

Practical no.1Basic of R-software

- (1) R is a software of data analysis and statistical computing.
- (2) It is a software by which, effective data handling and outcome storage is possible.
- (3) It is capable of graphical display
- (4) It is a free software.

Q1 
$$\begin{aligned} & 2^2 + 1 \cdot 5 + 4 \times 5 + 6 / 5 \\ & > 2^2 + \text{abs}(-5) + 4 * 5 + 6 / 5 \\ & [1] 30.2 \end{aligned}$$

Q2 
$$\begin{aligned} x &= 20 \\ y &= 2x \\ z &= x + y \\ \text{sqrt}(z) & \\ > x &= 20 \\ > y &= 2x \\ > z &= x + y \\ > \text{sqrt}(7) & \\ [1] & 4.746967 \end{aligned}$$

Q3 
$$\begin{aligned} x &= 10 \\ y &= 15 \\ z &= 5 \\ \text{(a)} & x + y + z \\ \text{(b)} & xyz \\ \text{(c)} & \sqrt{xyz} \\ \text{(d)} & \text{round } \sqrt{xyz} \end{aligned}$$

63:

>  $x = 10$

>  $y = 15$

>  $z = 5$

>  $x + y + z$

[1] 30

>  $x + y + z$

[1] 760

>  $8x + (y * z)$

[1] (27.38613)

A vector in R software is denoted by the syntax  
 $c(2,3,5,7)^{12}$

>  $x = c(2,3,5,7)$

>  $x^{12}$

[1] 4 9 25 49

$c(2,3,5,7)^{12}(2,3)$

4 27 25 343

$c(2,3,5,7)^{12}(2,3)$

warning message

$c(1,2,3,4,5,6)^{12}(2,3,4)$

[1] 1 8 9 64 25 216

$c(4,6,8,10) * 3$

12 18 24 30

$C(4,6,8,10) * C(-1,-2,-3,-4)$

[1] -4 -12 -24 -40

$C(2,3,5,7) * C(2,-3)$

[1] 0.2500000 0.37037037 0.40

$C(2,3,5,7) + 10$

12 13 15 17

$(C(2,3,5,7) + C(-2,-3,-1,0))$

$C(2,3,5,7) / 2$

[1] 1.0 1.5 2.5 3.5

Find the sum of product maximum and minimum for values of

$x = C(2,8,4,9,11,10,7,6)^{1/2}$

> sum(x)

[1] 455

> (x)

[1] 4425994784

> max(x)

[1] 121

> min(x)

[1] 4

24

AS

4 matrix (nrow=4, data=c(1,2,3,4,5,6,7,8))

> x  
[1] [1] [2]  
[1] 1 5  
[2] 2 6  
[3] 3 7  
[4] 4 8

$$\rightarrow \begin{bmatrix} 4 & 7 & 4 \\ 5 & 8 & 0 \\ 6 & 9 & 2 \end{bmatrix} + \begin{bmatrix} 6 & 11 & 9 \\ 4 & 8 & 7 \\ 5 & 12 & 4 \end{bmatrix}$$

x ← matrix(nrow=3, ncol=3, data=c(4,5,6,7,8,9,4,0,2)  
y ← matrix(nrow=3, ncol=3, data=c(6,4,5,11,12,8,7,4))

> x  
[1] [1] [2] [3]  
[1] 4 7 4  
[2] 5 8 0  
[3] 6 9 2

> y  
[1] [1] [2] [3]  
[1] 6 11 9  
[2] 4 12 2  
[3] 5 8 4

$x^*z$

	[1]	[2]	[3]
[1]	8	14	8
[2]	10	16	0
[3]	12	18	4

$y^*z$

	[1]	[2]	[3]
[1]	12	22	18
[2]	8	24	14
[3]	10	16	8

	[1]	[2]	[3]
[1]	10	18	13
[2]	9	20	7
[3]	11	17	6

$x^*y$

	[1]	[2]	[3]
[1]	24	77	36
[2]	20	96	0
[3]	30	92	8

Ans

## Binomial distribution

$n$  = total no. of trials

$P$  =  $P(\text{Success})$

$Q = P(\text{Failure})$

$x$  = no. of success out of  $n$

$$P(x) = {}^n C_x \cdot p^x \cdot q^{n-x}; x = 0, 1, \dots, n$$

$$f(x) = np$$

$$V(x) = npq$$

$$\text{dbinom}(x, n, p) \quad P(x)$$

$$n \neq p \quad E(x)$$

$$n \neq p \neq q \quad V(x)$$

$$P_{\text{binom}}(x, n, p) \quad P(r \leq x), \quad P(x > r) = 1 - P_{\text{binom}}(r | n, p)$$

Q.1) Toss a coin 10 times with probability (Head = 0.6)  
let  $x$  be the no. of heads

find the probability of :-

i) 7 Heads

ii) 4 Heads

iii) Atmost 4 Heads

iv) Atleast 6 Heads

v) No Heads

vi) All Heads

vii) expectation and variance.

```

> n = 10
> p = 0.6
> q = 0.4
> dbinom(4, 10, 0.6)
[1] 0.2149908
> dbinom(4, 10, 0.6)
[1] 0.114767
> pbisom(4, 10, 0.6)
[1] 0.1662386
> 1 - pbisom(6, 10, 0.6)
[1] 0.3822806
> dbisom(0, 10, 0.6)
[1] 0.0000048567
> dbisom(10, 10, 0.6)
[1] 0.006066618
> exp = 10 * 0.6
> exp
[1] 6
> var = 10 * 0.6 * 0.4
> var
[1] 2.4

```

Q.2 There are 12 MCQ in an English question paper and each question has 5 answers and only 2 of them is correct. Find the probability of having

- ① 4 correct answer
- ② atmost 4 correct answer
- ③ atleast 3 correct answer

$$n=12, p=1/4$$

(i)  $P(x=4)$

$$> \text{dbinom}(4, 12, 1/4)$$

[i] 0.1328456

(ii)  $P(x \leq 4)$

$$> \text{pbinom}(4, 12, 1/4)$$

[ii] 0.70929445

iii)  $P(x \geq 3) = P(x > 2)$

$$> 1 - \text{pbinom}(2, 12, 1/4)$$

[iii] 0.4416543

Q.3 Find complete binomial distribution where  $n=0.5$ ,  $p=0.1$

$$> \text{dbinom}(0.5, 0.1)$$

[i] 0.59049

$$> \text{dbinom}(1, 5, 0.1)$$

[ii] 0.32805

$$> \text{dbinom}(2, 5, 0.1)$$

[iii] 0.0729

$$> \text{dbinom}(3, 5, 0.1)$$

[iv] 0.0081

$$> \text{dbinom}(4, 5, 0.1)$$

[v] 0.0045

$$\text{dbinom}(5, 5, 0.1)$$

[vi] 1e-05

Q4 Find probability of exactly 10 success outcome 100 trials with  $p=0.1$

$\rightarrow \text{dbinom}(10, 100, 0.1)$

[1] 0.1318653

5)  $x$  follows binomial distribution with  $n=12$ ,  $p=0.25$   
find i)  $P(x \leq 5)$  ii)  $P(x > 7)$  iii)  $P(5 < x < 7)$

i)  $P(x \leq 5)$

$\rightarrow \text{pbinom}(5, 12, 0.25)$

[1] 0.9455978

(ii)  $1 - \text{pbinom}(7, 12, 0.25)$

[1] 0.00298151

(iii)  $P(5 < x < 7)$

[1] 0.04014945

Q6 There are 10 numbers in a committee prob. off any number attending a meeting 0.9 works probability that 7 or more members will present in meeting

