

AI1110 Assignment 1

Abhinav Yadav, cs21btech11002

March 28, 2022

Q11 (b)

The product of two consecutive natural numbers which are multiples of 3 is equal to 810. Find the two numbers.

Solution

Let the two consecutive natural numbers which are multiples of 3 be $3n$ and $3n + 3 \quad \exists n \in \mathbb{N}$

According to the question:

$$\begin{aligned} 3n(3n + 3) &= 810 \\ \Rightarrow 9n(n + 1) &= 810 \\ \Rightarrow n(n + 1) &= 90 \\ \Rightarrow n^2 + n - 90 &= 0 \\ \Rightarrow (n + 10)(n - 9) &= 0 \\ \Rightarrow n = -10 \quad \text{or} \quad n = 9 \end{aligned}$$

discarding $n = -10$ as $n \in \mathbb{N}$

$$\begin{aligned} \Rightarrow n &= 9 \\ \Rightarrow 3n &= 27 \\ \Rightarrow 3n + 3 &= 30 \end{aligned}$$

The two numbers are:

$$\boxed{27, 30}$$