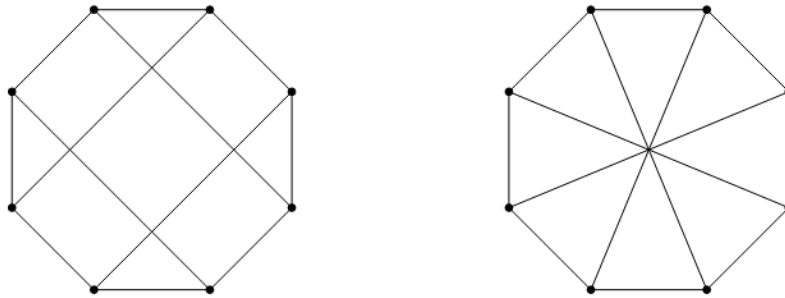


### Extra Exercises 1

1. Provide the following definitions for a graph  $G = (V, E)$ :
  - (a) Two nodes  $u, v \in G$  are adjacent if ...
  - (b) The neighbourhood  $N(v)$  of a node  $v \in G$  is defined by ...
  - (c) Two edges  $e_1, e_2 \in E$  are called parallel if ...
  - (d) A simple graph is ....
  - (e) A graph invariant is ...
2. Show that being bipartite is a graph invariant. (Let  $G$  and  $H$  be isomorphic graphs, and suppose  $G$  is bipartite. Then show that  $H$  is also bipartite.)
3. Use the previous problem to show that the following graphs are not isomorphic:



4. Provide two obvious indicators that two graphs  $G, H$  are not isomorph.
5. Draw the following graphs:
  - (a)  $2K_4$
  - (b)  $K_{1,5}$
  - (c)  $K_{4,4}$
  - (d)  $P_5$
  - (e)  $C_7$
  - (f)  $K_6$