

1. Blood glucose levels for obese patients have a mean of 100 with a standard deviation of 15. A researcher think that a diet high in raw cornstarch will have a positive effect on blood glucose levels. A sample of 36 patients who have tried the raw cornstarch diet have a mean glucose level of 108. Test the hypothesis that the raw cornstarch had an effect or not.

Soln: ->

Null Hypothesis  $H_0$  is  $\mu = 100$

alternate Hypothesis  $H_a$  is  $\mu \neq 100$

we assume standard significance level 0.05 for this problem as it is not mentioned

$$\alpha = 0.05$$

As this is two-tailed test

$$\alpha = 0.05/2 = 0.025$$



As this is two tail test and error area is 2.5% both side.

Remaining area for positive side = 47.5%

Z score for 0.475 is 1.96 as per Z-table

$$Z_{\text{score as per statistics}} = \frac{\bar{x} - \mu_0}{\sigma \sqrt{n}}$$

$$= \frac{108 - 100}{15 \times \sqrt{36}}$$

$$= \frac{8}{15 \times 6} = \frac{4}{45} = 0.088$$

If  $Z_{stat}$  lies between  $-1.96$  and  $1.96$  then we can accept the Hypothesis

$Z_{stat} = 0.088$  which lies between  $-1.96$  and  $1.96$

Hence Hypothesis is accepted means new coin stack had an effect.

2. In one state, 52% of voters are Republicans and 48% are Democrats. In a second state, 47% of voters are Republicans and 53% are Democrats. Suppose a simple random sample of 100 voters are surveyed from each state.

What is the probability that the survey will show a greater percentage of Republican voters in Second state than in the first state.

Soln

Mean of the difference in Republican proportion =

$$P_1 - P_2 = 0.52 - 0.47 = 0.05$$

Standard deviation of Republican difference in 2 states =

$$\begin{aligned} \sigma_d &= \sqrt{\left[ \frac{P_1(1-P_1)}{n_1} \right] + \left[ \frac{P_2(1-P_2)}{n_2} \right]} \\ &= \sqrt{\left[ \frac{0.52 \times 0.48}{100} \right] + \left[ \frac{0.47 \times 0.53}{100} \right]} \\ &= \sqrt{\frac{0.2496}{100} + \frac{0.2491}{100}} = \sqrt{\frac{0.4987}{100}} = \sqrt{0.004987} \\ &= 0.0706 \end{aligned}$$

we have to find out the probability that proportion of Republican voter in sample from first state ( $p_1$ ) is less than proportion of republican voter in sample from 2nd state ( $p_2$ )

probability to find out ( $p_1 - p_2$ ) is less than zero

$$\begin{aligned} Z_{(p_1 - p_2)} &= \frac{x - \mu_{p_1 - p_2}}{\sigma_d} \\ &= \frac{0 - 0.05}{0.0706} = -0.7082 \end{aligned}$$

As per Z-Table probability of a Z-score being  $-0.7082$  or less is  $0.24$

~~Proba~~ Probability to show greater percentage of republican voters in second state than first state =  $0.24$ .

3.

you take the SAT and score 1100. The mean score for the SAT is 1026 and the standard deviation is 209. How well did you score on test compared to the average test taker.

Soln

$$\begin{aligned} Z &= \frac{x - \mu}{\sigma} = \frac{1100 - 1026}{209} = \frac{74}{209} \\ &= 0.354 \end{aligned}$$



As per z table value of  $z = 0.1368$

• z table <sup>has</sup> shown score for the right of the mean.

That's why percentage of test-taker scored

$$\text{below you} = 0.1368 + 0.50 = 0.6368 = \cancel{63.68\%}$$

$$= 63.68\%$$

## TASK - 2

Q.1 :-

	High-school	Bachelors	Masters	Ph.d	Total
Female	<del>50</del> 60	54	46	41	201
Male	40	44	53	57	194
Total	100	98	99	98	395

Are gender and education level dependent at 5% level of significance? In other words, given the data collected above, is there a relationship between the gender of an individual and the level of education that they have obtained.

Soln

Hypothesis :-

$H_0$  :- Gender and education level are independent.

