

1. Blasius similarity equation is written as

$$\frac{d^3 f}{d\eta^3} + \frac{f}{2} \frac{df^2}{d\eta^2} = 0, \text{ with } f(0) = 0, f'(0) = 0, f'(\infty) = 1$$

Transformation into first order ODEs

$$\begin{aligned}\frac{df}{d\eta} &= g \\ \frac{dg}{d\eta} &= h \\ \frac{dh}{d\eta} + \frac{1}{2} f \cdot h &= 0\end{aligned}$$

After, discretizing on forward difference method,

$$\begin{aligned}f(i+1) &= f(i) + \Delta\eta \, g(i) \\ g(i+1) &= f(i) + \Delta\eta \, h(i) \\ h(i+1) &= h(i) - \frac{1}{2} \Delta\eta \, f(i) \cdot h(i)\end{aligned}$$

% Matlab coding for Blasius similarity equation and similarity energy equation

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clc;
clear all;

% Blasius similarity equation: f''' + (1/2)*f*f''=0 with f(0) = 0, f'(0) = 0, f'(\infty) = 1
% Transforming Blasius Equation into a system of first-order ODEs:
%      df/d(eta)= g
%      dg/d(eta)= h
%      dh/d(eta)+(1/2)*f*h = 0

% f=y1
% g=y2
% h=y3
% d(eta)=dn

%% Parameters of Blasius Equation
U_inf = 1;           %free stream velocity
L = 10;              %length of flat plate
mu = 1.789E-5;       %viscosity of air
rho = 1.225;          %density of air
nu = mu/rho;         %kinematic viscosity
A = sqrt(nu/U_inf);
% total number of nodes
N=1000;
% initial conditions
dn = 0.01;
y1(1) = 0;
y2(1) = 0;
y3(1) = 1;           % 1st Guess

% discretizing on forward difference method
for i = 1:N
    y3(i+1) = y3(i) - (1/2)*y1(i)*y3(i)*dn;
    y2(i+1) = y3(i)*dn + y2(i);
    y1(i+1) = y2(i)*dn + y1(i);
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end
    y2_end=y2(N);

y2_new(1) = 0;
y3_new(1) = 1.1; % 2nd Guess

for i = 1:N
    y3_new(i+1) = y3_new(i) - (1/2)*y1(i)*y3_new(i)*dn ;
    y2_new(i+1) = y2_new(i) + y3_new(i)*dn;
    y1(i+1) = y1(i) + y2_new(i)*dn ;
end
    y2_newend=y2_new(N);

while A > 1e-9 %error
    % Using 'Newton Raphson' Method
    y = y3_new(1) - (y2_newend-1)*(y3_new(1)-y3(1))/(y2_newend-y2_end);
    y3(1) = y3_new(1);
    y3_new(1) = y;
    y2_end=y2_newend;

    for i = 1:(N)
        y3_new(i+1) = y3_new(i) - ((1)/2)*y1(i)*y3_new(i)*dn;
        y2_new(i+1) = y3_new(i)*dn + y2_new(i);
        y1(i+1) = y2_new(i)*dn + y1(i);
    end

    y2_newend=y2_new(N);
    A = abs(y2_newend-1); %error estimation
end
eta = 0:dn:N*dn;

% Result
eta=[eta]';
f=[y1]';
g=[y2]';
h=[y3]';
finalsolution = table(eta, f, g, h)

% Energy equation: theta'' + (f/2)*pr*theta'=0 with theta(0)=1, theta(inf)=0
% Transforming into a system of first-order ODEs:
%      d(theta)/d(eta)= x
%      dx/d(eta)= -(1/2)*pr*f*x

pr = 100; %Prandtl number

% Initial condition
th1(1)=1;

x1(1)=1; %1st guess for energy equation
r= 0.1;
% discretizing on forward difference method
for i=1:N
    x1(i+1) = x1(i)-(1/2)*pr*y1(i)*x1(i)*dn;
    th1(i+1) = th1(i)+x1(i)*dn;
end

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th1_end = th1(N);

th2(1)=1;
x1_new(1)=1.1; %2nd guess for energy equation

for i=1:N
    x1_new(i+1) = x1_new(i)-(1/2)*pr*y1(i)*x1_new(i)*dn;
    th2(i+1) = th2(i)+x1_new(i)*dn;
end
th2_end = th2(N);

while r>1e-9 %error
    % using 'Newton-Raphson' Method
    x = x1_new(1)-(th2_end*(x1_new(1)-x1(1)))/(th2_end-th1_end);
    x1(1)=x1_new(1);
    x1_new(1)=x;th1_end = th2_end;

    for i=1:N
        x1_new(i+1) = x1_new(i)-(1/2)*pr*y1(i)*x1_new(i)*dn;
        th2(i+1) = th2(i)+x1_new(i)*dn;
    end

