

AI1110 Assignment 1

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ICSE class 10 paper 2019 Q11 (b)

The product of two consecutive natural numbers which are multiples of 3 is equal to 810. Find the two numbers.

Solution:

Let the two consecutive natural numbers which are multiples of 3 be $3n$ and $3n + 3 \quad \exists n \in \mathbb{N}$

According to the question:

$$\begin{aligned} & 3n(3n + 3) = 810 & (1) \\ \Rightarrow & 9n(n + 1) = 810 & (2) \\ \Rightarrow & n(n + 1) = 90 & (3) \\ \Rightarrow & n^2 + n - 90 = 0 & (4) \\ \Rightarrow & (n + 10)(n - 9) = 0 & (5) \\ \Rightarrow & n = -10 \quad \text{or} \quad n = 9 & (6) \end{aligned}$$

discarding $n = -10$ as $n \in \mathbb{N}$

$$\begin{aligned} \Rightarrow & n = 9 & (7) \\ \Rightarrow & 3n = 27 & (8) \\ \Rightarrow & 3n + 3 = 30 & (9) \end{aligned}$$

The two numbers are: 27, 30

Plot of Equation 4 is:

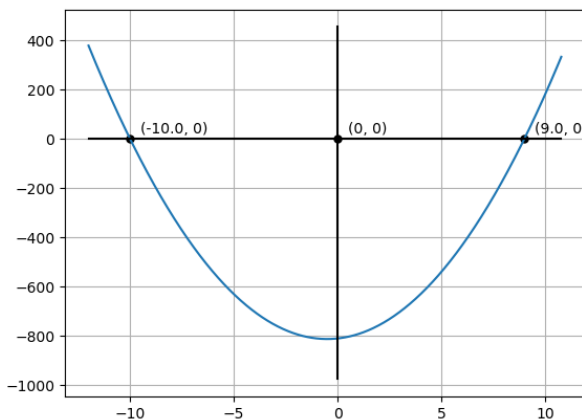


Fig. 1. Plot showing the polynomial in Equation 4

It can be easily verified by observing the plot in Figure 1 that the roots of Equation 4 are 9 and -10.

The output of the program used to find and verify these numbers is:

```
$ python find_nums.py
The consecutive natural numbers n1 and n2 s.t.
n1 % 3 == 0 and n2 % 3 == 0 and n1*n2 == 810 are:
n1=27 n2=30
```

Fig. 2. Output of the python program