$n=10, x=7, p=0.9$

$\rightarrow 1 - \text{pbinom}(6, 10, 0.9)$

[1] 0.9872048

Q.7 A salesman has 20% probability of making a sell on a typical day he will meet 50 customers what minimum no. of sell we will make with 88% probability

$$\Rightarrow n=50 \quad p=0.88$$

$$> qbinom(p, n, p)$$

$$> qbinom(0.88, 50, 0.2)$$

[ ] q

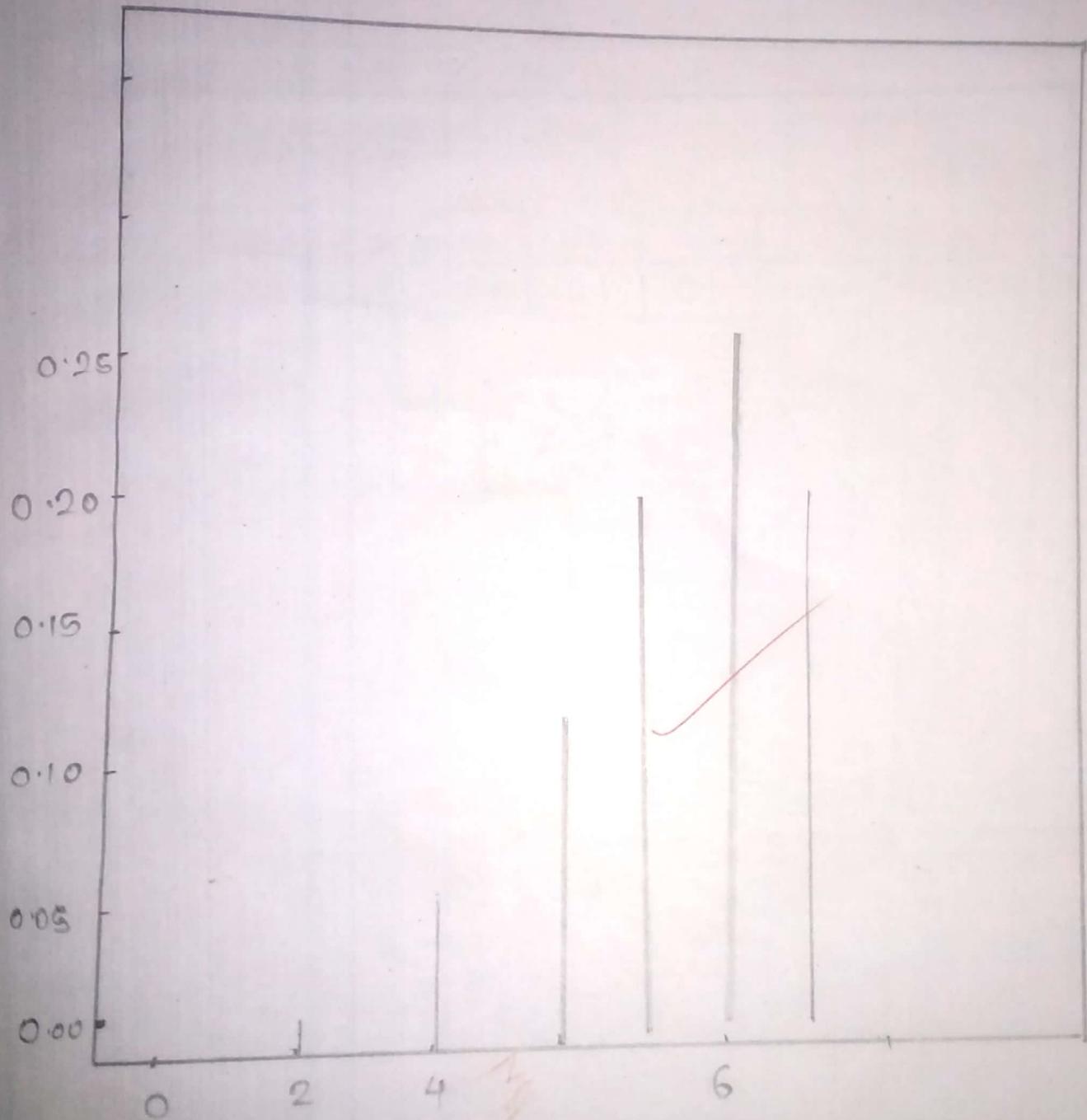
Q.8  $n=10$ ,  $p=0.6$  find the binomial distribution plot the graph of p.m.f & c.d.f

> n=10 ; p=0.6  
 > x=0:n  
 > bp=dbinom(x,n,p)  
 > d=data.frame("x-values": x, "probability": bp)  
 > print(d)

x	values	probability
1	0	0.0001048576
2	1	0.0015728640
3	2	0.0106168320
4	3	0.0424673280
5	4	0.11147673280
6	5	0.2006581248
7	6	0.2908926560
8	7	0.2149908480
9	8	0.121490840
10	9	0.04323520
11	10	0.00607120

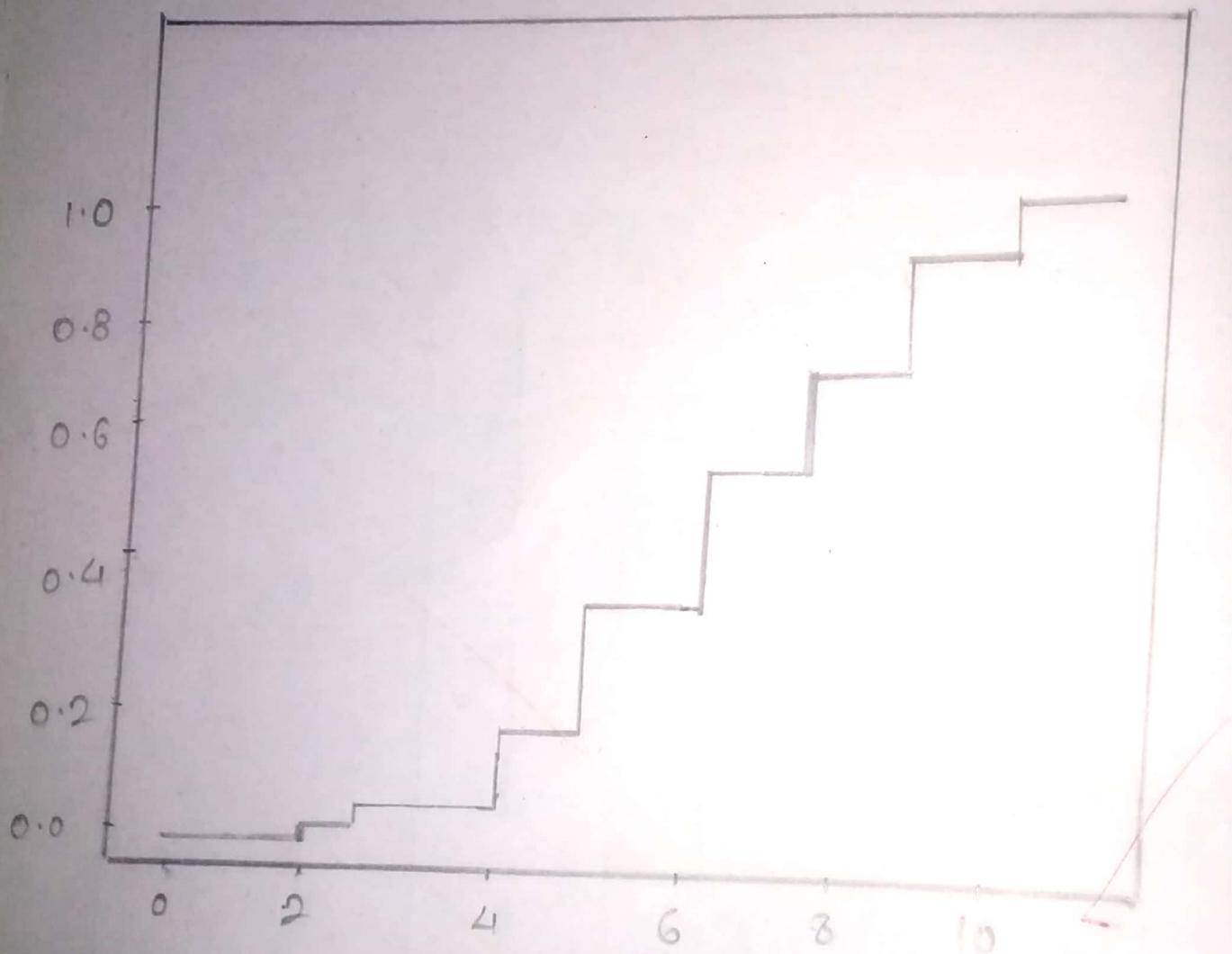
$\Rightarrow \text{plot}(x, \text{bp}, "h")$

28



BS

```
> CP = pbinom(x, n, p)  
> plot(x, CP, "s")
```



✓

### Practical no.3

- 29

▷ check the followings are p.m.f (probability mass function) or not.

