



BUSINESS PROCESS MANAGEMENT - EXERCISE

GENERIC MODEL QUERY LANGUAGE (GMQL)

GMQL - BASIC IDEA



- Recognize any model as two basic sets
 - Set V of model vertices
 - Set E of model edges
- Provide set-altering functions and operators that perform operations on these basic sets
- Nest functions and operators to assemble a query

PARAMETERS



- X = any set of elements (e.g., Z, V, E)
 - $Y_V =$ any set of vertices (e.g., V)
 - \bullet Y_F = any set of edges (e.g., E)
- t = a particular element type (e.g., event, f_e)
 - t_v = a particular vertex type (e.g., event, function)
 - t_E = a particular edge type (e.g., f_e, x_e)
- u = a particular value or data type (e.g., "*invoice*")
- \mathbf{n}_{x} = a natural number (e.g., 1, 2)



- Element characteristics
- Elements and their relationships
- Adjacent elements
- Element paths/loops

IVVI

ELEMENT CHARACTERISTICS

- ElementsOfType(X,t)
- ElementsWithAttributeOfValue(X,t_v,u)
- ElementsWithAttributeOfDataType(X,u)
- → return a simple set

Example: $\{v_1, v_2, v_3\}$

IVVI

ELEMENTS AND THEIR RELATIONSHIPS

- ElementsWithRelations(X,Y_E)
 - ElementsWithSuccRelations(X,Y_F)
 - ElementsWithPredRelations(X,Y_E)
- ElementsWithRelationsOfType(X,Y_E,t_E)
 - ElementsWithSuccRelationsOfType(X,Y_E,t_E)
 - ElementsWithPredRelationsOfType(X,Y_E,t_E)
- > return a set of sets

Example: $\{\{v_1,e_1\},\{v_2,e_2,e_3\}\}$



ELEMENTS AND THEIR RELATIONSHIPS

- ElementsWithNumberOfRelations(X,n,)
 - ElementsWithNumberOfSuccRelations(X,n_x)
 - ElementsWithNumberOfPredRelations(X,nx)
- ElementsWithNumberOfRelationsOfType(X,t_F,n_x)
 - ElementsWithNumberOfSuccRelationsOfType(X,t_F,n_x)
 - ElementsWithNumberOfPredRelationsOfType(X,t_F,n_x)
- → return a set of sets

Example: $\{\{v_1,e_1\},\{v_2,e_2,e_3\}\}$



ADJACENT ELEMENTS

• ElementsDirectlyRelated(X₁,X₂)

undirected edges

AdjacentSuccessors(X₁,X₂)

directed edges

→ return a set of sets

Example: $\{\{v_1, v_2, e_1\}, \{v_2, v_3, e_2\}\}$

IWVI

ELEMENT PATHS

- Paths (X_1, X_n)
 - PathsContainingElements(X₁,X_n,X_c)
 - PathsNotContainingElements(X₁,X_n,X_c)

undirected edges

- DirectedPaths(X₁,X_n)
 - DirectedPathsContainingElements(X₁,X_n,X_c)
 - DirectedPathsNotContainingElements(X₁, X_n, X_c)

directed edges

→ return a set of sets

ELEMENT LOOPS



- Loops(X)
 - LoopsContainingElements(X₁,X_c)
 - LoopsNotContainingElements(X₁,X_c)

undirected edges

- DirectedLoops(X)
 - DirectedLoopsContainingElements(X₁,X_c)
 - DirectedLoopsNotContainingElements(X₁,X_c)

directed edges

→ return a set of sets

GMQL OPERATORS



- Most operators take exactly two parameters
 - two simple sets or two sets of sets
 - (UNION, INTERSECTION, COMPLEMENT)
 - two sets of sets or one set of sets and one simple set
 - (INNERINTERSECTION, INNERCOMPLEMENT)
 - two sets of sets
 - (JOIN)
- Operators that turn sets of sets into simple sets only take one parameter
 - one set of sets
 - (SELFUNION, SELFINTERSECTION)

COMMON ERRORS - OPERATOR NESTING



• If you want to apply operators to more than two sets, you have to nest them

Example: the set of all connectors

```
UNION(

UNION(

EOT(V, XOR),

EOT(V, OR)),

EOT(V, AND))
```

DON'T DO THIS:

```
UNION(

EOT(V, XOR),

EOT(V, OR),

EOT(V, AND))
```

VARIABLES



- In order to keep your GMQL functions clear, you can make use of variables
- Idea: Define sets or sets of sets that you can then use in your actual functions

Example: All connectors with exactly one predecessor

C = UNION(UNION(EOT(V, XOR),EOT(V, OR)),EOT(V, AND))

EWNOPR(C,1)

SPLIT-JOIN-CONNECTORS



Connectors that have more than one predecessor and more than one successor

COMPLEMENT

- UNION of all connectors (nested, see previous slides)
- UNION of all connectors (nested)
 - with 0 predecessors
 - with 0 successors
 - with exactly 1 predecessor
 - with exactly 1 successor

COMMON ERRORS - OPERATORS

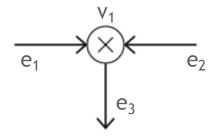


Think about what your sets/subsets look like, before applying operators

Example: the set of all connectors with exactly two incoming and one outgoing edge

C2 = EWNOPR(
$$\mathbb{C}$$
,2) $\rightarrow \{\{v_1,e_1,e_2\}\}$

C1 = EWNOSR(
$$\mathbb{C}$$
,1) $\rightarrow \{\{v_1,e_3\}\}$



C has to be defined beforehand!

GMQL VS. CTL



 Examples of GMQL functions that can be expressed by equivalent CTL formulas

GMQL	CTL
Adjacent Successors(X ₁ ,X ₂)	$M, x_1 \mid = EX x_2$
Paths(EWAOV(V,label,"o_boss"), EWAOV(V,label,"n_grant_credit"))	M, $x_0 \mid = EF(n_grant_credit \land o_boss)$

• CTL is not able to count elements (e.g., EWNOR) or detect loops

For further reference: Riehle, D. (2018). Checking Business Process Models for Compliance-Comparing Graph Matching and Temporal Logic. In *International Conference on Business Process Management* (pp. 403-415). Springer, Cham.





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