    th2_end = th2(N);
    r = abs(th2_end); % error estimation
end

% output

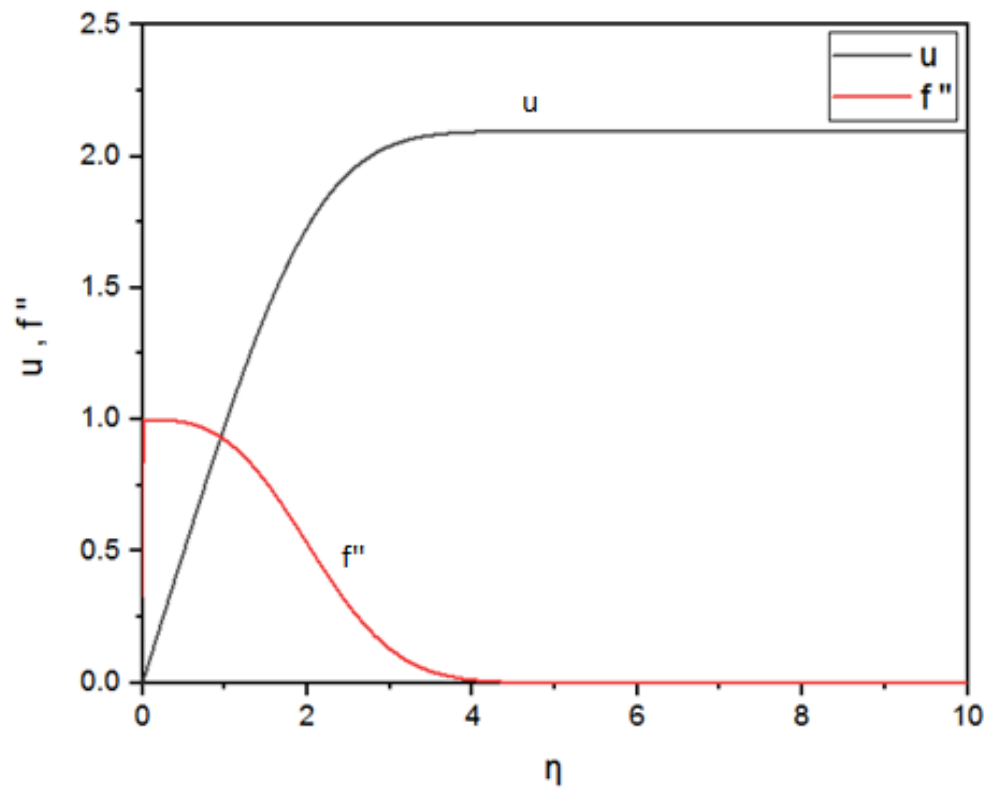
figure(1);
plot (eta,y2_new,'r','LineWidth',2)
hold on
plot (eta,y3_new,'k','LineWidth',2)
legend('f^{(1)}','f^{(2)}')
legend boxoff;
xlabel('\eta','FontSize',15);
ylabel('\it{ f^{(1)}, f^{(2)}}','FontSize',15);

figure(2);
eta = 0:dn:N*dn;
plot (eta,th2,'b','LineWidth',2);
legend('Pr=100')
legend boxoff;
xlabel('\eta','FontSize',15);
ylabel('\theta','FontSize',15);

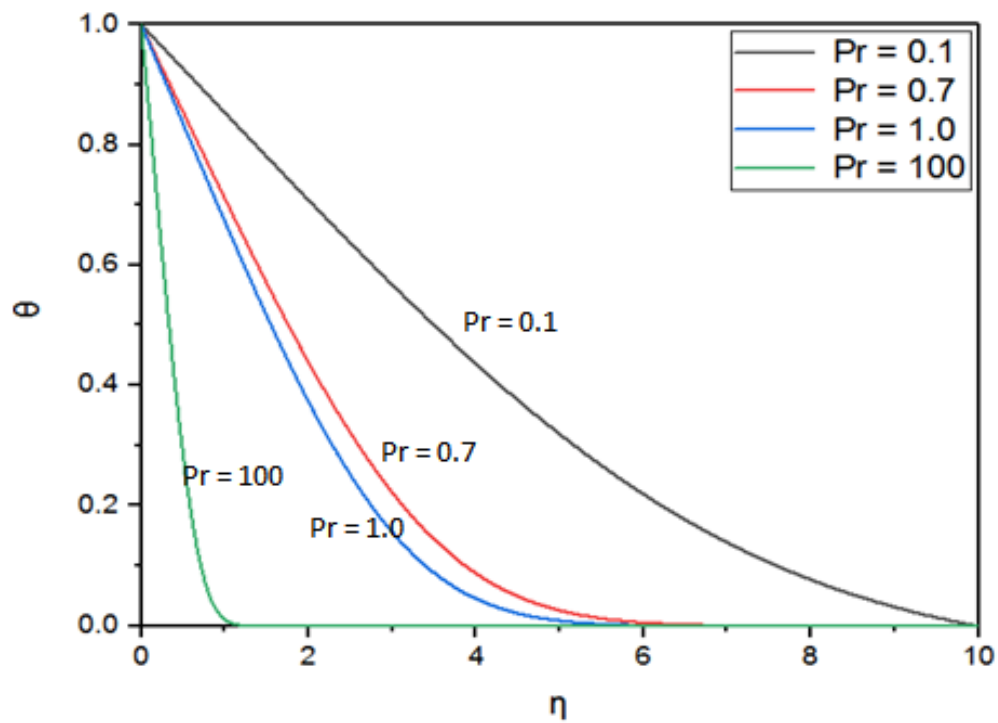
%end

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Plot: u vs η and f'' vs η



Plot: θ vs η



Result:

S. No	Pr	$\theta'(0)$
1	0.1	-0.146
2	0.7	-0.292
3	1	-0.330
4	100	-1.55

2. %Matlab coding for Nusselt Number

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clc;
clear all;

N= 2000;           %total nodes
Nu = 0.5;          %initial guess for Nu
dr = 0.001;

%Initial condition
th(1) = 0;
r(1) = 0;

err= 0.1;

while err>1e-9      %error

    Nu = Nu + 0.01;
    f(1) = Nu/2;

    %discretization on backward difference method

    for i = 2:N
        r(i) = r(i-1) + dr;
        f(i) = f(i-1) + dr*( f(i-1)/(1-r(i-1)) - (2*Nu*(1-(1-r(i-1))^2)*th(i-1)));
        th(i) = f(i-1)*dr + th(i-1);
    end

    err = f(N);      % error calculation

end

display(Nu)

% end

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Result:

Nu = 3.6700