -5.08000508e-01]
 [ -5.08000508e-01 -3.81000381e-01 -2.54000254e-01 -1.27000127e-01]
 [ -1.27000127e-01 -1.11022302e-16 -1.27000127e-01  0.00000000e+00]]
```

Camera world coordinates (C) - 1st method

```
[[ 1.]
 [-1.]
 [-1.]]
```

Camera world coordinates (C) - 2nd method

```
[[ 1.]
 [-1.]
 [-1.]]
```



#### 4. Structure from Motion

Translation vector of first camera ( $t_i$ )

[2.3684757858670008e-17, 8.2896652505345025e-17]

Affine camera matrix for first camera ( $M_i$ )

[[-7.50914219 3.30837904 -3.71763726]

[-4.53754376 -1.57773527 7.74574759]]

3D coordinates(x,y,z) for the first 10 world points

[(0.0057716262048463658, 0.064606281983365529, -0.024976152508609656),  
(0.00057609968845948717, 0.068853630512852607, -0.034581509689483828),  
(-0.042935849081986235, 0.063304789701081735, 0.028617113082434188),  
(0.047450383489819413, 0.049042065349057251, -0.012575472616124796),  
(-0.042101860262101248, 0.067892392631770271, 0.011751637042498885),  
(0.059619637747370981, 0.04605179976154497, -0.014383742867820598),  
(0.009091667080625334, 0.06002048918269999, -0.012299970374395071),  
(0.010394894790726692, 0.046020653847651312, 0.035292747610496743),  
(-0.025890805334956506, 0.05702972054986153, 0.033373747525897966),  
(0.017455976600106261, 0.040542636931378842, 0.047318593420524822)]

Scatter plot of the 3D world points (Final 3D object - Cube)