(I)	$x$	1	2	3	4	5
	$P(x)$	0.2	0.5	-0.5	0.4	0.4

(II)	$x$	10	20	30	40	50
	$P(x)$	0.3	0.2	0.3	0.1	0.1

(III)	$x$	0	1	2	3	4
	$P(x)$	0.4	0.2	0.3	0.2	0.1

Solution:-

$$(I) 0 \leq P(x) \leq 1$$

$$(II) \sum P(x) = 1$$

(I) since , it not satisfy the first condition.

∴ Soln:-

since all values of  $P(x)$  are more than zero and less than one, 1st condition is satisfied.

Also,

$$\begin{aligned} E(x) &= P(10) + P(20) + P(30) + P(40) + P(50) \\ &= 0.3 + 0.2 + 0.3, 0.1, 0.1 \\ &= 1 \end{aligned}$$

∴ 2nd condition is also satisfied .

→ Hence, it is a p.m.f

> prob = c(0.3, 0.2, 0.3, 0.1, 0.1)

> prob

[1] 0.3 0.2 0.3 0.1 0.1

> sum(prob)

> [1] 1

(iii) since, all the values of  $p(x)$  is between 0 to 1  
therefore condition 1 is satisfied.

But,

$$\begin{aligned}\sum p(x) &= p(0) + p(1) + p(2) + p(3) + p(4) \\ &= 0.4 + 0.2 + 0.3 + 0.2 + 0.1 \\ &= 1.2\end{aligned}$$

It is more than 1

It does not satisfy condition 2

It is not a ~~prob~~ p.m.f.

> prob = c(0.4, 0.2, 0.3, 0.2, 0.1)

> sum(prob)

[1] 1.2

$$\text{Mean} = E(x) = \sum x P(x) = 3.45$$

$$\begin{aligned}\text{Var} &= V(x) = \sum x^2 P(x) - [E(x)]^2 \\ &= 13.55 - (3.45)^2 \\ &= 1.6475\end{aligned}$$

Code:

```
> x = c(1, 2, 3, 4, 5)
> px = c(0.1, 0.15, 0.2, 0.3, 0.25)
> a = x * px
> sum(a)
[1] 3.45
> mean = sum(a)
> mean
[1] 3.45
> b = x * a
> sum(b)
[1] 13.55
> var = sum(b) - mean^2
> var
[1] 1.6475
```

Q2 Following is a p.m.f of  $x$

$x$	1	2	3	4	5
$p(x)$	0.1	0.15	0.2	0.3	0.25

find mean and variance of  $x$

$x$	$p(x)$	$x p(x)$	$x^2 p(x)$
1	0.1	0.1	0.1
2	0.15	0.3	0.6
3	0.2	0.6	1.8
4	0.3	1.2	4.8
5	0.25	1.25	6.25
		3.45	13.55

Q3 Find mean and variance of  $x$

$x$	5	10	15	20	25
$p(x)$	0.1	0.3	0.2	0.25	0.15

Q4 Find c.d.f of the following p.m.f and draw the graph of c.d.f

$x$	1	2	3	4
$p(x)$	0.4	0.3	0.2	0.1

$> x = c(5, 10, 15, 20, 25)$   
 $> prob = c(0.1, 0.3, 0.2, 0.25, 0.15)$   
 $> a = x * prob$   
 $> sum(a)$

