AI1110 Assignment 1

Abhinav Yadav, cs21btech11002

March 29, 2022

Q11 (b)

The product of two consecutive natural numbers which are multiples of 3 is equal to 810. Find the two numbers.

Solution

Let the two consecutive natural numbers which are multiples of 3 be $3n$ and $3n + 3 \quad \exists\, n \in \mathbb{N}$

According to the question:

$$3n(3n + 3) = 810$$
$$\Rightarrow 9n(n + 1) = 810$$
$$\Rightarrow n(n + 1) = 90$$
$$\Rightarrow n^2 + n - 90 = 0 \qquad - (1)$$
$$\Rightarrow (n + 10)(n - 9) = 0$$
$$\Rightarrow n = -10 \quad or \quad n = 9$$

discarding $n = -10$ as $n \in \mathbb{N}$

$$\Rightarrow n = 9$$
$$\Rightarrow 3n = 27$$
$$\Rightarrow 3n + 3 = 30$$

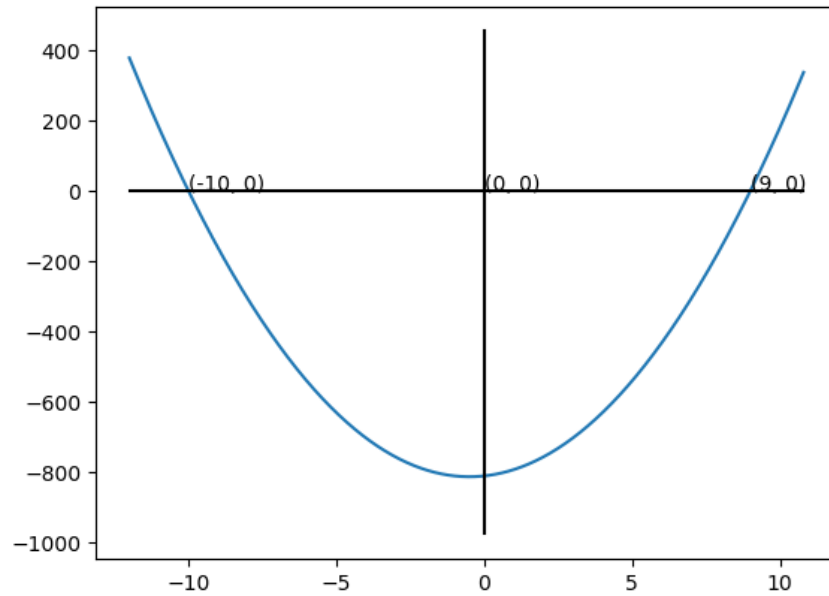The two numbers are:
$\boxed{27, 30}$

Figure 1: Plot showing the polynomial in $eq^n(1)$

It can be easily verified by observing the plot that the roots of $eq^n(1)$ are 9 and -10.

The output of the program used to find and verify these numbers is:

```
└$ python find_nums.py
The consecutive natural numbers n1 and n2 s.t.
n1 % 3 == 0   and   n2 % 3 == 0 and n1*n2 == 810 are:
n1=27    n2=30
```

Figure 2: Output of the python program