

Bhavan's Campus, Munshi Nagar, Andheri (West), Mumbai-400058-India (Autonomous College Affiliated to University of Mumbai)

Academic SEM: VII Year: 2022-23

Experiment: K Means Clustering

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Class:	BE EXTC
Batch:	В
Subject:	Data Analytics Lab

Objective: The focus of this lab is k-means clustering. We will look at the vanilla algorithm, its performance, and some better variants. Finally, we will use clustering for classifying the MNIST data set.

System Requirements: Python 3.9

Code:

```
def distance euclidean(p1, p2):
    p1: tuple: 1st point
    p2: tuple: 2nd point
    Returns the Euclidean distance b/w the two points.
    distance = None
    # TODO [task1]:
    # Your function must work for all sized tuples.
    dist = [(x1-x2)**2 \text{ for } x1, x2 \text{ in } zip(p1, p2)]
    distance = sqrt(sum(dist))
    return distance
def distance manhattan(p1, p2):
    1 1 1
    p1: tuple: 1st point
    p2: tuple: 2nd point
    Returns the Manhattan distance b/w the two points.
    # k-means uses the Euclidean distance.
    # Changing the distant metric leads to variants which can be
more/less robust to outliers,
    # and have different cluster densities. Doing this however, can
sometimes lead to divergence!
```



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```
distance = None
   # TODO [task1]:
   # Your function must work for all sized tuples.
   distance = sum([abs(x1-x2) for x1, x2 in zip(p1, p2)])
   return distance
def initialization forgy(data, k):
   data: list of tuples: the list of data points
   k: int: the number of cluster means to return
   Returns a list of tuples, representing the cluster means
   1 1 1
   means = []
   means = random.sample(data,k)
   # TODO [task1]:
   # Use the Forgy algorithm to initialize k cluster means.
   assert len(means) == k
   return means
def initialization kmeansplusplus(data, distance, k):
    1 1 1
   data: list of tuples: the list of data points
   distance: callable: a function implementing the distance metric
to use
   k: int: the number of cluster means to return
   Returns a list of tuples, representing the cluster means
   1 1 1
   means = []
   # TODO [task3]:
   # Use the kmeans++ algorithm to initialize k cluster means.
   # Make sure you use the distance function given as parameter.
   # NOTE: Provide extensive comments with your code.
   # The first centroid is randomly selected
   means.append(random.sample(data, 1)[0])
   # Current minimum distance squared from any centroid
```



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```
# The probability with which to select a point will be
proportional to this
    min dist = [float('Inf')] * len(data)
    # Going over means; adding 1 new mean in each loop
    for i in range (k-1):
        # Updating minimum for all points
        for j in range(len(data)):
            # Calculate minimum distance
            d = distance(means[i], data[j])
            # Squaring the distance since the probability will be
proportional to this.
            d = d*d
            if d < min dist[j]:</pre>
                min dist[j] = d
        # Normalising min dist array to get an array of
probabilities
        s = sum(min dist)
        prob = [i/s for i in min dist]
        # Choose a random index with probabilities proportional to
min dist
        idx = np.random.choice(len(data), 1, p=prob)[0]
        # Append the chosen point to means
        means.append(data[idx])
        # Note that in the next iteration, the min dist for points
in `means` will become 0
        # So they will not be chosen again
    assert len(means) == k
    return means
def initialization randompartition(data, distance, k):
    data: list of tuples: the list of data points
    distance: callable: a function implementing the distance metric
to use
    k: int: the number of cluster means to return
    Returns a list of tuples, representing the cluster means
    1 1 1
    means = []
    means.append(random.sample(data, 1)[0])
    # TODO [task3]:
    # Use the kmeans++ algorithm to initialize k cluster means.
    # Make sure you use the distance function given as parameter.
```



