

Referee response to BS14324 Patra

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We thank the referee for their comments and questions. We present our responses below (in blue).

Response to the fourth referee

Point 1.

While the work seems carefully done and is quite thorough, what was really achieved in the end is nothing really new or non-trivial.

Response:

We believe that the following results are new and interesting additions to the knowledge of multichannel Kondo physics that are obtained from our work:

- importance of the role of degeneracy and quantum-mechanical frustration in shaping the infrared physics of the MCK, specifically in the absence of any Fermi liquid component and the emergence of non-Fermi liquid behaviour, the thermodynamic properties, the orthogonality catastrophe, the breakdown of screening and in the strong-weak duality,
- derivation of a marginal Fermi liquid effective Hamiltonian for the non-Fermi liquid fixed point, hence revealing the microscopic source of the non-Fermi liquid behaviour in the overscreened regime; we have confirmed in the supplementary materials that the $\ln T$ behaviour of the impurity specific heat and susceptibility in the 2CKM arises from this effective Hamiltonian
- the presence of a spin Mott liquid in the effective interactions among the conduction electrons,
- demonstration of the orthogonality catastrophe in the ground state through entanglement measures.

The observation of the Mott liquid is particularly significant because it highlights a common theme that pervades much of fermionic quantum matter - the role of zero modes in determining the infrared physics. This can be seen, for instance, in the emergence of a Mott liquid from the 2D Hubbard model as seen from a URG analysis [1, 2, 3] and a Cooper pair insulator from the reduced 2D BCS Hamiltonian [4]. Importantly, we have also corroborated several of our analytic and numerical results for the MCK with those that exist in the literature.

Point 2.

Despite the motivation from a complex RG scheme, the authors simply investigate in the end the zero bandwidth 2-channel Kondo model (2CKM), which is the simple problem of a spin coupled to two fermions. This is already contained in the seminal paper of Nozières and Blandin in 1981. The authors claim this gives perspectives on the 2CKM fixed point, but on the contrary, the argument of Nozières and Blandin is to show that this zero-bandwidth fixed point is unstable, hence a non-trivial interacting state should arise.

Response:

First, we point out that we have studied much more than simply the zero-bandwidth model for the 2CKM. We have already stated in response to Point 1 above the important questions that we have answered for the MCK problem and which are beyond the purview of a zero-bandwidth model.

Second, we comment on the validity of our study of the zero-bandwidth model at the **intermediate coupling fixed point (ICFP)** of the MCK problem. Nozieres and Blandin indeed present an argument for why the zero-bandwidth model at the **strong coupling fixed point** ($J = \infty$) is unstable due to the existence of non-trivial RG relevant quantum fluctuations. The resulting RG flow of the Kondo coupling J to the ICFP resolves these quantum fluctuations. The RG stability of the Kondo coupling J at the ICFP then allows for a renormalised perturbation theory approach to studying the fixed point Hamiltonian. Specifically, the zero-bandwidth model can be safely extracted (in the RG sense) as the zeroth approximation of a renormalised perturbation theory in the ratio of the conduction bath hopping amplitude (t) to J . A study of the zero-bandwidth model at the ICFP offers, in turn, new perspectives into the problem, e.g., the ground state degeneracy and its relation to the breakdown of exact screening etc. It also informs us on the ground state manifold about which to carry out a systematic treatment of a renormalised perturbative expansion.

In response to point 3 below, we comment on our ability to capture the critical corrections to this zeroth approximation. Finally, we have added a few lines to the manuscript at the end of Subsection II-B in order to clarify the validity of our zero-bandwidth approximation. We believe that, taken together with our summary of main results, this offers adequate clarification of the approach taken and results achieved.

Point 3.

While this study could have some pedagogical value per se, it is often unnecessarily technical, and some statements are clearly incorrect. For instance, the authors failed to see that the $1/T$ susceptibility is a trivial feature of the zero-bandwidth toy-model, while the true 2CKM fixed point has critical corrections. I don't think these can be so easily captured by the expansion they propose.

Response:

As has been shown in considerable detail in Section IV A of the main manuscript and Section III of the supplementary materials, we have extracted analytically the effective theory for the low-lying excitations above the degenerate ground states of the zero-bandwidth model by carrying out a careful renormalised perturbation theory in t/J for both the 2CK and 3CK problems. We have demonstrated the non-Fermi liquid nature of these excitations, and also confirmed their critical nature by the computation of some thermodynamic quantities in Section IIIB for the 2CK. Indeed, in keeping with the point raised by the referee, we have obtained the well-known logarithmic dependence of the specific heat and susceptibility on temperature from our calculations. We trust that the referee will find this a satisfactory demonstration.

References

- [1] Anirban Mukherjee and Siddhartha Lal. Scaling theory for mott–hubbard transitions: I. $t = 0$ phase diagram of the $1/2$ -filled hubbard model. *New Journal of Physics*, 22(6):063007, jun 2020.
- [2] Anirban Mukherjee and Siddhartha Lal. Scaling theory for mott–hubbard transitions-II: quantum criticality of the doped mott insulator. *New Journal of Physics*, 22(6):063008, jun 2020.
- [3] Anirban Mukherjee and Siddhartha Lal. Superconductivity from repulsion in the doped 2d electronic hubbard model: an entanglement perspective. *J. Phys.: Condens. Matter*, 34:275601, 2022.
- [4] Siddhartha Patra and Siddhartha Lal. Origin of topological order in a cooper-pair insulator. *Phys. Rev. B*, 104:144514, Oct 2021.