

LOGISTIC REGRESSION

The logistic regression model transforms the linear regression function continuous value output into categorical value output using a sigmoid function, which maps any real-valued set of independent variables input into a value between 0 and 1. This function is known as the logistic function.

- The independent inputs are X , a matrix of dimension $n \times m$.
- Weights of each variable x_i are represented in the matrix W of dimension $n \times 1$.
- B is known as the bias term.
- Sigmoid function or σ , $\sigma(x) = 1/(1 + e^{-x})$, This ensures that the output lies between 0 and 1.

And the equation for logistic regression could be represented as :

$$y = \sigma(w^T X + b)$$

Logistic function is a simple strategy to map the linear combination “ z ”, lying in the $(-\infty, \infty)$ range to the probability interval of $[0, 1]$.

$$\text{logit}(p) = \log(p/1-p)$$

Linear regression uses mean squared error as its cost function. If this is used for logistic regression, then it will be a non-convex function of parameters (θ). Gradient descent will converge into global minimum only if the function is convex

Cost function :

$$\text{cost} = -\frac{1}{m} \sum_{i=1}^m [y * \log(a) + (1 - y) * \log(1 - a)]$$

Gradient Descent

$$dW = \frac{\partial \text{COST}}{\partial W} = (A - Y) * X^T \dots\dots \text{shape } (1 \times n)$$

$$dB = \frac{\partial \text{COST}}{\partial B} = (A - Y)$$

$$W = W - \alpha * dW^T$$

$$B = B - \alpha * dB$$