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```
# NOTE: Provide extensive comments with your code.
    for i in range (k-1):
        # Updating minimum for all points
        # Choose a random index with probabilities proportional to
min dist
        idx = np.random.choice(len(data), 1)[0]
        # Append the chosen point to means
       means.append(data[idx])
    # The first centroid is randomly selected
    #means.append(random.sample(data, 1)[0])
    # Current minimum distance squared from any centroid
    # The probability with which to select a point will be
proportional to this
    #min dist = [float('Inf')] * len(data)
    #indices = np.random.choice(range(0, k), replace = True, size =
data.shape[0])
    # Going over means; adding 1 new mean in each loop
    #for i in range(k):
        means.append(data[indices == i].mean(axis=0))
    return means
def iteration one(data, means, distance):
    data: list of tuples: the list of data points
   means: list of tuples: the current cluster centers
   distance: callable: function implementing the distance metric
   Returns a list of tuples, representing the new cluster means
after 1 iteration of k-means clustering algorithm.
   new means = []
   k = len(means)
   dimension = len(data[0])
    # TODO [task1]:
    # You must find the new cluster means.
    # Perform just 1 iteration (assignment+updation)
    new means = [tuple(0 for i in range(dimension))] * k
    counts = [0.0] * k
    for point in data:
       closest = 0
       min dist = float('Inf')
       for i in range(k):
```



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```
d = distance(point, means[i])
           if d < min dist:
               min dist = d
               closest = i
       new means[closest] = tuple([sum(x) for x in
zip(new means[closest], point)])
       counts[closest] += 1
    for i in range(k):
       # import pdb; pdb.set trace()
       if counts[i] == 0:
           new means[i] = means[i]
       else:
           new means[i] = tuple(t/counts[i] for t in new means[i])
    return new means
def hasconverged(old means, new means, epsilon=1e-1):
   old means: list of tuples: The cluster means found by the
previous iteration
    new means: list of tuples: The cluster means found by the
current iteration
   Returns true iff no cluster center moved more than epsilon
distance.
    1 1 1
   converged = False
   # TODO [task1]:
    # Use Euclidean distance to measure centroid displacements.
    for i in range(len(old means)):
       p = [abs(x1-x2) > epsilon for x1, x2 in zip(old means[i],
new means[i])]
       if True in p:
           return False
   converged = True
   return converged
def iteration many(data, means, distance, maxiter, epsilon=1e-1):
   maxiter: int: Number of iterations to perform
   Uses the iteration one function.
```



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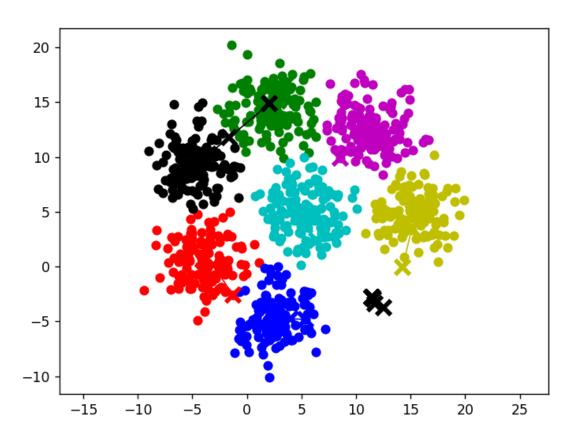
```
Performs maxiter iterations of the k-means clustering
algorithm, and saves the cluster means of all iterations.
    Stops if convergence is reached earlier.
   Returns:
    all means: list of (list of tuples): Each element of all means
is a list of the cluster means found by that iteration.
    all means = []
    all means.append(means)
    # TODO [task1]:
    # Make sure you've implemented the iteration one, hasconverged
functions.
    # Perform iterations by calling the iteration one function
multiple times.
    # Stop only if convergence is reached, or if max iterations
have been exhausted.
    # Save the results of each iteration in all_means.
    # Tip: use deepcopy() if you run into weirdness.
   means copy = deepcopy(means)
    for i in range (maxiter):
        new means = iteration one(data, means copy, distance)
        all means.append(new means)
        if hasconverged (means copy, new means, epsilon):
           break
        means copy = new means
    return all means
def performance SSE(data, means, distance):
    data: list of tuples: the list of data points
   means: list of tuples: representing the cluster means
   Returns: The Sum Squared Error of the clustering represented by
means, on the data.
   1 1 1
   sse = 0
    # TODO [task1]:
    # Calculate the Sum Squared Error of the clustering represented
by means, on the data.
```



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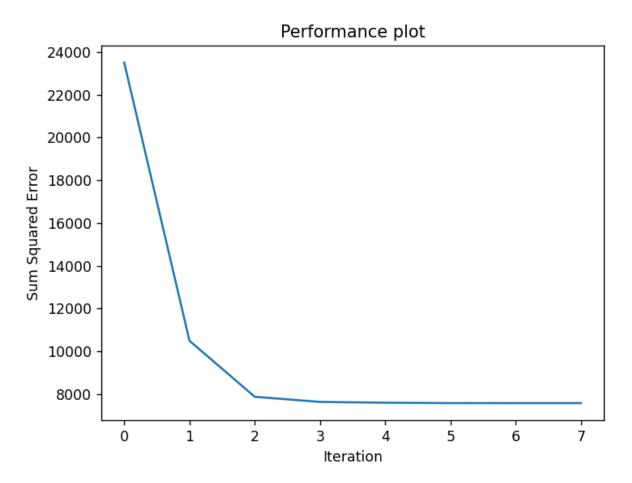
Results: Task1:





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Task2:

1. Run your code on datasets/garden.csv, with different values of k. Looking at the performance plots, does the SSE of k-means algorithm ever increase as the iterations are made? (1 mark)

Answer: In the k-means method, the SSE never rises. It can even be demonstrated that it will never rise. The first time the drop occurs is when we rename the points using the centroid that is closest to them. This indicates that the distance to the centroid closest to

Every point that has been relabelled has dropped, hence the SSE must drop overall. As the centroid of the present clusters, we now move on to step two, where we obtain new means. The SSE will again drop since we know that the sum of squared distance is the least from the mean (centroid). And the cycle continues. All of this was mathematically demonstrated in class as well.