[1] 15.25

$> b = x * a$   
 $> sum(b)$

[1] 271.25

$> var = sum(b) - (sum(a)^2)$

$> Var$

$\Rightarrow 38.6875$

Q4 Find C.D.F of the following p.m.f and draw the graph of C.D.F

$x$	1	2	3	4
$P(x)$	0.4	0.3	0.2	0.1

$> x = c(1, 2, 3, 4)$

$> probx = c(0.4, 0.3, 0.2, 0.1)$

$> a = cumsum(prob x)$

$> a$

[1] 0.4 0.7 0.9 1.0  
 $P(x) = 0 \quad x \leq 1$

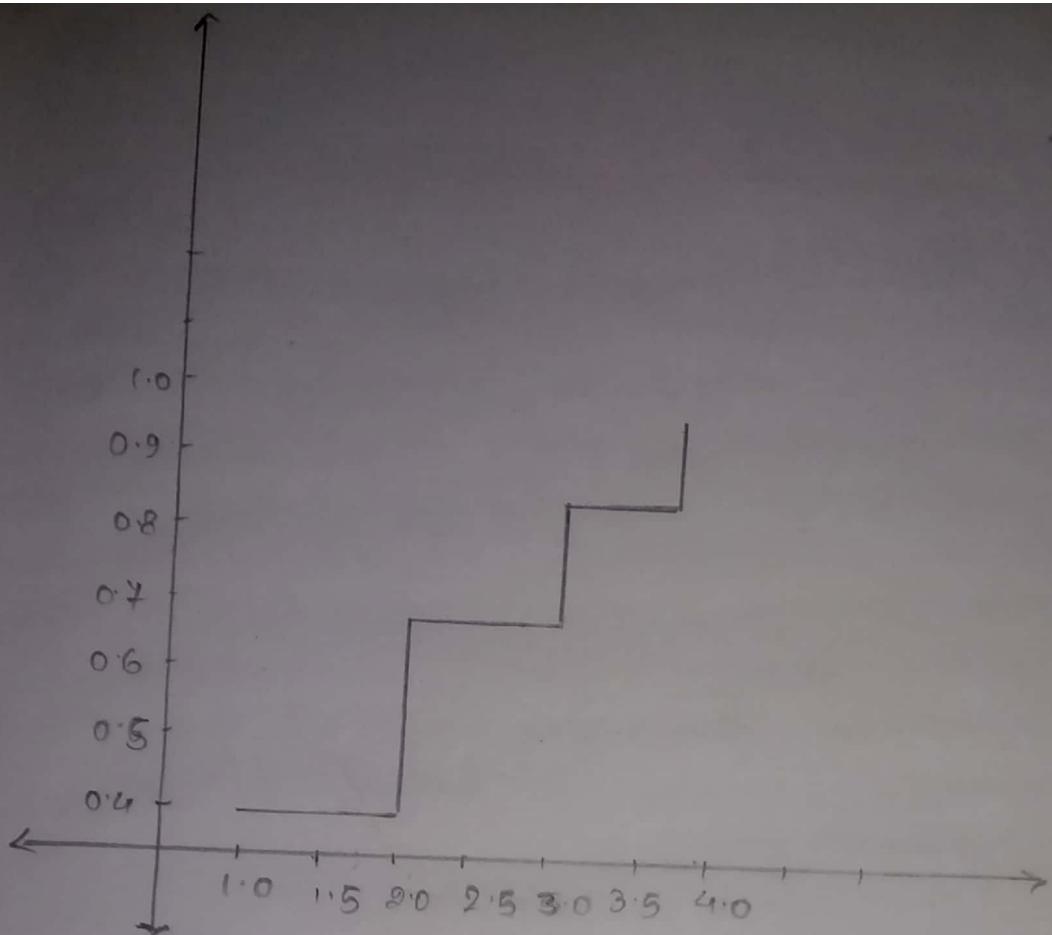
$= 0.4 \quad 1 \leq x < 2$

$= 0.7 \quad 2 \leq x < 3$

$= 0.9 \quad 3 \leq x < 4$

$= 1.0 \quad x \geq 4$

$\text{plot}(x, a, type = "l")$



<u>0.4</u>	$x$	0	2	4	6	8
	$P(x)$	0.2	0.3	0.2	0.2	0.1

$> x = c(0, 2, 4, 6, 8)$

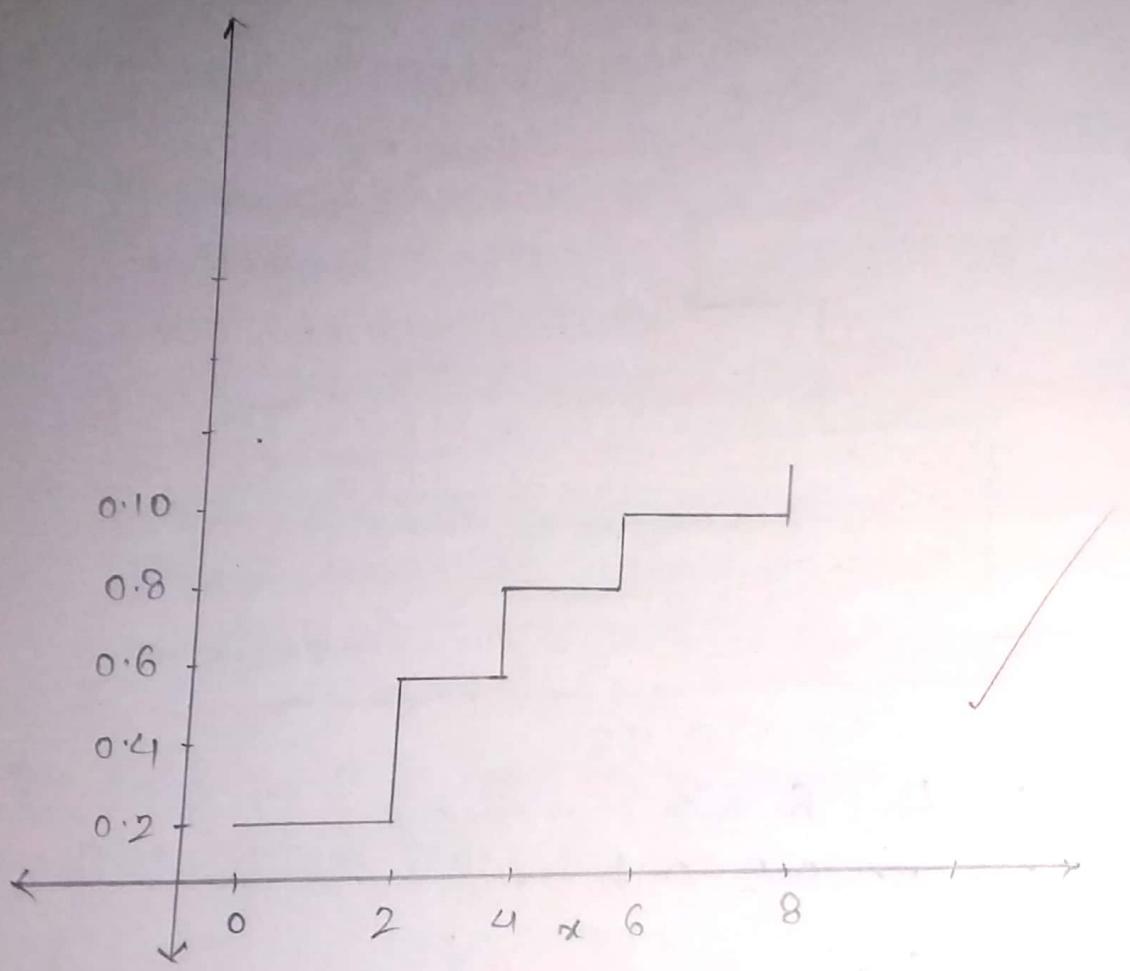
$> probx = c(0.2, 0.3, 0.2, 0.2, 0.1)$

$> a = cumsum(probx)$

$> a$

$$\begin{aligned}
 P(x) &= 0.2 & x < 0 \\
 &= 0.2 & 0 \leq x < 2 \\
 &= 0.5 & 2 \leq x < 4 \\
 &= 0.7 & 4 \leq x < 6 \\
 &= 0.9 & 6 \leq x < 8 \\
 &= 1.0 & x \geq 8
 \end{aligned}$$

$\text{plot}(x, a, "s")$



Ans  
2 3 1 2 1 9

Practice:-

Q] X follows binomial distribution with  $P=0.6$   $q=0.4$   
Find

$$a) P(X=7) \quad b) P(X \leq 3)$$

$$\rightarrow P(X=7) = {}^8C_7 (0.6)^7 (0.4)^{8-7} \\ = {}^8C_7 \times 0.2799 \times 0.4 \\ = 0.8957$$

$$P(X \leq 3) = P(0) + P(1) + P(2) + P(3) \\ = {}^8C_0 (0.6)^0 (0.4)^8 + {}^8C_1 (0.6)^1 (0.4)^7 \\ + {}^8C_2 (0.6)^2 (0.4)^6 + {}^8C_3 (0.6)^3 (0.4)^5 \\ = 1 \times 0.00065536 \times 8 \times 0.6 \times 0.0016384 \\ + 42 \times 0.36 \times 0.0004096 + 56 \times \\ 0.216 \times 0.101024 \\ = 0.1736704$$

~~$$P(X=2 \text{ or } 3) = P(2) + P(3) \\ = {}^8C_2 (0.6)^2 (0.4)^6 + {}^8C_3 (0.6)^3 (0.4)^5 \\ = 28 \times 0.36 \times 0.0004096 + 56 \times \\ 0.216 \times 0.101024 \\ = 0.04128768 + 0.12386304 \\ = 0.16515012$$~~

Practice:-

Q) X follows binomial distribution with  $P=0.6$   $q=0.4$   
Find

$$\text{a)} P(X=7) \quad \text{b)} P(X \leq 3)$$

$$\begin{aligned} \rightarrow P(X=7) &= {}^8C_7 (0.6)^7 (0.4)^{8-7} \\ &= {}^8C_7 \times 0.2799 \times 0.4 \\ &= 0.8957 \end{aligned}$$

$$\begin{aligned} P(X \leq 3) &= P(0) + P(1) + P(2) + P(3) \\ &= {}^8C_0 (0.6)^0 (0.4)^8 + {}^8C_1 (0.6)^1 (0.4)^7 \\ &\quad + {}^8C_2 (0.6)^2 (0.4)^6 + {}^8C_3 (0.6)^3 (0.4)^5 \\ &= 1 \times 0.00065536 \times 8 \times 0.6 \times 0.001638 \\ &\quad + 428 \times 0.36 \times 0.0004096 + 56 \times \\ &\quad 0.216 \times 0.101024 \\ &= 0.1736704 \end{aligned}$$

$$\begin{aligned} P[X=2 \text{ or } 3] &= P(2) + P(3) \\ &= {}^8C_2 (0.6)^2 (0.4)^6 + {}^8C_3 (0.6)^3 (0.4)^5 \\ &= 28 \times 0.36 \times 0.0004096 + 56 \times \\ &\quad 0.216 \times 0.101024 \\ &= 0.04128768 + 0.12386304 \\ &= 0.16515012 \end{aligned}$$

Q5

Practical No 5

Normal distribution:-

1] Normal distribution is an example of continuous probability distribution

$$X \sim N(\mu, \sigma^2)$$

a)  $P(X=x) = \text{norm}(x, \mu, \sigma)$

b)  $P(X < x) = \text{pnorm}(x, \mu, \sigma)$

c)  $P(X > x) = 1 - \text{pnorm}(x, \mu, \sigma)$

d) To find the value of  $K$  so that the command is  $\text{qnorm}(p, \mu, \sigma)$

$$K = P(X \geq K) = p$$

$$\text{qnorm}(p, \mu, \sigma)$$

e) To generate a random sample of size  $n$ ,  $\text{rnorm}(n, \mu, \sigma)$

Q.1] A random variable  $X \sim N(10, 2)$  find

1)  $P(X \leq 7)$  2)  $P(X \geq 12)$  3)  $P(5 \leq X \leq 12)$

4)  $P(X < K) = 0.4$  with  $\mu = 10, \sigma = 2$

Q.2]  $X \sim N(100, 36)$   $\sigma = \sqrt{36}$

1)  $P(X \leq 110)$  2)  $P(X \geq 105)$  3)  $P(X \leq 92)$

4)  $P(95 \leq X \leq 110)$  5)  $P(X \leq K) = 0.9$

Q.3] Generate 10 random sample and find the sample mean, median and variance, standard deviation.