$H_a$  :- Gender and education level are dependent.

The Significance level  $= \alpha = 0.05$

We are going to perform Chi-square test for independence.

$$\begin{aligned} \text{DF (Degree of Freedom)} &= (r-1) \times (c-1) \\ &= (2-1) \times (4-1) \\ &= 1 \times 3 = 3 \end{aligned}$$

$E_{rc}$  (Expected frequency count for 'r' and 'c') =

$$n_{r.} \times n_{.c} / n$$

$$E_{1,1} = \frac{201 \times \overset{20}{100}}{\underset{79}{395}} = \frac{402}{79} = \frac{4020}{79} = 50.886$$

$$E_{1,2} = \frac{201 \times 98}{395} = \frac{19698}{395} = 49.868$$

$$E_{1,3} = \frac{201 \times 99}{395} = \frac{19899}{395} = 50.377$$

$$E_{1,4} = \frac{201 \times 98}{395} = \frac{19698}{395} = 49.868$$

$$E_{2,1} = \frac{194 \times 100}{395} = \frac{19400}{395} = 49.113$$

$$E_{2,2} = \frac{194 \times 98}{395} = \frac{19012}{395} = 48.131$$

$$E_{2,3} = \frac{194 \times 99}{395} = \frac{19206}{395} = 48.623$$

$$E_{3,3} = \frac{194 \times 98}{395} = \frac{19012}{395} = 48.131$$

$$\chi^2 = \sum \left[ \frac{(O_{rc} - E_{rc})^2}{E_{rc}} \right]$$

$O_{rc}$   $\Rightarrow$  observed frequency count for 'r' and 'c'

$$\begin{aligned}
&= \frac{(60-50.886)^2}{50.886} + \frac{(54-49.868)^2}{49.868} + \\
&\quad \frac{(46-50.377)^2}{50.377} + \frac{(41-49.868)^2}{49.868} + \\
&\quad \frac{(40-49.113)^2}{49.113} + \frac{(44-48.131)^2}{48.131} + \\
&\quad \frac{(53-48.623)^2}{48.623} + \frac{(57-48.131)^2}{48.131} \\
&= \frac{88.064}{50.886} + \frac{17.0734}{49.868} + \frac{19.158}{50.377} + \frac{78.641}{49.868} + \\
&\quad \frac{83.047}{49.113} + \frac{17.065}{48.131} + \frac{19.158}{48.623} + \frac{78.659}{48.131} \\
&= 1.632 + 0.342 + 0.380 + 1.576 + 1.690 + 0.354 + \\
&\quad 0.394 + 1.635 \\
&= 8.003
\end{aligned}$$

The P-value is the probability that a chi-square statistic having 3 degrees of freedom is more extreme than 8.003

as per chi-square table  $= P(X^2 > 8.003) = 0.05$

Since P-value is similar to the significance level (0.05)

So we can accept the null hypothesis  
(i.e.) Gender and education level are independent.



Q2:-

using the following data, perform a oneway analysis of variance using  $\alpha = 0.05$ . write up the results in APA Format.

Group 1	Group 2	Group 3
51	23	56
45	43	76
33	23	74
45	43	87
67	45	56

Soln

$$SS_{total} = (\sum x_1^2 + \sum x_2^2 + \sum x_3^2) - \frac{(\sum x_1 + \sum x_2 + \sum x_3)^2}{N}$$

