

# Base Arithmetic (250 points)

## Introduction

A base-n number is a number that is made up of at most n symbols -

- Base-2 is a number with 0s and 1
- Base-10 is a number with digits in {0,1,2,3,4,5,6,7,8,9}
- Base-16 is a number with digits 0-9,A-F etc

For this problem, you are required to do the following:

- Given a number X (X will be a number in a base between base-2 and base-16), find the minimum base that can be associated with X.  
Example: The minimum base associated 385 is base-9 (as it needs to have a base that supports the digit 8 which is its highest value digit). Similarly, the minimum base associated with B95 is base-12.
- Convert X from this base to a value  $X_{10}$  in base-10.
- Do the same for another number Y and call its value in base-10 as  $Y_{10}$
- Print out the sum of these two numbers in base-10, ie  $X_{10} + Y_{10}$

## Input Specifications

Your program will take

- A number X in base-m ( $X \geq 0, 2 \leq m \leq 16$ )
- A number Y in base-n ( $Y \geq 0, 2 \leq n \leq 16$ )

You can assume that X and Y when converted to base-10 will fit in a long long (C++).

## Output Specifications

Based on the input, print out the sum of  $X_{10}$  and  $Y_{10}$

## Sample Input/Output

### Input

B95  
101101

### Output

1742

## Explanation

B95 is in base-12. In base-10, its value is 1697. 101101 is in base-2. In base-10, its value is 45.  $45 + 1697 = 1742$