> m = 10

> s = 2

> p1 = pnorm(7, m, s)

> cat("p(x <= 7) is =", p1)

p(x <= 7) is = 0.0668072 >

> p2 = 1 - pnorm(12, m, s)

> cat("p(x > 12) is =", p2)

p(x > 12) is = 0.15886553 >

> p3 = pnorm(12, m, s) - pnorm(5, m, s)

> cat("p(5 <= x <= 12) is =", p3)

p(5 <= x <= 12) is = 0.8351351

> k = qnorm(0.4, m, s)

> cat("p(x < k) = 0.4, k is =", k)

p(x < k) = 0.4, k = 9.493306 >

Q.2) Z m = 100

z\_s = sqrt(36)

zp1 = pnorm(110, m, s)

zcat("p(x <= 110) is =", p1)

zcat("p(x < 110) is = 0.9522096 >

zp2 = 1 - pnorm(105, m, s)

zcat("p(x > 105) is =", p2)

p(x > 105) is = 0.2023284 >

zp3 = pnorm(92, m, s)

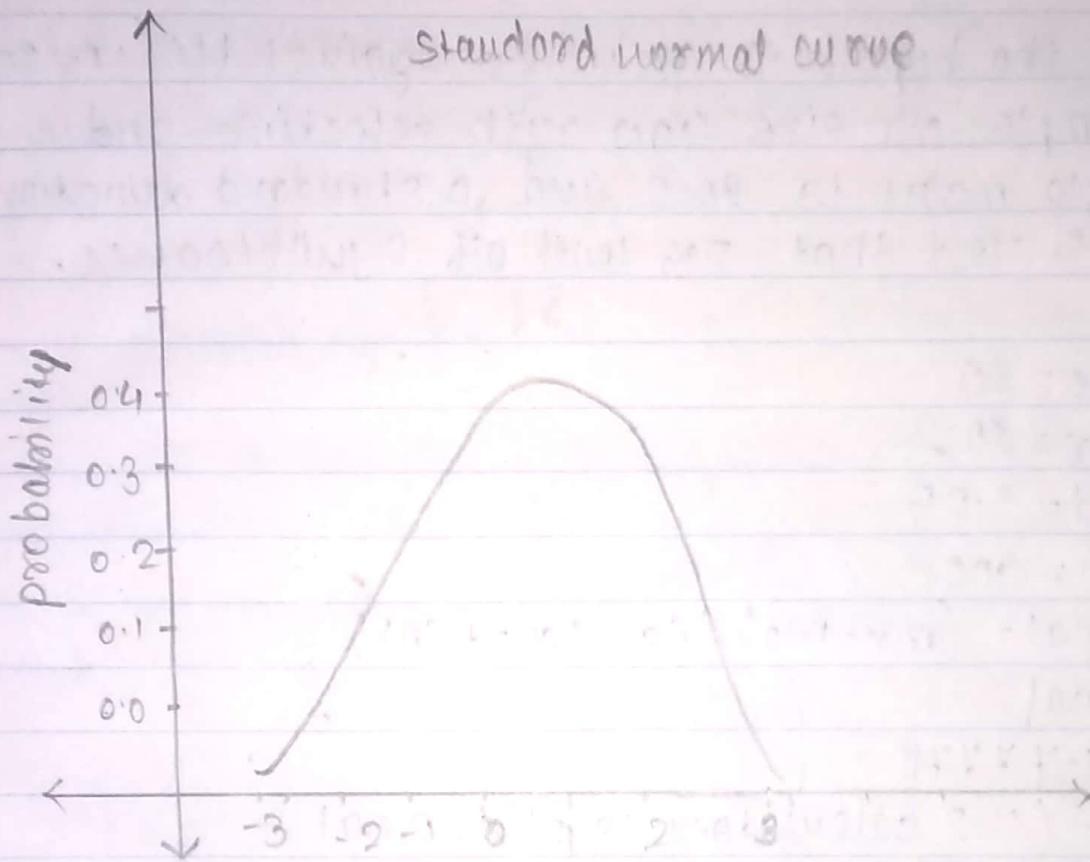
zcat("p(x <= 92) is =", p3)

p(x <= 92) is = 0.09121122 >

zp4 = pnorm(110, m, s) - pnorm(95, m, s)

zcat("p(95 < x <= 110) is =", p4)

p(95 < x <= 110) is = 0.7498813



$$0.5] X \sim N(50, 100)$$

Find 1]  $P(X \leq 60)$     2]  $P(X > 65)$   
 3]  $P(45 \leq X \leq 60)$

$$> \mu = 50$$

$$> s = \sqrt{100}$$

$$> s$$

$$\bar{x} = 10$$

$$> p1 = pnorm(60, \mu, s)$$

$$> p1$$

$$[1] 0.8413447$$

$$> p2 = 1 - pnorm(65, \mu, s)$$

$$> p2$$

$$[1] 0.668072$$

$$> p3 = pnorm(60, \mu, s) - pnorm(45, \mu, s)$$

$$[1] 0.5328072$$

22

## Practical no. 6

Q.1) Test the hypothesis  $H_0: \mu = 20$  against  $H_1: \mu > 20$ .  
A sample of size 400 with selective and sample mean is 20.2 and a standard deviation 2.25. Test that 5% level of significance.

$$\rightarrow m_0 = 20$$

$$> m_x = 20.2$$

$$> s_d = 2.25$$

$$> n = 400$$

$$> z_{cal} = (m_x - m_0) / (s_d / \sqrt{n})$$

$$> z_{cal}$$

$$[1] 1.44778$$

> cat ("2 calculator is 2" #, 2 cat)

> calculated is 1.77778

> pvalue

[1] 0.07544056

Since, p value is more than 0.05 we accept  
 $H_0: \mu = 20$

Q.2) We want to test the hypothesis  $H_0: \mu = 250$  against  $H_1: \mu > 260$ . A sample of size 100 has a mean of 275 and sd as 30. Test the hypothesis at 5% level of significance.

$$\rightarrow m_b = 250$$

$$> m_x = 275$$

$$> s_d = 30$$

$$> n = 100$$

$$> z_{cal} (m_x - m_b) / (s_d / \sqrt{n})$$

>zcal

[1] 8.333333

36

>cat("z calculated is = ", zcal)

>cat "z calculated is = 8.333333

>pvalue = 2 \* (1 - pnorm(abs(zcal)))

>pvalue

[1] 0

since p value is less than 0.05 we reject  $H_0$

Q.3 we want to test the hypothesis  $H_0: p = 0.2$  against  $H_1: p > 0.2$

if  $p$  = population proportion A sample of 400 is selected and the sample proportion is calculated 0.625. Test the hypothesis at 1% level of significance.

→ > p=0.2

> Q=1-p

> p=0.625

> n=400

>zcal=(p-p)/sqrt(p\*Q\*(n/n))

>zcal

[1]-3.75

>pvalue=2 \* (1 - pnorm(abs(zcal)))

>pvalue

[1] 0.001768346

Since p value is less than 0.05 we reject  $H_0$

>zcal

[1] 8.33333

36

>cat("z calculated is = ", zcal)

>cat("z calculated is = 8.33333")

>pvalue = 2 \* (1 - pnorm(abs(zcal)))

>pvalue

[1] 0

since p value is less than 0.05 we reject H<sub>0</sub>

Q.3 we want to test the hypothesis H<sub>0</sub>: P = 2 against H<sub>1</sub>: P > 0.2

→ p = population proportion A sample of 400 is selected and the sample proportion is calculated 0.625. Test the hypothesis at 1% level of significance.

