

# AI1110 - Probability and Random Variables

## Assignment 7

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May 21, 2022

## Question 6

From a lot of 30 bulbs which include 6 defectives, a sample of 4 bulbs is drawn at random with replacement. Find the probability distribution of the number of defective bulbs.

# Solution

Let us define **success** as **Ball drawn is not defective**

Then probability of success is  $p = \frac{6}{30} = \frac{4}{5}$

and probability of failure is  $q = \frac{1}{5}$

Let the random variable  $X \in \{0, 1, 2, 3, 4\}$  denote the number of defective bulbs

This is Bernauli trial. The probability of  $i \in \{0, 1, 2, 3, 4\}$  balls being defective is given by

$$\Pr(X = i) = \binom{4}{i} p^i q^{4-i} \quad (1)$$

Therefore, the probability distribution is

No. of defective balls	Probability
0	$\binom{4}{0} \times \left(\frac{4}{5}\right)^4 = \frac{256}{625}$
1	$\binom{4}{1} \times \frac{1}{5} \times \left(\frac{4}{5}\right)^3 = \frac{256}{625}$
2	$\binom{4}{2} \times \left(\frac{1}{5}\right)^2 \times \left(\frac{4}{5}\right)^2 = \frac{96}{625}$
3	$\binom{4}{3} \times \left(\frac{1}{5}\right)^3 \times \left(\frac{4}{5}\right)^1 = \frac{16}{625}$
4	$\binom{4}{4} \times \left(\frac{1}{5}\right)^4 \times \left(\frac{4}{5}\right)^0 = \frac{1}{625}$