2. Look at the files 3lines.png and mouse.png. Manually draw cluster boundaries around the 3 clusters visible in each file (no need to submit the hand drawn clusters). Test the k-means algorithm on the datasets datasets/3lines.csv and datasets/mouse.csv. How does the algorithm's clustering compare with the clustering you would do by hand? Why do you think this happens? (1 mark)

Answer: I naturally group the three lines in the dataset together to form three oblong clusters. On the other side, the algorithm provided a very different response. If the cluster centroids are in the middle of each of the three lines, separation should be easy since the perpendicular bisectors would identify the dividing zone.



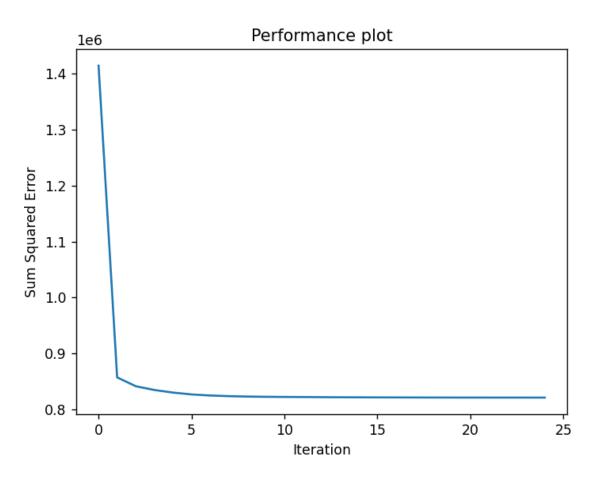
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But given that the SSE of such a scenario is higher, this is not where we are convergent in this case. Additionally, as we can see, the centroid is in close proximity in this instance, which is something we strive to avoid when using kmeans++, leading to a higher SSE. The SSE is greater because the distances between the lines' endpoints and middles are greater. Since we're measuring euclidean distances, it's best if the points are arranged in a circle around the centroids, putting the majority of the points in each cluster as close as they can be to the centroid.

I instinctively grouped the face and each ear in one cluster for the mouse dataset. Even though all three of these clusters are circular, the algorithm once more cannot match it. This time, we can see that the face extends into the ear clusters in certain places. This occurs as a result of the mouse's face's enormous circumference and the presence of the ears at the face's edge. The centroid for the face cluster would be near to the face's centre given the face's geometry. The ears are the same way. Due to the enormous radius, the spots on the face near the ears are now closer to the centroid of the ear than the centroid of the face.

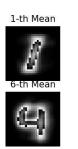
Task4





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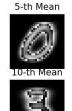
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1. For each dataset, with kmeansplusplus initialization algorithm, report "average SSE" and "average iterations". (1 mark)

Answer:

Dataset | Initialization | Average SSE | Average Iterations

100.csv	forgy 8472	2.64
100.csv	kmeans++ 8472	2.01
1000.csv	forgy 2133746	2 3.4
1000.csv	kmeans++ 19400	0000 3.25
10000.csv	forgy 1699462	236 22.1
10000.csv	kmeans++ 2078	3467 6.01

In every instance, the average SSE and the number of iterations are both less than forgy. This is as a result of our decision to use improved initializations for kmeans++. In kmeans, the initial centroids are chosen to be further apart from one another, making it more likely that every point will find at least one close-by centroid; in other words, for the majority of the points, the minimum distance from the initial centroids will be smaller than in the case of forgy. Therefore, the SSE is low right away. Faster convergence results from this. Additionally, better initializations increase the likelihood

Conclusion:

- K means may also be used to classify data from the MNIST dataset. However, we discovered that it was not very accurate and frequently misclassified photos.
- When there are clusters with different densities and sizes, k-means has problems clustering the data. You must generalise k-means in order to cluster such data.
- Before applying k means, data normalization is a crucial preprocessing step that makes sure
- Outliers may drag centroids or they may form their own cluster in place of being ignored. K
 means are therefore not resistant to outliers.