→ > p = 0.2

> Q = 1 - p

> p = 0.625

> n = 400

> zcal = (p - p) / sqrt(p \* Q \* (n / n))

>zcal

[1] -3.75

>pvalue = 2 \* (1 - pnorm(abs(zcal)))

>pvalue

[1] 0.001788346

since p value is less than 0.05 we reject H<sub>0</sub>

Q8) In a big city of 385 men out of 600 men were found to be self-employed. Use this information support the conclusion that exactly half of the men are self-employed.

$$\therefore P = 0.5$$

$$\therefore n = 600$$

$$\therefore p = 325/600$$

$$\therefore q = 1 - p$$

$$\therefore z_{\text{cal}} = (p - P) / \sqrt{q/p + (Pq/n)}$$

$$\therefore z_{\text{cal}}$$

$$[1] 2.041201$$

$$\therefore p\text{value} = 2 * (1 - \text{pnorm}(\text{abs } z_{\text{cal}}))$$

$$\therefore p\text{value}$$

$$[1] 0.04121683$$

Since, pvalue is less than 0.505 we reject H<sub>0</sub>.

5) Test the hypothesis of H<sub>0</sub> = 50 we reject H<sub>0</sub>.

A sample of 30 is collected.

50, 49, 52, 44, 45, 48, 46, 45, 49, 45, 40, 47, 55, 54, 46, 58, 47, 44, 59, 60, 61, 41, 52, 44, 55, 56, 46, 45, 48, 49.

$$\therefore m_0 = 50$$

$$\therefore x = c(50, 49, 52, \dots, 48, 49)$$

$$\therefore n = \text{length}(x) > n [1] 30$$

$$\therefore m_x = \text{mean}(x) > m_x [1] 49.3333$$

$$\therefore \text{variance} = (n-1)^{-1} \text{var}(x) / n [1] 30.45556$$

>  $sd = \text{sqrt}(\text{variance})$  >  $sd$  [1] 5.563772

>  $z_{\text{cal}} = (\bar{x} - m_0) / (sd / \sqrt{n})$

>  $z_{\text{cal}}$

[1] -0.6562964

>  $p\text{value} < 2 * (1 - pnorm(\text{abs}(z_{\text{cal}})))$

>  $p\text{value}$

[1] 0.5116234

Since,  $p$  value is more than 0.05 we accept

$H_0: \mu = 50$

M<sup>1</sup>

58

## Practical no. 7

### large sample test

Q Two random samples of size 1000 and 2000 were drawn from two populations with standard deviation 2 and 3 respectively. Test the hypothesis that population means are equal or not at 2% level of significance. Sample means are 67 and 68% respectively.

$$\rightarrow n_1 = 1000$$

$$\rightarrow n_1$$

$$[1] 1000$$

$$\rightarrow n_2 = 2000$$

$$[1] > n_2$$

$$[1] 2000$$

$$\rightarrow m_{x_1} = 67$$

$$\rightarrow m_{x_1}$$

$$\rightarrow 67$$

$$\rightarrow m_{x_2} = 68$$

$$\rightarrow m_{x_2}$$

$$[1] 68$$

$$\rightarrow Sd^2 = 2$$

$$\rightarrow Sd_1$$

$$[1] 2$$

$$\rightarrow Sd^2 = 3$$

$$\rightarrow Sd_2$$

$$[1] 3$$

$$z_{\text{cal}} = [m_{x1} - m_{x2}] / \sqrt{(s_{x1}^2/n_1) + (s_{x2}^2/n_2)}$$

38

> zcal

$$[1] -15.80684$$

> c0t (F2 calculated is = ; zcal )

> Z calculated is -15.80684

> pvalue = 2 \* (1 - pnorm(abs(zcal)))

> pvalue

$$[1] 0$$

< 0.05 we reject  $H_0: \mu_1 = \mu_2$

Q.2 A study on noise level to hospitals in each floor following  
data is calculated sample size and sample mean  
 $s.d_1 = 7.9$  sample size = 34 Sample mean 59.4  $s.d_2 = 7.8$   
 $H_0: \mu_1 = \mu_2$  against  $H_1: \mu_1 \neq \mu_2$  At 1% level of significance

> n1 = 34

> n2 = 34

[1] 34

> n2 = 34

> n2

[1] 34

$m_{x1} = 61.2$

> mx1

[1] 61.2

> mx2 = 59.6

> mx2

[1] 59.4

$s.d_1 = 7.8$

$s.d_1$

[1] 7.8

$$sd_2 = 7.8$$

[1] 7.8

$$> zcal = (mx_1 - mx_2) / \text{sqrt}(sd_1^2/n_1 + sd_2^2/n_2)$$

> zcal

[1] 1.31117

> cat ("z calculated is ", zcal)

> calculated is 1.31117

> pvalue = 2 \* (1 - pnorm(abs(zcal)))

> pvalue

[1] 0.258006

since pvalue is greater than 0.01 we accept

Q.3] From each of two population of oranges  
the following sample are collected whether  
the proportion of bad oranges are equal or not

1) Sample size = 250

2) Sample size = 200

3) No. of bad orange in 1st sample = 44

4) No. of bad orange in 2nd sample = 30

$$H_0: p_1 = p_2$$

$$H_1: p_1 \neq p_2$$

$$> n_1 = 256$$

$$> n_1$$

$$[1] 256$$

$$> n_2 = 200$$

$$> n_2$$

$$[1] 200$$

$H_0$ 

$$\checkmark P_1 = 0.44 / 250$$

$$\checkmark P_1$$

$$[1] 0.146$$

$$\checkmark P_2 = 30 / 200$$

$$\checkmark P_2$$

$$[1] 0.15$$

$$\checkmark P(n; *P_1 + n_2 * P_2) / n_1 + n_2$$

$$\checkmark P$$

$$[1] 0.164444$$

$$\checkmark Q^2 = 1 - p$$

$$\checkmark q$$

$$[1] 8.35556$$

$$\checkmark z_{cal} = (P_1 - P_2) / \sqrt{Q^2 + (P * p + (1/n_1 + 2/n_2))}$$

$$\checkmark z_{cal}$$

$$[1] 0.439358$$

Since p value is greater we accept

$$H_0 : P_1 = P_2$$

Accept

a)  $> n_1 > 100$

$> n_2 = 600$

$> p_1 = 200/600$

$> p_2 = 390/600$

$> p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$

$> q = 1 - p$

$> z_{\text{cal}} = (p_1 - p_2) / \sqrt{q} + (p_1 + p_2) / (n_1 + n_2)$

$> z_{\text{cal}}$

[1] 4.24751

$> \text{pvalue} = 2 * [1 - \text{pnormabs}(z_{\text{cal}})]$

$> \text{pvalue}$

[1] 2.303972e-06

since pvalue accepted  $H_0: p_1 = p_2$

⑧  $> x_1 = c(74, 72, 74, 73, 79, 76, 82, 72, 85, 78,$   
 $74, 78, 76, 76)$

$> x_1$

[1] 74, 74, 74, 73, 79, 76, 82, 72, 75, 78,  
74, 76, 76

$> n_1 = \text{length}(x_1)$

$> n_1$

[1] 14

$> mx_1 = \text{mean}(x_1)$

$> mx_1$

[1] 76.21429

$> \text{variance} = (n_1 - 1) * \text{var}(x_1) / n_1$

$> \text{variance}$

[1] 6.811224

> sd1 = sqrt(variance)

> sd1

[1] 2.512215

[1] 2.512215

> x = c(42, 16, 44, 40, 40, 48, 70, 42, 75, 79, 79, 74, 75, 78, 72, 74, 80)

> x1

[1] 22, 46, 74, 70, 70, 78, 70, 72, 75, 79, 79, 74, 75, 78, 72, 74, 80

> n2 = length(x2)

> n2

[1] 1

> mx2 = mean(x2)

> mx2

[1] 44.58824

> variance = (n2 - n2) \* var(x2) / n2

> variance

[1] 10.44751

> sd2 = sqrt(variance)

> sd2

[1] 3.6238898

> t.test(x1, x2)

p-value 0.1884

> 0.03 is accepted  $H_0: \mu_1 = \mu_2$

M

Q8.

