

HW-6

$$2.) \quad T_w(n) = \sum_{k=1}^{n-1} O((kn)^{1.59})$$

where k is number of iteration.

$$= O(n^{1.59}) \sum_{k=1}^{n-1} k^{1.59}$$

$$= O(n^{1.59}) O(n^{2.59})$$

$$= O(n^{4.18})$$

3.) divide the n bits string into two groups.

step 1: write formula

$$B_k(n, n) = B_k(n/2, n) + B_k(n/2, n) + O(n/2 \cdot n)^{1.59}$$

$$G(n) = 2G(n/2) + O\left(\frac{n^2}{2}\right)^{1.59}$$

Step 2: guess $G(n) = O(n^{2 \times 1.59})$

that is $T_w(n) \leq C \cdot n^{2 \times 1.59}$ for all n , for all some $C > 0$

Step 3.

$$\text{I.W. } \forall i < n, \ln(i) < c \cdot i^{2 \cdot 1.59}$$

$$\ln(n) = 2 \ln(n/2)^{2 \cdot 1.59} + O(n^{1.59})$$

$$= 2 C \left(\frac{n}{2} \right)^{2 \cdot 1.59}$$

$$= O\left(\frac{n}{2}\right)^{2 \cdot 1.59}$$