$$\sum x_1^2 = (51)^2 + (45)^2 + (33)^2 + (45)^2 + (67)^2$$

$$= 2601 + 2025 + 1089 + 2025 + 4489$$

$$= 12229$$

$$\sum x_2^2 = (23)^2 + (43)^2 + (23)^2 + (43)^2 + (45)^2$$

$$= 529 + 1849 + 529 + 1849 + 2025$$

$$= 6781$$

$$\sum x_3^2 = (56)^2 + (76)^2 + (74)^2 + (87)^2 + (56)^2$$

$$= 3136 + 5776 + 5476 + 7569 + 3136$$

$$= 25093$$

$$\sum x_1 = 241 \quad \sum x_2 = 177 \quad \sum x_3 = 349$$

$$SS_{total} = (12229 + 6781 + 25093) - \frac{(241 + 177 + 349)^2}{15}$$

$$= 44103 - \frac{(767)^2}{15} = 44103 - \frac{588289}{15}$$

$$= 44103 - 39219.2667 = 4883.73$$

$$SS_{\text{among}} = \left[ \frac{(\sum x_1)^2}{n_1} + \frac{(\sum x_2)^2}{n_2} + \frac{(\sum x_3)^2}{n_3} \right] - \frac{(\sum x_1 + \sum x_2 + \sum x_3)^2}{N}$$

~~$$= \left[ \frac{12229}{5} + \frac{6781}{5} + \frac{25093}{5} \right] - \frac{39219 \cdot 2667}{15}$$~~

~~$$= \left[ \frac{44103}{5} \right] - \frac{39219 \cdot 2667}{15}$$~~

$$= \left[ \frac{(241)^2}{5} + \frac{(177)^2}{5} + \frac{(349)^2}{5} \right] - \frac{39219 \cdot 2667}{15}$$

$$= \left[ \frac{58081}{5} + \frac{31329}{5} + \frac{121801}{5} \right] - \frac{39219 \cdot 2667}{15}$$

$$= \left[ \frac{42242.5}{8} \right] - \frac{39219 \cdot 2667}{15}$$

$$= 42242.5 - 39219 \cdot 2667$$

$$= 3023.2333$$

$$SS_{\text{within}} = SS_{\text{total}} - SS_{\text{among}}$$

$$= 4883.73 - 3023.23$$

$$= 1860.50$$

$$df_{\text{among}} = 3 - 1 = 3 - 1 = 2$$

$$df_{\text{within}} = N - 3 = 15 - 3 = 12$$



$$MS_{\text{among}} = \frac{SS_{\text{among}}}{df_{\text{among}}} = \frac{3023.23}{2} = 1511.615$$

$$MS_{\text{within}} = \frac{SS_{\text{within}}}{df_{\text{within}}} = \frac{1860.50}{12} = 155.04$$

$$F = \frac{MS_{\text{among}}}{MS_{\text{within}}} = \frac{1511.615}{155.04} = 9.75$$

APA Format Result :-

Source	SS	df	MS	F
Among	3023.2388	2	1511.615	9.75
Within	1860.50	12	155.04	

30 :-

Calculate F Test for given 10, 20, 30, 40, 50 and 5, 10, 15, 20, 25

For 10, 20, 30, 40, 50

Sol<sup>n</sup>

$$F \text{ Test} = \frac{\text{variance of } (10, 20, 30, 40, 50)}{\text{variance of } (5, 10, 15, 20, 25)}$$

$$\text{variance of } 10, 20, 30, 40, 50 = \cancel{S_1} N_1$$

$$\text{variance of } 5, 10, 15, 20, 25 = \cancel{S_2} N_2$$

$$\text{Mean of } 10, 20, 30, 40, 50 = \cancel{\bar{x}_1} \bar{x}_1$$

$$\text{Mean of } 5, 10, 15, 20, 25 = \bar{x}_2$$

$$\bar{x}_1 = \frac{10+20+30+40+50}{5} = \frac{150}{5} = 30$$

$$\bar{x}_2 = \frac{5+10+15+20+25}{5} = \frac{75}{5} = 15$$

$$s_1^2 = \frac{(10-30)^2 + (20-30)^2 + (30-30)^2 + (40-30)^2 + (50-30)^2}{5-1}$$

$$= \frac{400 + 100 + 0 + 100 + 400}{4}$$

$$= \frac{1000}{4} = 250$$

$$s_2^2 = \frac{(5-15)^2 + (10-15)^2 + (15-15)^2 + (20-15)^2 + (25-15)^2}{4}$$

$$= \frac{100 + 25 + 0 + 25 + 100}{4}$$

$$= \frac{250}{4} = 62.5$$

$$F_{Test} = \frac{s_1^2}{s_2^2} = \frac{250}{62.5} = 4$$

$$F_{Test} \text{ value} = 4$$