## Practical :- 8

Topic:- small sample test

1) A random sample of 15 observation is given by  
80, 100, 110, 105, 122, 140, 120, 110, 101, 88, 83, 95,  
89, 107, 125

Do this data support the assumption i.e. popular  
Mean = 100

→  $H_0: \mu = 100$

$x = c(80, 100, 110, 105, 122, 140, 120, 110, 101, 88, 83,$   
 $89, 107, 125)$

t-test(x)

one sample t-test

data: x

$t = 24.029 \quad df = 14 \quad p\text{-Value} = 8.819 \times 10^{-13}$

Alternative hypothesis: true mean is not equal to 100  
confidence interval:

91.37445 107.28892

sample estimates:

mean of x: 100.3333

Since, P value is less than 0.05 we reject

2)  $y_1 = c(18, 22, 21, 17, 20, 17, 23, 20, 22, 21)$

$y_2 = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)$

t-test(y1, y2)

data: y1 and y2

$t = 2.2573 \quad df = 16.876 \quad p\text{-Value} = 0.03798$

Alternative hypothesis: true difference in mean not  
equal to zero

mean of x mean of y

20.1 = 17.5

## The arithmetic mean of sample

Two type of medicines are used on two or seven patients for reducing their weight. The decreasing in the weight after using the medicines given below:

$$\text{med A} = 10, 12, 13, 11, 14$$

$$\text{med B} = 8, 9, 12, 14, 15, 10, 9$$

is there a significance difference in the efficiency of the medicines.

$$x = C(10, 12, 13, 11, 14)$$

$$y = C(8, 9, 12, 14, 15, 10, 9)$$

$$Z = 0.80384, df = 9.7594 \quad pvalue = 0.4406$$

alternative hypothesis; true difference in mean is not equal to 95 percent confidence interval.

$$= 1.781141 \quad 3.781141$$

sample estimates.

mean of x mean of y

12

11

since, pvalue is more than 0.05 we accept  
Ho:  $\mu_1 = \mu_2$  at 20.5

Q4) The weight reducing diet program is conducted and the observation is noted for 10 participant test whether the program is effective or not.

Before: 120, 125, 115, 130, 123, 119, 122, 127, 128, 118,

After: 111, 114, 104, 120, 115, 112, 112, 120, 119, 112,

Ans

$H_0$ , there is no significant different in weight H, the diet program reduce weight

$\gt x = c(120, 125, \dots, 128)$

$\gt y = c(111, 114, \dots, 112)$

$\gt t.test(x, y, paired = T, alternative = "less")$

data: x and y.

$t = 1.7$ ,  $df = 9$ ,  $pvalue = 1$

alternative hypothesis: true difference in means is less than 0 as percent confidence interval:

$Inf = 9.416556$

sample estimates

: mean of the difference 0.5

Q5) Sample(A) = 66, 67, 75, 76, 82, 84, 85, 90, 92

Sample (B) = 64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97

Test the population mean are equal as no.

$\gt x = c(66, 67, \dots, 90, 92)$

$\gt y = c(64, 66, \dots, 95, 97)$

$\gt t.test(x, y)$

data = x and y

t = -0.63938, df = 14.974 pvalue = 0.5304

Alternative hypothesis: True difference in means is  
mean equal to 0 as percentage

confidence interval:

-12.853992 6.853992

sample estimate:

mean of x mean of y  
80 83

since, pvalue is greater than 0.05 we accept x and 4% level of significance.

AM

## Practical 9

Aim: large and small sample space

- 1] Use arithmetic mean of a sample of a item from against an alternative if it is more than 55 at 5% LOS (level of significance)
- 2] In a big city 350 out of 750 males are found to be smokers, thus this information support that exactly half of the males in the city are smokers? Test at 1% level of significance.
- 3] Thousand article from a factory A are found to have 2% defectives 500 articles from a second factory B are found to have 1% defective. Test at 5% LOS that the two factory are similar or not.
- 4] A sample of size 400 was drawn and the sample mean is 99. Test at 5% LOS that the sample comes from a population with mean 100 and variance 64?
- 5] 10 flower stems are selected and the heights are found to be (cm) 63, 63, 68, 69, 71, 71, 72. Test the hypothesis that the mean height is 66 or not 1% LOS.
- 6] Two random sample were drawn from a normal population and their value are  $A = 66, 67, 75, 76, 82, 84, 88, 90, 92$ ,  $B = 64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97$ . Test whether the population have a same variance at 5% LOS

Solution:

$H_0: \mu_1 = \mu_2$  against .

> n = 100

> mx = 52

> m0 = 55

> sd = 7

> zcal =  $(mx - m0) / (sd / \sqrt{n})$

> zcal

[1] -4.285714

> pvalue =  $2 * (1 - pnorm(\text{abs}(zcal)))$

> pvalue

[1] 1.82153e-05

pvalue is  $< 0.05$  we rejected

2)  $H_0: \mu_1 = \mu_2$  against  $H_0: \mu_1 \neq \mu_2$

> p = 0.5

> p = 350 / 700

> p

t[1] 0.5

> n = 700

> q = 1 - p

> theta

[1] 0.5

> zcal =  $(p - theta) / \sqrt{(p * (1 - p) / n)}$

> zcal

[1] 0

> pvalue =  $2 * (1 - pnorm(\text{abs}(zcal)))$

> pvalue

E[1] 2 pvalue > 0.05 we accept .

$$3) H_0: \mu_1 = \mu_2$$

$$> n_1 = 1000$$

$$> n_2 = 1500$$

$$> p_1 = 20/100$$

$$> p_2 = (n_1 * p_1 + p_2 * p_2) / (1/n_1 + 1/n_2)$$

$$> p$$

$$[1] 0.014$$

$$> z_{cal} = (p_1 - p_2) / \text{sqrt}(p * q * (1/n_1 + 1/n_2))$$

$$> z_{cal}$$

$$[1] 2.082731$$

$$> pvalue = 2 * (1 - \text{pnorm}(\text{abs}(z_{cal})))$$

$$> pvalue$$

$$[1] 0.03727577$$

since, pvalue < 0.05

we reject pvalue.

$$4) H_0: \mu_1 = \mu_2$$

$$> n = 400$$

$$> m_x = 99$$

$$> m_0 = 100$$

$$> \text{variance} = 64$$

$$> \text{sd} = \text{sqrt}(\text{variance})$$

$$> \text{sd}$$

$$[1] 8$$

$$> z_{cal} = (m_x - m_0) / (\text{sd} / \text{sqrt}(n))$$

$$> z_{cal}$$

$$[1] -2.5$$

> pvalue = 2 \* (1 - pnorm(abs(zcal)))

> pvalue

[1] 0.01241933

Since, pvalue < 0.05

we reject.

⑤  $H_0: \mu_1 = \mu_2$

> x = c(63, 63, 68, 69, 71, 71, 72)

> t.test(x)

One sample t-test

data = x

t = 47.54, df = 6, p.value = 5.522e-09

alternative hypothesis : true mean is not equal to 0.

95% confidence interval

sample estimate

mean of x

68.14286

p value is < 0.05 we reject.

⑥  $H_0: \mu_1 = \mu_2$  against  $H_1: \mu_1 \neq \mu_2$

> x = c(66, 64, 68, 69, 70, 72)

> y = c(64, 66, 68, 70, 75, 77)

> f.var.test(x, y)

> F

F test to compare two variance

data: x and y

$F = 0.70686$ , num df=8, denom df=10, p-value  
Alternative hypothesis: ratio of variance is  
not equal to 1.

95% confidence interval.

0.1833662 3.0360393

Sample estimates

Ratio of variance

0.7068567

$H_0: H_1 = H_0$  against  $H_0: \rho_1 \neq \rho_2$   
p-value > 0.05 we accept  $H_0: H_1 = H_2$

(M)

5

1

6

Practical 10

Q) Use the following data to test whether the cleanliness of home and cleanliness of child is independent or not.

C.C.	C.H	Clean	Dirty
clean	40	50	
below clean	80	20	
Dirty	35	45	

Solution:  $H_0$ : CC and CH

$\rightarrow x = C(40, 80, 35, 50, 20, 45)$

$\rightarrow m = 3$

$\rightarrow n = 2$

$\rightarrow y = \text{matrix}(x, \text{mrow} = m, \text{ncol} = n)$

$\rightarrow y$

[1, ]	[, 1]	[, 2]
[2, ]	40	50
[3, ]	80	45

$\rightarrow PV = \text{chisq.test}(y)$

$\rightarrow PV$

percents chi-squared test

data: y

$\chi^2\text{-squared} = 25.646$ ,  $df = 2$ ,  $p\text{-value} = 2.69806$ .

Since, pvalue is less than 0.05, we get rejected.  
Hence, child cleanliness and home cleanliness are dependent.

Q22 Use the following data to find if vaccination and a particular disease are independent or not.

		Aut	not Aut
Vacc	Given	20	30
	not given	25	35

Soln:  $H_0$ : Vacc & Dis

$$\Rightarrow x = c(20, 25, 30, 35)$$

$$>m=2$$

$$>n=2$$

> y=matrix(x, nrow=m, ncol=n)

> y

	[1,1]	[1,2]
[1,1]	20	30
[2,1]	25	35

Pearson's chi-squared test with Yates' continuity correction

data=y

X-squared=0, df=1, pValue=1

Since, pvalue is more than 0.05, we accept  
Hence, the vaccine and disease independence  
of each other.

Q.3 perform ANOVA for the following data  
varieties

46

observation

A	50, 52
B	53, 55, 53
C	60, 58, 57, 56
D	52, 54, 54, 55

Soln: H<sub>0</sub>: The mean of the varieties are equal.

> x<sub>1</sub> = c(50, 52)

> x<sub>2</sub> = c(53, 55, 53)

> x<sub>3</sub> = c(60, 58, 57, 56)

> x<sub>4</sub> = c(52, 54, 54, 55)

> d = stack(list(b<sub>1</sub> = x<sub>1</sub>, b<sub>2</sub> = x<sub>2</sub>, b<sub>3</sub> = x<sub>3</sub>, b<sub>4</sub> = x<sub>4</sub>))

> names(d)

values ind

> oneway.test(values ~ ind, data = d, var.equal = T)

one-way analysis of means

data: values and ind

F = 3.326, numdf = 3, denomdf = 9, pvalue = 0.0

> anova = aov(values ~ ind, data = d)

> anova

call:

aov(formula = values ~ ind, data = d)

## Terms:

Sum of squares	ind residuals	71.5000
Deg. of freedom	49.26923	9
	3	9

Residual standard error: 1.420746

Estimated effects may be unbalanced.

Q4) The following data gives life of four types of four brands.

Type	Observation
A	20, 23, 18, 17, 18, 22, 24
B	19, 15, 17, 20, 16, 17
C	21, 19, 22, 14, 20
D	15, 14, 16, 18, 14, 16

Test the hypothesis that the average life of four brands is same.

H0: The average of four brands is same.

$$x_1 = c(20, 23, 18, 17, 18, 22, 24)$$

$$x_2 = c(19, 15, 17, 20, 16, 17)$$

$$x_3 = c(21, 19, 22, 14, 20)$$

$$x_4 = c(15, 14, 16, 18, 14, 16)$$

> d = stack(list(b1=x1, b2=x2, b3=x3, b4=x4))

> names(d)

> t("values", "ind")

> anova = ANOVA(values ~ ind, data=d)

>anova

call:

ANOVA (formula = values ~ ind, data = d)

Terms:

ind residuals

sum of squares	91.4381	89.0619
deg of freedom	3	20

Residual standard error: 2.110236

Estimated effects may be unbalanced.

oneway.test(values ~ ind, data = d, var.equal = T)

One-way analysis of means

data: values and ind

F = 6.8445, num df = 3, denom df = 20, p-value = 0.002349)

Q: one thousand student of a college graded according to the IQ and economic condition of their home. check that is there any association between IQ and ~~the~~ economic condition of the home.

E.C	Flight	T.Q	
		High	Low
	pred	160	140
	low	330	200
		240	160

Soln: H<sub>0</sub>: IQ & E.C.

$\Rightarrow x = c(460, 330, 240, 140, 200, 160)$

$\times m = 3$

$\times n = 2$

$\times y = \text{matrix}(x, \text{nrow}=m, \text{ncol}=n)$

$\times y$

	[1,1]	[1,2]
[1,1]	460	140
[2,1]	330	200
[3,1]	240	160

$\times p_v = \text{chisq.test}(y)$

$\times p_v$

pearson's chi-squared test

data: y

$\chi^2$ -squared = 39.726, df = 2, p-value = 2.364e-0.7

since, pvalue is less than 0.5, it rejected.

$\checkmark$   
 $\alpha = 0.05$

$H_0$ : population median is 625.

>  $x = c(612, 619, 631, 628, 643, \dots)$

>  $me = 625$

>  $sp = length(x[x > me])$

>  $sn = length(x[x < me])$

>  $n = sp + sn$

>  $n$

[1] 10

>  $pv = pbinom(sn, n, 0.5)$

>  $pV$

[1] 0.0546875

## Practical no. 11

49

### Non-parametric test

Following are the amounts of sulphur oxide emitted by industries in 20 days. Apply sign test to test the hypothesis that the population median is 21.5.

17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26.

$H_0$ : population median is 21.5.

>  $X = C(17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26)$

> median = 21.5

>  $Sp = \text{length}(x[x > \text{med}])$

>  $Sn = \text{length}(x[x < \text{med}])$

>  $n = Sp + Sn$

>  $n$

[1] 20

>  $PV = \text{pbinom}(Sp, n, 0.5)$

>  $PV$

[1] 0.4119015

② Following are the 10 distribution,  
612, 619, 631, 628, 643, 640, 655, 649, 670, 663.  
Apply sign test to test the hypothesis that the population median is 625 against the alternative it is greater than 625 and 1% LOS.

Note: If alternative is greater  
 $PV = \text{pbinom}(Sn)$

Q.3 Following are the distributions.  
36, 32, 21, 30, 24, 25, 20, 22, 20, 18

Using sign test, test the hypothesis that the population median is 25 against the alternative is less than 25 at 1% LOS.

>  $x = c(36, 32, 21, 30, 24, 25, 20, 22, 20, 18)$

>  $m_e = 25$  [H<sub>0</sub>: population median is 25]

>  $Sp = \text{length}(x[x > m_e])$

>  $Sn = \text{length}(x[x < m_e])$

>  $n = Sp + Sn$

>  $n$

[1] 9

>  $PV = \text{pbinom}(Sp, n, 0.5)$

>  $PV$

[1] 0.2539063

Q.4 Following are the distributions

63, 65, 80, 89, 61, 71, 58, 51, 69, 62, 63, 39, 72, 65

Using wilcoxon signed rank test, test hypothesis that the population median is 60. Against the alternative it is greater than 60 at 5% LOS.

H<sub>0</sub>: population median is 60

>  $x = c(63, 65, 60, 89, 61, 71, 58, 51, 69, 62, 63, 89, 72, 65)$   
> wilcox.test(x, alt = "greater", mu = 60) 50

wilcoxon signed rank test with continuity correction  
data: x

$$V = 68, p\text{-Value} = 0.06186$$

alternative hypothesis: true location is greater than 60.  
~~Warning messages:~~

Q.5 Following are the

20, 25, 27, 30, 18, test the hypothesis.

→  $x = c(20, 25, 27, 30, 18)$   $H_0$ : population median is 25  
> wilcox.test(x, alt = "two.sided", mu = 25)  
wilcoxon test. rank.test with continuity correction  
data: x

$$V = 23.5, p\text{-Value} = 0.7122$$

Alternative hypothesis: true location not equal to 25.

Q6

Following are the observation.

15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 26, use wilcoxon rank test.

```
> x = c(15, 17, 24, - - - )  
> wilcox.test(x, alt = "less", mu = 20)  
> x = c(15, 17, 24, 25,  
      data = x  
      V = 48.9, p.value = 0.9257
```

Alternative hypothesis true location is less than 20.

✓ q < 20